

現代控制理論 HW6

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1.

$$\dot{x}_1 = x_2$$

$$\dot{x}_2 = x_3$$

$$\dot{x}_3 = \alpha (x_1^2 \sin(x_2) + x_2^2 \sin(x_3)) + (x_1 + x_3^2) \cos(x_3) + u + d(t)$$

$$\text{令 } f = x_3 + 2\lambda x_2 + \lambda^2 x_1$$

則 \dot{f}_{dot}

$$= \dot{x}_3 + 2\lambda \dot{x}_2 + \lambda^2 \dot{x}_1$$

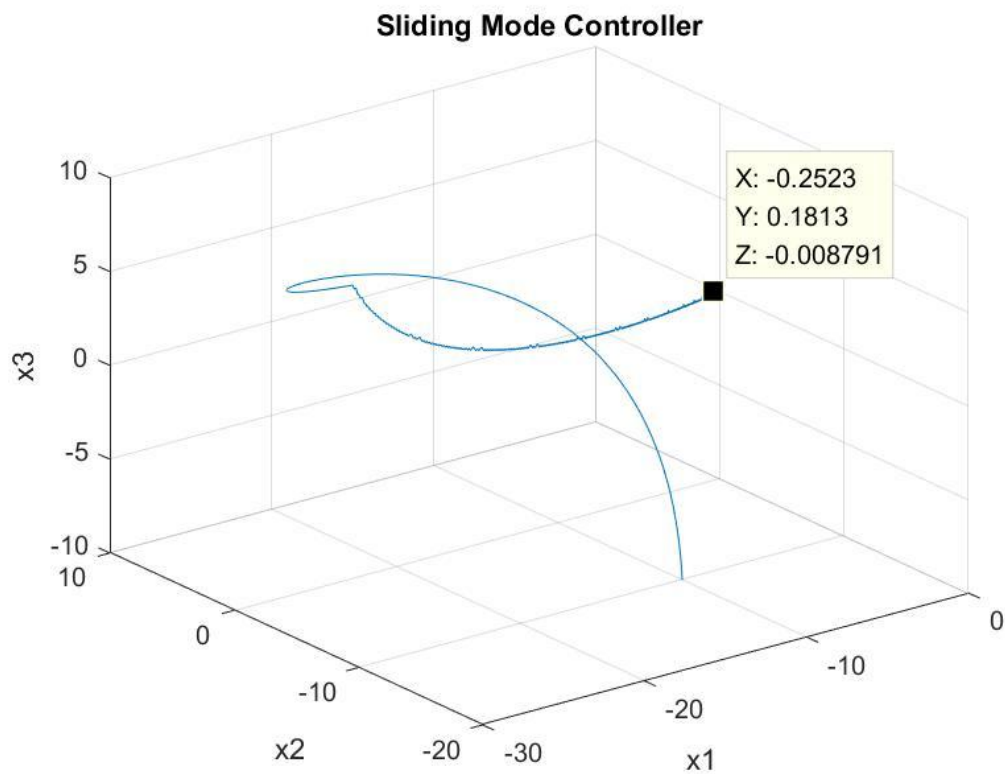
$$= \dot{x}_3 + 2\lambda x_3 + \lambda^2 x_2$$

$$= \alpha (x_1^2 \sin(x_2) + x_2^2 \sin(x_3)) + (x_1 + x_3^2) \cos(x_3) + u + d(t) + 2\lambda x_3 + \lambda^2 x_2$$

$$= -\text{sign}(f) * K$$

$$\text{設計 } u = -\text{sign}(f) * K - (\alpha (x_1^2 \sin(x_2) + x_2^2 \sin(x_3)) + (x_1 + x_3^2) \cos(x_3) + 2\lambda x_3 + \lambda^2 x_2)$$

模擬結果(初值(-10,-10,-10), $K=10$, $\lambda=1$) :



