

When is TSLS actually LATE?

When is TSLS weakly causal?

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1.1 The Common TSLS Recipe

Selection on unobservables

We have an outcome variable Y , a discrete, ordered treatment $T \in \mathcal{T} = \{t_0, t_1, \dots, t_J\}$, a discrete instrument $Z \in \mathcal{Z}$.

First Stage:

$$T = \alpha_1 + \beta_1 Z + v$$

Second Stage:

$$Y = \alpha_2 + \beta_{\text{tsls}} \hat{T} + \varepsilon$$

We assume:

- Relevance, i.e. $\text{Cov}(Z, T) \neq 0$,
- Exclusion, i.e. $\text{Cov}(Z, \varepsilon) = 0$.
- Monotonicity, i.e. no defiers.

$\beta_{\text{tsls}} = \frac{\text{Cov}(Y, Z)}{\text{Cov}(T, Z)}$ identifies LATE of compliers. There is nothing wrong with this classical setup.

1.1 The Common TSLS Recipe

Selection on unobservables & observables

We have $Y, T \in \mathcal{T} = \{t_0, t_1, \dots, t_J\}$, $Z \in \mathcal{Z}$, and an observed covariate matrix X .

First Stage:

$$T = \alpha_1 + \beta_1 Z + \gamma_1 X + v$$

Second Stage:

$$Y = \alpha_2 + \beta_{\text{tsls}} \hat{T} + \gamma_2 X + \varepsilon$$

We additionally assume **exogeneity (EX)**: conditional on X , the assignment of Z is independent of both the potential treatment and potential outcomes, i.e. $(\{T(z)\}_{z \in \mathcal{Z}}, \{Y(t)\}_{t \in \mathcal{T}}) \perp Z \mid X$.

Typically, β_{tsls} does not have a causal interpretation and is not LATE.

1.1 The Common TSLS Recipe

Angrist and Pischke, 2009:

“TSLS with covariates produces an average of covariate-specific LATEs.” – under saturated covariates **and** instrument (Saturate and weight, SW).

IV Paper (n=122)	N	%	TSLS + Covariates (n=99)	N
Used TSLS	112	92	Followed SW	1
TSLS + Covariates	99	81	Saturated in covariates	4
TSLS + Covariates, as LATE	30	25	Not saturated in covariates	94

General critiques on IV-LATE: (Robins and Greenland, 1996; Heckman, 1997; Angrist and Imbens, 1999; Deaton, 2010; Imbens, 2010; Swanson and Hernan, 2014)

- complier-specific, misleading for population analysis;
- vulnerable to heterogeneous treatment effects;
- assumptions like EX are hard to empirically justify.

1.2 Motivation

Def. Saturate and weight (SW):

Given a treatment variable T , let X take values in $\mathcal{X} = \{x_1, \dots, x_L\}$, and Z in $\mathcal{Z} = \{z_1, \dots, z_K\}$. The TSLS model takes C as covariates and I as instrument, where:

- $C = [1, \mathbb{I}(X = x_l) : l = 2, \dots, L]'$, i.e., one coefficient for each possible x on its entire support;
- $I = [\mathbb{I}(Z = z_k), \mathbb{I}(Z = z_k)\mathbb{I}(X = x_l) : l = 2, \dots, L; k = 2, \dots, K]'$, i.e. the instrument vector consists of each Z value and the interaction term between each specific z, x on their supports.

SW is **not possible** if any of the variables takes continuous values, and is rarely feasible for empirical studies that include many covariates.

SW may also incur **many instruments bias** due to the excessive instruments generated from $\mathbb{I}(Z = z_k)\mathbb{I}(X = x_l)$, biasing it towards the OLS estimator.

1.2 Motivation

Practical relevance:

- TSLS with covariates is popular, with β_{tsls} often interpreted as LATE of compliers;
- SW is a highly theoretical setup, and is not favoured by empirical studies;
- Without SW, does the LATE interpretation still apply?

