# Shortest Path Algorithm with Heaps

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# **Chapter 1: Introduction**

In the project, it's required to implement the Dijkstra's algorithm to calculate the shortest paths using two different heap structures and one of which must be Fibonacci heap. We choose the priority queue and the Fibonacci heap.

## **Chapter 2: Data Structure / Algorithm Specification**

In the chapter, we will briefly discuss the Dijkstra's algorithm, priority queue and the Fibonacci heap.

## 2.1 Dijkstra's Algorithm

Dijkstra's algorithm is an algorithm for finding the shortest paths between nodes in a graph, which may represent, for example, traffic networks. It was conceived by computer scientist Edsger W. Dijkstra in 1956 and published in 1959. For a given source node in the graph, the algorithm finds the shortest path between that node and every other. It can also be used for finding the shortest paths from a single node to a single destination node by stopping the algorithm once the shortest path to the destination node has been determined.

## Pseudocode for the original algorithm:

```
function Dijkstra(Graph, source):
    create vertex set Q
    for each vertex v in Graph:
        dist[v] ← INFINITY
        prev[v] ← UNDEFINED
        add v to Q
```

```
dist[source] ← 0
while Q is not empty:
    u ← vertex in Q with min dist[u]

remove u from Q
    for each neighbor v of u: // only v that are still in Q
    alt ← dist[u] + length(u, v)
    if alt < dist[v]:
        dist[v] ← alt
        prev[v] ← u

return dist[], prev[]</pre>
```

# 2.2 Priority Queue

A min-priority queue is an abstract data type that provides 3 basic operations: add\_with\_priority(), decrease\_priority() and extract\_min(). Using such a data structure can lead to faster computing times than using a basic queue.

# Pseudocode for the algorithm:

```
function Dijkstra(Graph, source):
   dist[source] ← 0
                                      // Initialization
   create vertex priority queue Q
   for each vertex v in Graph:
       if v ≠ source
           dist[v] \leftarrow INFINITY // Unknown distance from source to v
           prev[v] ← UNDEFINED
                                     // Predecessor of v
       Q.add_with_priority(v, dist[v])
                                     // The main Loop
   while Q is not empty:
       u ← Q.extract min()
                                      // Remove and return best vertex
       for each neighbor v of u: // only v that are still in Q
           alt ← dist[u] + length(u, v)
           if alt < dist[v]</pre>
               dist[v] ← alt
               prev[v] ← u
               Q.decrease_priority(v, alt)
   return dist, prev
```

## 2.3 Fibonacci Heap

A Fibonacci heap is a collection of trees satisfying the minimum-heap property, that is, the key of a child is always greater than or equal to the key of the parent. This implies that the minimum key is always at the root of one of the trees. Compared with binomial heaps, the structure of a Fibonacci heap is more flexible. The trees do not have a prescribed shape and in the extreme case the heap can have every element in a separate tree. This flexibility allows some operations to be executed in a lazy manner, postponing the work for later operations. For example, merging heaps is done simply by concatenating the two lists of trees, and operation decrease key sometimes cuts a node from its parent and forms a new tree.

Using such a data structure can lead to faster computing times than using a basic queue.

#### Pseudocode for the algorithm:

```
AdjVertex tmpV = tmpNode->index;
        if (visit[tmpV])
            continue;
        visit[tmpV] = true;
        for (PAdjEdge i = G->HeadList[tmpV]; i; i = i->nextEdge)
            AdjVertex to = i->toVertex;
            if (!visit[to] && dis[tmpV] + i->dis < dis[to])</pre>
                dis[to] = dis[tmpV] + i->dis;
                FibNode = CreateAFibonacciNode(dis[to], to);
                InsertToFibonacciHeap(FibHeap, FibNode); //
            }
        }
    }
    Dis ret = dis[end];
    return ret;
}
```

# **Chapter 3: Testing Results**

#### 3.1 Test Environment

Our test environment is just as following:

OS: Windows 10 Pro for Workstations, Build 18363.720

Compiler: gcc 8.1.0, x86\_64-posix-seh-rev0

Compile command: g++ -Wall -std=c++14 source.cpp -o source -O2

RAM: 64GiB

# 3.2 Test Results and Analysis

We test six cases. The 1<sup>st</sup>, 2<sup>nd</sup> and 3<sup>rd</sup> cases are and the 4<sup>th</sup>, 5<sup>th</sup> and 6<sup>th</sup> cases are provided by teachers.

