Exercise 3.5.3

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Exercise. Let ω and ν be the following 1-forms:

$$\omega(\langle dx, dy \rangle) = 2dx - 3dy.$$

$$\nu(\langle dx, dy \rangle) = dx + dy.$$

Find a constant c such that $\omega \wedge \nu = c dx \wedge dy$.

 $\mathit{Solve.} \ \ \mathrm{For \ any} \ \ V_1 = \langle \alpha_1, b_1 \rangle, V_2 = \langle \alpha_2, b_2 \rangle.$

$$dx \wedge dy(V_1, V_2) = \begin{vmatrix} a_1 & b_1 \\ a_2 & b_2 \end{vmatrix} = a_1b_2 - a_2b_1.$$

$$\omega \wedge \nu(V_1, V_2) = \begin{vmatrix} \omega(V_1) & \nu(V_1) \\ \omega(V_2) & \nu(V_2) \end{vmatrix} = 5(\alpha_1 b_2 - \alpha_2 b_1).$$

So c = 5.

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