Unsolved problem:

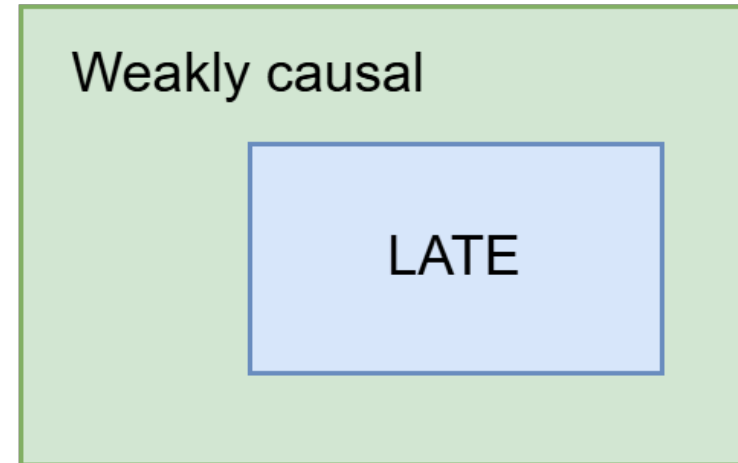
- Angrist and Krueger, 1999: [With IV estimates in models with unsaturated covariates], it seems reasonable to assume that some sort of approximate weighted average is being generated, but we are unaware of a precise causal interpretation that fits all cases.

Related effort:

- Słoczyński, 2020, 2024: focuses on incorrect monotonicity and thus the impact of negative weights.
- Evdokimov & Kolesár, 2018: on treatment effect heterogeneity, and sufficient conditions for LATE.
- Abadie, 2003: theoretical refinement under constant treatment effect assumption.

1.2 Motivation

$$\beta_{\text{tsls}} \notin$$



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2 Binary T and Z

How education affects income? From Card (1995), adapted.

- $N = 3010$ individuals
- Y : continuous, log hourly wage
- T : binary, received education > 12 yrs
- Z : binary, presence of college nearby
- X : 4 binary covariates: work experience > 8 yrs, 3 indicators for race and location of residence.

We assume:

1. Exogeneity: $Z \perp (Y(0), Y(1), T(1), T(0)) \mid X$;
2. Monotonicity: $\mathbb{P}[T(1) \geq T(0)] = 1$ (no defiers).

2 Binary T and Z

Since T, Z, X are binary, we can do SW.

```

1 # OLS
2 lm(Y ~ D + X)
3 # IV without saturation:
4 ivreg(Y ~ X + D | X + Z)
5 # IV with saturated covariates:
6 Z_int <- cbind(Z, Z * X1, Z * X2, Z * X3, Z * X4, Z *
7 X1 * X2, Z * X1 * X3, Z * X1 * X4, Z * X2 * X3, Z *
X2 * X4, Z * X3 * X4, Z * X1 * X2 * X3, Z * X1 * X2 *
X4, Z * X1 * X3 * X4, Z * X2 * X3 * X4, Z * X1 * X2 *
X3 * X4)
7 ivreg(Y ~ X1*X2*X3*X4 + D | X1*X2*X3*X4 + Z_int)

```

Method	Coefficient on D	SE
OLS	0.185 ***	0.016
TSLs, no covar.	1.317 ***	0.232
TSLs, unsaturated	0.778 *	0.353
TSLs, SW	0.412 *	0.179

RESET-test on `lm(Z~X)`: $p = 0.000$, i.e. no rich covariates.

Overestimated causal effect: $\frac{\beta_{\text{tsls}} - \beta_{\text{sw}}}{\beta_{\text{tsls}}} = 47\%$?

Overestimated selection bias: $\left| \frac{\beta_{\text{tsls}} - \beta_{\text{sw}}}{\beta_{\text{ols}} - \beta_{\text{sw}}} \right| = 161\%$?

Consider many instruments bias.

2 Binary T and Z

We divide the population into groups according to potential treatment:

$$G := (T(0), T(1)) = \begin{cases} (0, 1) =: \text{CP} \\ (1, 1) =: \text{AT} \in \mathcal{G} \\ (0, 0) =: \text{NT} \end{cases}$$

Denote the conditional average treatment effect as $\text{CATE}(g, x) := \mathbb{E}[Y(1) - Y(0) \mid G = g, X = x]$.

We introduce one of the key findings, [Prop.2](#), in a minimalist style.

