## 习题

$$1.(1) \int_0^1 \frac{1}{1+x^2} dx$$

$$(2)\int_0^1 \sin \pi x dx$$

$$5.(2) \diamondsuit f(x) = 2^{-\sin x}$$

$$\because x \in [0,\pi]$$

$$\therefore \sin x \in [0, 1]$$

$$6.\int_{n}^{n+1} e^{-x^{2}} dx = e^{-\xi^{2}} \cdot 1 \to 0(\xi > n)$$

$$7.3 \int_{1}^{\frac{2}{3}} f(x) dx = f(\xi) = (0)$$

由罗尔定理可得

$$8.(1)$$
假设 $\exists x_0 \in [a,b]$ 使得 $f(x_0) > 0$ 

又
$$:: f(x)$$
连续,

$$\therefore \exists \varepsilon > 0$$
使得 $f(x)$ 在 $(x_0 - \varepsilon, x_0 + \varepsilon)$ 

上有
$$f(x) > 0$$
,

$$\int_{a}^{b} f(x)dx = \int_{a}^{x_{0}-\varepsilon} f(x)dx + \int_{x_{0}-\varepsilon}^{x_{0}+\varepsilon} f(x)dx + \int_{x_{0}+\varepsilon}^{b} f(x)dx > 0$$

与假设不符

$$(2)$$
令 $F(x) = f(x) - g(x)$ 由 $(1)$ 的结论可证