程式碼：

```
clc;clear;

delta=0.01;
totalTime=10;
totalStep=totalTime/delta;

x1array=[1:totalStep]*0;x2array=x1array;x3array=x1array;
x1array(1)=-10;x2array(1)=-10;x3array(1)=-10;%init condition
alpha=0.9;
K=10;lambda=1;
for i=1:totalStep
    x1=x1array(i);x2=x2array(i);x3=x3array(i);

    f=x3+2*lambda*x2+lambda^2*x1;

    u=-sign(f)*K-(alpha*(x1^2*sin(x2)+x2^2*sin(x3))+(x1+x3^2)*cos(x3)+2*lambda*x3+lambda^2*x2);

    d(i)=0.2*sin(i)+0.1*cos(5*i+pi);
    x1_dot=x2;
    x2_dot=x3;

    x3_dot=alpha*(x1^2*sin(x2)+x2^2*sin(x3))+(x1+x3^2)*cos(x3)+u+d(i);

    x1array(i+1)=x1+x1_dot*delta;
    x2array(i+1)=x2+x2_dot*delta;
    x3array(i+1)=x3+x3_dot*delta;
end

plot3(x1array,x2array,x3array);
grid on;

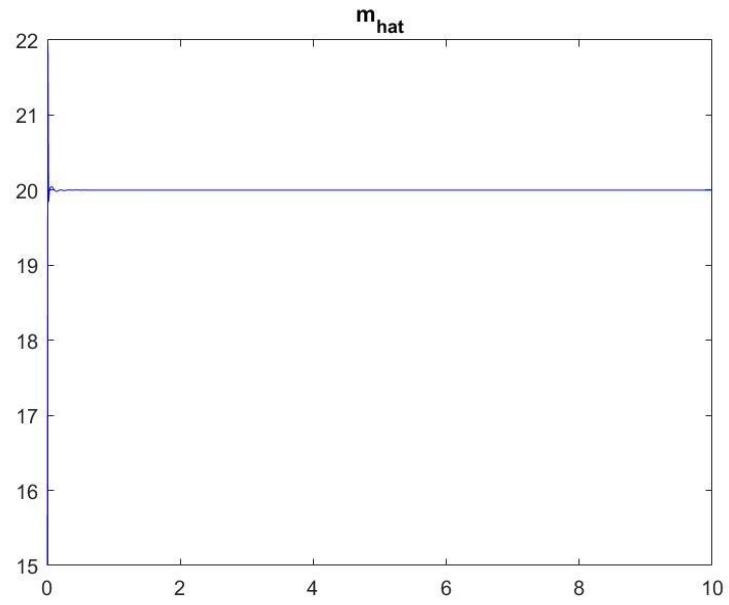
xlabel('x1');
ylabel('x2');
zlabel('x3');
title('Sliding Mode Controller');
```

2.

測試1：

```
disturbance(i)=10*(-1+rand);
```

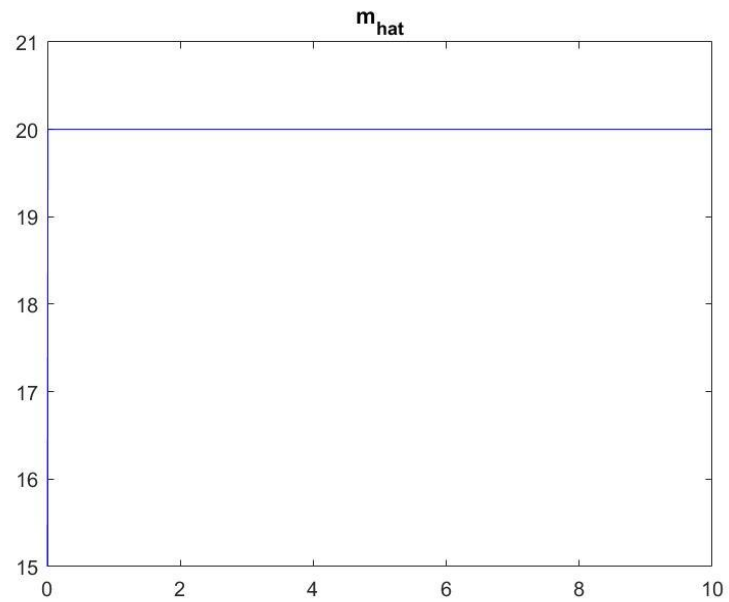
```
noise(i)=0.001*sin(25*i)+0.005*cos(100*i+pi);
```