Proposition 2. Assume potential outcome is linearly predicted by X .

Then, the β_{tsls} can be decomposed into the sum of weighted average of CATEs of CP, AT, and NT. That is:

$$\beta_{\text{tsls}} = \sum_{g \in \mathcal{G}} \mathbb{E}[\omega(g, x) \cdot \text{CATE}(g, x)]$$

where for AT and NT, $\omega(g, x) = \mathbb{E}[\tilde{Z}|X] \mathbb{P}[G = g|X] \mathbb{E}[\tilde{Z}T]^{-1}$, while $\omega(\text{CP}, x) > 0$.

2 Binary T and Z

- The signs of weights on AT and NT are determined by $\mathbb{E}[\tilde{Z}|X]$.
- \tilde{Z} is the residuals from the regression $Z \sim X$.
- If and only if $\mathbb{E}[\tilde{Z}|X] = 0$, a condition defined as having **rich covariates**, β_{tsls} only reflects the positively weighted treatment effects on compliers, and is thus LATE.
- If without rich covariates, β_{tsls} reflects all three groups. As $\mathbb{E}[\tilde{Z}|X]$ is possible to take negative values for any data, AT and NT can be negatively weighted, thus biasing the direction of treatment effect interpretation.
- Negative weighting on some treatment groups is a violation to what the authors define as **weakly causal**.

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3 What is Weak Causality?

Assume throughout that we have $T \in \{0, 1\}$, $Z \in \{0, 1\}$.

Def. Weakly causal (WC): an estimand β is WC iff :

$\forall g \in \mathcal{G}$, and every $x \in \mathcal{X}$, if $\text{CATE}(g, x) \geq 0$, then $\beta \geq 0$

$\forall g \in \mathcal{G}$, and every $x \in \mathcal{X}$, if $\text{CATE}(g, x) \leq 0$, then $\beta \leq 0$

Intuitively, if taking the treatment always gives higher potential outcome for every group, then the estimator should also be positive. A WC estimator is not systematically wrong in its direction.

Under this weak criterion, the trivial estimand $\beta = 0$ is also WC.

We want to further investigate some parametric or semi-parametric settings that translate into weak causality.

3 What is Weak Causality?

The decomposition in [Prop.2](#) can be rewritten with a different definition of weights as:

Proposition 3.

$$\beta = \sum_{g,x} \overbrace{\omega_0(g,x) \mathbb{E}[Y(0)|g,x]}^{\text{baseline level w/o treatment}} + \sum_{g,x} \overbrace{\omega_1(g,x) \text{CATE}(g,x)}^{\text{diff. in outcome w. treatment}}$$

where $\omega_0(g,x) = \mathbb{E}[\tilde{Z}T]^{-1} \mathbb{E}[\tilde{Z}|g,x] \mathbb{P}(g,x)$, and $\omega_1(g,x) = \mathbb{E}[\tilde{Z}T]^{-1} \mathbb{E}[\mathbb{I}(T=1)\tilde{Z}|g,x] \mathbb{P}(g,x)$

Proposition 4. Given **BF**, **EX**, and suppose further **GR**, then β is WC iff

1. (Non-negative weights): $\forall g, x, \omega_1(g, x) \geq 0$;
2. (Baseline irrelevance): $\forall g, x, \omega_0(g, x) = 0$.

Intuitively,

- Each choice group is strictly non-negatively weighted;
- The baseline level of outcome where the treatment is absent does not flow into β .

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4 When do we have WC?

For binary T and Z .

Assumption EX: $Z \perp (Y(0), Y(1), T(1), T(0)) \mid X$

Def. Rich covariates (RC): Let $\mathbb{L}[Z|X = x]$ be the population fitted values at $X = x$ from the linear regression $Z \sim X$. An IV specification has RC if:

$$\forall x \in \mathcal{X}, \mathbb{L}[Z|X = x] = \mathbb{E}[Z|X = x] \Leftrightarrow \forall x \in \mathcal{X}, \mathbb{E}[\tilde{Z}|X] = 0$$

Saturation guarantees **RC**. If we have **RC** without saturating, it's called “correctly specified”.