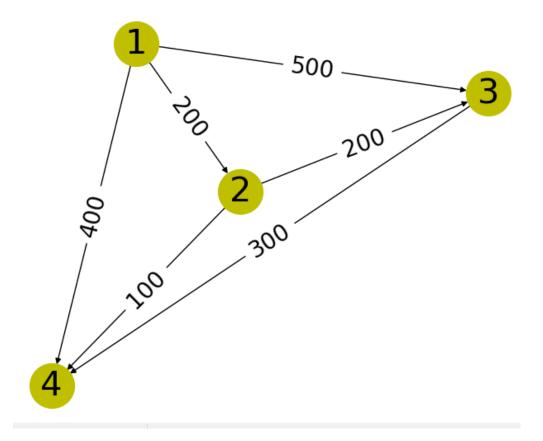
Format description of input data:

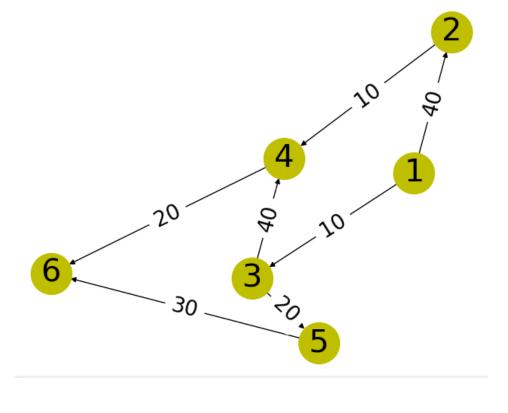
The first row of the input data consists of three integers V, E and Q, representing the number of vertices, the number of edges, and the number of queries, respectively.

In the following E rows, three integers a\_i, b\_i, c\_i, in each line, represents an arrow from a\_i to b\_i and the weights of this arrow is c\_i.

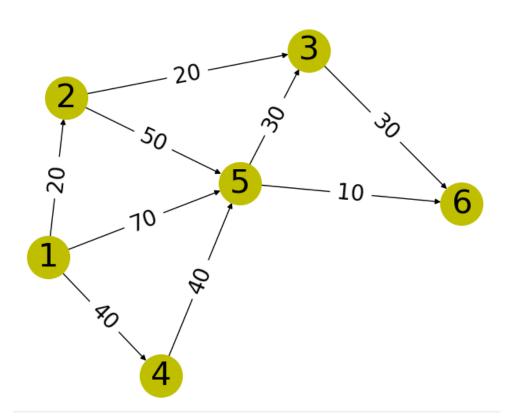
The last Q rows of the input data contains two integers in each row, indicating the label of the starting point and the label of the terminal point of a group of queries.

1 st





3<sup>rd</sup>



The results all agree with our expectations.

# **Chapter 4: Analysis and Comments**

## 4.1 Time Complexity Analysis

As we all know, for the original Dijkstra's algorithm on a graph with edges E and vertices V, the time complexity is  $O(|E|T_{dk}+|V|T_{em})$  where  $T_{dk}$  and  $T_{em}$  are the complexities of the decrease-key and extract-minimum operations in data structure Q.

For priority queue,  $T_{dk} = log|V|$  (time complexity for a binary search) and  $T_{em} = |V|$ . It's  $O(|V|^2 + |E|log|V|)$ .

For Fibonacci heap, it's  $O(|E|+|V|\log|V)$ .

# 4.2 Space Complexity Analysis

For priority queue implement case, if we implement Disjkstra's shortest path algorithm using a MinHeap and also if we use an array to store the values of the shortest distance for every node in the graph, the space complexity will be O(V) + O(V) = O(2V) = O(V).

For Fibonacci heap implement case, it's  $O(V^2)$ .

# **Appendix: Source Code**

The source code folder consists of four files: FibonacciHeap.hpp, PriorityQueue.hpp, ShortestPath.hpp and the source.cpp.

