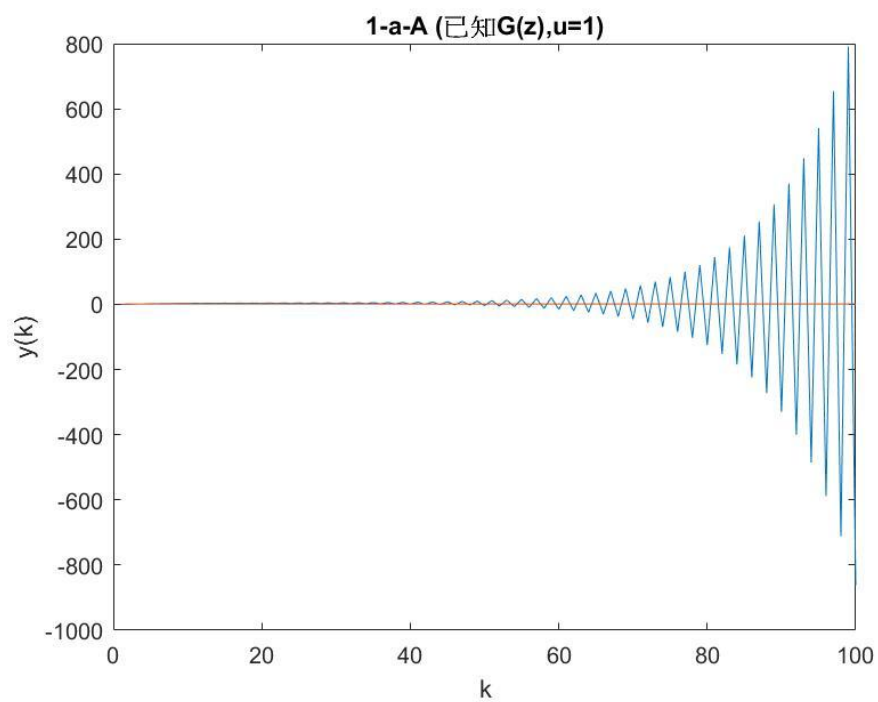


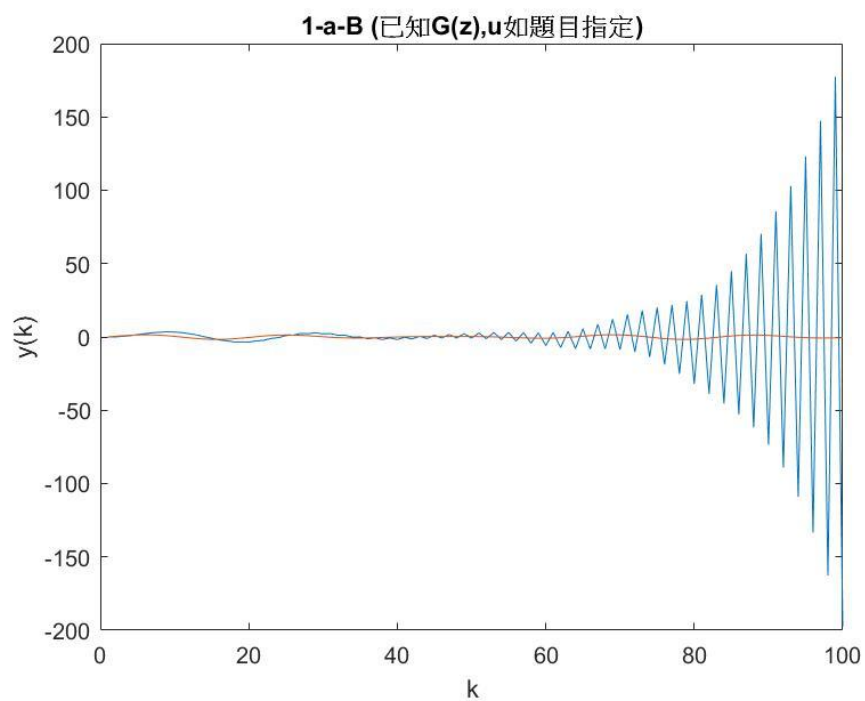
現代控制理論 HW7

104303206 黃筱晴

1-a-A 已知 $G(z)$ 求輸出 ($u=1$)



1-a-B 已知 $G(z)$ 求輸出 (u =一堆弦波的合成)



1-b-A

$$a_1=0.301561 \text{ (error}=0.001561 \text{)}$$

$$a_2=-0.879581 \text{ (error}=0.000419 \text{)}$$

$$b_1=0.896623 \text{ (error}=-0.003377 \text{)}$$

$$b_2=0.611703 \text{ (error}=0.011703 \text{)}$$

1-b-B

$$a_1=0.299716 \text{ (error}=-0.000284 \text{)}$$

$$a_2=-0.880222 \text{ (error}=-0.000222 \text{)}$$

$$b_1=0.901349 \text{ (error}=0.001349 \text{)}$$

$$b_2=0.598834 \text{ (error}=-0.001166 \text{)}$$

1-b-C

看起來差不多，我測了很久都看不出來.....

Note:在做 1-b-A 的時候，計算到 $\theta = [\sum \varphi(k-1) \varphi(k-1)^T]^{-1} (\sum y(k) \varphi(k-1))$ 時，因為奇異方陣沒辦法算反矩陣卡住。將 u 的第一筆先改成零後解決。但是之後測試過程也常常遇到 Matlab 說太接近奇異方陣的 Warning 訊息。

1-c

(1)pole assignment

目標極點位置 $0.5+0.5j, 0.5-0.5j, 0.82$

$$\varphi(z) = (z-0.5+0.5j)(z-0.5-0.5j)(z-0.82) = z^3 - 1.82z^2 + 1.32z - 0.41$$

設計 $C(z) = (\beta_0 z + \beta_1) / (z + \alpha_1)$ ，單回授系統，令等效開環轉移函數分母

$$(z + \alpha_1)(z^2 + a_1 z + a_2) + (\beta_0 z + \beta_1)(b_1 z + b_2) = z^3 - 1.82z^2 + 1.32z - 0.41。比較係數法。$$

$$\text{解聯立方程式矩陣 } \begin{bmatrix} 1 & b_1 & 0 & \alpha_1 \\ a_1 & b_2 & b_1 & \beta_0 \\ a_2 & 0 & b_2 & \beta_1 \end{bmatrix} \begin{bmatrix} \alpha_1 \\ \beta_0 \\ \beta_1 \end{bmatrix} = \begin{bmatrix} -1.82 - a_1 \\ 1.32 - a_2 \\ -0.41 \end{bmatrix} \text{ 得到 } \alpha_1, \beta_0, \beta_1$$

<1>用正確系統參數算的：

$$\alpha_1 = 4.435315, \beta_0 = -7.283683, \beta_1 = 5.821795$$

<2>用 dataA 算的：

$$\alpha_1 = 4.282014 \text{ (error=0.153301)}$$

$$\beta_0 = -6.976490 \text{ (error=0.307193)}$$

$$\beta_1 = 4.282014 \text{ (error=1.539781)}$$

<3>用 dataB 算的：

$$\alpha_1 = 3.820601 \text{ (error=0.614714)}$$

$$\beta_0 = -6.449869 \text{ (error=0.833814)}$$

$$\beta_1 = 3.820601 \text{ (error=2.001194)}$$

(2)回授控制程式實作(程式碼於附錄)

