



東南大學  
SOUTHEAST UNIVERSITY

# OPERATING SYSTEM CONCEPTS

.....

## Chapter 9. Virtual Memory

A/Prof. Kai Dong



## Warm-up

### What Happens when OS is Booting?

**OS @boot  
(kernel mode)**

**Hardware**

---

initialize trap table

remember addresses of ...

system call handler

timer handler

illegal mem-access handler

illegal instruction handler

start interrupt timer

start timer; interrupt after X ms

initialize process table

initialize free list



## Warm-up

### What Happens when OS is Running?

**OS @run  
(kernel mode)**

**Hardware**

**Program  
(user mode)**

**To start process A:**

- allocate entry in process table
- allocate memory for program
- set *base/limit registers*
- return-from-trap* (into A)

- restore registers of A
- move to *user mode*
- jump to A's (initial) PC

- translate virtual address  
and perform fetch

- if explicit load/store:
  - ensure address is in-limit;
  - translate virtual address
  - and perform load/store

...

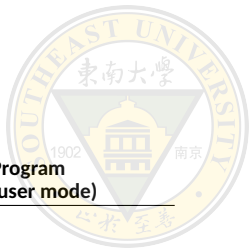
**Timer interrupt**

- move to *kernel mode*
- jump to interrupt handler

**Process A runs**

- fetch instruction

- execute instruction



## Warm-up

### What Happens when an Exception Takes Place?

**OS @run**  
**(kernel mode)**

**Hardware**

**Program**  
**(user mode)**

**Timer interrupt**  
move to *kernel mode*  
jump to interrupt handler

#### **Handle the *trap***

call *switch()* routine

save regs(A) to proc-struct(A)

(including *base/limit*)

restore regs(B) from proc-struct(B)

(including *base/limit*)

***return-from-trap*** (into B)

restore regs of B  
move to *user mode*  
jump to B's PC

**Process B runs**  
***execute bad load***

***load is out-of-limit***  
move to *kernel mode*  
jump to trap handler

#### **Handle the *trap***

decide to terminate process B

***de-allocate B's memory***

free B's entry in process table

# Objectives



- To describe the benefits of a virtual memory system
- To explain the concepts of demand paging, page-replacement algorithms, and allocation of page frames
- To discuss the principle of the working-set model
- To examine the relationship between shared memory and memory-mapped files
- To explore how kernel memory is managed



## Contents

1. Background
2. Demand Paging
3. Copy-on-Write
4. Page Replacement
5. Allocation of Frames
6. Thrashing
7. Memory-Mapped Files
8. Allocating Kernel Memory
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  - Each program takes less memory while running → more programs run at the same time
    - » Increased CPU utilization and throughput with no increase in response time or turnaround time



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  - Less I/O needed to load or swap programs into memory → each user program runs faster



## Background

- **Virtual memory** — separation of user logical memory from physical memory
  - Only part of the program needs to be in memory for execution
  - Logical address space can therefore be much larger than physical address space
  - Allows address spaces to be shared by several processes
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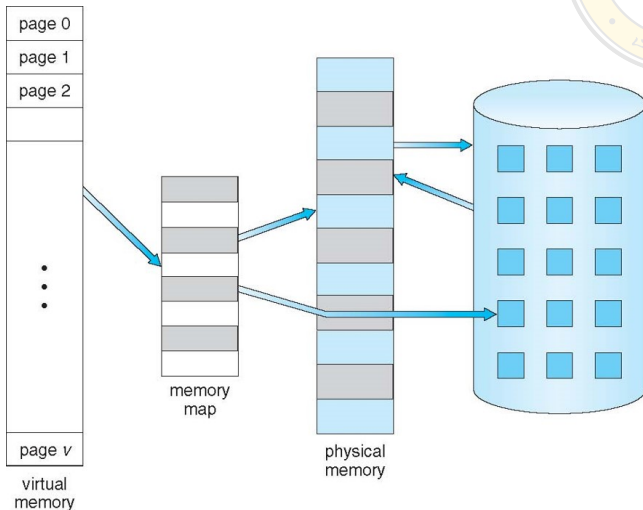


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- Virtual memory can be implemented via:
  - Demand paging
  - Demand segmentation

## Background

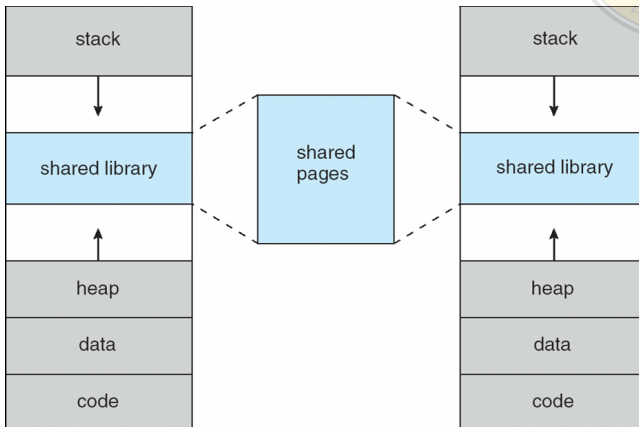
### *Virtual Memory that is Larger than Physical Memory*





## Background

### *Shared Library Using Virtual Memory*





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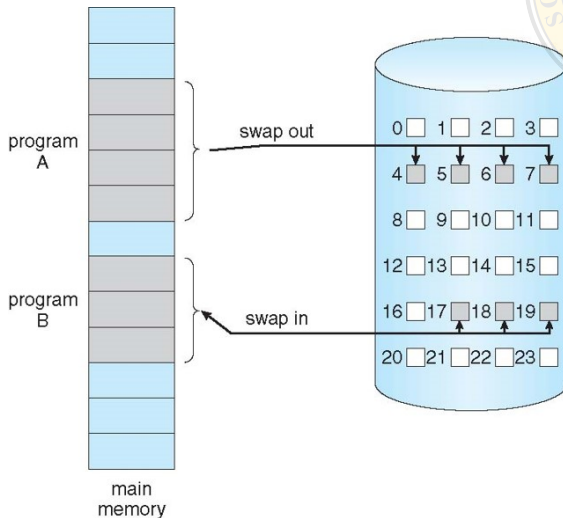
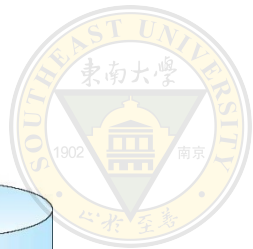
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  - not-in-memory  $\Rightarrow$  bring to memory