## The FibonacciHeap.hpp:

```
#ifndef FibonacciHeap_Hpp
// head files preprocessing
#define FibonacciHeap Hpp
// head files preprocessing
typedef int Dis;
typedef int AdjVertex;
The struct for the nodes in the Fibonacci Heap
typedef struct FibonacciNodeStruct *PFibonacciNode;
// struct for the Fibonacci node
typedef struct FibonacciNodeStruct
// struct for the Fibonacci node
{
    Dis key;
 // the temporary distance from the start node to the node.
    PFibonacciNode left, right, child;
// nodes
    AdjVertex index;
 // index
    int degree;
// node's degree
} FibonacciNode;
/*
The struct for the Fibonacci Heap
typedef struct FibonacciHeapStruct *PFibonacciHeap;
// struct for the Fibonacci heap
typedef struct FibonacciHeapStruct
// struct for the Fibonacci heap
{
    int sumNodes;
 // the sum of the nodes
    PFibonacciNode minTree;
// the pointer to the tree whose top node is min
} FibonacciHeap;
//The declarations of the functions
PFibonacciHeap BuildAFibonacciHeap();
// function to build an empty fibonacci heap
void InsertToFibonacciHeap(PFibonacciHeap FibHeap, PFibonacciNode FibNo
de);// function to insert the FibNode into the FibHeap
```

```
PFibonacciNode CreateAFibonacciNode(Dis key, AdjVertex index);
// function to create a fibonacci node with key and index
PFibonacciNode PopMinFibonacciHeap(PFibonacciHeap FibHeap);
// function to return the min Node in the FibHeap and delete it
void AddNodeToList(PFibonacciNode rootNode, PFibonacciNode FibNode);
// function to insert FibNode to the right of rootNode in the doubly li
nked List
void RemoveNodeFromList(PFibonacciNode FibNode);
// function to remove the FibNode from the doubly list it exists in
void UpdateFibonacciHeap(PFibonacciHeap FibHeap);
// functin to update the heap after deleting the min node
//The definitions of the functions
PFibonacciHeap BuildAFibonacciHeap()
// function to build an empty fibonacci heap
{
    PFibonacciHeap FibHeap = (PFibonacciHeap)malloc(sizeof(FibonacciHea
p));
   FibHeap->minTree = NULL;
// initial value for minTree
    FibHeap->sumNodes = 0;
 // initial value for sumNdes
    return FibHeap;
// terminate the function and return
PFibonacciNode CreateAFibonacciNode(Dis key, AdjVertex index)
// function to create a fibonacci node with key and index
    PFibonacciNode FibNode = (PFibonacciNode)malloc(sizeof(FibonacciNod
e));
    FibNode->key = key;
 // initial value for the key
    FibNode->child = NULL;
 // initial value for the child
    FibNode->left = FibNode->right = FibNode;
 // initial values
   FibNode->degree = 0;
 // initial value for the degree
    FibNode->index = index;
 // initial value for the index
    return FibNode;
// terminate the function and return
```

```
void AddNodeToList(PFibonacciNode rootNode, PFibonacciNode FibNode)
// function to insert FibNode to the right of rootNode in the doubly L
inked list
{
    FibNode->right = rootNode->right;
// set value
    rootNode->right->left = FibNode;
// set value
   rootNode->right = FibNode;
// set value
   rootNode->right = FibNode;
// set value
   FibNode->left = rootNode;
// set value
}
void RemoveNodeFromList(PFibonacciNode FibNode)
// function to remove the FibNode from the doubly list it exists in
{
   if (FibNode->right == FibNode)
// if the FibNode's right is equal to FibNode
       return;
// terminate the function and return
   FibNode->right->left = FibNode->left;
// set value
    FibNode->left->right = FibNode->right;
// set value
   FibNode->left = FibNode->right = FibNode;
// set value
