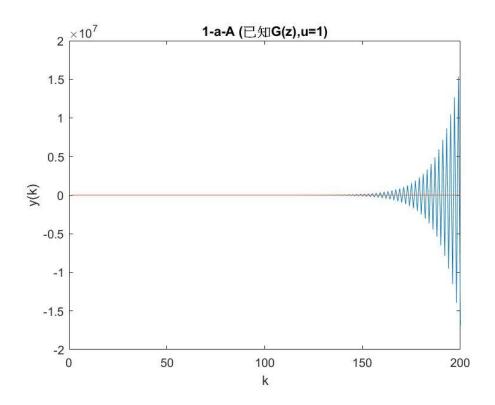
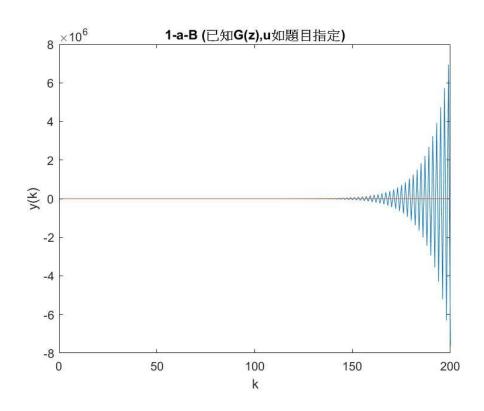
現代控制理論 HW7

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1-a-A 已知 G(z)求輸出 (u=1)



1-a-B 已知 G(z)求輸出 (u=一堆弦波的合成)

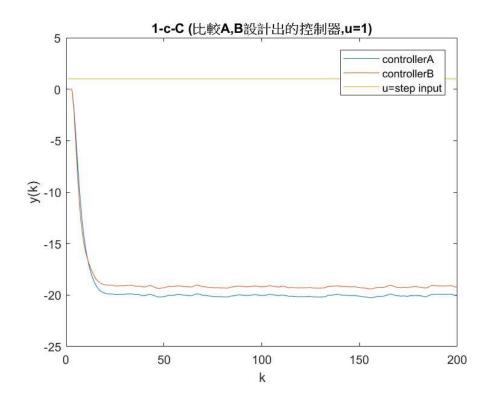


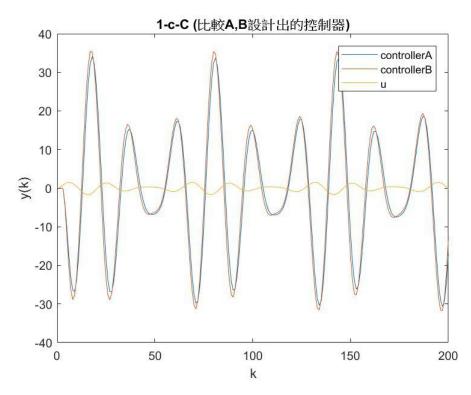
```
a1=0.298118 (error=-0.001882)
a2=-0.881307 (error=-0.001307)
b1=0.940994 (error=0.040994)
b2=0.543759 (error=-0.056241)

1-b-B
a1=0.299174 (error=-0.000826)
a2=-0.881930 (error=-0.001930)
b1=0.922097 (error=0.022097)
b2=0.575913 (error=-0.024087)
```

大部分測試結果是 A(unit step 輸入)較精準

Note:在做 1-b-A 的時候,欲使用最佳化方法($\partial J/\partial \theta=0$)求參數。其中計算到 $\theta=[\Sigma \phi(k-1) \phi(k-1)^T]^{-1}(\Sigma y(k)\phi(k-1))$ 時,因為奇異方陣沒辦法算反矩陣而住。將 u 的第一筆先改成零後解決。但是之後測試過程也常常遇到 Matlab 說太接近奇異方陣的 Warning 訊息。





Note:當 K 再多一點(千筆以上)兩個控制器因為參數不完全精準,系統都會發散。所以要用下一題(1-d)的 adaptive control。

(1)pole assignment

目標極點位置 0.5+0.5j,0.5-0.5j,0.82

$$\phi(z)=(z-0.5+0.5j)*(z-0.5+0.5j)*(z-0.82)=z^3-1.82z^2+1.32z-0.41$$

設計 $C(z)=(\beta_0z+\beta_1)/(z+\alpha_1)$, 單回授系統, 令等效開環轉移函數分母

$$(z+\alpha_1)(z^2+a_1z+a_2)+(\beta_0z+\beta_1)(b_1z+b_2)=z^3-1.82z^2+1.32z-0.41$$
。比較係數法。

$$1$$
 b1 0 α1 $-1.82-a1$ 解聯立方程式矩陣 [a1 b2 b1][β 0]=[$1.32-a2$] 得到 α_1 、 β_0 、 β_1 a2 0 b2 β 1 -0.41

