

Pre-Condition:  $A$  is an array of elements with a total order.

Invariant: Before running the for loop with value  $j \geq 2$  the input elements  $A[1, \dots, j-1]$  at positions  $1, \dots, j-1$  are sorted in increasing order. Running the for loop with value  $j$ , takes element  $A[j]$ , shifts all elements whose value is larger than  $A[j]$  one position to the "right" and places  $A[j]$  at the first position  $i$  where  $A[i-1]$  is not greater than  $A[j]$  (you can formalize this with another invariant). Hence after having finished the for loop for value  $j$  the input elements  $A[1, \dots, j]$  at positions  $1, \dots, j$  are sorting in increasing order. Hence before running the for-loop for  $j+1$ , the input elements  $A[1, \dots, j]$  at positions  $1, \dots, j$  are sorting in increasing order.

Post-condition: For loop has been executed with  $j = N$  at termination. Hence, before running the for-loop with  $j=N+1$ , the given input elements are sorted in increasing order.