Assumption MN: Monotonicity. $\forall x \in \mathcal{X}, \mathbb{P}[T(0) \leq T(1) \mid X = x] = 1$.

Intuitively, receiving the instrument does not decrease potential treatment, for all x .¹

¹Strong monotonicity. For results under weaker restrictions see Blandhol et al. 2022 (pre-revision).

4 When do we have WC?

Theorem 1. Suppose **EX** and **MN** are satisfied, then β_{tsls} is WC if and only if **RC**.

Intuitively, **Th.1** states that without **RC**, then baseline-irrelevance in **Prop.4 & 5** does not hold, and the estimator is not WC.

Recall **baseline irrelevance**, which requires:

$$\forall g, x, \omega_0(g, x) = \mathbb{E}[\tilde{Z}T]^{-1} \mathbb{E}[\tilde{Z}|G = g, X = x] \mathbb{P}(g, x) = 0$$

From **EX**, we have $\tilde{Z} \perp G \mid X$. Therefore, $\mathbb{E}[\tilde{Z}|G = g, X = x] = \mathbb{E}[\tilde{Z}|X = x]$. With $\mathbb{P}(g, x) > 0$, this holds iff $\mathbb{E}[\tilde{Z}|X = x] = 0$, i.e. **RC**.

The \tilde{Z} problem stems from the practice of interpreting the linear TSLS estimator through yet a nonparametric setup. The linear-regression-based TSLS was meant to serve linear IV models.

4 When do we have WC?

If **MN** fails, **RC** does not imply an WC estimator¹. We have to additionally restrict treatment effect homogeneity.

Assumption CLE: constant, linear effects. Order T into $\{t_0, t_1, \dots, t_J\}$. There exists an $\delta \in \mathbb{R}$, such that $\mathbb{E}[Y(t_j) - Y(t_{j-1}) | g, x] = \delta(t_j - t_{j-1})$ for every $j \geq 1, g \in \mathcal{G}, x \in \mathcal{X}$.

Intuitively, the mean difference in potential outcome is linearly proportional to the difference in treatment levels, for all groups and all x .

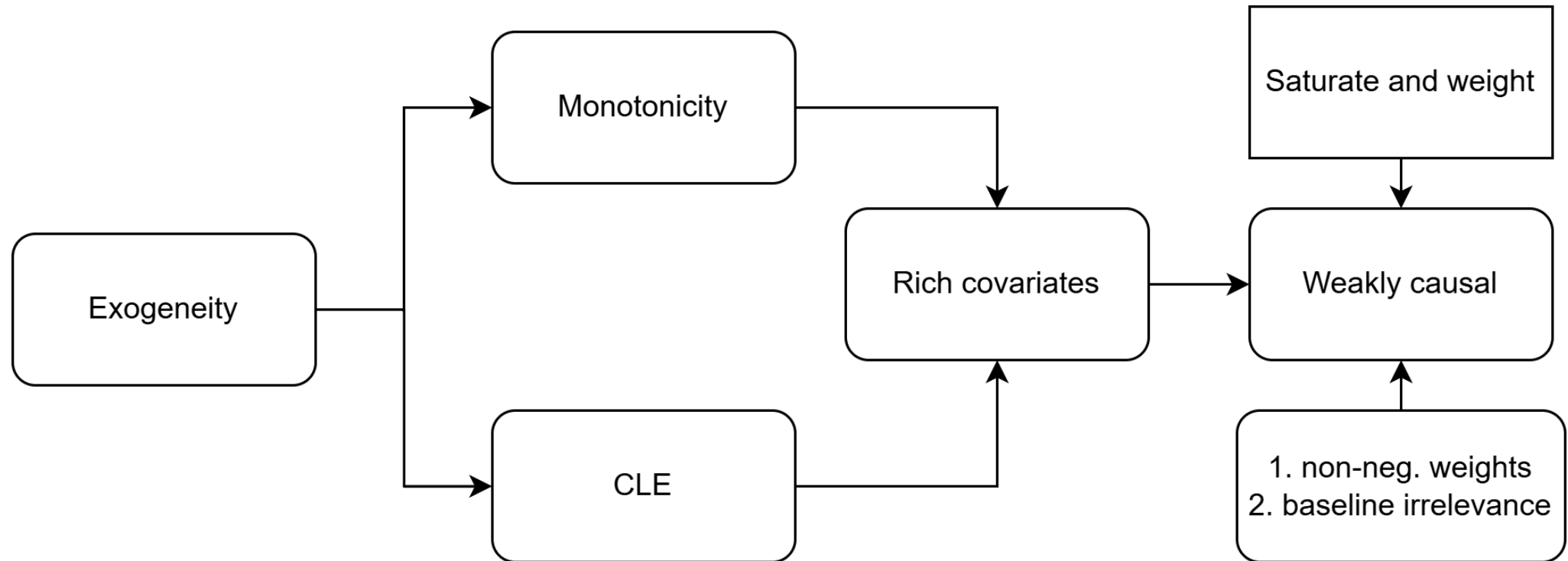
For binary T, Z , this simplifies to $\forall g, x, \text{CATE}(g, x) = \delta$.

