

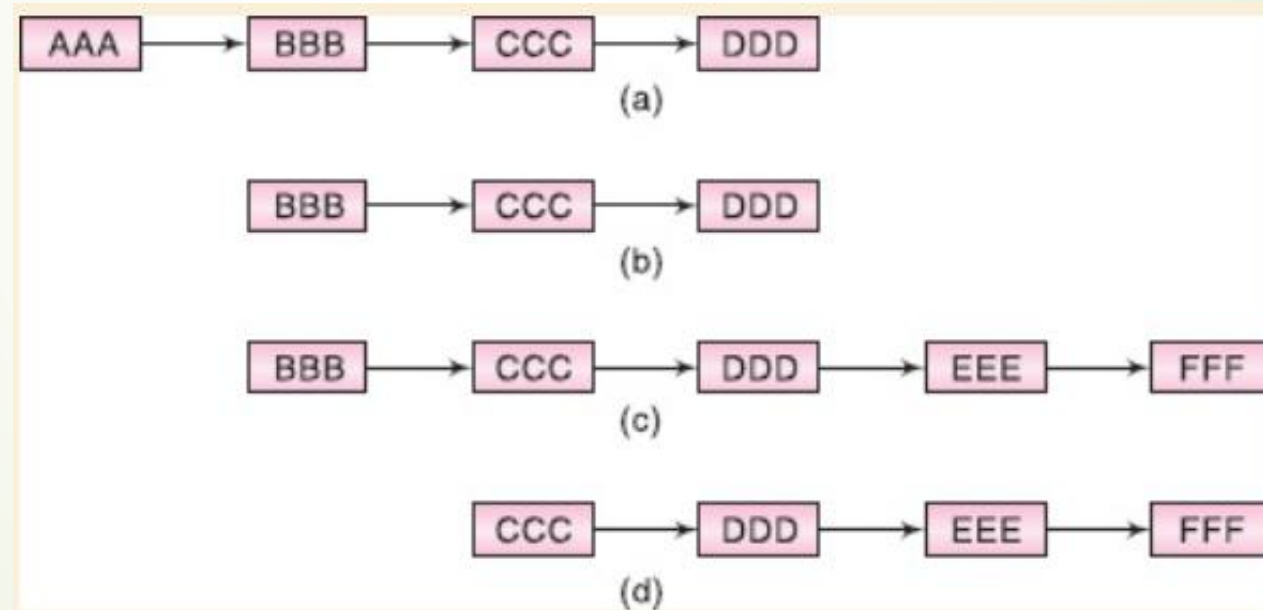
QUEUE

# Queue

- A queue is a linear list of elements in which
  - deletion can take place only at one end called Front, and
  - Insertion takes place only at other end called Rear

# Queue

- Queues are also known as First-In- First-Out (FIFO) list





# Queue

- Queue are represented in two-ways
  - Linear Array
  - One-way Linked List

# Array representation of Queue

- A queue is maintained by a
  - linear array QUEUE
  - Two pointer variable
    - FRONT : Containing the location of the front element of the queue
    - REAR : Containing
- FRONT == NULL indicates that the queue is empty

# Queue

FRONT: 1

REAR: 4

AA	BB	CC	DD				...	
1	2	3	4	5	6	7		N

**Delete an element**

FRONT: 2

REAR: 4

	BB	CC	DD				...	
1	2	3	4	5	6	7		N

Whenever an element is deleted from the queue, the value of FRONT is increased by 1