void InsertToFibonacciHeap(PFibonacciHeap FibHeap, PFibonacciNode FibNo
de)// function to insert the FibNode into the FibHeap
{
   FibHeap->sumNodes++;
// increment sumNodes by 1
    if (!FibHeap->minTree)
// empty heap
       FibHeap->minTree = FibNode;
// set value
   else
    {
        AddNodeToList(FibHeap->minTree, FibNode);
// lazy insertion
        if (FibNode->key < FibHeap->minTree->key)
 // update the min node
```

```
FibHeap->minTree = FibNode;
// set value
   }
}
PFibonacciNode PopMinFibonacciHeap(PFibonacciHeap FibHeap)
// function to return the min Node in the FibHeap and delete it
    PFibonacciNode minNode = FibHeap->minTree;
// minimum node
    PFibonacciNode tmpNode = minNode->child;
// tmp node
   PFibonacciNode t;
   while (tmpNode)
// add the children of the minNode into the Root List
   {
       if (tmpNode->right == tmpNode)
// if the tmpNode's right equals to the tmpNode
           t = NULL;
// set t to NULL
        else
           t = tmpNode->right;
// set value
       RemoveNodeFromList(tmpNode);
 // remove the child from its origin doubly list
       minNode->child = t;
       AddNodeToList(minNode, tmpNode);
// add the child into the root list
       tmpNode = t;
   if (minNode->right == minNode)
// judge
       t = NULL;
 // set t to NULL
   else
       t = minNode->right;
// set value
    RemoveNodeFromList(minNode);
 // remove the minNode
   FibHeap->minTree = t;
   UpdateFibonacciHeap(FibHeap);
// update the FibHeap Structure
   FibHeap->sumNodes--;
// decrement sumNodes by 1
   return minNode;
```

```
}
void UpdateFibonacciHeap(PFibonacciHeap FibHeap)
// functin to update the heap after deleting the min node
{
   if (!FibHeap->minTree)
        return;
    int hashTableSize = ceil(log2(FibHeap->sumNodes)) + 1;
// use a hashTable to obtain the trees with the same degree
   PFibonacciNode *hashTable = new PFibonacciNode[hashTableSize];
   for (int i = 0; i < hashTableSize; i++)</pre>
        hashTable[i] = NULL;
// re-aggregate the trees on the Root List into the hashtable. We will
 link those trees with the same degree
   while (FibHeap->minTree)
   {
        PFibonacciNode minNode = FibHeap->minTree, t;
 // define new nodes
        int degree = minNode->degree;
        if (minNode->right == minNode)
 // judge
           t = NULL;
 // set t to NULL
        else
           t = minNode->right;
 // set value
       RemoveNodeFromList(minNode);
// remove node minNode from list
        while (hashTable[degree])
 // aggregate trees until there doesn't exist any trees having the same
 dearee
        {
            PFibonacciNode eNode = hashTable[degree];
// we always set the tree in the hash table as the child of the tree f
rom the Root List
// so we should make it sure that the eNode->key is larger than the mi
nNode->key
            if (eNode->key < minNode->key)
// if the eNode's key is greater than the minimum node's key
                PFibonacciNode t = eNode;
 // new a node eode
```

```
eNode = minNode;
// set the new node to the minimum node
               minNode = t;
           }
           if (!minNode->child)
// if the minimum node's child is NULL
               minNode->child = eNode;
// set the minimum nodes' child to eNode
           eLse
               AddNodeToList(minNode->child, eNode);
// add the node to the list
           minNode->degree++;
// increment degree by 1
          hashTable[degree++] = NULL;
// the degree has been enlarged after aggregating two trees
       hashTable[degree] = minNode;