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- Page is needed  $\Rightarrow$  reference to it
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  - not-in-memory  $\Rightarrow$  bring to memory
- **Lazy swapper** — never swaps a page into memory unless page will be needed
  - Swapper that deals with pages is a **pager**

# Demand Paging







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## Basic Concepts

- With swapping, **pager** guesses which pages will be used before swapping out again



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- If page needed and not memory resident
  - Need to detect and load the page into memory from storage
    - » Without changing program behavior
    - » Without programmer needing to change code



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- If page needed and not memory resident
  - Need to detect and load the page into memory from storage
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- How to determine that set of pages?
  - Need new MMU functionality to implement demand paging



## Demand Paging

### Valid-Invalid Bit

- With each page table entry a valid-invalid bit is associated ( $v \Rightarrow$  in-memory — memory resident,  $i \Rightarrow$  not-in-memory)
  - Present bit
- Initially valid-invalid bit is set to  $i$  on all entries



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- Example of a page table snapshot:

Frame #	v/i
	v
	v
	i
	v
	i
	i
	i
...	



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- Example of a page table snapshot:

Frame #	v/i
	v
	v
	i
	v
	i
	i
	i
...	

- During MMU address translation, if valid-invalid bit in page table entry is  $i \Rightarrow$  page fault





## Demand Paging

Page Table when Some Pages are not in Main Memory

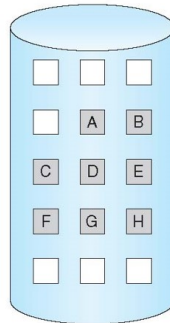
0	A
1	B
2	C
3	D
4	E
5	F
6	G
7	H

logical  
memory

valid-invalid bit		
frame		
0	4	v
1		i
2	6	v
3		i
4		i
5	9	v
6		i
7		i

page table

0
1
2
3
4
5
6
7
8
9
10
11
12
13
14
15





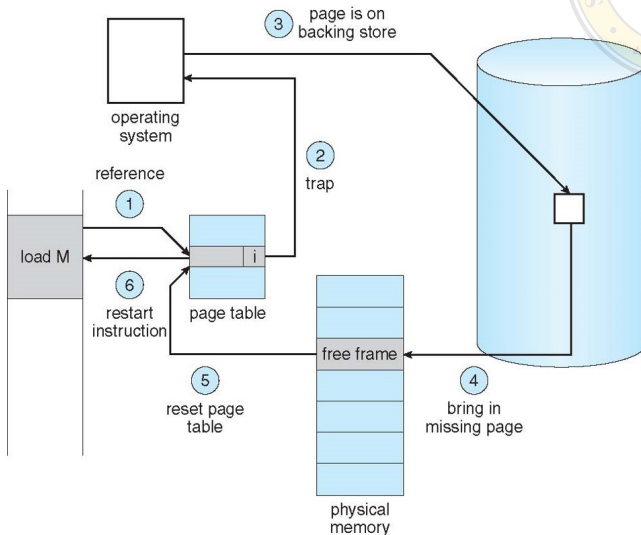
# Demand Paging

## Page Fault

- **Page fault** — If there is a reference to a page, first reference to that page will trap to operating system.
  1. Operating system looks at another table to decide:
    - » Invalid reference  $\Rightarrow$  abort
    - » Just not in memory
  2. Find free frame
  3. Swap page into frame via scheduled disk operation
  4. Reset tables to indicate page now in memory  
Set validation bit =  $v$
  5. Restart the instruction that caused the page fault

# Demand Paging

## Page Fault Handling





## Demand Paging

### Page-Fault Control Flow Algorithm (Hardware)

```
1  VPN = (VirtualAddress & VPN_MASK) >> SHIFT
2  (Success, TlbEntry) = TLB_Lookup(VPN)
3  if (Success == True)    // TLB hit
4      if (CanAccess(TlbEntry.ProtectBits) == True)
5          Offset = VirtualAddress & OFFSET_MASK
6          PhysAddr = (TlbEntry.PFN<<SHIFT) | Offset
7          AccessMemory(PhysAddr)
8      else
9          RaiseException(PROTECTION_FAULT)
10 else
11     // TLB miss
12     PTEAddr = PTBR + (VPN * sizeof(PTE))
13     PTE = AccessMemory(PTEAddr)
14     if (PTE.Valid == False)
15         RaiseException(SEGMENTATION_FAULT)
16     else if (CanAccess(PTE.ProtectBits) == False)
17         RaiseException(PROTECTION_FAULT)
18     else if (PTE.Present == True)
19         TLB_Insert(VPN, PTE.PFN, PTE.ProtectBits)
20         RetryInstruction()
21     else if (PTE.Present == False)
22         RaiseException(PAGE_FAULT)
```



## Demand Paging

### Page-Fault Control Flow Algorithm (Software)

```
1 PFN = FindFreePhysicalPage ()
2 if (PFN == -1)           // no free page found
3     PFN = EvictPage ()   // run replacement algorithm
4 DiskRead (PTE.DiskAddr, pfn)           // sleep (waiting for I/O)
5 PTE.present = True       // update page table with present
6 PTE.PFN = PFN           // bit and translation (PFN)
7 RetryInstruction ()      // retry instruction
```



## Demand Paging

### *Aspects of Demand Paging*

- Extreme case — start process with no pages in memory
  - OS sets instruction pointer to first instruction of process, non-memory-resident → page fault
  - And for every other process pages on first access
  - Pure demand paging



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- Actually, a given instruction could access multiple pages → multiple page faults
  - Consider fetch and decode of instruction which adds 2 numbers from memory and stores result back to memory
  - Pain decreased because of locality of reference



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  - Consider fetch and decode of instruction which adds 2 numbers from memory and stores result back to memory
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- Hardware support needed for demand paging
  - Page table with valid / invalid bit
  - Secondary memory (swap device with swap space)
  - Instruction restart

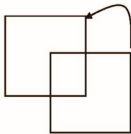




## Demand Paging

### *Instruction Restart*

- Consider an instruction that could access several different locations
  - block move



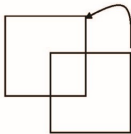
- auto increment/decrement location
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- auto increment/decrement location
- Restart the whole operation?
  - » What if source and destination overlap?