測試2：

```
disturbance(i)=10*(-1+rand);
```

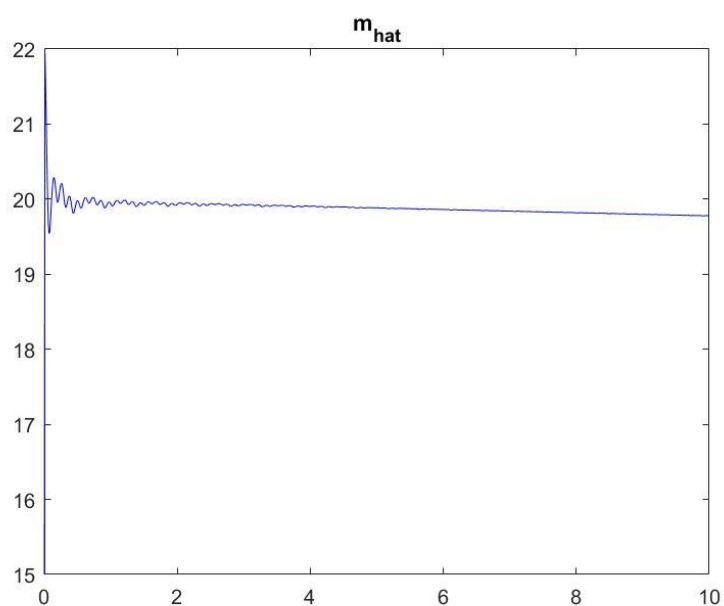
```
noise(i)=0
```



測試3：

$\text{disturbance}(i)=0$

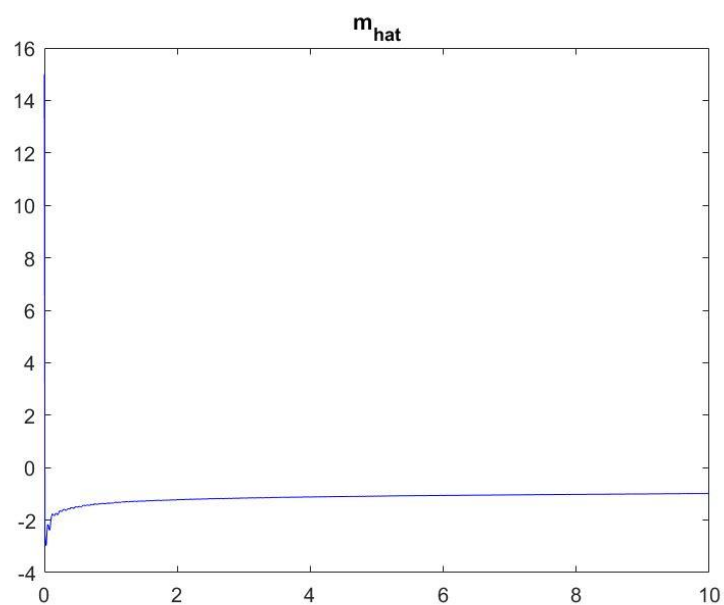
$\text{noise}(i)=0.001*\sin(25*i)+0.005*\cos(100*i+\pi)$;



測試4(noise很大則 m_{hat} 無法收斂到 $m=20$):

$\text{disturbance}(i)=10*(-1+\text{rand})$;

$\text{noise}(i)=0.001*\sin(25*i)+0.005*\cos(100*i+\pi)$;



經多次測試結論：

1. m_{hat} 收斂情形受到 disturbance 影響很小，但是對 noise 非常敏感。
2. 兩條線重疊，用 m 和 m_{dot} 做出來的結果一模一樣 @@ ???????????