// set to minimum node
       FibHeap->minTree = t;
// set to t
  }
  for (int i = 0; i < hashTableSize; i++)</pre>
// move the trees in the hash table to the root list
       if (hashTable[i])
// judge
           if (FibHeap->minTree)
// if the FibHeap's minTree is not false or null.
               AddNodeToList(FibHeap->minTree, hashTable[i]);
// add the node to list
               if (hashTable[i]->key < FibHeap->minTree->key)
// judge
                   FibHeap->minTree = hashTable[i];
// set value
           else
               FibHeap->minTree = hashTable[i];
// set value
       }
   }
  delete [] hashTable;
// delete the hash table
```

```
}
#endif
// head files preprocessing
The PriorityQueue.hpp:
#ifndef PriorityQueue_Hpp
// head files preprocessing
#define PriorityQueue_Hpp
// head files preprocessing
typedef int Dis;
typedef int AdjVertex;
typedef struct HeapNodeStruct
// the heap node struct
    Dis key;
// the dis from the start node to this node
    AdjVertex index;
// the index of vertexes
} HeapNode, *PHeapNode;
typedef struct HeapStruct
// the heap struct
    int size;
// current size of the heap
    int space;
 // current space of the heap
    PHeapNode nodeList;
} Heap;
typedef struct HeapStruct *PriorityQueue;
// define the priority queue data sruct
//The declarations of the functions
PriorityQueue BuildAHeap(int sumVertexes);
// build an empty heap with sumVertexes nodes
void InsertToPriorityQueue(HeapNode x, PriorityQueue H);
// insert an node x into the heap H. You should create the node yourse
Lf
HeapNode PopMinPriorityQueue(PriorityQueue H);
// return the min node in the heap H and delete it.
bool IsEmptyPriorityQueue(PriorityQueue H);
// check the heap whether empty or not
//The definitions of the functions
PriorityQueue BuildAHeap(int sumVertexes)
// function to build a heap
{
```

```
PriorityQueue H = (PriorityQueue)malloc(sizeof(HeapStruct));
// malloc the memory
   H \rightarrow size = 0;
// initial value
   H->nodeList=(PHeapNode)malloc(sizeof(HeapNode) * (sumVertexes + 1))
;// initial value
   H->nodeList[0].key = -1;
// initial value
   return H;
// return result
void InsertToPriorityQueue(HeapNode x, PriorityQueue H)
// function to insert into priority queue
{
   int i;
   for (i = ++H-)size; H-)nodeList[i / 2].key > x.key; i /= 2)
// add the node to the tail of the list and percolate up it
        H->nodeList[i] = H->nodeList[i / 2];
   H->nodeList[i] = x;
// set value
HeapNode PopMinPriorityQueue(PriorityQueue H)
// fuction to pop minimum priority queue
{
    int i, child;
   HeapNode minNode = H->nodeList[1],
// define the minimum node
             LastNode = H->nodeList[H->size--];
// delete the node at the tail of the list, and replace it with the to
p node
   for (i = 1; i * 2 <= H->size; i = child)
// percolate down the LastNode
   {
        child = i * 2;
        if (child != H->size && H->nodeList[child + 1].key < H->nodeLis
t[child].key)// judge
            child++;
        if (LastNode.key > H->nodeList[child].key)
// if the last node's key is greater than the key of the current child
's node
            H->nodeList[i] = H->nodeList[child];
        eLse
            break;
// find the minumum node
```

```
}
H->nodeList[i] = LastNode;

// set the value
    return minNode;

// retur the result
}
bool IsEmptyPriorityQueue(PriorityQueue H)

// function to judge if the priority queue is empty
{
    return H->size == 0 ? true : false;

// if the priority queue is empty, return true. return false otherwise
.
}
#endif
```