# Demand Paging

## *Performance of Demand Paging*

- Stages in Demand Paging
  1. Trap to the operating system
  2. Save the user registers and process state
  3. Determine that the interrupt was a page fault
  4. Check that the page reference was legal and determine the location of the page on the disk
  5. Issue a read from the disk to a free frame:
    - 5.1 Wait in a queue for this device until the read request is serviced
    - 5.2 Wait for the device seek and/or latency time
    - 5.3 Begin the transfer of the page to a free frame
  6. While waiting, allocate the CPU to some other user
  7. Receive an interrupt from the disk I/O subsystem (I/O completed)
  8. Save the registers and process state for the other user
  9. Determine that the interrupt was from the disk
  10. Correct the page table and other tables to show page is now in memory
  11. Wait for the CPU to be allocated to this process again
  12. Restore the user registers, process state, and new page table, and then resume the interrupted instruction

## Demand Paging

### *Performance of Demand Paging (cont.)*

- Besides the context switch





## Demand Paging

### *Performance of Demand Paging (cont.)*

- Besides the context switch
- Three major activities
  - Service the interrupt — careful coding means just several hundred instructions needed
  - Read the page — lots of time
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- Effective Access Time (EAT)

$$EAT = (1 - p) \times T_{memory\_access} + p \times (T_{page\_fault\_overhead} + T_{swap\_page\_out} + T_{swap\_page\_in})$$



## Demand Paging

### Demand Paging Example

- Memory access time = 200 nanoseconds
- Average page-fault service time = 8 milliseconds

$$\begin{aligned}EAT &= (1 - p) \times 200 + p \times (8 \text{ milliseconds}) \\&= (1 - p) \times 200 + p \times 8,000,000 \\&= 200 + p \times 7,999,800\end{aligned}$$

- If one access out of 1,000 causes a page fault, then  
 $EAT = 8.2 \text{ microseconds}$ . This is a slowdown by a factor of 40!!
- If want performance degradation < 10 percent

$$220 > 200 + 7,999,800 \times p \Rightarrow p < 0.0000025$$





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- Demand page in from program binary on disk, but discard rather than paging out when freeing frame
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  - Still need to write to swap space
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  - Still need to write to swap space
    - » Pages not associated with a file (like stack and heap)
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- Mobile systems
  - Typically don't support swapping
  - Instead, demand page from file system and reclaim read-only pages



## Demand Paging

### *Inverted Page Tables*

- Inverted page table no longer contains complete information about the logical address space of a process.
- That information is required if a referenced page is not currently in memory.
- Demand paging requires this information to process page faults.
- For the information to be available, an external page table (one per process) must be kept (can be on the backing store).
- A page fault may now cause the virtual memory manager to generate another page fault as it pages in the external page table it needs to locate the virtual page on the backing store.



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  - Pool should always have free frames for fast demand page execution

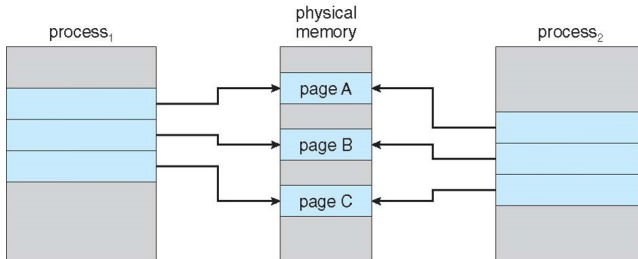


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- *vfork()* variation on *fork()* system call has parent suspend and child using copy-on-write address space of parent
  - Designed to have child call *exec()*
  - Very efficient

## Copy-on-Write

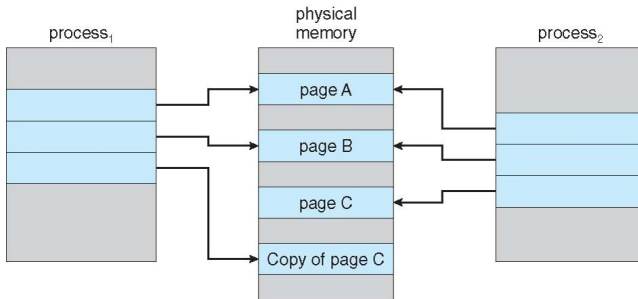
*Before Process<sub>1</sub> Modifies Page C*





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- Same page may be brought into memory several times



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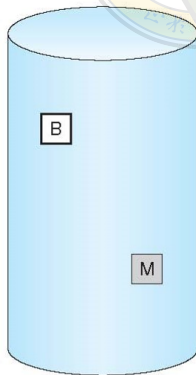
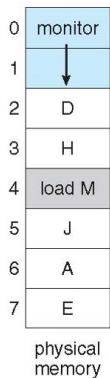
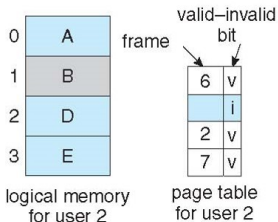
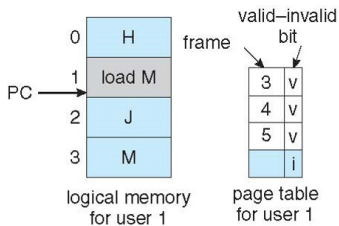


## Page Replacement

- Prevent **over-allocation** of memory by modifying page-fault service routine to include page replacement
- Use **modify (dirty) bit** to reduce overhead of page transfers – only modified pages are written to disk
- Page replacement completes separation between logical memory and physical memory — large virtual memory can be provided on a smaller physical memory

# Page Replacement

## Need For Page Replacement





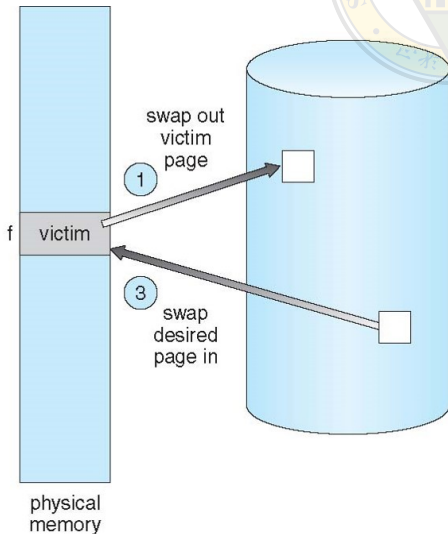
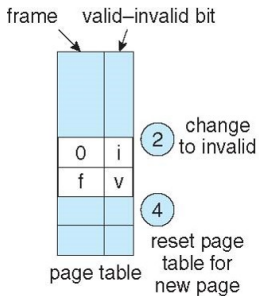
# Page Replacement