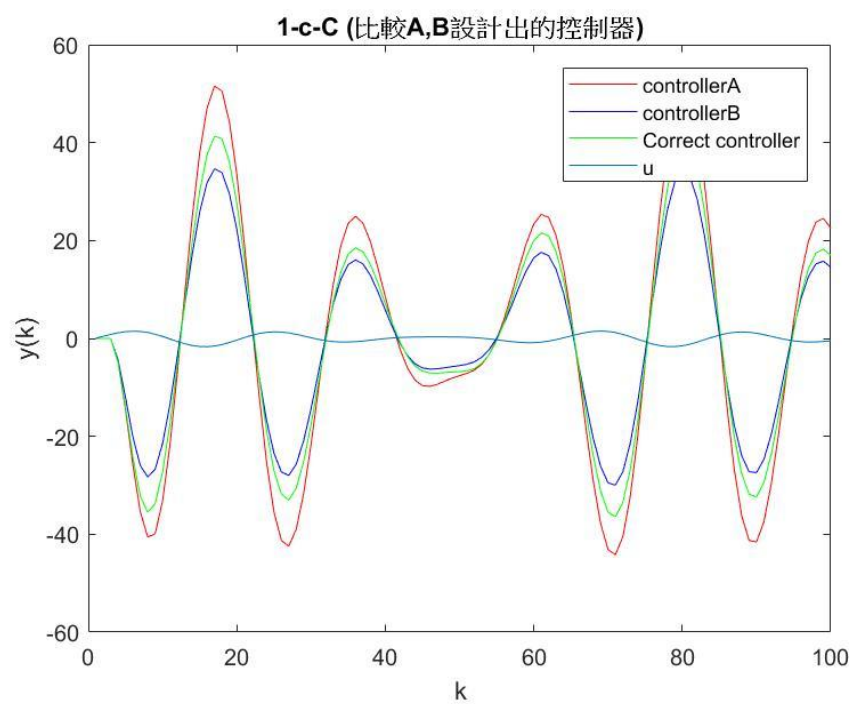
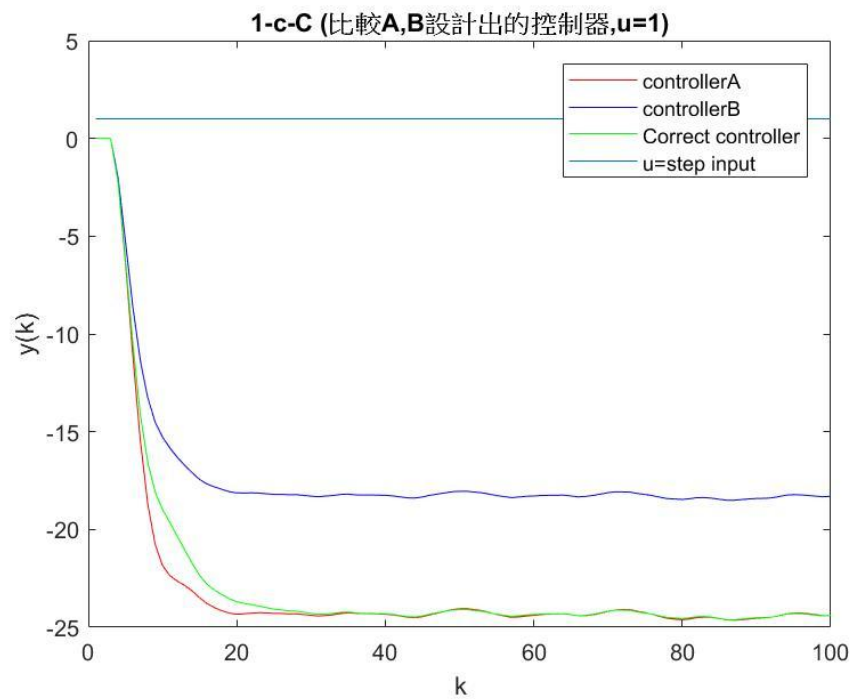
<1>等效開環轉移函數 $\frac{C(z)G(z)}{1+C(z)G(z)}$ 。

<2>寫一個(E=R-Y)的迴圈來疊代

```
r(k+1)=1;  
e(k+1)=r(k+1)-y(k+1);          %%這裡好奇怪@@???  
u(k+1)=- $\alpha$  u(k)+ $\beta$  e(k+1)+ $\beta$  e(k);  
y(k+2)=-a1y(k+1) -a2y(k)+b1u(k+1)+b2u(k)+d(k+2);
```

但是剛開始做的時候一直發散，後來反覆嘗試修改步數的地方，終於試出一組答案，能做出和使用等效開環轉移函數相同的結果。

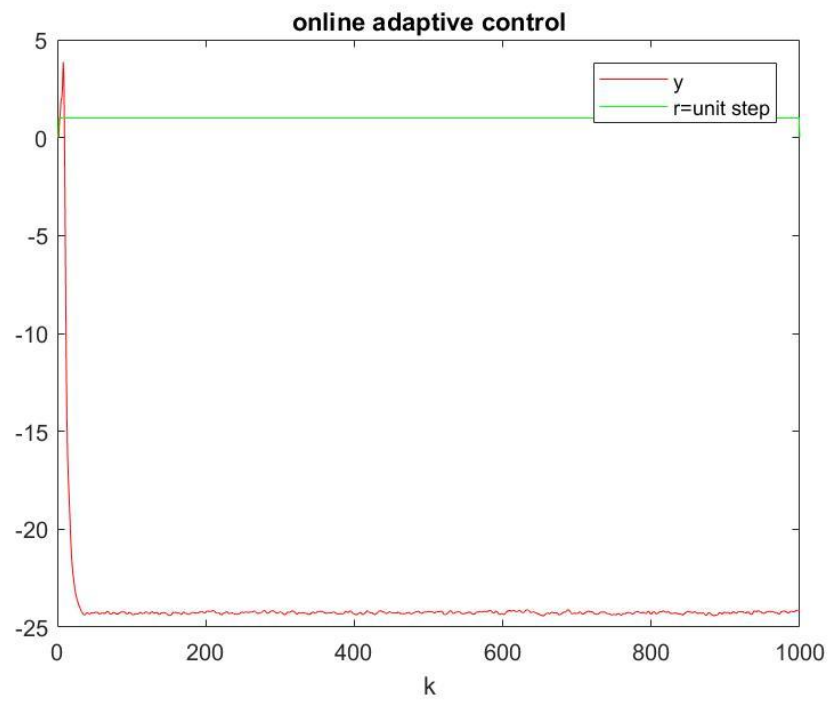
(3)測試



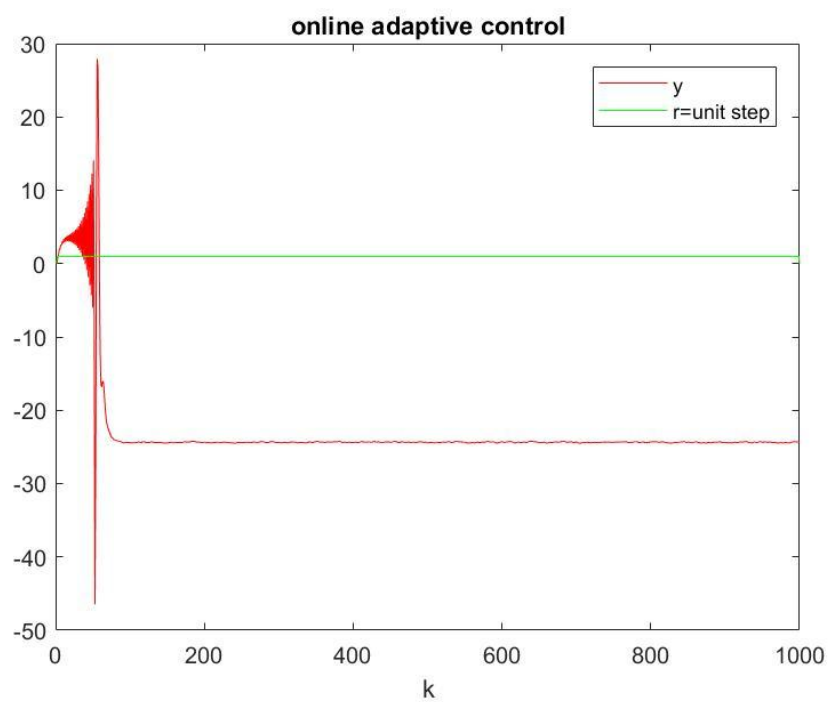
Note：當再跑久一點，資料筆數 300 以上，因為控制器參數不完全正確，A 和 B 都會發散。