**FRONT = FRONT + 1**

# Queue

FRONT: 2

REAR: 4

	BB	CC	DD				...	
1	2	3	4	5	6	7		N

**Insert an element**

FRONT: 2

REAR: 5

	BB	CC	DD	EE			...	
1	2	3	4	5	6	7		N

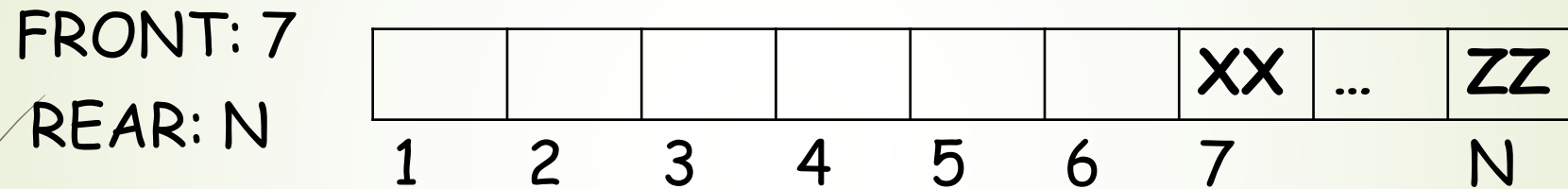
Whenever an element is inserted into the queue, the value of REAR is increased by 1

**REAR = REAR + 1**



# Queue

- REAR = N and Insert an element into queue



Move the entire queue to the beginning of the array

Change the FRONT and REAR accordingly

Insert the element

This procedure is too expensive



# Queue

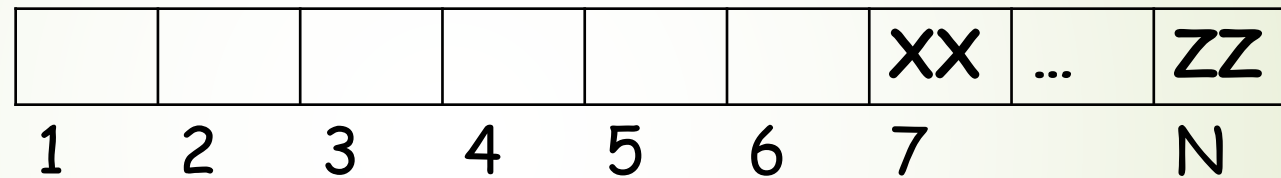
- Queue is assumed to be circular
- `QUEUE[1]` comes after `QUEUE[N]`
- Instead of increasing `REAR` to `N + 1`, we reset `REAR = 1` and then assign  
`QUEUE[REAR] = ITEM`

# Queue

- $\text{FRONT} = N$  and an element of QUEUE is Deleted

FRONT:  $N$

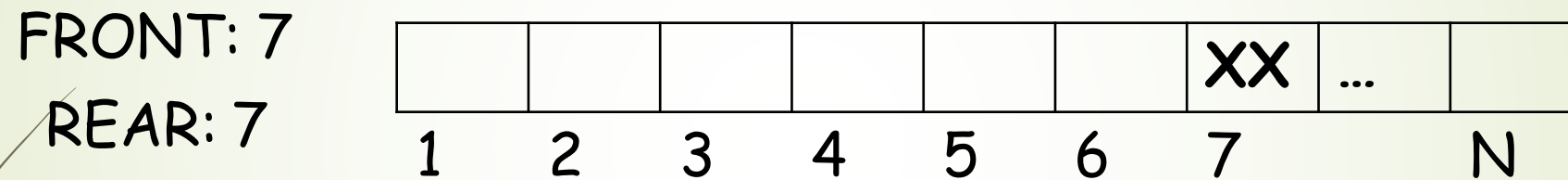
REAR:



We reset  $\text{FRONT} = 1$ , instead of increasing  $\text{FRONT}$  to  $N + 1$

