

❖ Problem Link : <https://codeforces.com/problemset/problem/1475/B>

### ❖ Introduction

Polycarp loves the years **2020** and **2021**, and he wants to express a number **n** as a sum using only these two values.

Your task is to determine whether such a representation is possible for each test case.

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### ❖ Problem Explanation

Given a number **n**, we want to check whether :

$$n = (2020 \times a) + (2021 \times b)$$

for some non-negative integers **a** , **b**

➤ Examples :

- $4041 = 2020 + 2021 \rightarrow \text{YES}$
- $4042 = 2021 + 2021 \rightarrow \text{YES}$
- $8079$  cannot be formed  $\rightarrow \text{NO}$

### ❖ Full Python Code :

```
t = int(input())
for _ in range(t):
    n = int(input())
    y = n // 2020
    x = n % 2020
    if x <= y:
        print("YES")
    else:
        print("NO")
```

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### ❖ Algorithm Explanation

#### Key idea :

➤ **Observation:**

We want to check if a number **n** can be formed using:

- $2020 \times a$
- $2021 \times b$

where a and b are non-negative integers.

### So we want :

$$N = 2020a + 2021b$$

Notice that :

$$2021 = 2020 + 1$$

So a 2021-value is just a 2020-value plus 1.

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### Simple Calculation :

Try to use as many 2021's as possible because each 2021 contributes one extra on top of 2020.

Let's rewrite n like this:

$$n = 2020a + (2020 + 1)b = 2020(a + b) + b$$

This means:

n is possible if and only if the remainder when dividing by 2020 is  $\leq$  the number of 2021s you use.

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### Simpler explanation for beginners :

- Buying a 2021-package is like buying a 2020-package plus 1 extra.
- So if you use b copies of 2021, you get b extra units.
- Therefore, you only need to check:

Does n leave a remainder  $a \leq b$  when divided by 2020?

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### Example (easy steps) :

**n = 4041**

Try  $b = 1$  (one 2021) :

$$4041 - 2021 = 2020$$

2020 is divisible by 2020  $\rightarrow$  YES

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**n = 4042**

Try  $b = 2$  :

$$4042 - 2 \times 2021 = 0$$

0 is divisible  $\rightarrow$  YES

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**n = 8079**

Try b = 1 :

$$8079 - 2021 = 6058 \text{ ( not divisible by 2020 )}$$

Try b = 2 :

$$8079 - 4042 = 4037 \text{ ( not divisible )}$$

Try b = 3 :

$$8079 - 6063 = 2016 \text{ ( not divisible )}$$

No value works → NO

**Thus :**

- Let  $x = n \% 2020$  ( the remainder when dividing by 2020 ).
- Let  $y = n // 2020$  .

Then representation is possible **if and only if** :  $x \leq y$

Because every time you replace one 2020 by 2021, the total increases by 1.

$$2021 = 2020 + 1,$$

each time you use a 2021 instead of a 2020, the total increases by +1.

So 2021s let you add extra 1s on top of a combination of 2020s.

**Here :**

( / ) → represents normal division which gives ( int + float ) output .

( // ) → represents Floor division which gives ( int ) output .

( % ) → represents modulo which gives remainder of a division .

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❖ **Step-by-Step Working**

**Input:**

5  
1  
4041  
4042  
8081  
8079

## Working:

### 1. $n = 1$

- $n // 2020 = 0$
- $n \% 2020 = 1$
- $1 \leq 0 \rightarrow \text{NO}$

### 2. $n = 4041$

- $4041 // 2020 = 2$
- $4041 \% 2020 = 1$
- $1 \leq 2 \rightarrow \text{YES}$

### 3. $n = 4042$

- $4042 // 2020 = 2$
- $4042 \% 2020 = 2$
- $2 \leq 2 \rightarrow \text{YES}$

### 4. $n = 8081$

- $8081 // 2020 = 4$
- $8081 \% 2020 = 1$
- $1 \leq 4 \rightarrow \text{YES}$

### 5. $n = 8079$

- $8079 // 2020 = 4$
- $8079 \% 2020 = -$  actually  $8079 \% 2020 = ??$   
 $2020 \times 3 = 6060$   
 $2020 \times 4 = 8080 \rightarrow \text{too big}$   
So  $8079 \% 2020 = 8079 - 6060 = 2019$
- $2019 \leq 4 \rightarrow \text{NO}$

## Output

NO

YES

YES

YES

NO

## ❖ Time & Space Complexity

Operations	Complexity
Per test calculation	$O(1)$
For $t$ test cases	$O(t)$
Space usage	$O(1)$
Total Time Complexity	$O(t)$

## ❖ Conclusion

The key insight is that the remainder when dividing  $n$  by 2020 must be less than or equal to the quotient. This mathematical trick removes the need for loops and makes the solution efficient for up to  $10^4$  test cases.

## One sentence result

A number  $n$  can be written as  $2020 \cdot a + 2021 \cdot b$   
if the remainder when dividing by 2020 is not larger than the quotient .

# Thank You