Proposition 5. Suppose **EX** and **CLE** are satisfied, then β_{tsls} is WC iff **RC**.

¹Suggested reading: Słoczyński 2024, When Should We (Not) Interpret Linear IV Estimands as LATE?

4 When do we have WC?

Wrap-up:



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5.1 The New Recipe

1. If covariates are not essential for justifying instrument exogeneity, then do TSLS without covariates.
2. If covariates need to be included, think twice on including **which** covariates. The more included, the more likely that the specification is not rich in covariates.
3. Use RESET-test (Ramsey, 1969) **lmtest::resettest()** to examine covariate richness.
4. In general, the linear TSLS estimator can be complemented with:
 - DDML-PLIV, which produces $\beta_{\text{pliv}} \approx \beta_{\text{rich}}$.
 - If Z, T are binary, DDML-LATE identifies LATE of compliers.

5.2 Intuition

We have discussed that \tilde{Z} became a problem because we tried to impose the linear IV model onto an unknown data structure which, in practice, is hardly linear.

Instead, we consider the following **partially linear IV model (PLIV)**:

$$Y = \beta_{\text{pliv}}T + f(X) + \varepsilon, \quad \mathbb{E}[\varepsilon|X, Z] = 0$$

$$Z = g(X) + v, \quad \mathbb{E}[v|X] = 0$$

That is, we only assume linearity on T , and try to approximate the non-linear functions f, g . A reasonable way is to do **machine learning**.

Problems: causal interpretation is vulnerable to overfitting, regularization bias and estimation error. **DDML** (Double/debiased machine learning) uses orthogonalization and data splitting to solve these.

5.2 Intuition

DDML also applies a group of base learners, e.g. OLS, LASSO, XGBoost, RF, and then outputs the β_{pliv} estimate from an ensemble model.

It can be proven that β_{pliv} approximates β_{rich} under correctly specified linear IV, without additional parametric assumptions.

If we have $T \in \{0, 1\}$ and $Z \in \{0, 1\}$, then a three-stage framework will approximate the LATE estimator for compliers β_{late} .

Implemented in the R-Package **ddml** (Chernozhukov et al., 2018; Ahrens et al., 2024).

$\beta_{\text{rich}} \neq \beta_{\text{late}}$! Under binary T, Z ,

- β_{late} is the simple mean effect for covariate-specific complier groups, thus LATE.
- β_{rich} imposes weights on subgroups dependent on $\mathbb{V}[Z|X]$ – preference for subgroups with more variance in Z .

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6.1 Card (1995)

We extend the previous adapted Card (1995) experiment.

```
1 library(ddml)
2 set.seed(123)
3 # Estimate the PLIV using short-stacking with base
  learners ols, rlasso, random forest, and xgboost.
4 learners_multiple <- list(list(fun = ols), list(fun
  = mdl_glmnet), list(fun = mdl_ranger), list(fun =
  mdl_xgboost))
5 pliv_fit_short <- ddml_pliv(Y, D, Z, X,
6   learners = learners_multiple,
7   ensemble_type = c('nnls', 'singlebest', 'average'),
8   shortstack = TRUE,
9   sample_folds = 10, cv_folds = 10)
```

