Exercise 3.18

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Exercise. Find a 2- form which is not the product of 1- forms.

Proof. If w and v are two 1-forms on $T_p \mathbf{R}^4$, namely,

$$w = a_1 dx + b_1 dy + c_1 dz + d_1 du, v = a_2 dx + b_2 dy + c_2 dz + d_2 du,$$

then

$$w \wedge v =$$

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