this is how I would define higher order regressions

b0= baseline

E= is summatory of the individual variables

PI= is the interaction of the order in question

and max subset is self explanatory although not math precise

e= represents the noise

n is the order from 3 to whatever

for the pairs: