

PSY 503: Foundations of Statistical Methods in Psychological Science

Bootstrapping

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The statistical inference problem

- We want to estimate population parameters.
- But we only have data from a sample
- This introduces uncertainty
- And we try to estimate uncertainty

Think like a frequentist...

- Take many samples from the population
- Calculate your statistic each time
- See how much it varies - that's your sampling distribution
- But wait - we only have ONE sample...
- **Theory to the rescue**
 - theory gives us formulas for standard errors
 - $SE = SD/\sqrt{n}$
 - We can build confidence intervals from this

Think like a frequentist (Confidence Intervals)

- If we repeated our study many times...
 - For each experiment we calculate
 - Mean (estimated mean of population)
 - Confidence interval around the mean estimate
 - *This interval may or may not contain the true mean*
 - Across experiments, 95% of these intervals contain the true mean
- CI for means: $\bar{X} \pm t^* \times (SD/\sqrt{n})$
- Similarly for,
 - Difference in means, regression coefficients, etc.
 - Works by making sampling distributions normal
 - Sampling variation has a direct connection to uncertainty in statistic

But for some statistics it's not as straightforward

- Median
 - Requires sorting data
 - Variation depends on density around median
 - We only have one sample
 - Very different behaviors for different population distributions
 - (Uniform vs. Bimodal vs. Normal)
- Correlation
 - Requires multiplying deviations from mean (products, not sums)
 - Variation depends on true correlation
 - Very different behavior for different population distributions
 - (Height & IQ) vs (Test vs Re-test)
- Ratio..

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NOTE: CLT still holds

- **But we don't know the spread of this Gaussian**
- **Formulas exist (for very large N)**

The Bootstrap idea

- Forget formulas
- Your sample has some information, and is your best guess
 - Shape
 - Variability
 - Relationship
- Your sample is like a mini-population
 - Take samples of this sample
 - Construction a 'sampling distribution' of the ***statistic***
 - Calculate the variation of this distribution
 - SD
 - Percentiles