# Queue

- QUEUE contain one element  
 $\text{FRONT} = \text{REAR} \neq \text{NULL}$



$\text{FRONT} = \text{NULL}$  and  $\text{REAR} = \text{NULL}$

# Queue

		QUEUE										
(a) Initially empty:	FRONT: 0 REAR: 0	<table><tr><td></td><td></td><td></td><td></td><td></td></tr><tr><td>1</td><td>2</td><td>3</td><td>4</td><td>5</td></tr></table>						1	2	3	4	5
1	2	3	4	5								
(b) A, B and then C inserted:	FRONT: 1 REAR: 3	<table><tr><td>A</td><td>B</td><td>C</td><td></td><td></td></tr></table>	A	B	C							
A	B	C										
(c) A deleted:	FRONT: 2 REAR: 3	<table><tr><td></td><td>B</td><td>C</td><td></td><td></td></tr></table>		B	C							
	B	C										
(d) D and then E inserted:	FRONT: 2 REAR: 5	<table><tr><td></td><td>B</td><td>C</td><td>D</td><td>E</td></tr></table>		B	C	D	E					
	B	C	D	E								
(e) B and C deleted:	FRONT: 4 REAR: 5	<table><tr><td></td><td></td><td></td><td>D</td><td>E</td></tr></table>				D	E					
			D	E								
(f) F Inserted:	FRONT: 4 REAR: 1	<table><tr><td>F</td><td></td><td></td><td>D</td><td>E</td></tr></table>	F			D	E					
F			D	E								
(g) D deleted:	FRONT: 5 REAR: 1	<table><tr><td>F</td><td></td><td></td><td></td><td>E</td></tr></table>	F				E					
F				E								
(h) G and then H inserted:	FRONT: 5 REAR: 3	<table><tr><td>F</td><td>G</td><td>H</td><td></td><td>E</td></tr></table>	F	G	H		E					
F	G	H		E								
(i) E deleted:	FRONT: 1 REAR: 3	<table><tr><td>F</td><td>G</td><td>H</td><td></td><td></td></tr></table>	F	G	H							
F	G	H										
(j) F deleted:	FRONT: 2 REAR: 3	<table><tr><td></td><td>G</td><td>H</td><td></td><td></td></tr></table>		G	H							
	G	H										
(k) K inserted:	FRONT: 2 REAR: 4	<table><tr><td></td><td>G</td><td>H</td><td>K</td><td></td></tr></table>		G	H	K						
	G	H	K									
(l) G and H deleted:	FRONT: 4 REAR: 4	<table><tr><td></td><td></td><td></td><td>K</td><td></td></tr></table>				K						
			K									
(m) K deleted, QUEUE empty:	FRONT: 0 REAR: 0	<table><tr><td></td><td></td><td></td><td></td><td></td></tr></table>										

# Queue: overflow

FRONT: 1

REAR: N

AA	BB	CC	DD	EE	FF	XX	...	ZZ
1	2	3	4	5	6	7		N

FRONT = 1 and REAR = N

FRONT: 7

REAR: 6

AA	BB	CC	DD	EE	FF	XX	...	ZZ
1	2	3	4	5	6	7		N

FRONT = REAR + 1

# Algorithm to Insert in Q

- 1 If  $\text{FRONT} = 1$  **and**  $\text{REAR} = N$  **or** if  $\text{FRONT} = \text{REAR} + 1$  then Print: Overflow and Exit
- 2 If  $\text{FRONT} = \text{NULL}$  **then**  
    Set  $\text{FRONT} = 1$  and  $\text{REAR} = 1$   
    Else If  $\text{REAR} = N$  then  
        Set  $\text{REAR} = 1$   
    Else  
        Set  $\text{REAR} = \text{REAR} + 1$
- 3 Set  $\text{QUEUE}[\text{REAR}] = \text{ITEM}$
- 4 Exit


# Algorithm to Delete from Q

- [1] If FRONT = NULL then Print: Underflow and Exit
- [2] Set ITEM = QUEUE[FRONT]
- 3     If FRONT = REAR **then**  
        Set FRONT = NULL and REAR = NULL  
    Else If FRONT = N then  
        Set FRONT = 1  
    Else  
        Set FRONT = FRONT + 1
- 4     Exit



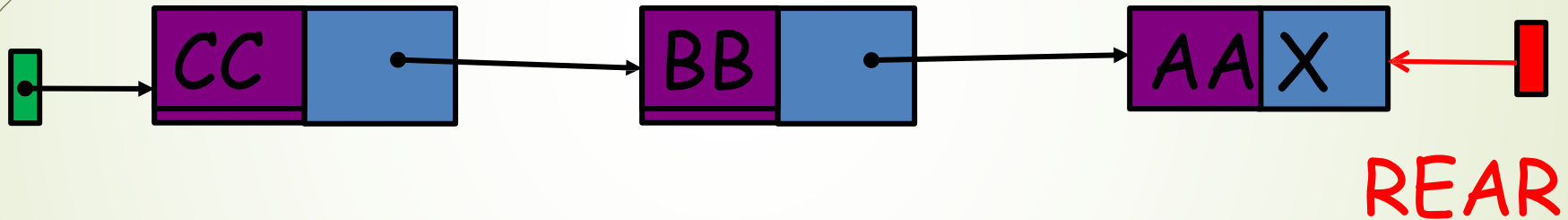


# Linked List Representation of Queue

- A linked queue is a queue implemented as linked list with two pointer variable FRONT and REAR pointing to the nodes which is in the FRONT and REAR of the queue
- 

