

Homework #4

Math 131 - Spring 2017

DUE on 3/14/17 at 1:30pm (online submission through Catcourses).

NOTE: *Your answers will be graded for correctness as well as comprehensiveness, completeness, and legibility of your solution.*

1. Write a MATLAB function, called `Lagrange_poly` that inputs a set of data points $(\mathbf{x}; \mathbf{y}) = (\mathbf{datx}, \mathbf{daty})$, a set x of numbers at which to interpolate, and outputs the polynomial interpolant, y , evaluated at x using Lagrange polynomial interpolation. Your function header should look something like:

```
function y = Lagrange_poly(x,datx,daty)
```

2. Use the code you developed in Problem 1 to interpolate the functions

(a) $f(x) = e^{-x^2}$

(b) $f(x) = \frac{1}{1+x^2}$.

using the data points `datx=-5:1:5`. Interpolate at the points `x=-5:0.001:5`. Plot the results and comment on the error.

3. Write a MATLAB function, called `Newton_poly` that inputs a set of data points $(\mathbf{x}; \mathbf{y}) = (\mathbf{datx}, \mathbf{daty})$, a set x of numbers at which to interpolate, and outputs the polynomial interpolant, y , evaluated at x using Newton polynomial interpolation. Your function header should look something like:

```
function y = Newton_poly(x,datx,daty)
```

4. Use the code you developed in Problem 3 to interpolate the function

$$f(x) = \frac{1}{1+x^2}$$

using the data points `datx=-5:1:5`. Interpolate at the points `x=-5:0.001:5`. Plot the results and compare them to what you got in problem 2(b). Explain why you get what you get.