

1 10.a

$$\frac{x^2 + x - 6}{x - 2} = x + 3$$

This equation is false if $x = 2$
Singularity may happen in type

$$\frac{c}{0} \quad ; \quad c \in \mathbb{R}$$

2 10.b

$$\lim_{x \rightarrow 2} \frac{x^2 + x - 6}{x - 2} = \lim_{x \rightarrow 2} x + 3$$

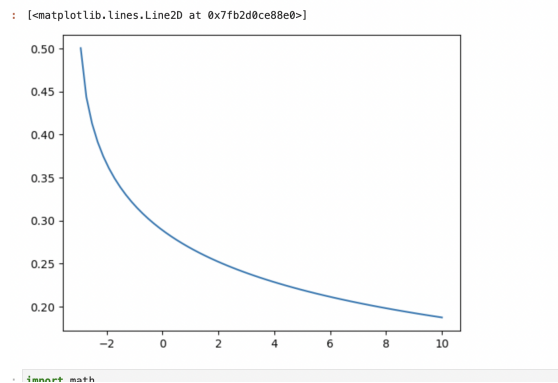
Is corrected because when x is approaching to 2 means it's not equals 2 so it's not make any singularity

$$\lim_{x \rightarrow 2} \frac{(x+3)\cancel{(x-2)}}{\cancel{(x-2)}} = \lim_{x \rightarrow 2} (x+3)$$

$$\lim_{x \rightarrow 2} (x+3) = \lim_{x \rightarrow 2} x + 3$$

$$5 = 5$$

3 36.a



$$\lim_{x \rightarrow 0} f(x) = 0$$

4 36.b

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def f(x):
    y = (sq(3 + x) - sq(3)) / x
    return y

for element in [0.1, 0.01, 0.001, 0.0001]:
    e = element
    a, b = f(-e), f(e)
    a, b = round(a, 4), round(b, 4)
    print(f"e : {e} \t f(-e) = {a}, f(e) = {b}")
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e : 0.1          f(-e) = 0.2911, f(e) = 0.2863
e : 0.01         f(-e) = 0.2889, f(e) = 0.2884
e : 0.001        f(-e) = 0.2887, f(e) = 0.2887
e : 0.0001       f(-e) = 0.2887, f(e) = 0.2887
```

| :

from table we can see the pattern that if e is approach to 0 then limit value is almost the same at 0.2887

5 36.c

consider $f(x)$

$$\begin{aligned}
 &= \frac{(\sqrt{3+x} - \sqrt{3})(\sqrt{3+x} + \sqrt{3})}{(x)(\sqrt{3+x} + \sqrt{3})} \\
 &= \frac{(3+x) - 3}{(x)(\sqrt{3+x} + \sqrt{3})} \\
 &= \frac{x}{(x)(\sqrt{3+x} + \sqrt{3})} \\
 &= \frac{1}{(\sqrt{3+x} + \sqrt{3})} \quad (1)
 \end{aligned}$$

$$\begin{aligned}
 \lim_{x \rightarrow 0} f(x) &= \frac{1}{(\sqrt{3+0} + \sqrt{3})} \\
 &= \frac{1}{(\sqrt{3} + \sqrt{3})} \\
 &= \frac{1}{2\sqrt{3}} \\
 &\approx 0.2887
 \end{aligned} \tag{2}$$