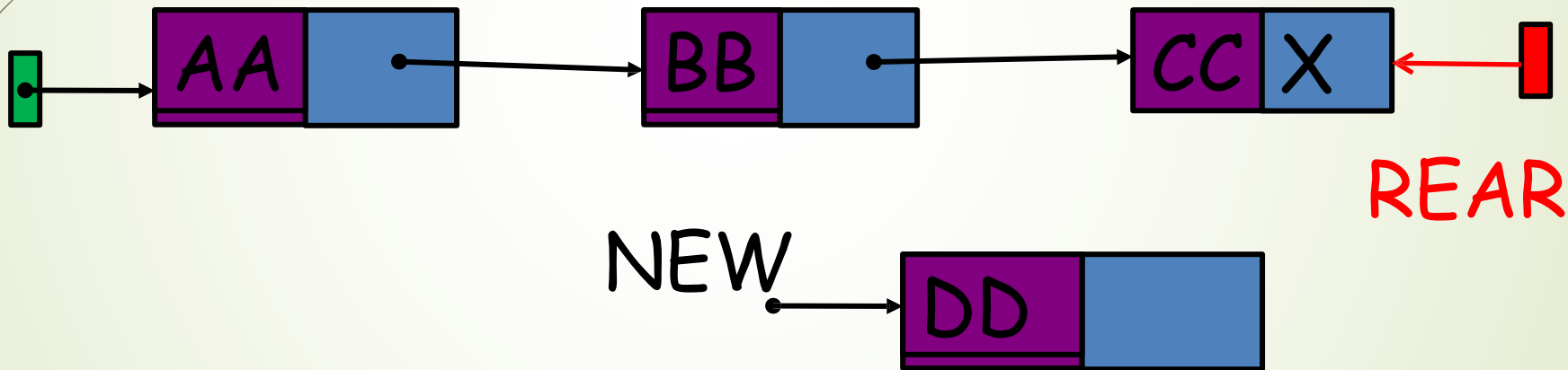
# Linked List Representation of Queue

FRONT



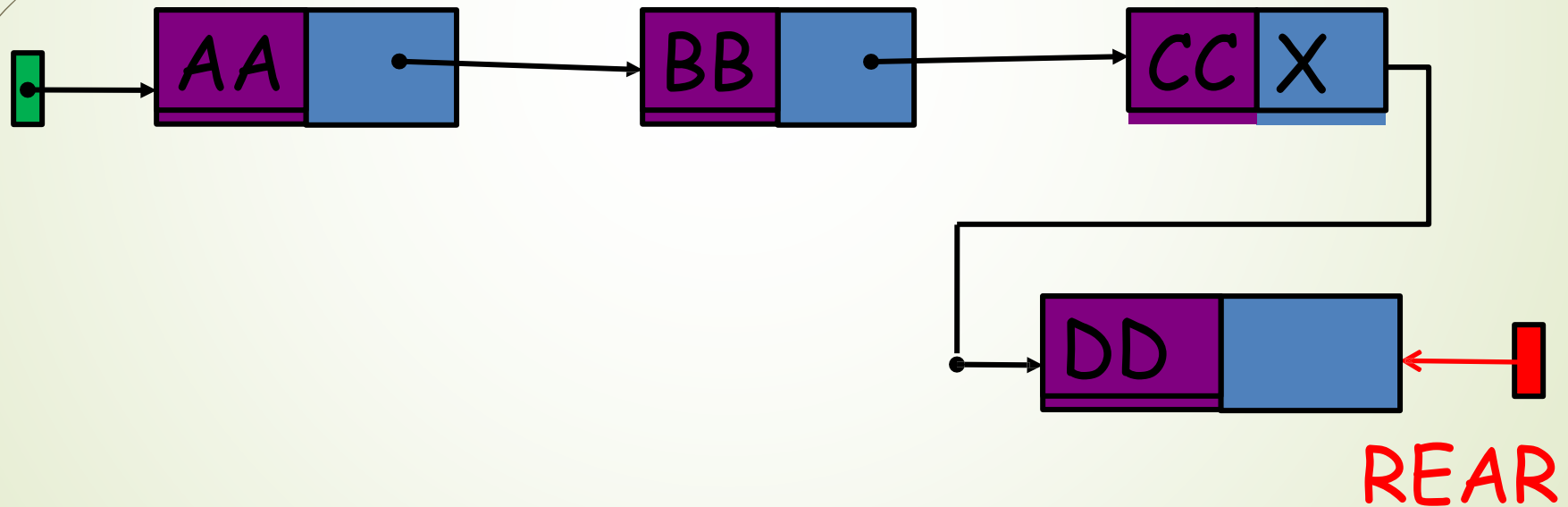
# Insertion in a Queue

FRONT



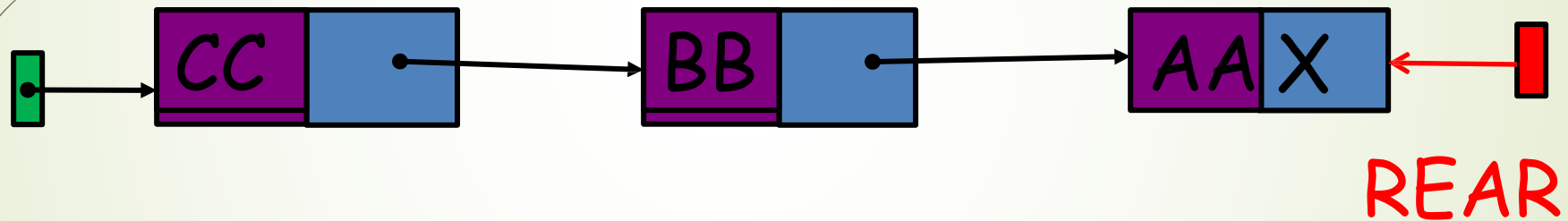
# Insertion in a Queue

FRONT



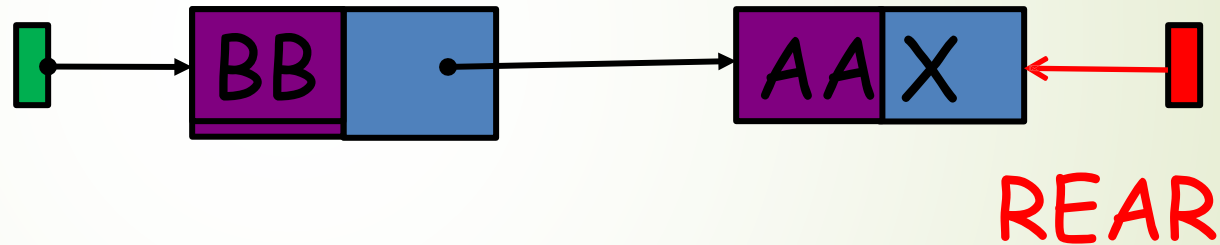
# Delete from a Queue

FRONT




# Delete from a Queue

FRONT





# Linked Queue

- No need to check for overflow condition during insertion
  - No need to view it as circular for efficient management of space
- 



## Insertion

- 1     $NEW \rightarrow INFO = ITEM$   
      $NEW \rightarrow LINK = NULL$
- 2    If  $(FRONT = NULL)$  then  
          $FRONT = REAR = NULL$   
     else  
         Set  $REAR \rightarrow LINK = NEW$   
          $REAR = NEW$
- 3    Exit

# Insertion

LINKQ\_INSERT(INFO, LINK, FRONT, REAR, AVAIL, ITEM)