## *Basic Page Replacement*

1. Find the location of the desired page on disk
  2. Find a free frame:
    - If there is a free frame, use it
    - If there is no free frame, use a page replacement algorithm to select a victim frame
    - Write victim frame to disk if dirty
  3. Bring the desired page into the (newly) free frame; update the page and frame tables
  4. Continue the process by restarting the instruction that caused the trap
- Note now potentially 2 page transfers for page fault — increasing EAT

# Page Replacement

## Page Replacement





# Page Replacement

## *Page and Frame Replacement Algorithms*

- **Frame-allocation algorithm** determines
  - How many frames to give each process
  - Which frames to replace



# Page Replacement

## *Page and Frame Replacement Algorithms*

- **Frame-allocation algorithm** determines
  - How many frames to give each process
  - Which frames to replace
- **Page-replacement algorithm**
  - Want lowest page-fault rate on both first access and re-access





# Page Replacement

## *Page and Frame Replacement Algorithms*

- **Frame-allocation algorithm** determines
  - How many frames to give each process
  - Which frames to replace
- **Page-replacement algorithm**
  - Want lowest page-fault rate on both first access and re-access
- Evaluate algorithm by running it on a particular string of memory references (reference string) and computing the number of page faults on that string
  - String is just page numbers, not full addresses
  - Repeated access to the same page does not cause a page fault
  - Results depend on number of frames available



# Page Replacement

## *Page and Frame Replacement Algorithms*

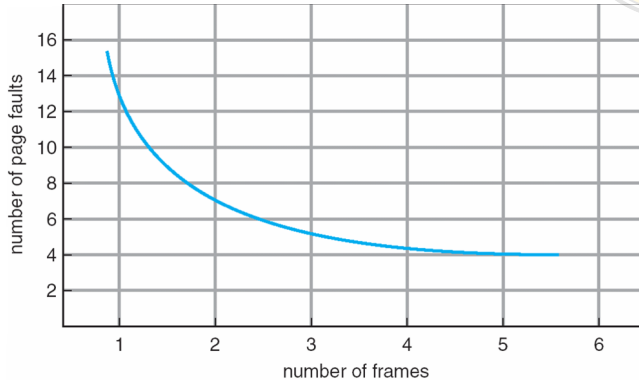
- **Frame-allocation algorithm** determines
  - How many frames to give each process
  - Which frames to replace
- **Page-replacement algorithm**
  - Want lowest page-fault rate on both first access and re-access
- Evaluate algorithm by running it on a particular string of memory references (reference string) and computing the number of page faults on that string
  - String is just page numbers, not full addresses
  - Repeated access to the same page does not cause a page fault
  - Results depend on number of frames available
- In all our examples, the **reference string** of referenced page numbers is

7, 0, 1, 2, 0, 3, 0, 4, 2, 3, 0, 3, 0, 3, 2, 1, 2, 0, 1, 7, 0, 1



## Page Replacement

### Graph of Page Faults Versus the Number of Frames





# Page Replacement

## Optimal Algorithm

- Bélády's MIN algorithm in 1966
- Replace page that will not be used for longest period of time
  - 3 frames, 9 page faults

reference string

7 0 1 2 0 3 0 4 2 3 0 3 2 1 2 0 1 7 0 1

7	7	7	2		2		2		2				2				7		
	0	0	0		0		0		0				0				0		
		1	1		3		3		3				1				1		

page frames



# Page Replacement

## Optimal Algorithm

- Bélády's MIN algorithm in 1966
- Replace page that will not be used for longest period of time
  - 3 frames, 9 page faults

reference string

7 0 1 2 0 3 0 4 2 3 0 3 2 1 2 0 1 7 0 1

7	7	7	2		2		2		2		2		2			7		
	0	0	0		0		0		0		0		0			0		
		1	1		3		3		3		3		1			1		

page frames

- How do you know this?
  - Can't read the future



## Page Replacement

### *Optimal Algorithm*

- Bélády's MIN algorithm in 1966
- Replace page that will not be used for longest period of time
  - 3 frames, 9 page faults

reference string

7 0 1 2 0 3 0 4 2 3 0 3 2 1 2 0 1 7 0 1

7	7	7	2		2		2		2				2				7		
	0	0	0		0		0		0				0				0		
		1	1		3		3		3				1				1		

page frames

- How do you know this?
  - Can't read the future
- Used for measuring how well your algorithm performs



## Page Replacement

### First-In-First-Out (FIFO) Algorithm

- Reference string: 7, 0, 1, 2, 0, 3, 0, 4, 2, 3, 0, 3, 2, 1, 2, 0, 1, 7, 0, 1
- 3 frames (3 pages can be in memory at a time per process)

reference string

7 0 1 2 0 3 0 4 2 3 0 3 2 1 2 0 1 7 0 1

7	7	7	2
	0	0	0
		1	1

2	2	4	4	4	0
3	3	3	2	2	2
1	0	0	0	3	3

0	0
1	1
3	2

7	7	7
1	0	0
2	2	1

page frames

- 15 page faults



## Page Replacement

### First-In-First-Out (FIFO) Algorithm

- Reference string: 7, 0, 1, 2, 0, 3, 0, 4, 2, 3, 0, 3, 2, 1, 2, 0, 1, 7, 0, 1
- 3 frames (3 pages can be in memory at a time per process)

reference string

7 0 1 2 0 3 0 4 2 3 0 3 2 1 2 0 1 7 0 1

7	7	7	2
	0	0	0
		1	1

2	2	4	4	4	0
3	3	3	2	2	2
1	0	0	0	3	3

0	0
1	1
3	2

7	7	7
1	0	0
2	2	1

page frames

- 15 page faults
- How to track ages of pages?
  - Just use a FIFO queue





## Page Replacement

### First-In-First-Out (FIFO) Algorithm

- Reference string: 7, 0, 1, 2, 0, 3, 0, 4, 2, 3, 0, 3, 0, 3, 2, 1, 2, 0, 1, 7, 0, 1
- 3 frames (3 pages can be in memory at a time per process)

reference string

7 0 1 2 0 3 0 4 2 3 0 3 0 3 2 1 2 0 1 7 0 1

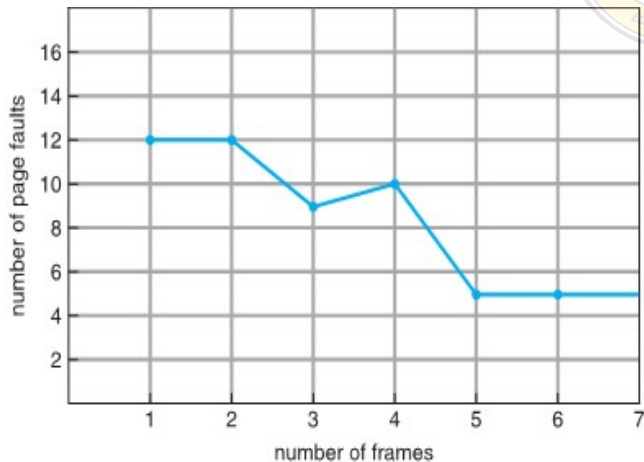
7	7	7	2																		
	0	0	0																		
			1	1																	

page frames

- 15 page faults
- How to track ages of pages?
  - Just use a FIFO queue
- Can vary by reference string: consider 1, 2, 3, 4, 1, 2, 5, 1, 2, 3, 4, 5
  - Adding more frames can cause more page faults! — **Bélády's Anomaly**