Method	Coefficient on D	SE
OLS	0.185	0.016
TSLs, no covar.	1.317	0.232
TSLs, unsaturated	0.778	0.353
TSLs, SW	0.412	0.179
TSLs, sat. in X	0.913	0.439
DDML-PLIV	0.912	0.432
DDML-LATE	0.662	0.325

- Speculated many instruments bias: 38%
- Overestimated causal effect: $\frac{\beta_{\text{tsls}} - \beta_{\text{pliv}}}{\beta_{\text{tsls}}} = -17\%$
- Overestimated selection bias: $\left| \frac{\beta_{\text{tsls}} - \beta_{\text{pliv}}}{\beta_{\text{ols}} - \beta_{\text{pliv}}} \right| = 18\%$

6.1 Card (1995)

The original Card (1995) data:

- $N = 3010$ individuals
- Y : cont. log hourly wage
- T : cont. years of education
- Z : binary, presence of college nearby
- X : cont. years of experience, and indicators on race, location of residence, etc. (14 co-variates)
- RESET-test on $\text{lm}(Z \sim X)$: $p = 0.000$

Method	Coefficient on D	SE
OLS	0.075	0.003
TSLS, no covar.	0.188	0.026
TSLS, unsaturated	0.132	0.054
TSLS, SW	-	-
TSLS, sat. in X	-	-
DDML-PLIV	0.138	0.050
DDML-LATE	0.068	0.043

- Overestimated causal effect: -4.5%
- Overestimated selection bias: 9.5%
- Relatively low bias among other works.

6.2 Nunn and Wantchekon (2011)

Effect of the slave trade on modern day level of trust in Africa. The data¹:

- $N = 16679$ individuals
- Y : cat. level of trust in neighbors
- T : cont. log of total slave exports
- Z : cont. distance from the nearest coast
- X : 93 covariates.
- RESET-test on $\text{lm}(Z \sim X)$: $p = 0.000$

Method	Coefficient on D	SE
OLS	-0.203	0.033
TSLS, no covar.	-0.190	0.111
TSLS, unsaturated	-0.271	0.088
TSLS, SW	-	-
TSLS, sat. in X	-	-
DDML-PLIV	-0.071	0.091
DDML-LATE	-	-

- Overestimated causal effect: 73.8%
- Overestimated selection bias: 151.5%
- The authors' key finding was invalid!
- Cited by 2800+.

¹Result of this table is currently cited from Table 3(2), Blandhol et al. 2025.

6.3 MacDonald et al. (2018)

Increased human-forest interaction = more Lyme disease incidence? The data¹:

- $N = 514$ counties, USA
- Y : cont. log Lyme disease incidence
- T : cont. population% living near forest
- Z : cont, land use regulation score
- X : year, forest%, forest edge density, average forest patch area in county (4 cont.)
- Binary: $T > \text{median}$, $Z > 0$.

	Original	Binary
OLS	0.008 (0.004)	0.332 (0.262)
TSLS, no covar.	0.037 (0.009)	2.995 (0.967)
TSLS, unsaturated	0.037 (0.014)	3.473 (1.910)
DDML-PLIV	0.030 (0.009)	2.872 (1.522)
DDML-LATE	-	0.922 (0.693)
RESET p-Value	0.579	0.0001

- Careful theoretical justification
- Ignored saturation, but had RC (by chance?)
- Interpreted as in simple linear relationship, not directly mentioning LATE or causality.
- Systematic bias of DDML is visible.

¹Only complete cases, used cluster-robust standard errors with contiguous counties as clusters.

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Contributions

- Extended Angrist and Krueger 1999, by providing a precise interpretation for the TSLS estimate with covariates that is generally applicable.
- Proved that TSLS with covariates, if not under strong assumptions, cannot provide weakly causal interpretation, and thus cannot identify LATE.
- Extended previous efforts from, e.g. Słoczyński and Kolesár, by combining covariate richness, treatment effect heterogeneity, and monotonicity under a more holistic investigation with more general setups.
- For empirical researchers, it showed TSLS with covariates is a common practice, urges caution when doing so, provided a guided recipe on choosing IV specifications, and also discussed a few alternative methods to linear IV.