1. [Available space?] If AVAIL = NULL, then Write

OVERFLOW and Exit

2. [Remove first node from AVAIL list]

Set NEW := AVAIL and AVAIL := LINK[AVAIL]

3. Set INFO[NEW] := ITEM and LINK[NEW] = NULL

[Copies ITEM into new node]

4. If (FRONT = NULL) then FRONT = REAR = NEW

[If Q is empty then ITEM is the first element in the queue Q]

else set LINK[REAR] := NEW and REAR = NEW

[REAR points to the new node appended to  
the end of the list]

5. Exit.

# Deletion

- 1 If (FRONT = NULL) then  
Print: Underflow, and Exit
- 2 FRONT = FRONT -> LINK
- 3 Exit


# Deletion

LINKQ\_DELETE (INFO, LINK, FRONT, REAR, AVAIL, ITEM)

1. [Linked queue empty?] if (FRONT = NULL) then Write: UNDERFLOW and Exit
2. Set TEMP = FRONT [If linked queue is nonempty, remember FRONT in a temporary variable TEMP]
3. ITEM = INFO (TEMP)
4. FRONT = LINK (TEMP) [Reset FRONT to point to the next element in the queue]
5. LINK(TEMP) = AVAIL and AVAIL = TEMP [return the deleted node TEMP to the AVAIL list]
6. Exit.



# Deque

- A deque is a linear list in which elements can be added or removed at either end but not in the middle
  - Deque is implemented by a circular array `DEQUEUE` with pointers **LEFT** and **RIGHT** which points to the two end of the deque
- 

## Deque

- LEFT = NULL indicate deque is empty

LEFT: 4

RIGHT: 7

			AA	BB	CC	DD	
1	2	3	4	5	6	7	8

LEFT: 7

RIGHT: 2

yy	zz					ww	xx
1	2	3	4	5	6	7	8



# Variation of deque

- There are two variation of deque
  - 1 Input-restricted queue: Deque which allows insertions at only one end of the list but allows deletion at both ends of the list
  - 2 Output-restricted queue: Deque which allows deletion at only one end of the list but allows insertion at both ends of the list



