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Check one:

☒ I completed this assignment without assistance or external resources.

☐ I completed this assignment with assistance from ____
and/or using these external resources: ____

2A: All strings (over $\{0,1\}$) consisting of a substring w followed by its reverse.

$$S = 0S0 \mid 1S1 \mid \varepsilon$$

Derivation for 010010:

$$S \rightarrow 0S0 \rightarrow 01S10 \rightarrow 010S010 \rightarrow 010\varepsilon010 \rightarrow 010010$$

2B: All strings (over $\{a,b,c\}$) of the form $a^i b^j c^k$: an equal number of as and bs, followed by any number of cs.

$$S1 = aS1b \mid \varepsilon$$

$$S2 = S2c \mid \varepsilon$$

$$S = S1S2$$

(Example) Derivation of aabbccccc:

$$S \rightarrow S1S2 \rightarrow aS1bS2c \rightarrow aaS1bbS2cc \rightarrow aa\varepsilon bbS2ccc \rightarrow aabbS2cccc \rightarrow aabb\varepsilon cccc \rightarrow aabbccccc$$

2C: All strings (over $\{a,b,c\}$) of the form $a^i b^j c^k$: any number of as, followed by an equal number of bs and cs.

$$S1 = aS1 \mid \varepsilon$$

$$S2 = bS2c \mid \varepsilon$$

$$S = S1S2$$

(Example) Derivation of aaaabbcc:

$$S \rightarrow S1S2 \rightarrow aS1bS2c \rightarrow aaS1bbS2cc \rightarrow aaaS1bb\varepsilon cc \rightarrow aaaaS1bbcc \rightarrow aaaa\varepsilon bbcc \rightarrow aaaabbcc$$

2D: Give two distinct grammars that produce the strings described by the regular expression $(ab)^*$

Grammar 1:

$S = Sab \mid \epsilon$

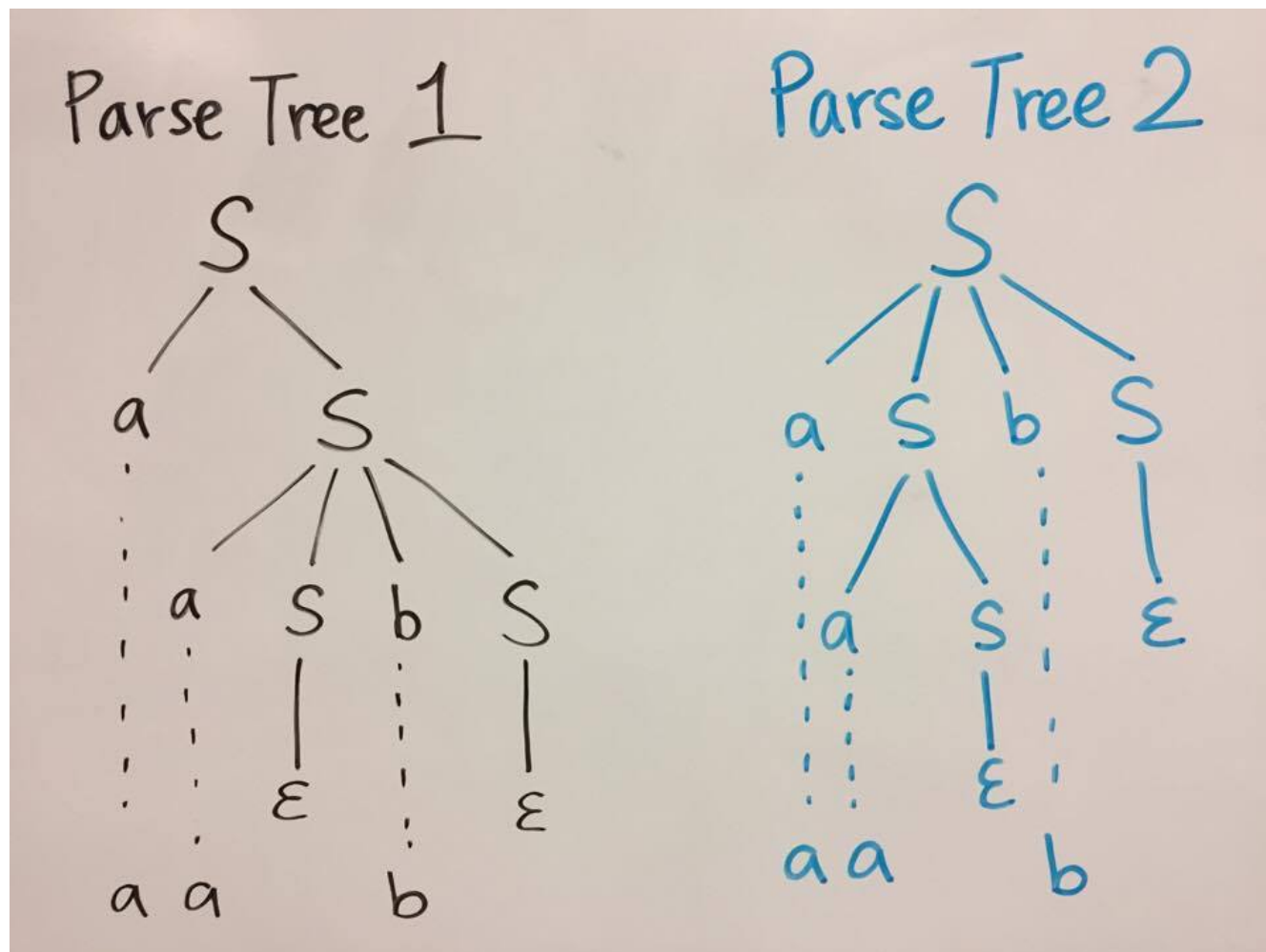
Grammar 2:

$S1 = S1a \mid aS1 \mid \epsilon$

$S2 = S2b \mid bS2 \mid \epsilon$

$S = S1S2$

4A:



4B: Leftmost derivations:

Derivation 1:

$S \rightarrow aS \rightarrow aaSbS \rightarrow aa\epsilon bS \rightarrow aab\epsilon \rightarrow aab$

Derivation 2:

$S \rightarrow aSbS \rightarrow aaSbS \rightarrow aa\epsilon bS \rightarrow aabS \rightarrow aab\epsilon \rightarrow aab$

4C: Rightmost derivations:

Derivation 1:

$S \rightarrow aSbS \rightarrow aSb\epsilon \rightarrow aaSb \rightarrow aa\epsilon b \rightarrow aab$

Derivation 2:

$S \rightarrow aS \rightarrow aaSbS \rightarrow aaSb\epsilon \rightarrow aa\epsilon b \rightarrow aab$