1-d-A

(1) 1~5 蒐集數據，6~900 online adaptive control，901~1000 不再修改控制器。

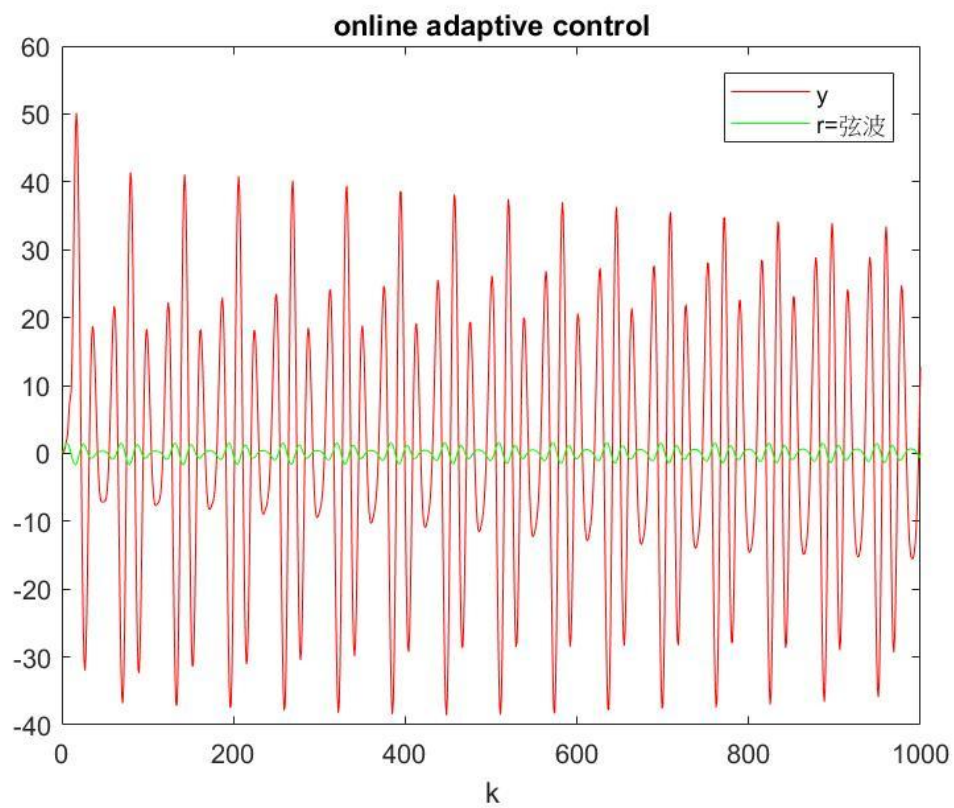


(2) 1~50 蒐集數據，51~900 online adaptive control，901~1000 不再修改控制器。

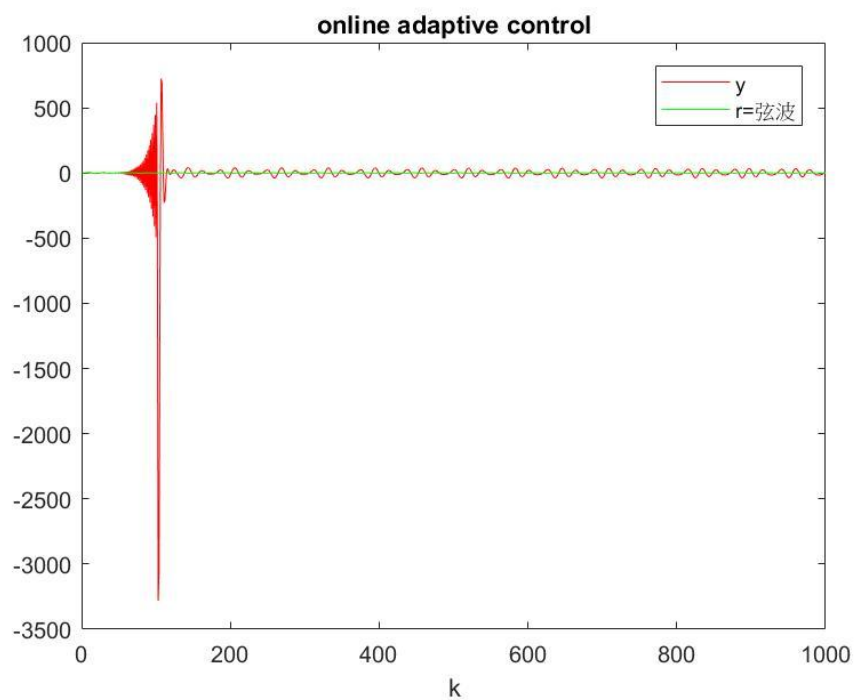


1-d-B

(1) 1~5蒐集數據，6~900 online adaptive control，901~1000不再修改控制器。

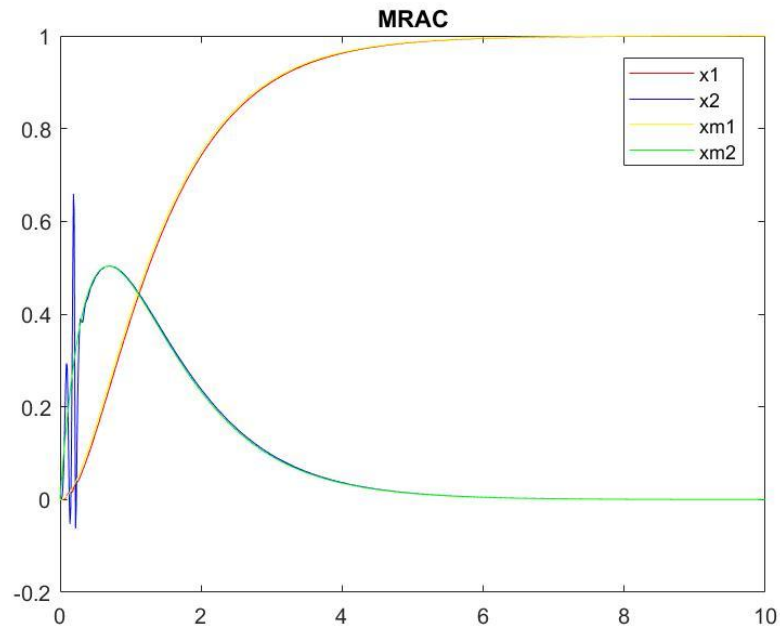


(2) 1~100蒐集數據，101~900 online adaptive control，901~1000不再修改控制器。



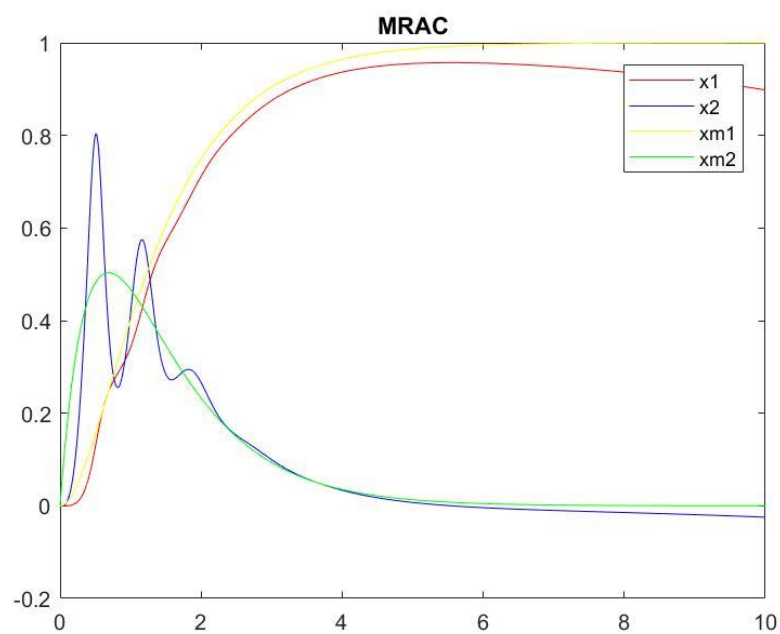
2-A. MRAC unit step 輸入模擬

(1) unit step 對照組 $\gamma_0=0.025$ $\gamma_1=0.5$ $\gamma_2=0.005$ $Q_{22}=1000$



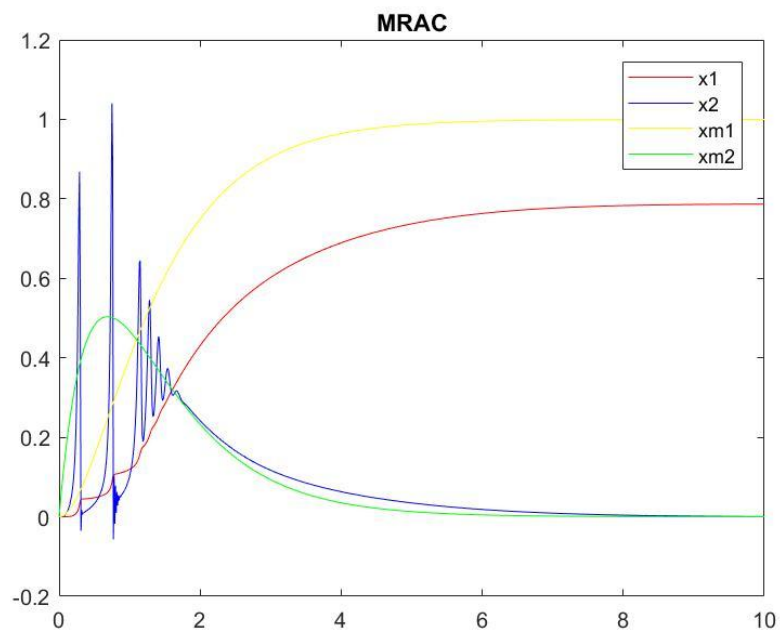
(2) $Q = \begin{bmatrix} 1 & 0 \\ 0 & q \end{bmatrix}$, 明顯 Q_{22} 值越大，系統越穩定，若 Q_{22} 值不夠系統會發散。

降低 Q_{22} ($\gamma_0=0.025$ $\gamma_1=0.5$ $\gamma_2=0.005$ $Q_{22}=10$)