# Deque

LEFT: 2

RIGHT: 4

	<b>A</b>	<b>C</b>	<b>D</b>		
1	2	3	4	5	6

F is added to the right

LEFT: 2

RIGHT: 5

	<b>A</b>	<b>C</b>	<b>D</b>	<b>F</b>	
1	2	3	4	5	6

# Deque

LEFT: 2

RIGHT: 5

	<b>A</b>	<b>C</b>	<b>D</b>	<b>F</b>	
1	2	3	4	5	6

Two Letters on right is deleted

LEFT: 2

RIGHT: 3

	<b>A</b>	<b>C</b>			
1	2	3	4	5	6

# Deque

LEFT: 2

RIGHT: 3

	<b>A</b>	<b>C</b>			
1	2	3	4	5	6

K, L and M are added to the Left

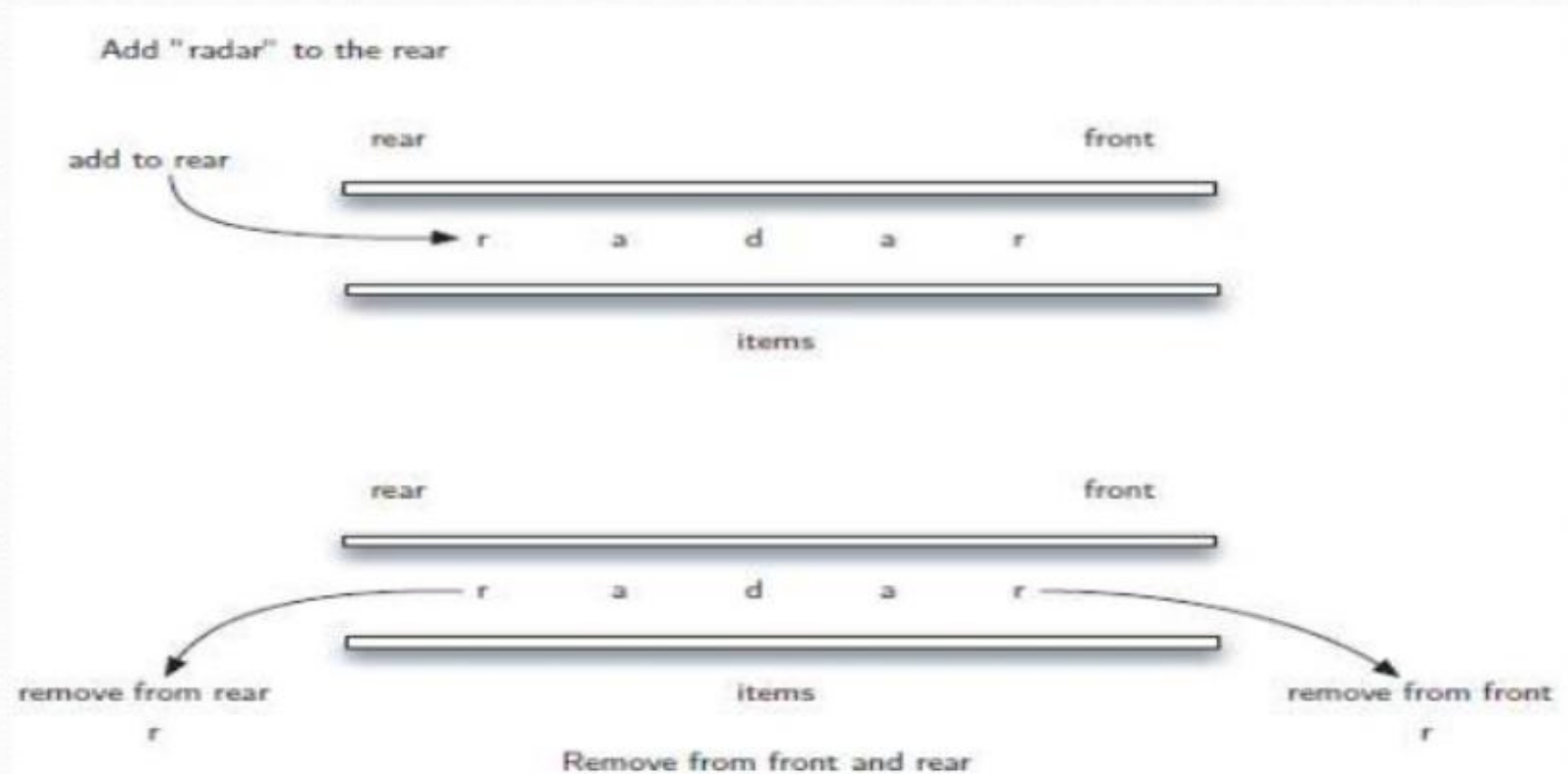
LEFT: 5

RIGHT: 3

<b>K</b>	<b>A</b>	<b>C</b>		<b>M</b>	<b>L</b>
1	2	3	4	5	6

# Applications of deque

## Palindrome-checker






# Applications of deque

## **A-Steal job scheduling algorithm**

- The A-Steal algorithm implements task scheduling for several processors(multiprocessor scheduling).
- The processor gets the first element from the deque.
- When one of the processor completes execution of its own threads it can steal a thread from another processor.
- It gets the last element from the deque of another processor and executes it.

# Priority Queue

- A priority queue is a collection of elements such that each element has been assigned a priority and such that the order in which elements are deleted and processed comes from the following rules:
  - 1 Elements of higher priority are processed before any elements of lower priority
  - 2 Two elements with the same priority are processed according to the order in which they were added to the queue



# Two types

- Ascending priority queue
  - only lowest priority element can be removed
- Descending priority queue
  - only highest priority element can be removed





# Priority

- Intrinsic: based on one or several fields
  - Integer or alphabetical order
  - Ex: telephone directory ordered by last name
- External priority
  - An external value defines the priority of the element
- If time of insertion is used as priority of element
  - A stack may be viewed as descending priority queue whose element are ordered by time of insertion
  - A queue may be viewed as ascending priority queue whose element are ordered by time of insertion