# Page Replacement

## *Bélády's Anomaly*





# Page Replacement

## *Least Recently Used (LRU) Algorithm*

- Use past knowledge rather than future
- Replace page that has not been used in the most amount of time
- Associate time of last use with each page

reference string

7 0 1 2 0 3 0 4 2 3 0 3 2 1 2 0 1 7 0 1

7	7	7	2		2		4	4	4	0		1		1		1
	0	0	0		0		0	0	3	3		3		0		0
		1	1		3		3	2	2	2		2		2		7

page frames

- 12 faults — better than FIFO but worse than OPT
- Generally good algorithm and frequently used



# Page Replacement

## Least Recently Used (LRU) Algorithm

- Use past knowledge rather than future
- Replace page that has not been used in the most amount of time
- Associate time of last use with each page

reference string

7 0 1 2 0 3 0 4 2 3 0 3 2 1 2 0 1 7 0 1

7	7	7	2		2		4	4	4	0		1		1		1
	0	0	0		0		0	0	3	3		3		0		0
		1	1		3		3	2	2	2		2		2		7

page frames

- 12 faults — better than FIFO but worse than OPT
- Generally good algorithm and frequently used
- But how to implement?



## Page Replacement

### *LRU Algorithm (contd.)*

- Counter implementation
  - Every page entry has a counter; every time page is referenced through this entry, copy the clock into the counter
  - When a page needs to be changed, look at the counters to find smallest value
    - » Search through table needed



## Page Replacement

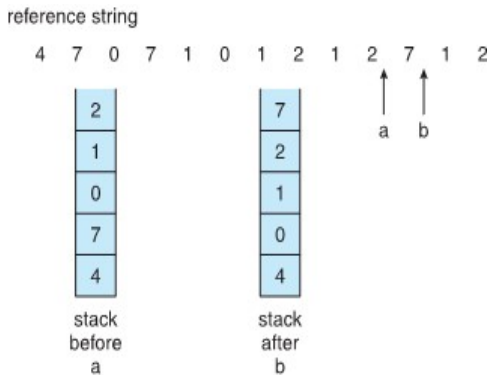
### *LRU Algorithm (contd.)*

- Counter implementation
  - Every page entry has a counter; every time page is referenced through this entry, copy the clock into the counter
  - When a page needs to be changed, look at the counters to find smallest value
    - » Search through table needed
- Stack implementation
  - Keep a stack of page numbers in a double link form:
  - Page referenced:
    - » move it to the top
    - » requires 6 pointers to be changed (why?)
  - But each update more expensive
  - No search for replacement (why?)
    - » LRU page is always at the bottom



## Page Replacement

*Use of a Stack to Record Most Recent Page References*





## Page Replacement

### LRU Algorithm (contd.)

- LRU and OPT are cases of **stack algorithms** that do **NOT** have **Bélády's Anomaly**
- Proof?
  - A stack algorithm is an algorithm for which it can be shown that **the set of pages in memory for  $n$  frames is always a subset of the set of pages that would be in memory with  $n + 1$  frames**. For LRU replacement, the set of pages in memory would be the  $n$  most recently referenced pages. If the number of frames is increased, these  $n$  pages will still be the most recently referenced and so will still be in memory.



# Page Replacement

## *LRU Approximation Algorithms*

- LRU needs special hardware and still slow





# Page Replacement

## *LRU Approximation Algorithms*

- LRU needs special hardware and still slow
- **Reference bit**
  - With each page associate a bit, initially = 0
  - When page is referenced bit set to 1
  - Replace any with reference bit = 0 (if one exists)
    - » We do not know the order, however



# Page Replacement

## *LRU Approximation Algorithms*

- LRU needs special hardware and still slow
- **Reference bit**
  - With each page associate a bit, initially = 0
  - When page is referenced bit set to 1
  - Replace any with reference bit = 0 (if one exists)
    - » We do not know the order, however
- **Additional-Reference-Bits Algorithm**
  - Keep an 8-bit byte for each page
  - At regular intervals shifts the bits right 1 bit, shift the reference bit into the high-order bit
  - Interpret these 8-bit bytes as unsigned integers, the page with lowest number is the LRU page



## Page Replacement

### *LRU Approximation Algorithms (contd.)*

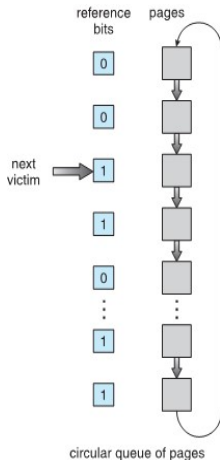
- **Second-chance algorithm**

- Generally FIFO, plus hardware-provided reference bit
- **Clock replacement**
- If page to be replaced has:
  - Reference bit = 0 → replace it
  - Reference bit = 1 then:
    - » set reference bit 0, leave page in memory
    - » replace next page, subject to same rules

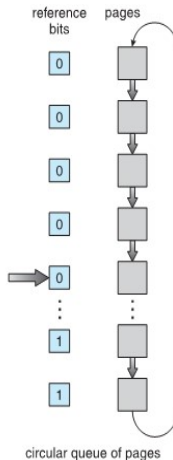


# Page Replacement

## Second-Chance (Clock) Page Replacement Algorithm



(a)



(b)



## Page Replacement

### *Enhanced Second-Chance Algorithm*

- Improve algorithm by using reference bit and modify bit (if available) in concert
- Take ordered pair (reference, modify)
  1. (0, 0) neither recently used nor modified — best page to replace
  2. (0, 1) not recently used but modified — not quite as good, must write out before replacement
    - » How can a page be modified without used?
  3. (1, 0) recently used but clean — probably will be used again soon
  4. (1, 1) recently used and modified — probably will be used again soon and need to write out before replacement
- When page replacement called for, use the clock scheme but use the four classes replace page in lowest non-empty class
- Might need to search circular queue several times