# The ShortestPath.hpp

```
#ifndef ShortestPath_Hpp
// head files preprocessing
#define ShortestPath Hpp
// head files preprocessing
#include <cmath>
#include <cstdio>
#include <cstdlib>
#include <cstring>
#include "FibonacciHeap.hpp"
#include "PriorityQueue.hpp"
#define INF 2147483647
// global constant
typedef int Dis;
// global variable int
Adjacency list is used to describe the graph
*/
typedef int AdjVertex;
// the index of vertexes. Notice that the index should begin as 0
The struct storing the edges in the adjacency list.
typedef struct AdjEdgeStruct *PAdjEdge;
// padjedge
typedef struct AdjEdgeStruct
// adjedge
{
```

```
Dis dis;
// the length of the edge
   AdjVertex fromVertex, toVertex;
// the vertexes the edge connects
    PAdjEdge nextEdge;
// the following edges whose FROM VERTEX is the same
} AdjEdge;
// the struct and the pointer to an edge
typedef PAdjEdge *AdjList;
// the adjacency list
typedef struct GraphStruct
// the graph
{
   int sumVertexes;
// the sum of all the vertexes in the graph;
   int sumEdges;
// the sum of all the edges in the graph;
   AdjList HeadList;
// the head list
} * PGraph;
// end
//The declarations of the functions
PGraph BuildAGraph(int sumVertexes, int sumEdges);
// build an empty adjacency list with sumVertexes vertexes
void AddEdge(PGraph G, AdjVertex fromV, AdjVertex toV, Dis dis);
// add an edge from fromV to toV
Dis DijkstraUsingFibonacciHeap(PGraph G, AdjVertex start, AdjVertex end
);// Dijkstra algorithm using fibonacci heap
Dis DijkstraUsingPriorityQueue(PGraph G, AdjVertex start, AdjVertex end
);// Dijkstra algorithm using priority queue
//The definitions of the functions
PGraph BuildAGraph(int sumVertexes, int sumEdges)
// build an empty adjacency list with sumVertexes vertexes
    PGraph Graph = (PGraph)malloc(sizeof(struct GraphStruct));
// new graph
    Graph->sumVertexes = sumVertexes;
// set value
   Graph->sumEdges = sumEdges;
// set value
    Graph->HeadList = (AdjList)malloc(sizeof(PAdjEdge) * sumVertexes);
// set value
   for (int i = 0; i < sumVertexes; i++)</pre>
 // recurse
```

```
{
       Graph->HeadList[i] = NULL;
// set value
   }
   return Graph;
// terminate the function and return
void AddEdge(PGraph G, AdjVertex fromV, AdjVertex toV, Dis dis)
// build an empty adjacency list with sumVertexes vertexes
   PAdjEdge edge = (PAdjEdge)malloc(sizeof(AdjEdge));
   edge->fromVertex = fromV;
// set value
    edge->toVertex = toV;
// set value
   edge->dis = dis;
// set value
   edge->nextEdge = G->HeadList[fromV];
// set value
   G->HeadList[fromV] = edge;
// set value
Dis DijkstraUsingFibonacciHeap(PGraph G, AdjVertex start, AdjVertex end
)// Dijkstra algorithm using fibonacci heap
{
   PFibonacciHeap FibHeap = BuildAFibonacciHeap();
   Dis *dis = (Dis *)malloc(sizeof(Dis) * G->sumVertexes);
// the temporary dis from the start to the node
   bool *visit = (bool *)malloc(sizeof(bool) * G->sumVertexes);
// malloc new variable
   for (int i = 0; i < G->sumVertexes; i++)
// recurse
   {
       dis[i] = INF;
// set value
       visit[i] = 0;
 // set value
   dis[start] = 0;
// set value
   PFibonacciNode FibNode = CreateAFibonacciNode(∅, start);
    InsertToFibonacciHeap(FibHeap, FibNode);
// insert the startNode into the fibonacci heap
```

```
while (FibHeap->minTree)
   {
        PFibonacciNode tmpNode = PopMinFibonacciHeap(FibHeap);
// malloc new variable
        AdjVertex tmpV = tmpNode->index;
 // get the node which has the min dis from startNode
        if (visit[tmpV])
// if visit[tmpV] is false
            continue;
// skip it if the node has been visited
        visit[tmpV] = true;
 // mark the node
       for (PAdjEdge i = G->HeadList[tmpV]; i; i = i->nextEdge)
// use the tmpV to relax all the advancency nodes
        {
            AdjVertex to = i->toVertex;
// set value
            if (!visit[to] && dis[tmpV] + i->dis < dis[to])</pre>
// judge
            {
                dis[to] = dis[tmpV] + i->dis;
// set value
                FibNode = CreateAFibonacciNode(dis[to], to);
// create new node
                InsertToFibonacciHeap(FibHeap, FibNode);
// insert the node that is been relaxed into the heap
        }
    }
   Dis ret = dis[end];
// set value
   free(FibNode);
// free space
   free(dis);
// free space
   free(visit);
// free space
   free(FibHeap);
// free space
   return ret;
// terminate the function and return
Dis DijkstraUsingPriorityQueue(PGraph G, AdjVertex start, AdjVertex end
)// Dijkstra algorithm using priority queue
```

```
{
   Dis *dis = (Dis *)malloc(sizeof(Dis) * G->sumVertexes);
// malloc new variable
