

HW3 CS 314

1.

LL(1) parsing definition

($A ::= \alpha$ and $A ::= \beta$) implies $FIRST+(\alpha) \cap FIRST+(\beta) = \emptyset$

Therefore, we need to check First+ set for non-terminal symbol that have 2 rules, and its rules are mutually disjoint.

– we need to check $\langle \text{morestmts} \rangle$, $\langle \text{stmt} \rangle$, $\langle \text{expr} \rangle$, $\langle \text{var} \rangle$, $\langle \text{digit} \rangle$

1. $\langle \text{program} \rangle ::= \text{prog} \langle \text{block} \rangle$.
2. $\langle \text{block} \rangle ::= \text{begin} \langle \text{stmtlist} \rangle \text{end}$
3. $\langle \text{stmtlist} \rangle ::= \langle \text{stmt} \rangle \langle \text{morestmts} \rangle$
4. $\langle \text{morestmts} \rangle ::= ; \langle \text{stmtlist} \rangle \mid$
5. ϵ
6. $\langle \text{stmt} \rangle ::= \langle \text{assign} \rangle \mid$
7. $\langle \text{ifstmt} \rangle \mid$
8. $\langle \text{repeatstmt} \rangle \mid$
9. $\langle \text{block} \rangle$
10. $\langle \text{assign} \rangle ::= \langle \text{var} \rangle = \langle \text{expr} \rangle$
11. $\langle \text{ifstmt} \rangle ::= \text{if } \langle \text{testexpr} \rangle \text{ then } \langle \text{stmt} \rangle \text{ else } \langle \text{stmt} \rangle$
12. $\langle \text{repeatstmt} \rangle ::= \text{repeat} \langle \text{stmt} \rangle \text{ until } \langle \text{testexpr} \rangle$
13. $\langle \text{testexpr} \rangle ::= \langle \text{var} \rangle \leq \langle \text{expr} \rangle$
14. $\langle \text{expr} \rangle ::= + \langle \text{expr} \rangle \langle \text{expr} \rangle \mid$
15. $- \langle \text{expr} \rangle \langle \text{expr} \rangle \mid$
16. $* \langle \text{expr} \rangle \langle \text{expr} \rangle \mid$
17. $\langle \text{var} \rangle \mid$
18. $\langle \text{digit} \rangle$
19. $\langle \text{var} \rangle ::= a \mid$
20. $b \mid$
21. $c \mid$

22. $\langle \text{digit} \rangle ::= 0 \mid$

23. $1 \mid$

24. $2 \mid$

$\langle \text{morestmts} \rangle$

rule 4:

$\text{First}+(\langle \text{stmtlist} \rangle) = \text{First}(;) = \{;\}$

rule 5:

$\text{First}(\epsilon) = \{\epsilon\} - \{\epsilon\} + \text{Follow}(\langle \text{morestmts} \rangle)$
 $= \{\text{end}\}$

Therefore, $\text{First}+$ set are disjoint

$\langle \text{stmt} \rangle$

rule 6:

$\text{First}(\langle \text{assign} \rangle) = \text{First}(\langle \text{var} \rangle) = \text{First}(\langle \text{var} \rangle) = \{a, b, c\}$

rule 7:

$\text{First}(\langle \text{ifstmt} \rangle) = \text{First}(\text{if}) = \{\text{if}\}$

rule 8:

$\text{First}(\langle \text{repeatstmt} \rangle) = \text{First}(\text{repeat}) = \{\text{repeat}\}$

rule 9:

$\text{First}(\langle \text{block} \rangle) = \text{First}(\text{begin}) = \{\text{begin}\}$

Therefore, $\text{First}+$ set are disjoint

$\langle \text{expr} \rangle$

rule 14:

$\text{First}+(\langle \text{expr} \rangle \langle \text{expr} \rangle) = \text{First}(+) = \{+\}$

rule 15:

$\text{First}+(\langle \text{expr} \rangle \langle \text{expr} \rangle) = \text{First}(-) = \{-\}$

rule 16:

$\text{First+} (*\langle\text{expr}\rangle\langle\text{expr}\rangle) = \text{First+}(*) = \{*\}$

rule 17:

$\text{First+} (\langle\text{var}\rangle) = \text{First}(\langle\text{var}\rangle) = \{a,b,c\}$

rule 18:

$\text{First+} (\langle\text{digit}\rangle) = \text{First}(\langle\text{digit}\rangle) = \{0,1,2\}$

Therefore, First+ set are disjoint

$\langle\text{var}\rangle$

rule 19:

$\text{First+}(a) = \{a\}$

rule 20:

$\text{First+}(b) = \{b\}$

rule 21:

$\text{First+}(c) = \{c\}$

Therefore, First+ set are disjoint

$\langle\text{digit}\rangle$

rule 22:

$\text{First+}(0) = \{0\}$

rule 23:

$\text{First+}(1) = \{1\}$

rule 24:

$\text{First+}(2) = \{2\}$

Therefore, First+ set are disjoint

Therefore, this grammar is LL(1)

2.parse table

$\langle\text{program}\rangle$

rule 1:

$\text{First}+(\text{prog } \langle \text{block} \rangle .) = \text{First}+(\text{prog}) = \{\text{prog}\}$

$\langle \text{block} \rangle$

rule 2:

$\text{First}+(\text{begin} \langle \text{stmtlist} \rangle \text{end}) = \text{First}+(\text{begin}) = \{\text{begin}\}$

$\langle \text{stmtlist} \rangle$

rule 3:

$\text{First}+(\langle \text{stmt} \rangle \langle \text{morestmts} \rangle) = \text{First}+(\langle \text{stmt} \rangle) = \text{First}+(\langle \text{assign} \rangle) + \text{First}(\langle \text{ifstmt} \rangle) + \text{First}(\langle \text{repeatstmt} \rangle) + \text{First}(\langle \text{block} \rangle)$

$= \{a, b, c, \text{if}, \text{repeat}, \text{begin}\}$

$\langle \text{assign} \rangle$

rule 10:

$\text{First}+(\langle \text{var} \rangle = \langle \text{expr} \rangle) = \text{First}(\langle \text{var} \rangle) = \{a, b, c\}$

$\langle \text{ifstmt} \rangle$

rule 11:

$\text{First}+(\text{if} \langle \text{testexpr} \rangle \text{then} \langle \text{stmt} \rangle \text{else} \langle \text{stmt} \rangle) = \text{First}(\text{if}) = \{\text{if}\}$

$\langle \text{repeatstmt} \rangle$

rule 12:

$\text{First}+(\text{repeat} \langle \text{stmt} \rangle \text{until} \langle \text{testexpr} \rangle) = \text{First}(\text{repeat}) = \{\text{repeat}\}$

$\langle \text{testexpr} \rangle$

rule 13:

$\text{First}(\langle \text{var} \rangle <= \langle \text{expr} \rangle) = \text{First}(\langle \text{var} \rangle) = \{a, b, c\}$

	prog	begin	end	;	if	then	else	repeat	until
Program	1								
Block		2							
Stmtlist		3			3			3	
Morestmts			5	4					
Stmt		9			7			8	
Assign									
Ifstmt					11				
Repeatstmt								12	
Testexpr									
expr									
Var									
digit									

	<=	+	-	*	=	a	b	c	0	1	2	.	eof
Program													
Block													
Stmtlist						3	3	3					
Morestmts													
Stmt						6	6	6					
Assign						10	10	10					
Ifstmt													
Repeatstmt													
Testexpr						13	13	13					
expr		14	15	16		17	17	17	18	18	18		
Var						19	20	21					
digit									22	23	24		

3+4 (red line is for #4)

```
main() {  
    int num_biop = 0;  
  
    token := next_token();  
    call program();  
    if (token == eof) {  
        print ('number of binary operators:' + num_biop)  
        accept;  
    }else{  
        error;  
    }  
}
```

```
program(){  
    switch token{  
        case 'prog':  
            token := next_token();  
            call block()  
            if token == '{'  
                token := next_token();  
                break;  
            }else{  
                error;  
                exit;  
            }  
        default:  
            error; exit;  
    }  
}
```

```
}
```

```
block(){
```

```
  switch token{
```

```
    case 'begin':
```

```
      token := next_token();
```

```
      call stmtlist();
```

```
      if token == 'end'{
```

```
        token := next_token();
```

```
        break;
```

```
      }else{
```

```
        error;
```

```
        exit;
```

```
      }
```

```
    default:
```

```
      error; exit;
```

```
  }
```

```
}
```

```
stmtlist(){
```

```
  switch token{
```

```
    case 'begin':
```

```
    case 'if':
```

```
    case 'repeat':
```

```
    case 'a':
```

```
    case 'b':
```

```
    case 'c':
```

```
      call stmt();
```

```
      call morestmts();
```

```
        break;
    default:
        error; exit;
    }
}
```

```
morestmts(){
    switch token{
        case 'end':
            break;
        case ';':
            token := next_token();
            call stmtlist();
            break;
        default:
            error; exit;
    }
}
```

```
stmt(){
    switch token{
        case 'begin':
            call block();
            break;
        case 'if':
            call ifstmt();
            break;
        case 'repeat':
            call repeatstmt();
```



```
        break;
    case 'a':
    case 'b':
    case 'c':
        call var();
        break;
    default:
        error; exit;
    }
}
```

```
assign(){
    switch token{
        case 'a':
        case 'b':
        case 'c':
            call var();
            if token == '='{
                token := next_token();
                call expr();
                break;
            }else{
                error;
                exit;
            }
        default:
            error; exit;
    }
}
```

```
ifstmt(){  
    switch token{  
        case 'if':  
            token := next_token();  
            call testexpr();  
            if token != 'then'{  
                error; exit;  
            }  
            token := next_token();  
            call stmt();  
            if token != 'else'{  
                error; exit;  
            }  
            token := next_token();  
            call stmt();  
            break;  
        default:  
            error; exit;  
    }  
}
```

```
repeatstmt(){  
    switch token{  
        case 'repeat':  
            token := next_token();  
            call stmt();  
            if token != 'until'{  
                error; exit;  
            }  
    }  
}
```

```
    }  
    token := next_token();  
    call testexpr();  
    break;  
default:  
    error; exit;  
}  
}
```

```
testexpr(){  
    switch token{  
        case 'a':  
        case 'b':  
        case 'c':  
            call var();  
            if token != '<=' {  
                error; exit;  
            }  
            token := next_token();  
            call expr();  
            num_biop++;  
            break;  
        default:  
            error; exit;  
    }  
}
```

```
expr(){  
    switch token{
```

```
case '+':  
case '-':  
case '*':  
    token := next_token();  
    call expr();  
    call expr();  
    num_biop++;  
    break;  
case 'a':  
case 'b':  
case 'c':  
    call var();  
    break;  
case '0':  
case '1':  
case '2':  
    call digit();  
    break;  
default:  
    error; exit;  
}  
}
```

```
var(){  
    case 'a':  
    case 'b':  
    case 'c':  
        token:= next_token();  
        break;
```

```
    default:
        error; exit;
    }
}

digit(){
    case '0':
    case '1':
    case '2':
        token:= next_token();
        break;
    default:
        error; exit;
    }
}
```