## Page Replacement

### Counting Algorithms

- Keep a counter of the number of references that have been made to each page
- **NOT** common
- **Least Frequently Used (LFU) Algorithm**: replaces page with smallest count
- **Most Frequently Used (MFU) Algorithm**: based on the argument that the page with the smallest count was probably just brought in and has yet to be used



## Page Replacement

### Page-Buffering Algorithms

- Keep a pool of free frames, always
  - Then frame available when needed, not found at fault time
  - Read page into free frame and select victim to evict and add to free pool
  - When convenient, evict victim
- Possibly, keep list of modified pages
  - When backing store otherwise idle, write pages there and set to non-dirty
- Possibly, keep free frame contents intact and note what is in them
  - If referenced again before reused, no need to load contents again from disk
  - Generally useful to reduce penalty if wrong victim frame selected





## Page Replacement

### *Applications and Page Replacement*

- All of these algorithms have OS guessing about future page access
- Some applications have better knowledge — e.g., databases
- Memory intensive applications can cause double buffering
  - OS keeps copy of page in memory as I/O buffer
  - Application keeps page in memory for its own work
- Operating system can give direct access to the disk, getting out of the way of the applications
  - Raw disk mode
- Bypasses buffering, locking, etc



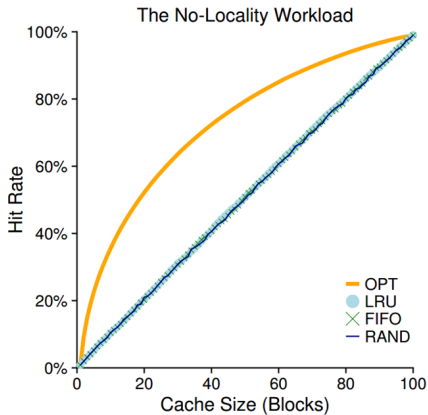
# Page Replacement

## *An Example Benchmark*

- Random Algorithm
  - Simply picks a random page to replace.
  - How Random does depends on the luck of the draw
- Workload examples
  - The no locality workload
    - » each reference is to a random page within the set of accessed pages.
  - The “80-20” locality workload
    - » 80% of the references are made to 20% of the pages (the “hot” pages); the remaining 20% of the references are made to the remaining 80% of the pages (the “cold” pages).
  - The Looping-Sequential Workload
    - » Loop for accesses to a sequence of pages.

# Page Replacement

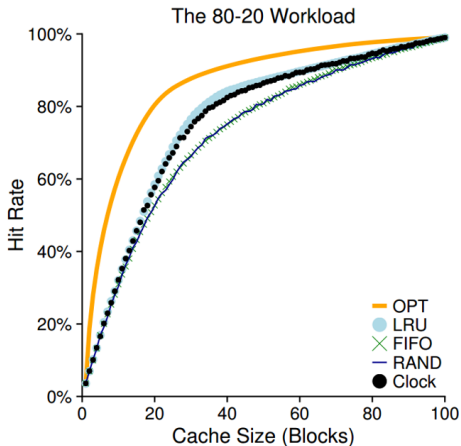
## Performance of Page Replacement Algorithms





## Page Replacement

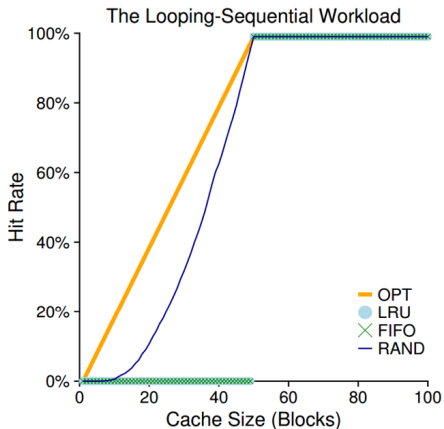
### Performance of Page Replacement Algorithms (contd.)





## Page Replacement

### Performance of Page Replacement Algorithms (contd.)





## Page Replacement

### *In Class Exercise*

Consider the reference page sequence is 1, 2, 3, 4, 1, 2, 5, 1, 2, 3, 4, 5, and the number of page frame is 3.

- (a) How many page faults for FIFO algorithm?
- (b) How many page faults for LRU algorithm?
- (c) How many page faults for OPT algorithm?



# Contents

1. Background
2. Demand Paging
3. Copy-on-Write
4. Page Replacement
- 5. Allocation of Frames**
6. Thrashing
7. Memory-Mapped Files
8. Allocating Kernel Memory
9. Other Considerations



## Allocation of Frames

- Each process needs **minimum** number of frames
- Examples:
  - IBM 370 — 6 pages to handle MVC instruction:
    - » instruction is 6 bytes, might span 2 pages
    - » 2 pages to handle from
    - » 2 pages to handle to
  - The MVC instruction may be the operand of an *EXECUTE* instruction
  - One (or more but limited) level indirect addressing
- **Maximum** of course is total frames in the system
- Two major allocation schemes
  - **Fixed allocation**
  - **Priority allocation**
- Many variations





## Allocation of Frames

### Fixed Allocation

- **Equal allocation** — For example, if there are 100 frames (after allocating frames for the OS) and 5 processes, give each process 20 frames
  - Keep some as free frame buffer pool
- **Proportional allocation** — Allocate according to the size of process
  - Dynamic as degree of multiprogramming, process sizes change

$m$  = total number of frames

$$m = 64$$

$s_i$  = size of process  $p_i$

$$s_1 = 10$$

$$s_2 = 127$$

$a_i$  = allocation for  $p_i = (s_i / \sum s_i) \times m$

$$a_1 = 10/137 \times 62 \approx 4$$

$$a_2 = 127/137 \times 62 \approx 57$$



# Allocation of Frames

## Priority Allocation

- Use a proportional allocation scheme using priorities rather than size
- If process  $P_i$  generates a page fault,
  - select for replacement one of its frames, OR
  - select for replacement a frame from a process with lower priority number



## Allocation of Frames

### *Global vs. Local Allocation*

- **Global replacement** — process selects a replacement frame from the set of all frames; one process can take a frame from another
  - But process cannot control its own page-fault rate
  - But greater throughput so more common
- **Local replacement** — each process selects from only its own set of allocated frames
  - More consistent per-process performance
  - But possibly underutilized memory