    bool *visit = (bool *)malloc(sizeof(bool) * G->sumVertexes);
// malloc new variable
   for (int i = 0; i < G->sumVertexes; i++)
// recurse
   {
       dis[i] = INF;
// set value
       visit[i] = 0;
 // set value
   }
   dis[start] = 0;
// set value
    PriorityQueue heap = BuildAHeap(G->sumVertexes + G->sumEdges);
   HeapNode newNode;
   newNode.index = start;
// set value
    newNode.key = 0;
// set value
    InsertToPriorityQueue(newNode, heap);
// insert the startNode into the fibonacci heap
   while (!IsEmptyPriorityQueue(heap))
   {
        HeapNode tmpNode = PopMinPriorityQueue(heap);
        AdjVertex tmpV = tmpNode.index;
        if (visit[tmpV])
// judge if the visit[tmpV] is empty
            continue;
// skip it if the node has been visited
       visit[tmpV] = true;
 // mark the node
       for (PAdjEdge i = G->HeadList[tmpV]; i; i = i->nextEdge)
 // use the tmpV to relax all the advancency nodes
        {
            AdjVertex to = i->toVertex;
// define new variable
            if (!visit[to] && dis[tmpV] + i->dis < dis[to])</pre>
// judge
            {
                dis[to] = dis[tmpV] + i->dis;
// set value
```

```
newNode.index = to;
 // set value
                newNode.key = dis[to];
// set value
                InsertToPriorityQueue(newNode, heap);
 // insert the node that is been relaxed into the heap
        }
    }
    Dis ret = dis[end];
 // set value
   free(dis);
 // free space
   free(visit);
 // free space
   free(heap);
 // free space
   return ret;
// terminate the function and return
#endif
// head files preprocessing
The source.cpp
#include <cstdio>
#include <cstring>
#include <cmath>
#include <iostream>
#include <cstdlib>
#include <ctime>
#include "ShortestPath.hpp"
using namespace std;
typedef struct QueryPairStruct
// the query pair struct
    int start, end;
// struct members
} QueryPair;
int main()
// the main function
    char filename[30];
    FILE* PFileIn = fopen("data.in", "r");
 // open the input data file
```

```
clock_t begin, finish;
// timer variables
   int n, m, q;
   fscanf(PFileIn,"%d %d %d",&n,&m,&q);
// read the input data
   PGraph G = BuildAGraph(n, m);
// build graph
   QueryPair *QueryPairs = (QueryPair *)malloc(sizeof(QueryPair) * q);
   for (int i = 0; i < m; i++)</pre>
// recurse
   {
        int f, t, d;
       fscanf(PFileIn,"%d %d %d",&f,&t,&d);
// read the input data
        AddEdge(G, f - 1, t - 1, d);
 // add edge to the graph
   for (int i = 0; i < q; i++)
// recurse
   {
        int s, e;
       fscanf(PFileIn,"%d %d",&s,&e);
// read the input data
       QueryPairs[i].start = s - 1;
// record the query pairs
       QueryPairs[i].end = e - 1;
// record the query pairs
   }
   fclose(PFileIn);
// close the fle
    sprintf(filename, "PriorityQueue.out");
// help word
   FILE *PFileOut=fopen(filename, "w");
// define the output file string
   fprintf(PFileOut, "The result using Priority Queue is: \n");
// help word
   begin = clock();
// begin the timer
   for (int i = 0; i < q; i++)
        Dis ans = DijkstraUsingPriorityQueue(G, QueryPairs[i].start, Qu
eryPairs[i].end);
       fprintf(PFileOut, "%d\n", ans);
```

```
}
   finish = clock();
// terminate the timer
    fprintf(PFileOut, "The time using Priority Queue is: %d", (finish -
begin) / CLOCKS PER SEC);
   fclose(PFileOut);
// close the written file string
   cout << "The function using Priority Queue completed!" << endl;</pre>
// help word
    sprintf(filename, "FibonacciHeap.out");
   PFileOut=fopen(filename, "w");
// open the written file string
   fprintf(PFileOut, "The result using Fibonacci Heap is: \n");
   begin = clock();
// begin the timer
   for (int i = 0; i < q; i++)
        Dis ans = DijkstraUsingFibonacciHeap(G, QueryPairs[i].start, Qu
eryPairs[i].end);
        fprintf(PFileOut,"%d\n", ans);
// print the output
   }
   finish = clock();
// terminate the timer
    fprintf(PFileOut, "The time using Fibonacci Heap is: %d", (finish -
begin) / CLOCKS_PER_SEC);
   fclose(PFileOut);
    printf("The function using Priority Queue completed!");
// print the output
   return 0;
}
```

#### References

- [1] Author, "Title of the article", *Name of the journal*, page no., (year)
- [2] Author, "Title of the book", Name of the publisher, year
- [3] Author, "Title of the article", Web site links

# **Author List**

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# **Declaration**

We hereby declare that all the work done in this project titled "XXX" is of our independent effort as a group.

# **Signatures**

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