Focus on LK Regularization

 $X = (x_1, ..., x_n)$, $Box Q = INN | I|xIIq = <math>\sqrt{\sum |x|^n}$ Q = 0, $I|xII_0 = \sqrt{\sum |x| + 0}$ $Indicator Function: <math>I_{x_1} = \frac{1}{2}x_1 + 0$

I- Focus on la Regularization

Lo Regularization refers to minimizing the number of nonzero weights in a model Good: remove unnecessary parameters and make the network sparse interpretable - expect: pruning = forces some weights to be exactly zero

=) lecouse of its "Standard Grabient Descent for Regularization UNUSABLE : X 2 = Loss (W) + >11 W16 total regular loss (o perolly loss (cike HSE)

=> We need a continuous approximation

(seules 110 sterrit fo noises bexoler) : notulistical Distribution : (neloxed varion of sincete 012 values)

- I. Instead of directly pauring weights (0 or. 1), we assign a probability that a weight is
- 2. We sample values from a stretched signard function (=0,12) to approximate Virary becisions.
- 3. This Maur grabient-Rosed learning, moking to Regularization trainable.
- · ProPolitistic Relaxation: a mathematical trick used to approximate non-differentiable discrete becisions (e.g., relecting whether a weight should be attice or zero) with continuous and differentiable approximations.
- · Why concrete in the Hand Concrete distribution?
 - . The Connete Distribution (or Redexed Bernsulli Distribution) is a continuous approximation of a biscrete Consulli (01) Distribution.
- · Why Hard in the Hard Concrete Distribution? (most ought ready Generally Generally Generally Generally Generally
 - . Even though the function is continuous the output strongly resembles a lineary decision Dase to O or 1.

The Hard Concrete Cistibution modifies the Connete Historiation by obding abbitional stretching on Dipping.

Mathematical Trick: Hard Concrete Kishibution $Z = 5 \left(\frac{\log(u) + \log(1 - u) + \log(\alpha)}{8} \right) \left(\frac{2}{3} - \frac{1}{3} \right) + \frac{1}{3}$ · U ~ U(0,1), a sample from a Virgon (0,1) Distribution constag juticises stocked interest of lestern of lestern the course commoder with the contract of them on them is a modern that course commoder them on a contract of the course of them on the charge a log(v) a log(1-v), (logistic Noise), a transformation of we that maps it to a range from - works - transforms Winform D into a Logistic D, which halps in approximating living choices in a most -> consues that somell differences in a leads to most charges in the final output 2, making the · log (d), a hoirable parameter controlling hour likely a weight is to be zeroch out (sparity)

- Daws the model to learn which cornections to remove discountly busing training a large of the weight is more likely to be prused, a somall of the weight is more likely to stay a B + Temperature Parameter (Softening the Decision) a scaling factor that controls the sharpness of a IP travilla - controls hour mostly or shorp the transition is from becoping a weight to priving it - a large B = smoother transitions (gradually learning sparsity), small B=) horder thresholding (place to) - 5() & some Activation : or to \$\frac{1}{24e^{-2i}}\$

I smoothly raps the transformed value into the range [891]

I ensures that the function is differentiable so gradient-based aptimization works . (3-8) 48 - Stating & Stilling, Acoles and shift the signed output - ordered that the mask is can be in the range [15] instal of just [0:1] -> Y (regative shift): prevent weights from being to close to zero buring having -> E (printine state): ensures that the purction can reach exactly I when reeded Charging & Retiscer C and I: 7 = Jamp (2,0,1) - o Birol step to Parce 7 to stay Return O and I I ever with smooth templanations or could nonetimes exceed these limits so we dip it -> ensures - Docharles likes of proper publishing most a Mark: a metrix M with could reflectly Return (8:1) on E0,15, applied Dement-vise to another terson X : X'= MOX - Mij = I: the concerporting element Xij is kept - Hijzo: the corresponding Doment Xiz is renord out (groved)
- OK Hij (I: represents a probability mode allowing gradient-based learning