## Allocation of Frames

### Non-Uniform Memory Access (NUMA)

- So far all memory accessed equally
- Many systems are **NUMA** — speed of access to memory varies
  - Consider system boards containing CPUs and memory, interconnected over a system bus
- Optimal performance comes from allocating memory “close to” the CPU on which the thread is scheduled
  - And modifying the scheduler to schedule the thread on the same system board when possible
  - Solved by Solaris by creating **lggroups**
    - » Structure to track CPU / Memory low latency groups
    - » Used my schedule and pager
    - » When possible schedule all threads of a process and allocate all memory for that process within the lgroup



## Contents

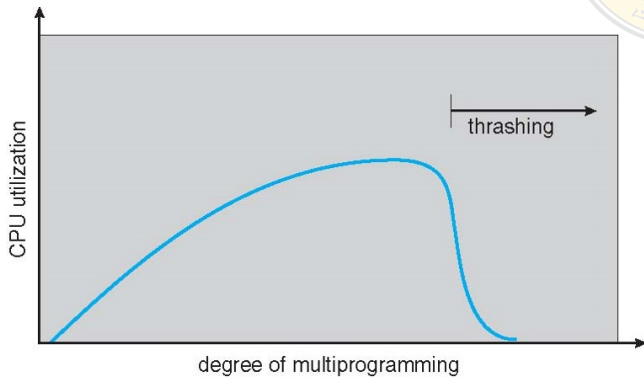
1. Background
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## Thrashing

- If a process does not have “enough” pages, the page-fault rate is very high
  - Page fault to get page
  - Replace existing frame
  - But quickly need replaced frame back
  - This leads to:
    - » Low CPU utilization
    - » Operating system thinking that it needs to increase the degree of multiprogramming
    - » Another process added to the system
- **Thrashing** — a process is busy swapping pages in and out

# Thrashing





# Thrashing

## *Demand Paging and Thrashing*

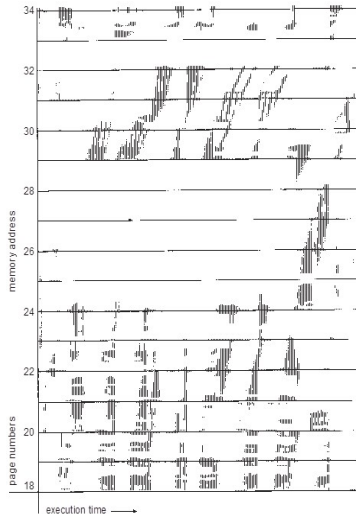
- Why does demand paging work?
- **Locality model**
  - Process migrates from one locality to another
  - Localities may overlap
- Why does thrashing occur?
- $\Sigma$  size of locality > total memory size
  - Limit effects by using local or priority page replacement





# Thrashing

## *Locality in a Memory-Reference Pattern*





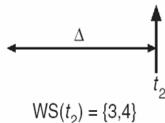
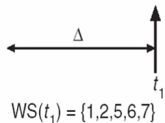
# Thrashing

## Working-Set Model

- $\Delta \equiv$  working-set window  $\equiv$  a fixed number of page references
- $WSS_i$  (working set size of Process  $P_i$ ) = total number of pages referenced in the most recent  $\Delta$  (varies in time)
  - if  $\Delta$  too small will not encompass entire locality
  - if  $\Delta$  too large will encompass several localities
  - if  $\Delta = \infty \Rightarrow$  will encompass entire program
- $D = \sum WSS_i \equiv$  total demand frames
  - Approximation of locality
- if  $D > m \Rightarrow$  Thrashing
- Policy if  $D > m$ , then suspend or swap out one of the processes

page reference table

... 2 6 1 5 7 7 7 5 1 6 2 3 4 1 2 3 4 4 4 3 4 3 4 4 4 1 3 2 3 4 4 4 3 4 4 4 ...





# Thrashing

## Keeping Track of the Working Set

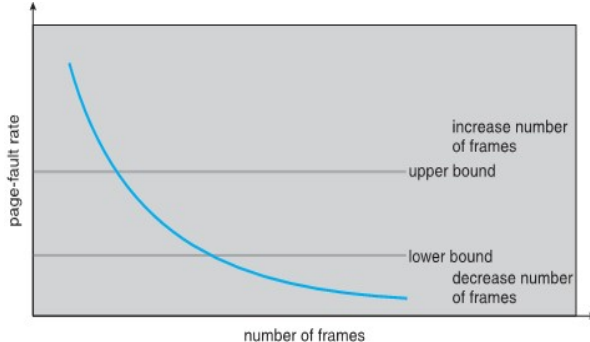
- Approximate with interval timer interrupt + a reference bit
- Example:  $\Delta = 10,000$ 
  - Timer interrupts after every 5000 time units
  - Keep in memory 2 bits for each page
  - Whenever a timer interrupts copy and sets the values of all reference bits to 0
  - If one of the bits in memory = 1  $\Rightarrow$  page in working set
- Why is this not completely accurate?
- Improvement = 10 bits and interrupt every 1000 time units
  - cost to service the interrupts is higher



# Thrashing

## Page-Fault Frequency

- More direct approach than WSS
- Establish “acceptable” **page-fault frequency** (PFF) rate and use local replacement policy
  - If actual rate too low, process loses frame
  - If actual rate too high, process gains frame

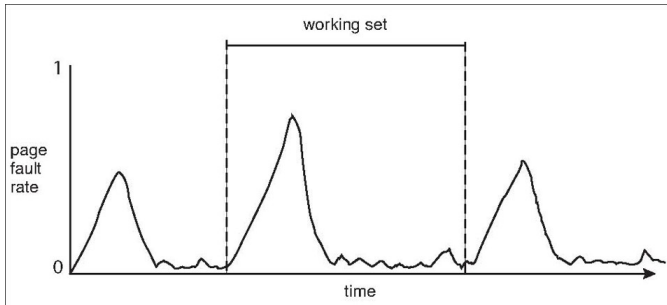




# Thrashing

## Working Sets and Page Fault Rates

- Direct relationship between working set of a process and its page-fault rate
- Working set changes over time
- Peaks and valleys over time





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## Memory-Mapped Files

- Memory-mapped file I/O allows file I/O to be treated as routine memory access by mapping a disk block to a page in memory
- A file is initially read using demand paging
  - A page-sized portion of the file is read from the file system into a physical page
  - Subsequent reads/writes to/from the file are treated as ordinary memory accesses
- Simplifies and speeds file access by driving file I/O through memory rather than *read()* and *write()* system calls
- Also allows several processes to map the same file allowing the pages in memory to be shared
- But when does written data make it to disk?
  - Periodically and / or at file *close()* time
  - For example, when the pager scans for dirty pages