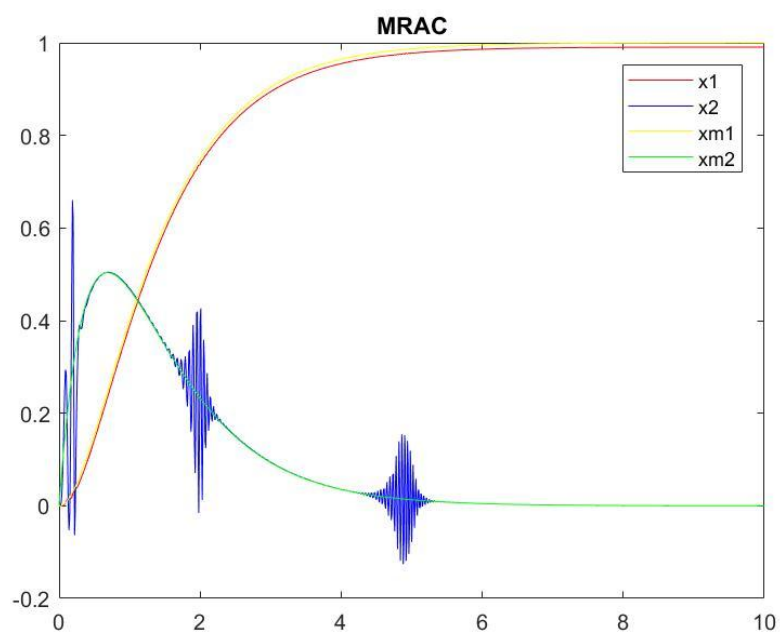
(3) γ_0 越大， x_1 穩態誤差越糟， x_1, x_2 震盪情形持續較久。

增大 γ_0 ($\gamma_0=2.5$ $\gamma_1=0.5$ $\gamma_2=0.005$ $Q_{22}=10$)



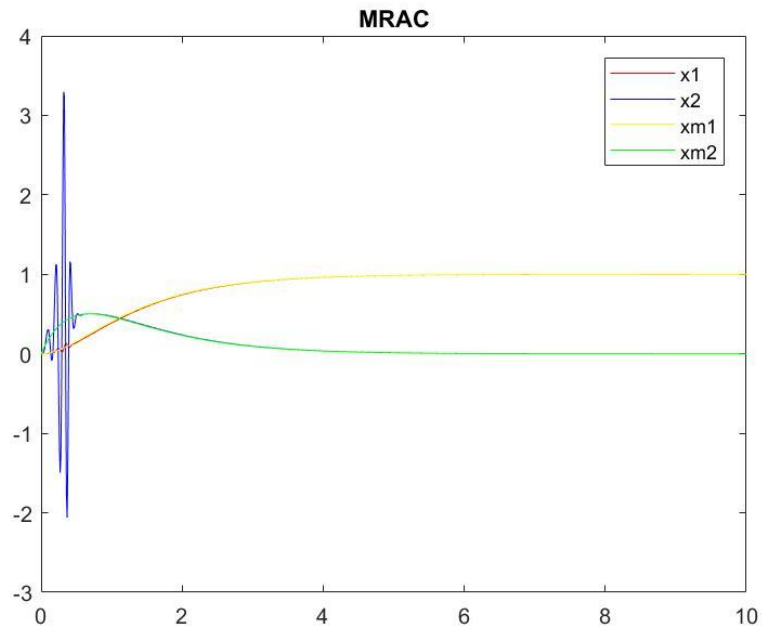
(4) γ_1 越小， x_2 震盪越久。貌似越大越好，也不會發散，但是往上調至定值後看起來效果都一樣。

降低 γ_1 ($\gamma_0=0.025$ $\gamma_1=0.005$ $\gamma_2=0.005$ $Q_{22}=1000$)



(5) γ_2 越大， x_1 、 x_2 的振幅都會變大也會振比較久，其中 x_2 影響非常嚴重。

增加 γ_2 ($\gamma_0=0.025$ $\gamma_1=0.5$ $\gamma_2=0.5$ $Q_{22}=1000$)

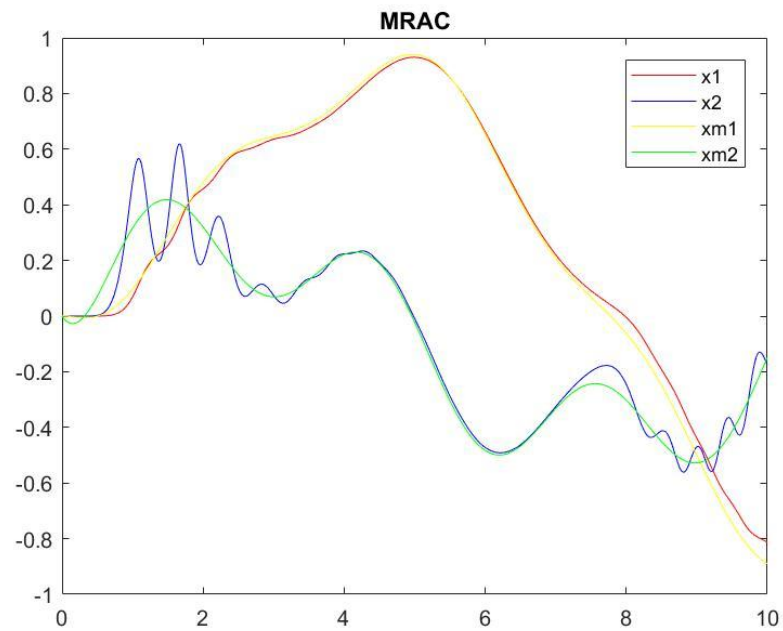


經多次測試結論：

Q_{22} 要大、 γ_0 要小 γ_1 可大 γ_2 盡量小，但這些參數太小系統都容易發散。
在三個 γ 中 γ_2 最為敏感也最重要。

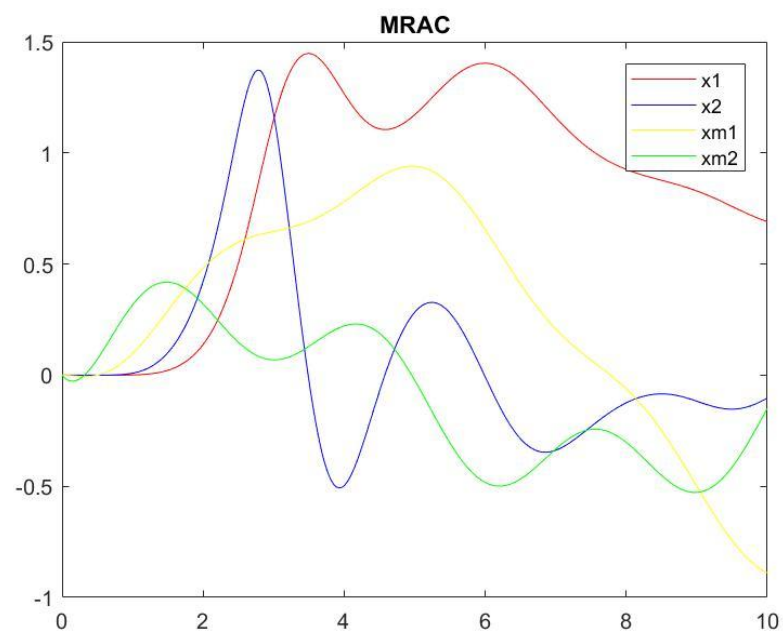
2-B.MRAC 弦波輸入模擬

(1)弦波對照組 $\gamma_0=1$ $\gamma_1=0.5$ $\gamma_2=0.4$ $Q_{22}=1000$



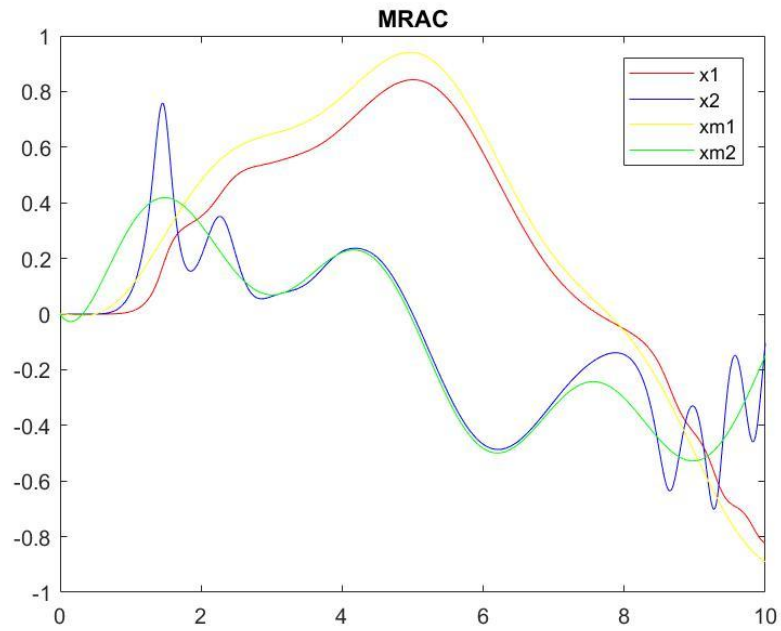
(2)同樣 Q_{22} 越大越穩定

降低 Q_{22} ($\gamma_0=1$ $\gamma_1=0.5$ $\gamma_2=0.4$ $Q_{22}=10$)

