

Lemma. *If α and β are 1-forms on $T_p\mathbf{R}^3$ and V is a nonzero vector in the plane spanned by $\langle\alpha\rangle$ and $\langle\beta\rangle$, then there is a vector W , in this plane such that*

$$\alpha \wedge \beta = \langle V \rangle^{-1} \wedge \langle W \rangle^{-1}. \quad (1)$$

Proof. Let V_1, V_2 be two linearly independent vectors in $T_p\mathbf{R}^3$. In order to prove formula (1), we only need to prove that there exists W in the plane spanned by $\langle\alpha\rangle$ and $\langle\beta\rangle$ such that

$$\alpha \wedge \beta(V_1, V_2) = \langle V \rangle^{-1} \wedge \langle W \rangle^{-1}(V_1, V_2).$$

□