

❖ **Problem Link :** <https://codeforces.com/problemset/problem/1475/B>

❖ Introduction

Polycarp loves the years **2020** and **2021** , and he wants to express a number **n** as a sum using only these two values.

Your task is to determine whether such a representation is possible for each test case.

❖ Problem Explanation

Given a number **n**, we want to check whether :

$$n = (2020 \times a) + (2021 \times b)$$

for some non-negative integers **a** , **b**

➤ Examples :

- $4041 = 2020 + 2021 \rightarrow \text{YES}$
- $4042 = 2021 + 2021 \rightarrow \text{YES}$
- 8079 cannot be formed $\rightarrow \text{NO}$

❖ Full Python Code :

```
t = int(input())
for _ in range(t):
    n = int(input())
    y = n // 2020
    x = n % 2020
    if x <= y:
        print("YES")
    else:
        print("NO")
```

❖ Algorithm Explanation

Key idea :

➤ **Observation:**

We want to check if a number **n** can be formed using:

- $2020 \times a$
- $2021 \times b$

where a and b are non-negative integers.

So we want :

$$N = 2020a + 2021b$$

Notice that :

$$2021 = 2020 + 1$$

So a 2021- value is just a 2020-value plus 1.

Simple Calculation :

Try to use as many 2021's as possible because each 2021 contributes one extra on top of 2020.

Let's rewrite n like this:

$$n = 2020a + (2020 + 1)b = 2020(a + b) + b$$

This means:

n is possible if and only if the remainder when dividing by 2020 is \leq the number of 2021s you use.

Simpler explanation for beginners :

- Buying a 2021 - package is like buying a 2020-package plus 1 extra.
- So if you use b copies of 2021, you get b extra units.
- Therefore, you only need to check:

Does n leave a remainder $a \leq b$ when divided by 2020?

Example (easy steps) :

$n = 4041$

Try $b = 1$ (one 2021) :

$$4041 - 2021 = 2020$$

2020 is divisible by 2020 \rightarrow YES

$n = 4042$

Try $b = 2$:

$$4042 - 2 \times 2021 = 0$$

0 is divisible \rightarrow YES

n = 8079

Try $b = 1$:

$8079 - 2021 = 6058$ (not divisible by 2020)

Try $b = 2$:

$8079 - 4042 = 4037$ (not divisible)

Try $b = 3$:

$8079 - 6063 = 2016$ (not divisible)

No value works \rightarrow NO

Thus :

- Let $x = n \% 2020$ (the remainder when dividing by 2020) .
- Let $y = n // 2020$.

Then representation is possible **if and only if** : $x \leq y$

Because every time you replace one 2020 by 2021, the total increases by 1.

$2021 = 2020 + 1$,

each time you use a 2021 instead of a 2020, the total increases by +1.

So 2021s let you add extra 1s on top of a combination of 2020s.

Here :

$(/) \rightarrow$ represents normal division which gives (int + float) output .

$(//) \rightarrow$ represents Floor division which gives (int) output .

$(\%) \rightarrow$ represents modulo which gives remainder of a division .

❖ Step-by-Step Working

Input:

5

1

4041

4042

8081

8079

Working:

1. $n = 1$

- $n // 2020 = 0$
- $n \% 2020 = 1$
- $1 \leq 0 \rightarrow \text{NO}$

2. $n = 4041$

- $4041 // 2020 = 2$
- $4041 \% 2020 = 1$
- $1 \leq 2 \rightarrow \text{YES}$

3. $n = 4042$

- $4042 // 2020 = 2$
- $4042 \% 2020 = 2$
- $2 \leq 2 \rightarrow \text{YES}$

4. $n = 8081$

- $8081 // 2020 = 4$
- $8081 \% 2020 = 1$
- $1 \leq 4 \rightarrow \text{YES}$

5. $n = 8079$

- $8079 // 2020 = 4$
- $8079 \% 2020 = -$ actually $8079 \% 2020 = ??$
 $2020 \times 3 = 6060$
 $2020 \times 4 = 8080 \rightarrow \text{too big}$
So $8079 \% 2020 = 8079 - 6060 = 2019$
- $2019 \leq 4 \rightarrow \text{NO}$

Output

NO

YES

YES

YES

NO

❖ Time & Space Complexity

Operations	Complexity
Per test calculation	$O(1)$
For t test cases	$O(t)$
Space usage	$O(1)$
Total Time Complexity	$O(t)$

❖ Conclusion

The key insight is that the remainder when dividing n by 2020 must be less than or equal to the quotient. This mathematical trick removes the need for loops and makes the solution efficient for up to 10^4 test cases.

One sentence result

A number n can be written as $2020 \cdot a + 2021 \cdot b$
if the remainder when dividing by 2020 is not larger than the quotient .

Thank You