# Representation of Priority Queue

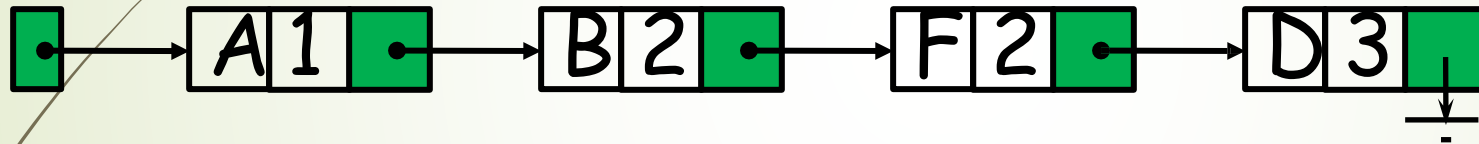
- 1 One-way List
  - a) Ordered
  - b) unordered
- 2 Array
  - a) Single
    - i. Ordered
    - ii. unordered
  - b) Multiple

# One-Way (ordered) List Representation of a Priority Queue

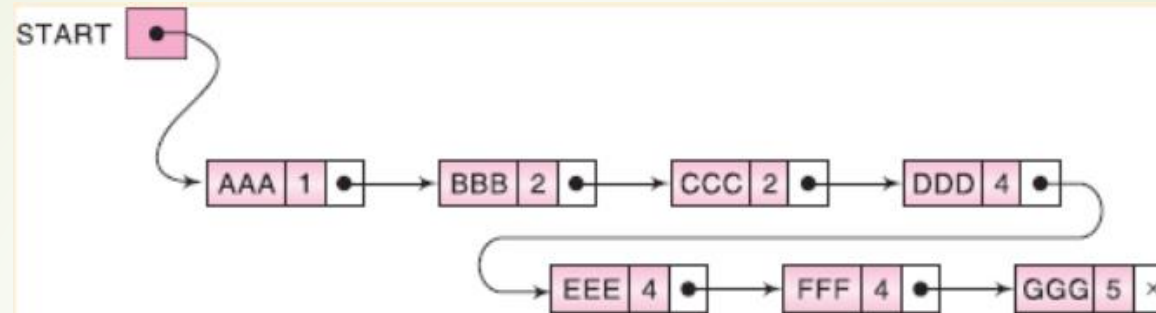
- 1 Each node in the list will contain three items of information: **an information field INFO, a priority number PRN, and a link number LINK**
- 2 A node X precedes a node Y in the list
  - (a) when X has **higher priority** than Y or
  - (b) when both have same priority but X was **added to the list before** Y

# Priority Queue

Head



# Priority Queue



	INFO	PRN	LINK
1	BBB	2	6
2			7
3	DDD	4	4
4	EEE	4	9
5	AAA	1	1
6	CCC	2	3
7			10
8	GGG	5	0
9	FFF	4	8
10			11
11			12
12			0


START 5

AVAIL 2


# Insertion and Deletion

- Deletion : Delete the first node in the list.
- Insertion: Find the location of Insertion and add an ITEM with priority number N
  - a. Traverse the list until finding a node X whose priority exceeds N. Insert ITEM in front of node X
  - b. If no such node is found, insert ITEM as the last element of the list





## (Multiple) Array representation of Priority Queue

- Multiple arrays are used and each array is maintained as circular queue
  - Separate queue for each level of priority
  - Each queue will appear in its own circular array and must have its own pair of pointers, FRONT and REAR
  - If each queue is given the same amount space then a 2D queue can be used
- 



FRONT

REAR

QUEUE

1	2	2
2	1	3
3	0	0
4	5	1
5	4	4

	1	2	3	4	5
1		AA			
2	BB	CC	DD		
3					
4	FF			DD	EE
5			GG		



# Deletion Algorithm for Ascending Queue

- 1 Find the smallest  $K$  such that  $FRONT[K] \neq NULL$
- 2 Delete and process the front element in row  $K$  of  $QUEUE$
- 3 Exit



# Insertion Algorithm

Insert a new element ITEM with priority M

1 Insert ITEM as the rear element in row M of QUEUE

2 Exit