

## Exercise 2.3

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**Exercise.** Let  $R$  be the rectangle in the  $xy$ -plane with vertices at  $(1, 0), (2, 0), (1, 3), (2, 3)$ . Integrate the following functions over  $R$ .

- $x^2y^2$ .
- $1$ .
- $x^2 + y^2$ .
- $\sqrt{x + \frac{2}{3}y}$ .

- $\int_0^3 \int_1^2 x^2 y^2 dx dy = \int_0^3 \left( \frac{1}{3} x^3 y^2 \Big|_1^2 \right) dy = \int_0^3 \frac{7}{3} y^2 dy = 21$ .
- $\int_0^3 \int_1^2 dx dy = 3$ .
- $\int_0^3 \int_1^2 (x^2 + y^2) dx dy = \int_0^3 \left( \frac{1}{3} x^3 + xy^2 \right) \Big|_1^2 dy = 16$ .
- $\int_0^3 \int_1^2 \sqrt{x + \frac{2}{3}y} dx dy = \int_0^3 \left( \frac{2}{3} \left( x + \frac{2}{3}y \right)^{\frac{3}{2}} \Big|_1^2 \right) dy = 0.4(9 - 3^{\frac{3}{2}} - 2^{\frac{5}{2}})$ .

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