

TP 3  
Techniques of AI [INFO-H-410]  
Correction  
v1.0.0

Source files, code templates and corrections related to practical sessions can be found on the UV or on github (<https://github.com/iridia-ulb/INFOH410>).

**Calculating the size of the hypothesis space**

**Question 1.** Suppose there are  $m$  attributes in a learning task and that every attribute  $i$  can take  $k_i$  possible values. What will be the size of the hypothesis space?

**Answer:** syntactically different:  $(k_i + 2)^m$  (+2 accounts for empty and don't care),  
semantically different:  $1 + (k_i + 1)^m$  (full empty attribute + attributes with don't care)

**Order of training instances**

**Question 2.** In candidate elimination, suppose you have  $n$  training instances  $T_1 \dots T_n$ . After the  $n_{th}$  training instance, candidate elimination learned the boundaries  $S$  and  $G$ . Will  $S$  and  $G$  differ or not when providing the training instances in reverse order:  $T_n \dots T_1$ ? Explain why (not).

**Answer:** The concept of version space aims at invariance to instance order, keeping not a single concept description but a set of possible descriptions that evolves as new instances are presented, so order does not matter.

**Question 3.** What is the version space while tracing the candidate elimination algorithm with the following examples?

$Architecture \in \{Gothic, Romanesque\}$

$Size \in \{Small, Large\}$

$Steeple \in \{Zero, One, Two\}$

Architecture	Size	Steeple	Classified ?
G	S	2	True
R	S	2	False
G	L	2	True
G	S	0	False
R	L	2	True

**Answer:**  $S_0 = \{\emptyset, \emptyset, \emptyset\}$  and  $G_0 = \{?, ?, ?\}$   
 $S_1 = \{G, S, 2\}$  and  $G_1 = \{?, ?, ?\}$   
 $S_2 = \{G, S, 2\}$  and  $G_2 = \{G, ?, ?\}$   
 $S_3 = \{G, ?, 2\}$  and  $G_3 = \{G, ?, ?\}$   
 $S_4 = \{G, ?, 2\}$  and  $S_4 = \{G, ?, 2\}$   
 $S_5 = G_5 = \emptyset$

### Rectangular version spaces and candidate elimination

**Question 4.** Consider the instance space consisting of integer points in the  $x, y$  plane and the set of hypotheses  $H$  consisting of rectangles. More precisely, hypotheses are of the form  $a \leq x \leq b, c \leq y \leq d$ , where  $a, b, c$  and  $d$  can be any integers. Consider the version space with respect to the set of positive (+) and negative (-) training examples:

$-(1, 3) \quad -(2, 6)$   
 $+(6, 5) \quad +(5, 3)$   
 $-(9, 4) \quad -(5, 1)$   
 $+(4, 4) \quad -(5, 8)$

- What is the  $S$  boundary of the version space in this case? Write a diagram with the training data and the  $S$  boundary.
- What is the  $G$  boundary of this version space? Draw that in the diagram as well.
- Use python to find the  $S$  and the  $G$  boundary and plot them (you can use the code template (see page 1)).
- Suppose the learner may suggest a new  $x, y$  instance and ask the trainer for its classification. Suggest a query guaranteed to reduce the size of the version space, regardless how the trainer classifies it. Suggest one that will not.
- Now assume you are the teacher, attempting to reach a particular target concept,  $3 \leq x \leq 5, 2 \leq y \leq 9$ . What is the smallest number of training examples you can provide so that the Candidate- Elimination algorithm will perfectly learn the concept?

**Answer:** (a)  $S = \{4, 6, 3, 5\}$   
 (b)  $G = \{3, 8, 2, 7\}$   
 (c) see github for implementation.  
 (d) To reduce the VS:  $(4, 6)$  or  $(7, 3)$ , instances with no impact on the VS:  $(5, 4)$  or  $(3, 9)$ .  
 (e) 6 points:  $+(3, 9), +(5, 2), -(2, 5), -(4, 1), -(6, 5), -(4, 10)$ .

### Finding a maximally specific consistent hypothesis

**Question 5.** Consider a concept learning problem in which each instance is a real number and in which each hypothesis is an interval over the reals. More precisely, each hypothesis in  $H$  is of the form:  $a < x < b$  as in  $4.5 < x < 6.1$ , meaning that all real numbers between 4.5 and 6.1 are classified as positive examples and all others are classified as negative examples.

- a) Explain informally why there cannot be a maximally specific consistent hypothesis for any set of positive training examples.
- b) Suggest a modification to the hypothesis representation so this will not happen.

**Answer:** (a)  $a < x < b$  is not a well defined hypothesis representation,  
(b)  $a \leq x \leq b$

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Found an error? Let us know: <https://github.com/iridia-ulb/INFOH410/issues>