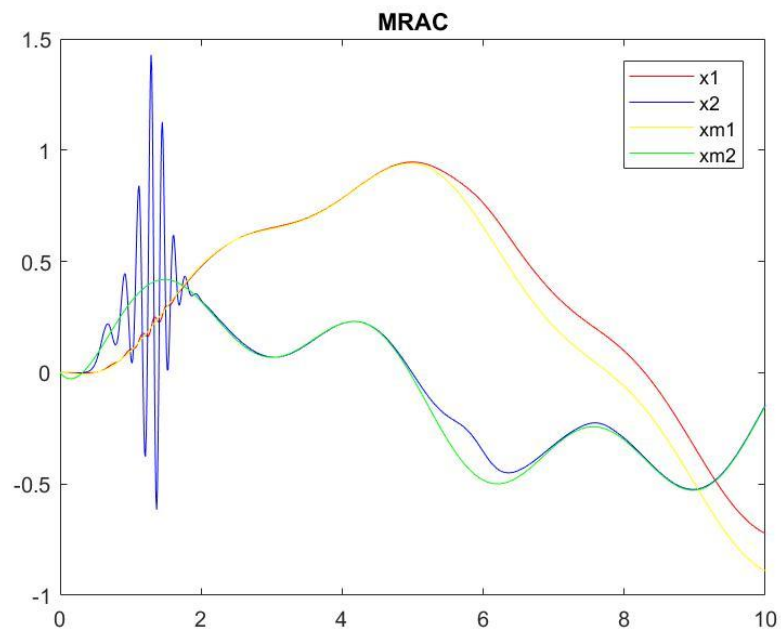


(3)

增加 γ_0 ($\gamma_0=10$ $\gamma_1=0.5$ $\gamma_2=0.4$ $Q_{22}=1000$)，誤差變大

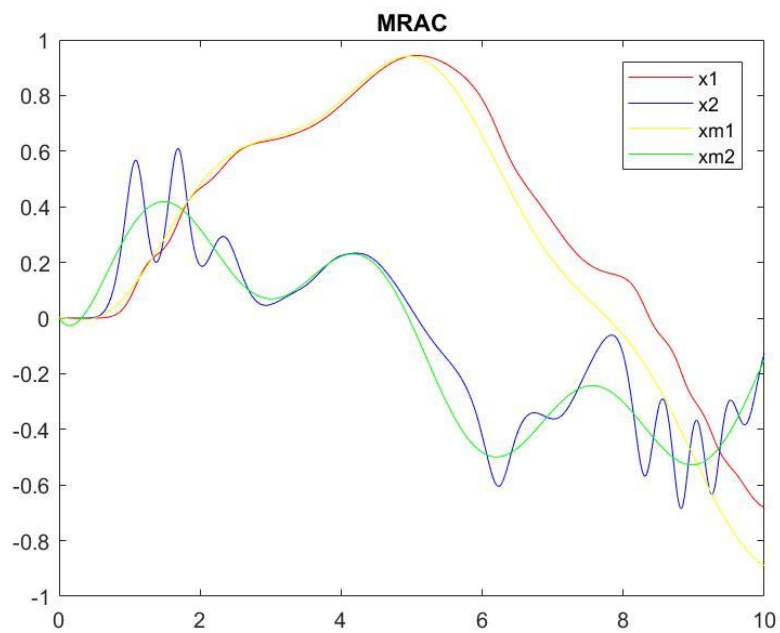


降低 γ_0 ($\gamma_0=0.05$ $\gamma_1=0.5$ $\gamma_2=0.4$ $Q_{22}=1000$)，暫態響應的震盪變嚴重。

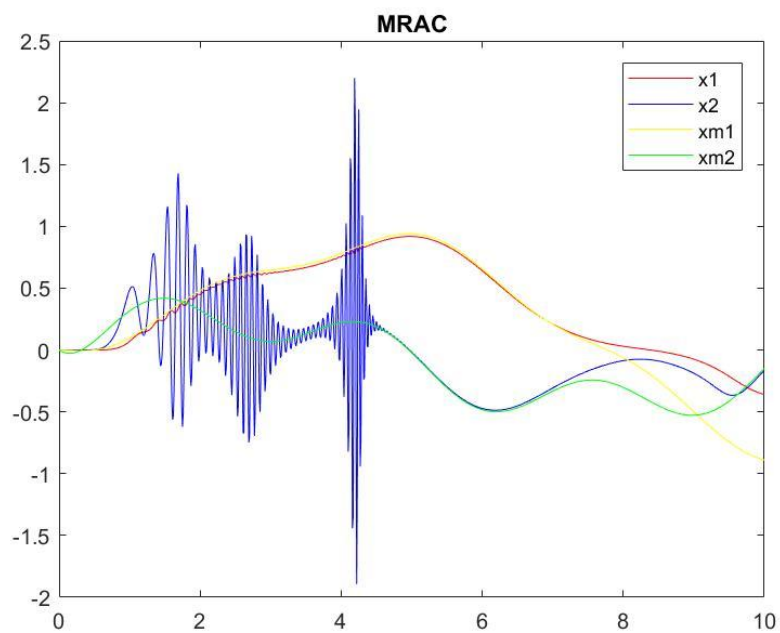


(4)

增加 γ_1 ($\gamma_0=1$ $\gamma_1=5$ $\gamma_2=0.4$ $Q_{22}=1000$)，誤差變大。

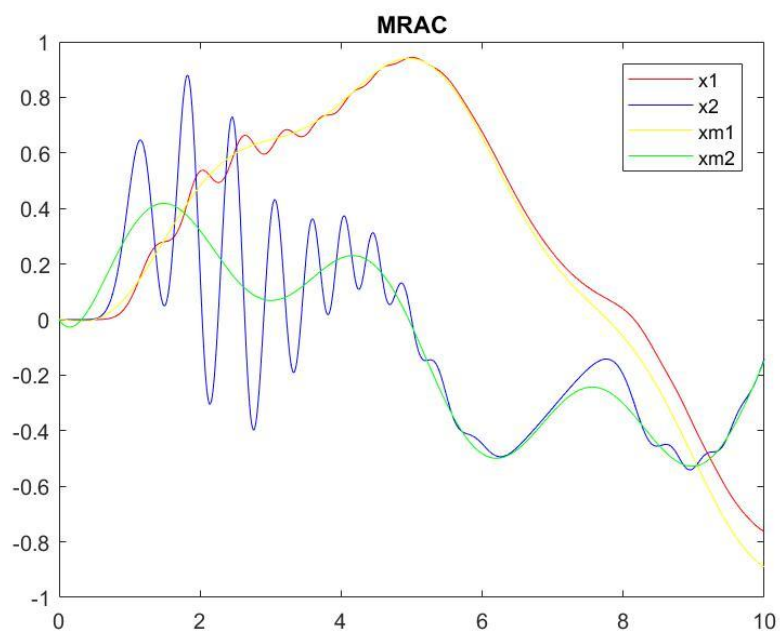


降低 γ_1 ($\gamma_0=1$ $\gamma_1=0.005$ $\gamma_2=0.4$ $Q_{22}=1000$)，震盪情形持續較久。

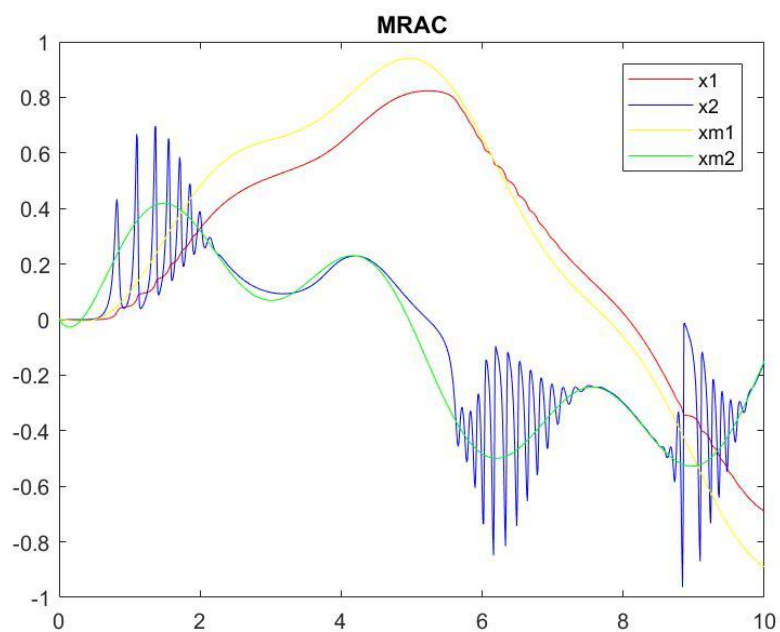


(5)