7 Discussion

Limitations

- It is clear that $LATE \Rightarrow WC$, but how WC relates to $LATE$ needs to be specified. At least we know, empirically, $\beta_{\text{rich}} \neq \beta_{\text{late}}$. The weights are empirically inaccessible.
- Similarly, the estimator DDML-PLIV is generally hard to interpret. Only in binary cases, we get DDML-LATE for compliers. Further research is needed.

Notes

- Further theoretical and empirical investigation could be done on analogous methods, e.g. 2SRI. Consider a more thorough survey on previous empirical results in diverse fields.
- Call for good practice: Discussed results from 13 papers, selected based on publicly available data and reproducible results, out of 99 surveyed in total. Itself does not publish code.
- My codes are available on GitHub: https://github.com/Yc-Han/Causal_TSLs.

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Blandhol, C., Bonney, J., Mogstad, M., & Torgovitsky, A. (2022). When is TSLS actually late? (No. w29709). Cambridge, MA: National Bureau of Economic Research.

Abadie, A. (2003). Semiparametric instrumental variable estimation of treatment response models. *Journal of econometrics*, 113(2), 231-263.

Ahrens, A., Hansen, C., Schaffer, M., & Wiemann, T. (2024). ddml: Double/Debiased Machine Learning. R package version 0.3.0, <https://CRAN.R-project.org/package=ddml>.

Angrist, J. D., & Krueger, A. B. (1999). Empirical strategies in labor economics. In *Handbook of labor economics* (Vol. 3, pp. 1277-1366). Elsevier.

Angrist, J. D., & Pischke, J. S. (2009). *Mostly harmless econometrics: An empiricist's companion*. Princeton university press.

Angrist, J. D., Imbens, G. W., & Krueger, A. B. (1999). Jackknife instrumental variables estimation. *Journal of Applied Econometrics*, 14(1), 57-67.

Card, D. (1995). Using Geographic Variation in College Proximity to Estimate the Return to Schooling. In *Aspects of Labour Market Behaviour: Essays in Honour of John Vanderkamp*, edited by L. N. Christofides, K. E. Grant, and R. Swidinsky, Toronto: University of Toronto Press, 201-222.

Chernozhukov, V., Chetverikov, D., Demirer, M., Duflo, E., Hansen, C., Newey, W., & Robins, J. (2018). Double/debiased machine learning for treatment and structural parameters.

Deaton, A. (2010). Instruments, randomization, and learning about development. *Journal of economic literature*, 48(2), 424-455.

Evdokimov, K. S., & Kolesár, M. (2018). Inference in Instrumental Variables Analysis with Heterogeneous Treatment Effects.

Heckman, J. (1997). Instrumental variables: A study of implicit behavioral assumptions used in making program evaluations. *Journal of human resources*, 441-462.

Imbens, G. W. (2010). Better LATE than nothing: Some comments on Deaton (2009) and Heckman and Urzua (2009). *Journal of Economic literature*, 48(2), 399-423.

Kolesár, M. (2013). Estimation in an Instrumental Variables Model with Treatment Effect Heterogeneity. Working paper.

MacDonald, A. J., Larsen, A. E., & Plantinga, A. J. (2019). Missing the people for the trees: Identifying coupled natural–human system feedbacks driving the ecology of Lyme disease. *Journal of Applied Ecology*, 56(2), 354-364.

Nunn, N., & Wantchekon, L. (2011). The slave trade and the origins of mistrust in Africa. *American economic review*, 101(7), 3221-3252.

Ramsey, J. B. (1969). Tests for specification errors in classical linear least-squares regression analysis. *Journal of the Royal Statistical Society Series B: Statistical Methodology*, 31(2), 350-371.

Robins, J. M., & Greenland, S. (1996). Identification of causal effects using instrumental variables: comment. *Journal of the American Statistical Association*, 91(434), 456-458.

Słoczyński, T. (2020). When should we (not) interpret linear iv estimands as late?. arXiv preprint arXiv:2011.06695.

Swanson, S. A., & Hernán, M. A. (2014). Think globally, act globally: an epidemiologist's perspective on instrumental variable estimation. *Statistical science: a review journal of the Institute of Mathematical Statistics*, 29(3), 371.