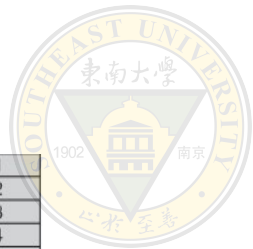
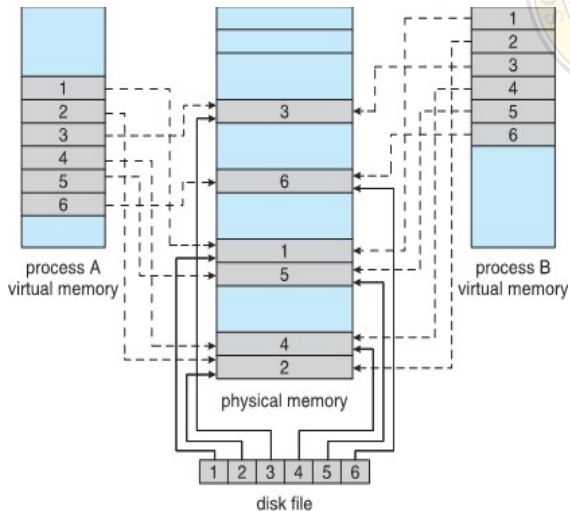
## Memory-Mapped Files

### *Memory-Mapped File Technique for All I/O*

- Some OSes use memory mapped files for standard I/O
- Process can explicitly request memory mapping a file via `mmap()` system call
  - Now file mapped into process address space
- For standard I/O (`open()`, `read()`, `write()`, `close()`), `mmap` anyway
  - But map file into kernel address space
  - Process still does `read()` and `write()`
    - » Copies data to and from kernel space and user space
  - Uses efficient memory management subsystem
    - » Avoids needing separate subsystem
- COW can be used for read/write non-shared pages
- Memory mapped files can be used for shared memory (although again via separate system calls)



# Memory-Mapped Files





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## Allocating Kernel Memory

- Treated differently from user memory
- Often allocated from a free-memory pool
  - Kernel requests memory for structures of varying sizes
  - Some kernel memory needs to be contiguous
    - » I.e. for device I/O



# Allocating Kernel Memory

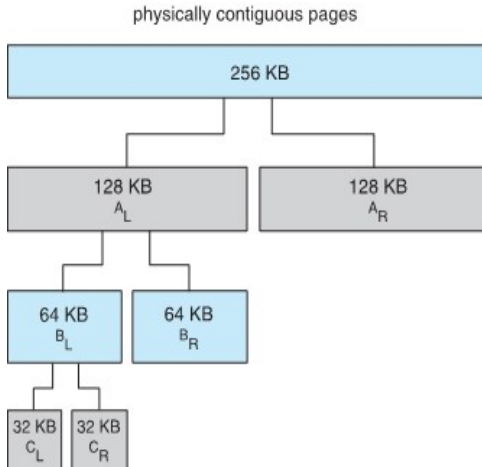
## Buddy Allocator

- Allocates memory from fixed-size segment consisting of physically-contiguous pages
- Memory allocated using power-of-2 allocator
  - Satisfies requests in units sized as power of 2
  - Request rounded up to next highest power of 2
  - When smaller allocation needed than is available, current chunk split into two buddies of next-lower power of 2
    - » Continue until appropriate sized chunk available
- For example, assume 256KB chunk available, kernel requests 21KB
  - Split into  $A_L$  and  $A_R$  of 128KB each
  - One further divided into  $B_L$  and  $B_R$  of 64KB
  - One further into  $C_L$  and  $C_R$  of 32KB each — one used to satisfy request
- Advantage — quickly coalesce unused chunks into larger chunk
- Disadvantage — fragmentation



## Allocating Kernel Memory

### Buddy Allocator (contd.)





# Allocating Kernel Memory

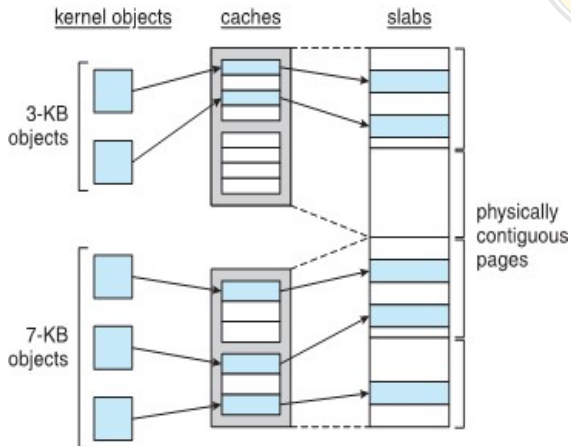
## Slab Allocator

- Alternate strategy
- **Slab** is one or more physically contiguous pages
- **Cache** consists of one or more slabs
- Single cache for each unique kernel data structure
  - Each cache filled with **objects** — instantiations of the data structure
- When cache created, filled with objects marked as *free*
- When structures stored, objects marked as *used*
- If slab is full of used objects, next object allocated from empty slab
  - If no empty slabs, new slab allocated
- Benefits include no fragmentation, fast memory request satisfaction



## Allocating Kernel Memory

### Slab Allocator (contd.)





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## Other Considerations

### Prepaging

- To reduce the large number of page faults that occurs at process startup
- Prepage all or some of the pages a process will need, before they are referenced
- But if prepagged pages are unused, I/O and memory was wasted
- Assume  $s$  pages are prepagged and  $\alpha$  of the pages is used
  - Is cost of  $s \times \alpha$  save pages faults  $>$  or  $<$  than the cost of prepaging  $s \times (1 - \alpha)$  unnecessary pages?
  - $\alpha$  near zero  $\Rightarrow$  prepaging loses



## Other Considerations

### Program Structure

```
1  int [128,128] data;
```

- Each row is stored in one page
- Program #1:  $128 \times 128 = 16,384$  page faults

```
1  for (j = 0; j < 128; j ++)  
2      for (i = 0; i < 128; i ++)  
3          data[i, j] = 0;
```

- Program #2: 128 page faults

```
1  for (i = 0; i < 128; i ++)  
2      for (j = 0; j < 128; j ++)  
3          data[i, j] = 0;
```



## Other Considerations

### *I/O interlock*

- I/O Interlock — Pages must sometimes be locked into memory
- Consider I/O — Pages that are used for copying a file from a device must be locked from being selected for eviction by a page replacement algorithm
- Pinning of pages to lock into memory