增加 γ_2 ($\gamma_0=1$ $\gamma_1=0.5$ $\gamma_2=4$ $Q_{22}=1000$)，X 要花更多時間追上 X_m 。



降低 γ_2 ($\gamma_0=1$ $\gamma_1=0.5$ $\gamma_2=0.005$ $Q_{22}=1000$)，後期震盪變明顯。



經多次測試結論：

Q_{22} 要大，三個 γ 都有其較適當的範圍，不能太大或太小。

附錄(程式碼)

(1)閉迴路控制器

```
%close loop control
%result same as using equivalent open loop transfer func.
clear;clc;
totalStep=1000;
a1=0.3;a2=-0.88;b1=0.9;b2=0.6;%system
for k=1:totalStep
    d(k)=0.01*(rand-0.5);
end

poly=conv([1,-0.82],conv([1,-0.5+0.5i],[1,-0.5-0.5i]));%pole
assignment
A=[1 b1 0;a1 b2 b1;a2 0 b2];
b=[poly(2)-a1;poly(3)-a2;poly(4)];
x=inv(A)*b;
alpha1=x(1);beta0=x(2);beta1=x(3);

y=[1:totalStep]*0;
u=[1:totalStep]*0;
r=[1:totalStep]*0;
e=[1:totalStep]*0;
r(1)=0;
r(2)=1;
r(3)=1;
for k=1:totalStep-2
    r(k+1)=1;
    e(k+1)=r(k+1)-y(k+1);
    u(k+1)=(-alpha1*u(k)+beta0*e(k+1)+beta1*e(k));
    y(k+2)=-a1*y(k+1)-a2*y(k)+b1*u(k+1)+b2*u(k)+d(k+2);
end
figure(1)
plot(y,'b');hold on;plot(u,'g');hold on;plot(r,'y');plot(e,'r');
xlabel("k");
legend('y','u','r','e');
title("3333$U^{\mu}X-t|^{\pm}F (r=unit step)");
```



```

y=[1:totalStep]*0;
u=[1:totalStep]*0;
r=[1:totalStep]*0;
e=[1:totalStep]*0;

r(1)=sin(6*1/20)+0.5*cos(6*1/15+3.2)+0.2*sin(2.57*1/13+1.36);
r(2)=sin(6*2/20)+0.5*cos(6*2/15+3.2)+0.2*sin(2.57*2/13+1.36);
r(3)=sin(6*3/20)+0.5*cos(6*3/15+3.2)+0.2*sin(2.57*3/13+1.36);

for k=1:totalStep-2

    r(k+1)=sin(6*(k+1)/20)+0.5*cos(6*(k+1)/15+3.2)+0.2*sin(2.57*(k+1)/13+
1.36);

    e(k+1)=r(k+1)-y(k+1);

    u(k+1)=(-alpha1*u(k)+beta0*e(k+1)+beta1*e(k));

    y(k+2)=-a1*y(k+1)-a2*y(k)+b1*u(k+1)+b2*u(k)+d(k+2);

end

figure(2)

plot(y,'b');hold on;plot(u,'g');hold on;plot(r,'y');plot(e,'r');

xlabel("k");

legend('y','u','r','e');

title("³á³á³á$Ú°uYX-t| ^±ÂF (r=Q^i)");

```

(2)閉迴路控制器使用等效開環轉移函數

```
%design C(z) and using equivalent open loop transfer func.
clear;clc;
totalStep=1000;
a1=0.3;a2=-0.88;b1=0.9;b2=0.6;%system
for k=1:totalStep
    d(k)=0.01*(rand-0.5);
end

poly=conv([1,-0.82],conv([1,-0.5+0.5i],[1,-0.5-0.5i]));%pole
assignment
A=[1 b1 0;a1 b2 b1;a2 0 b2];
b=[poly(2)-a1;poly(3)-a2;poly(4)];
x=inv(A)*b;
alpha1=x(1);beta0=x(2);beta1=x(3);
fprintf("alpha1=%f;beta0=%f;beta1=%f;\n",alpha1,beta0,beta1);

num=conv([b1,b2],[beta0,beta1]);%C(z)*G(z)
den=conv([1,a1,a2],[1,alpha1]);%C(z)*G(z)
fb_num=num;%equivalent open loop sys.
fb_den=[0,num]+den;%equivalent open loop sys.

y=[1:totalStep]*0;
u=[1:totalStep]*0;
r=[1:totalStep]*0;
y(1)=0;y(2)=0;y(3)=0;
u(1)=0;u(2)=1;u(3)=1;
for k=1:totalStep-3
    u(k+3)=1;

    y(k+3)=-fb_den(2)*y(k+2)-fb_den(3)*y(k+1)-fb_den(4)*y(k)+fb_num(1)*u(k+2)+fb_num(2)*u(k+1)+fb_num(3)*u(k)+d(k+3);
end
figure(1);
plot(y);hold on;plot(u);
legend('y','u=unit step');
title("design C(z) and using equivalent open loop transfer func.");
```

```

y=[1:totalStep]*0;
u=[1:totalStep]*0;
r=[1:totalStep]*0;
y(1)=0;y(2)=0;y(3)=0;
u(1)=sin(6*1/20)+0.5*cos(6*1/15+3.2)+0.2*sin(2.57*1/13+1.36);
u(2)=sin(6*2/20)+0.5*cos(6*2/15+3.2)+0.2*sin(2.57*2/13+1.36);
u(3)=sin(6*3/20)+0.5*cos(6*3/15+3.2)+0.2*sin(2.57*3/13+1.36);
for k=1:totalStep-3
    u(k+3)=sin(6*(k+2)/20)+0.5*cos(6*(k+2)/15+3.2)+0.2*sin(2.57*(k+2)/13+
1.36);
    y(k+3)=-fb_den(2)*y(k+2)-fb_den(3)*y(k+1)-fb_den(4)*y(k)+fb_num(1)*u(
k+2)+fb_num(2)*u(k+1)+fb_num(3)*u(k)+d(k+3);
end
figure(2);
plot(y);hold on;plot(u);
legend('y','u=@T^i');
title("design C(z) and using equivalent open loop transfer func.");

```

(3) 1-a,b,c 總程式碼

```
clear;clc;
totalStep=1000;
a1=0.3;a2=-0.88;b1=0.9;b2=0.6;%system
for k=1:totalStep
    d(k)=0.1*(rand-0.5);
end
%1-a-A%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
%%%
%just run with unit step input
y1A=[1:totalStep]*0;
u1A=[1:totalStep]*0;
y1A(1)=0;y1A(2)=0;u1A(1)=0;u1A(2)=1;
for k=1:totalStep-2
    u1A(k+2)=1;
    y1A(k+2)=-a1*y1A(k+1)-a2*y1A(k)+b1*u1A(k+1)+b2*u1A(k)+d(k+2);
end
figure(1);
plot(y1A);hold on;plot(u1A);
xlabel("k");
ylabel("y(k)");
title("1-a-A (w^a_3G(z),u=1)");
%
%1-a-B%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
%%%
%just run with the given input
y1B=[1:totalStep]*0;
u1B=[1:totalStep]*0;
y1B(1)=0;y1B(2)=0;
u1B(1)=sin(6*1/20)+0.5*cos(6*1/15+3.2)+0.2*sin(2.57*1/13+1.36);
u1B(2)=sin(6*2/20)+0.5*cos(6*2/15+3.2)+0.2*sin(2.57*2/13+1.36);
for k=1:totalStep-2
    u1B(k+2)=sin(6*(k+2)/20)+0.5*cos(6*(k+2)/15+3.2)+0.2*sin(2.57*(k+2)/13+1.36);
    y1B(k+2)=-a1*y1B(k+1)-a2*y1B(k)+b1*u1B(k+1)+b2*u1B(k)+d(k+2);
end
figure(2);
```

[illegible]

