

# PERUI: A General Framework of Reduced Variance Stochastic Gradient Gradient and the Hybrid Implementation

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**Algorithm 1** The general framework of variance reduced SGD: PERUI

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**Require:**  $\omega^0 \in \mathbb{R}^d$ .  $\forall i \in [n]$ , and  $[n]$  represents  $\{1, 2, \dots, n\}$ .  
1: **Probability:**  $[i_t] \leftarrow \mathcal{P}([n])$  where  $i_t \in \{1, 2, \dots, n\}$ .  $t$  is a positive integer;  
2: **Epoch:** the sequence of the epoch size  $\{m^0, m^1, \dots, m^S\} \leftarrow \mathcal{E}([i_t])$ ;  
3: **for**  $s = 0, 1, 2, \dots, S$  **do**  
4:    $\omega_0^s = \tilde{\omega}^s$ ;  
5:    $g = \frac{1}{n} \sum_i 1^n \nabla f_i(\tilde{\omega}^s)$ ;  
6:   **for**  $t < m^s$  **do**  
7:     **Reduced variance:**  $v = \mathcal{R}(\nabla f_{i_t}(\omega_{i_t}^t) - \nabla f_{i_t}(\tilde{\omega}^s))$ ;  
8:      $\gamma_t^s = v + g$ ;  
9:     **Update:**  $\omega_{t+1}^s = \mathcal{U}(\eta_t, \omega_t^s, \gamma_t^s)$ ;  
      **Identification:**  $\tilde{\omega}^{s+1} \leftarrow \mathcal{I}([\omega_j^s])$  with  $j \in \{1, 2, \dots, m^s\}$ ;  
**return**  $\tilde{\omega}^S$ .

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**Introduction**

**Related work**

**The general hybrid framework of SGD**

**Convergence analysis**

**Optimization**

**Constant learning rate with an acceleration factor**

**Adaptive update sharing strategy**

**Discussion**

**Performance evaluation**

**Convergence**

**Speed up**

**Wait time**

**Parallel threads**

**Conclusion**

**Acknowledgements**

**Abstract**