程式碼：

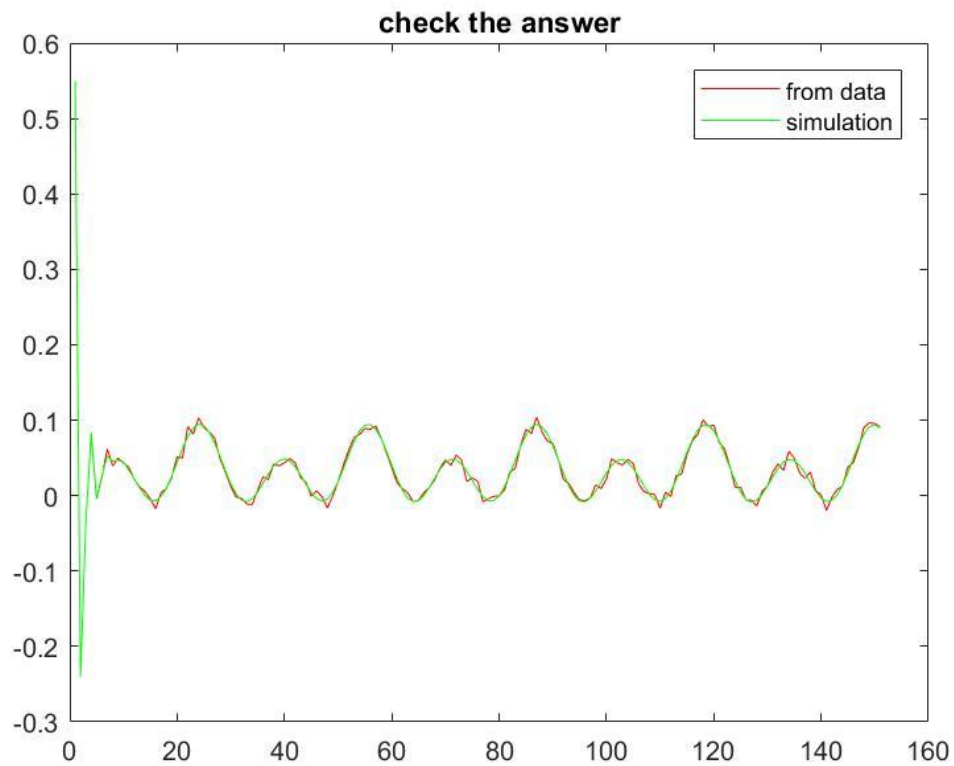
```
clear;clc;
totaltime=10;
delta=0.01;
totalstep=totaltime/delta;
%
m=20;
m_hat1(1)=15;
u(1)=1;
%make n,d
for i=1:totalstep
    disturbance(i)=10*(-1+rand);
    noise(i)=0.001*sin(25*i)+0.005*cos(100*i+pi);
end
% use m
for i=1:totalstep
    yarray(i)=(u(i)/m)+noise(i);
%
    num=delta*sum(yarray.*u);
    den=delta*sum(yarray.*yarray);
    m_hat1(i+1)=(num/den);
    u(i+1)=m_hat1(i+1)*(yarray(i))+disturbance(i);
end;
%clear var.
yarray=[0:1:totalstep-1]*0;
u=yarray;
m_hat2(1)=15;
u(1)=1;
%use m_dot
for i=1:totalstep
    yarray(i)=(u(i)/m)+noise(i);
%
    num=(u(i)-m_hat2(i)*yarray(i))*yarray(i);
    den=delta*sum(yarray.*yarray);
    m_hat_dot(i)=(num/den);
```

```
m_hat2(i+1)=m_hat2(i)+m_hat_dot(i)*delta;  
u(i+1)=m_hat2(i+1)*(yarray(i))+disturbance(i);  
end;  
  
plot([0:1:totalstep]*delta,m_hat1,'r');  
hold on;  
plot([0:1:totalstep]*delta,m_hat2,'b');  
title('m_h_a_t');
```

3.

算出答案： $a_1=0.453557$ $a_2=0.250984$ $b_1=-0.356244$ $b_2=0.168191$ 。

使用算出的答案和同樣u做模擬，並和所給的y做比較：



Matlab程式碼：

```
clear;clc;

%read data%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
Data=textread('hw6Data.txt','%f');
y=zeros(1,length(Data)/2);u=zeros(1,length(Data)/2);k=1;
for i=1:length(Data)
    if mod(i,2)==0
        y(k)=Data(i);
        k=k+1;
    else
        u(k)=Data(i);
    end
end
%find matrix phi%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
for k=3:length(y)+1
    phi(k-1,1)=y(k-1);
```



```

    phi(k-1,2)=y(k-2);
    phi(k-1,3)=u(k-1);
    phi(k-1,4)=u(k-2);
end
%find matrix theta%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
tmpA=[0 0 0 0;0 0 0 0;0 0 0 0;0 0 0 0];
tmpB=[0 0 0 0];
for k=3:151
    for i=1:4
        for j=1:4
            tmpA(i,j)=tmpA(i,j)+phi(k-1,j)*phi(k-1,i);
        end
        tmpB(i)=tmpB(i)+y(k)*phi(k-1,i);
    end
end
theta=inv(tmpA)*tmpB';
a1=-theta(1);
a2=-theta(2);
b1=theta(3);
b2=theta(4);
fprintf('a1=%f a2=%f b1=%f b2=%f \n',a1,a2,b1,b2);
%check the answer%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
yy(1)=y(1);yy(2)=y(2);
for k=3:151
    yy(k)=-a1*yy(k-1)-a2*yy(k-2)+b1*u(k-1)+b2*u(k-2);
end
plot(y,'r');
hold on;
plot(yy,'g');
legend('from data','simulation');
title('check the answer');

```