[illegible]

```

%pole assignment
poly=conv([1,-0.82],conv([1,-0.5+0.5i],[1,-0.5-0.5i]));%characteristi
c poly.
const=[1 b1A 0;a1A b2A b1A;a2A 0 b2A];
b=[poly(2)-a1A;poly(3)-a2A;poly(4)];
x=inv(const)*b;
alpha1A=x(1);beta0A=x(2);beta1A=x(3);

%1-c-B%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
%%%%%

%pole assignment
poly=conv([1,-0.82],conv([1,-0.5+0.5i],[1,-0.5-0.5i]));%characteristi
c poly.
const=[1 b1B 0;a1B b2B b1B;a2B 0 b2B];
b=[poly(2)-a1B;poly(3)-a2B;poly(4)];
x=inv(const)*b;
alpha1B=x(1);beta0B=x(2);beta1B=x(3);
%the correct one (just for
comparison)%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
%pole assignment
poly=conv([1,-0.82],conv([1,-0.5+0.5i],[1,-0.5-0.5i]));%characteristi
c poly.
const=[1 b1 0;a1 b2 b1;a2 0 b2];
b=[poly(2)-a1;poly(3)-a2;poly(4)];
x=inv(const)*b;
Correctalpha1=x(1);Correctbeta0=x(2);Correctbeta1=x(3);

%1-c-C%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
%%%%%

%compare the control design from dataA and dataB
fprintf('Controller A:\n');
fprintf('alpha1=%f (error=%f)\n',alpha1A,abs(Correctalpha1-alpha1A));
fprintf('beta0=%f (error=%f)\n',beta0A,abs(Correctbeta0-beta0A));
fprintf('beta1=%f (error=%f)\n',alpha1A,abs(Correctbeta1-alpha1A));
fprintf('Controller B:\n');
fprintf('alpha1=%f (error=%f)\n',alpha1B,abs(Correctalpha1-alpha1B));
fprintf('beta0=%f (error=%f)\n',beta0B,abs(Correctbeta0-beta0B));
fprintf('beta1=%f (error=%f)\n',alpha1B,abs(Correctbeta1-alpha1B));
%controller A

```

```

numA=conv([b1,b2],[beta0A,beta1A]);%C(z)*G(z)
denA=conv([1,a1,a2],[1,alpha1A]);%C(z)*G(z)
fb_numA=numA;%equivalent open loop sys.
fb_denA=[0,numA]+denA;%equivalent open loop sys.
%controller B
numB=conv([b1,b2],[beta0B,beta1B]);%C(z)*G(z)
denB=conv([1,a1,a2],[1,alpha1B]);%C(z)*G(z)
fb_numB=numB;%equivalent open loop sys.
fb_denB=[0,numB]+denB;%equivalent open loop sys.
%the correct one (just for comparison)
numCorrect=conv([b1,b2],[Correctbeta0,Correctbeta1]);%C(z)*G(z)
denCorrect=conv([1,a1,a2],[1,Correctalpha1]);%C(z)*G(z)
fb_numCorrect=numCorrect;%equivalent open loop sys.
fb_denCorrect=[0,numCorrect]+denCorrect;%equivalent open loop sys.

%controller A with unit step input
y3A=[1:totalStep]*0;
u3A=[1:totalStep]*0;
y3A(1)=0;y3A(2)=0;y3A(3)=0;
u3A(1)=1;u3A(2)=1;u3A(3)=1;
for k=1:totalStep-3
    u3A(k+3)=1;

y3A(k+3)=-fb_denA(2)*y3A(k+2)-fb_denA(3)*y3A(k+1)-fb_denA(4)*y3A(k)+f
b_numA(1)*u3A(k+2)+fb_numA(2)*u3A(k+1)+fb_numA(3)*u3A(k)+d(k+3);
end
%controller B with unit step input
y3B=[1:totalStep]*0;
u3B=[1:totalStep]*0;
y3B(1)=0;y3B(2)=0;y3B(3)=0;
u3B(1)=1;u3B(2)=1;u3B(3)=1;
for k=1:totalStep-3
    u3B(k+3)=1;

y3B(k+3)=-fb_denB(2)*y3B(k+2)-fb_denB(3)*y3B(k+1)-fb_denB(4)*y3B(k)+f
b_numB(1)*u3B(k+2)+fb_numB(2)*u3B(k+1)+fb_numB(3)*u3B(k)+d(k+3);
end
%the correct controller with unit step input

```



```

y3Correct=[1:totalStep]*0;
u3Correct=[1:totalStep]*0;
y3Correct(1)=0;y3Correct(2)=0;y3Correct(3)=0;
u3Correct(1)=1;u3Correct(2)=1;u3Correct(3)=1;
for k=1:totalStep-3
    u3Correct(k+3)=1;

y3Correct(k+3)=-fb_denCorrect(2)*y3Correct(k+2)-fb_denCorrect(3)*y3Correct(k+1)-fb_denCorrect(4)*y3Correct(k)+fb_numCorrect(1)*u3Correct(k+2)+fb_numCorrect(2)*u3Correct(k+1)+fb_numCorrect(3)*u3Correct(k)+d(k+3);
end
figure(3);
plot(y3A,'r');hold on;plot(y3B,'b');hold on;plot(y3Correct,'g');hold on;plot(u3B);
xlabel("k");
ylabel("y(k)");
legend('controllerA','controllerB','Correct controller','u=step input');
title("1-c-C (a_n,uA,B^3]-pYX^a^o+1^1_4^1,u=1)");

%controller A with given input
y3A=[1:totalStep]*0;
u3A=[1:totalStep]*0;
y3A(1)=0;y3A(2)=0;y3A(3)=0;
u3A(1)=sin(6*1/20)+0.5*cos(6*1/15+3.2)+0.2*sin(2.57*1/13+1.36);
u3A(2)=sin(6*2/20)+0.5*cos(6*2/15+3.2)+0.2*sin(2.57*2/13+1.36);
u3A(3)=sin(6*3/20)+0.5*cos(6*3/15+3.2)+0.2*sin(2.57*3/13+1.36);
for k=1:totalStep-3

u3A(k+3)=sin(6*(k+3)/20)+0.5*cos(6*(k+3)/15+3.2)+0.2*sin(2.57*(k+3)/13+1.36);

y3A(k+3)=-fb_denA(2)*y3A(k+2)-fb_denA(3)*y3A(k+1)-fb_denA(4)*y3A(k)+fb_numA(1)*u3A(k+2)+fb_numA(2)*u3A(k+1)+fb_numA(3)*u3A(k)+d(k+3);
end

%controller B with given input

```

```

y3B=[1:totalStep]*0;
u3B=[1:totalStep]*0;
y3B(1)=0;y3B(2)=0;y3B(3)=0;
u3B(1)=sin(6*1/20)+0.5*cos(6*1/15+3.2)+0.2*sin(2.57*1/13+1.36);
u3B(2)=sin(6*2/20)+0.5*cos(6*2/15+3.2)+0.2*sin(2.57*2/13+1.36);
u3B(3)=sin(6*3/20)+0.5*cos(6*3/15+3.2)+0.2*sin(2.57*3/13+1.36);
for k=1:totalStep-3
    u3B(k+3)=sin(6*(k+3)/20)+0.5*cos(6*(k+3)/15+3.2)+0.2*sin(2.57*(k+3)/13+1.36);
    y3B(k+3)=-fb_denB(2)*y3B(k+2)-fb_denB(3)*y3B(k+1)-fb_denB(4)*y3B(k)+fb_numB(1)*u3B(k+2)+fb_numB(2)*u3B(k+1)+fb_numB(3)*u3B(k)+d(k+3);
end
%the correct controller with given input
y3Correct=[1:totalStep]*0;
u3Correct=[1:totalStep]*0;
y3Correct(1)=0;y3Correct(2)=0;y3Correct(3)=0;
u3Correct(1)=sin(6*1/20)+0.5*cos(6*1/15+3.2)+0.2*sin(2.57*1/13+1.36);
u3Correct(2)=sin(6*2/20)+0.5*cos(6*2/15+3.2)+0.2*sin(2.57*2/13+1.36);
u3Correct(3)=sin(6*3/20)+0.5*cos(6*3/15+3.2)+0.2*sin(2.57*3/13+1.36);
for k=1:totalStep-3
    u3Correct(k+3)=sin(6*(k+3)/20)+0.5*cos(6*(k+3)/15+3.2)+0.2*sin(2.57*(k+3)/13+1.36);
    y3Correct(k+3)=-fb_denCorrect(2)*y3Correct(k+2)-fb_denCorrect(3)*y3Correct(k+1)-fb_denCorrect(4)*y3Correct(k)+fb_numCorrect(1)*u3Correct(k+2)+fb_numCorrect(2)*u3Correct(k+1)+fb_numCorrect(3)*u3Correct(k)+d(k+3);
end
figure(4);
plot(y3A,'r');hold on;plot(y3B,'b');hold on;plot(y3Correct,'g');plot(u3B);
xlabel("k");
ylabel("y(k)");
legend('controllerA','controllerB','Correct controller','u');
title("1-c-C (u_n,uA,B^3]-pYX^a+±i34)");

```

(4)1-d Online Adaptive Control (A、B 程式碼小題大同小異只附上一個)

```
%online adaptive control
%(unit step input)
clear;clc;
totalStep=1000;step1=50;step2=900;
a1=0.3;a2=-0.88;b1=0.9;b2=0.6;%system
Correctalpha1=4.435315;%C(z) design from the real sys.
Correctbeta0=-7.283683;
Correctbeta1=5.821795;
for k=1:totalStep
    d(k)=0.01*(rand-0.5);
end
%
y=[1:totalStep]*0;
u=[1:totalStep]*0;
r=[1:totalStep]*0;
e=[1:totalStep]*0;
%
%k=1~step1%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
%%%%
%just run with unit step input
r(1)=0;r(2)=1;r(3)=1;%unit stpe input
u(1)=0;u(2)=1;u(3)=1;
for k=1:step1
    r(k+2)=1;%unit stpe input
    u(k+2)=r(k+2);
    y(k+2)=-a1*y(k+1)-a2*y(k)+b1*u(k+1)+b2*u(k)+d(k+2);
end
%
%first time to find the system parameter
%find matrix phi%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
for k=3:step1
    phiA(k-1,1)=y(k-1);
    phiA(k-1,2)=y(k-2);
    phiA(k-1,3)=u(k-1);
    phiA(k-1,4)=u(k-2);
end
```

```

%find matrix theta%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
tmp1A=[0 0 0 0;0 0 0 0;0 0 0 0;0 0 0 0];
tmp2A=[0 0 0 0];
for k=3:step1
    for i=1:4
        for j=1:4
            tmp1A(i,j)=tmp1A(i,j)+phiA(k-1,j)*phiA(k-1,i);
        end
        tmp2A(i)=tmp2A(i)+y(k)*phiA(k-1,i);
    end
end
thetaA=inv(tmp1A)*tmp2A';
a1A=-thetaA(1);
a2A=-thetaA(2);
b1A=thetaA(3);
b2A=thetaA(4);
fprintf("a1=%f (error=%2f )\n",a1A,(a1A-a1));
fprintf("a2=%f (error=%2f )\n",a2A,(a2A-a2));
fprintf("b1=%f (error=%2f )\n",b1A,(b1A-b1));
fprintf("b2=%f (error=%2f )\n",b2A,(b2A-b2));

%design C(z) with optimal parameter (pole assignment)
poly=conv([1,-0.82],conv([1,-0.5+0.5i],[1,-0.5-0.5i]));%characteristi
c poly.
const=[1 b1A 0;a1A b2A b1A;a2A 0 b2A];
b=[poly(2)-a1A;poly(3)-a2A;poly(4)];
x=inv(const)*b;
alpha1A=x(1);beta0A=x(2);beta1A=x(3);%C(z) with optimal parameter
fprintf("alpha1=%f (err=%f) \n",alpha1A,abs(Correctalpha1-alpha1A));
fprintf("beta0=%f (err=%f) \n",beta1A,abs(Correctbeta0-beta0A));
fprintf("beta1=%f (err=%f) \n",beta1A,abs(Correctbeta1-beta1A));

%k=step1+1~step2%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
%%%%
%online adaptive
%close loop control & redesign C(z)
for k=step1+1:step2

```

```

fprintf("Now Step:k=%d !!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!\n",k);
r(k+1)=1;
e(k+1)=r(k+1)-y(k+1);
u(k+1)=(-alpha1A*u(k)+beta0A*e(k+1)+beta1A*e(k));
y(k+2)=-a1*y(k+1)-a2*y(k)+b1*u(k+1)+b2*u(k)+d(k+2);
%
%
%
%redesign C(z)
%find matrix phi%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
for i=3:k
    phiA(i-1,1)=y(i-1);
    phiA(i-1,2)=y(i-2);
    phiA(i-1,3)=u(i-1);
    phiA(i-1,4)=u(i-2);
end
%find matrix theta%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
tmp1A=[0 0 0 0;0 0 0 0;0 0 0 0;0 0 0 0];
tmp2A=[0 0 0 0];
for m=3:k
    for i=1:4
        for j=1:4
            tmp1A(i,j)=tmp1A(i,j)+phiA(m-1,j)*phiA(m-1,i);
        end
        tmp2A(i)=tmp2A(i)+y(m)*phiA(m-1,i);
    end
end
thetaA=inv(tmp1A)*tmp2A';
a1A=-thetaA(1);
a2A=-thetaA(2);
b1A=thetaA(3);
b2A=thetaA(4);
fprintf("a1=%f (error=%2f )\n",a1A,(a1A-a1));
fprintf("a2=%f (error=%2f )\n",a2A,(a2A-a2));
fprintf("b1=%f (error=%2f )\n",b1A,(b1A-b1));
fprintf("b2=%f (error=%2f )\n",b2A,(b2A-b2));
%
%design C(z) (pole assignment)

```

```

poly=conv([1,-0.82],conv([1,-0.5+0.5i],[1,-0.5-0.5i]));%characteristic
c poly.

const=[1 b1A 0;a1A b2A b1A;a2A 0 b2A];
b=[poly(2)-a1A;poly(3)-a2A;poly(4)];
x=inv(const)*b;
alpha1A=x(1);beta0A=x(2);beta1A=x(3);%C(z) with optimal parameter
fprintf('alpha1=%f (err=%f)
\n',alpha1A,abs(Correctalpha1-alpha1A));
fprintf('beta0=%f (err=%f) \n',beta1A,abs(Correctbeta0-beta0A));
fprintf('beta1=%f (err=%f) \n',beta1A,abs(Correctbeta1-beta1A));
end

%k=step2+1~end%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
%%%%%
%close loop control only
for k=step2+1:totalStep-2
    r(k+1)=1;
    e(k+1)=r(k+1)-y(k+1);
    u(k+1)=(-alpha1A*u(k)+beta0A*e(k+1)+beta1A*e(k));
    y(k+2)=-a1*y(k+1)-a2*y(k)+b1*u(k+1)+b2*u(k)+d(k+2);
end

plot(y,'r');hold on;plot(r,'g');
xlabel('k');
legend('y','r=unit step');
title('online adaptive control');

```

(5)MRAC

```
%MRAC
clear;clc;
totaltime=10;
delta=0.01;
totalstep=totaltime/delta;

%model
xm1(1)=0;xm2(1)=0;
for k=1:totalstep
%    r(k)=1;
    r(k)=sin(0.5*k*delta)+0.3*cos(2*k*delta+4);
    xm1_dot(k)=xm2(k);
    xm2_dot(k)=-2*xm1(k)-3*xm2(k)+2*r(k);
    xm1(k+1)=xm1(k)+xm1_dot(k)*delta;
    xm2(k+1)=xm2(k)+xm2_dot(k)*delta;
end

%select para.
Q=[1 0;0 1000];
Am=[0 1;-2 -3];bm=2;
b=1;
P=lyap(Am,Q);
gamma0=1;gamma1=0.5;gamma2=4;

theta0(1)=0;theta1(1)=0;theta2(1)=0;
x1(1)=0;x2(1)=0;
for k=1:totalstep
%    r(k)=1;
    r(k)=sin(0.5*k*delta)+0.3*cos(2*k*delta+4);
    u(k)=theta0(k)*r(k)+theta1(k)*x1(k)+theta2(k)*x2(k);

    x1_dot(k)=x2(k);
    x2_dot(k)=0.4*x1(k)+1.8*x2(k)+1*u(k);
    x1(k+1)=x1(k)+x1_dot(k)*delta;
    x2(k+1)=x2(k)+x2_dot(k)*delta;
```

```

    e1(k)=xm1(k)-x1(k);
    e2(k)=xm2(k)-x2(k);
    zeta(k)=0.5*(P(1,2)*e1(k)+P(2,2)*e2(k));
    theta0_dot(k)=zeta(k)*r(k)/(b*gamma0);
    theta1_dot(k)=zeta(k)*x1(k)/(b*gamma1);
    theta2_dot(k)=zeta(k)*x2(k)/(b*gamma2);
    
    theta0(k+1)=theta0(k)+theta0_dot(k)*delta;
    theta1(k+1)=theta1(k)+theta1_dot(k)*delta;
    theta2(k+1)=theta2(k)+theta2_dot(k)*delta;
    
end

```



```

plot([0:1:totalstep]*delta,x1,'r');hold on;
plot([0:1:totalstep]*delta,x2,'b');hold on;
plot([0:1:totalstep]*delta,xm1,'y');hold on;
plot([0:1:totalstep]*delta,xm2,'g');hold on;
legend('x1','x2','xm1','xm2');
title('MRAC');

```