(2)回授控制程式實作(程式碼於附錄)

<1>等效開環轉移函數
$$\frac{C(z)G(z)}{1+C(z)G(z)}$$

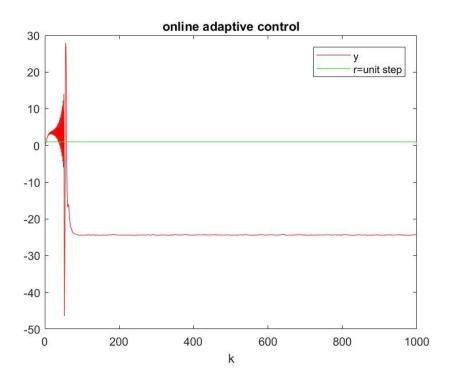
<2>寫一個這種迴圈來疊代

$$r(k+1)=1;$$
 $e(k+1)=r(k+1)-y(k+1);$ %%(這裡好奇怪@@) $u(k+1)=-\alpha \ \iota u(k)+\beta \ \iota e(k+1)+\beta \ \iota e(k);$ $y(k+2)=-a\iota y(k+1)-a\iota y(k)+b\iota u(k+1)+b\iota u(k)+d(k+2);$

但是極高機率會發散,後來反覆嘗試修改步數(k=???),終於不小心被我試出一組答案可用(但是邏輯上怪怪的?)。做出來的結果跟使用等效開環轉移函數的結果相同。

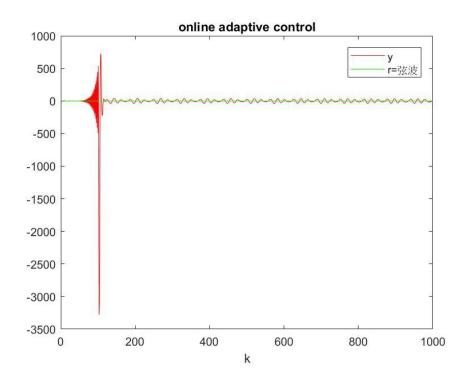
1-d-A

1~50 蒐集數據,51~900 online adaptive control,901~1000 不再修改控制器。



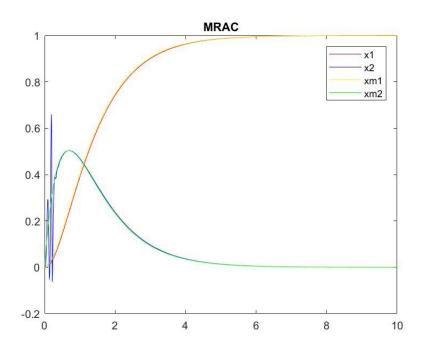
1-d-B

1~100蒐集數據,51~900 online adaptive control,901~1000不再修改控制器。



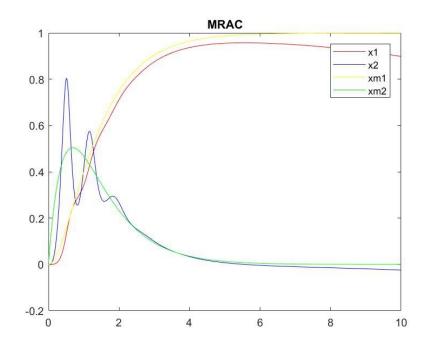
2-A. unit step 輸入測試

(1) unit step 對照組 Y ₀=0.025 Y ₁=0.5 Y ₂=0.005 Q₂₂=1000

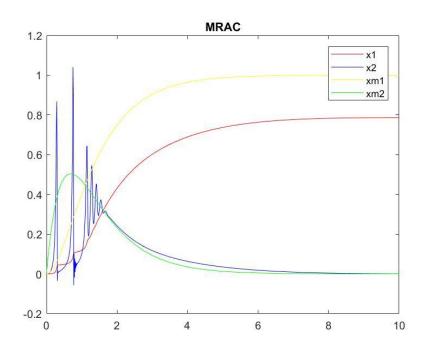


 $(2)Q=\begin{bmatrix}1&0\\0&q\end{bmatrix}$,明顯 Q_{22} 值越大,系統越穩定,若 Q_{22} 值不夠系統會發散。

降低 Q_{22} (γ $_0$ =0.025 γ $_1$ =0.5 γ $_2$ =0.005 Q_{22} =10)

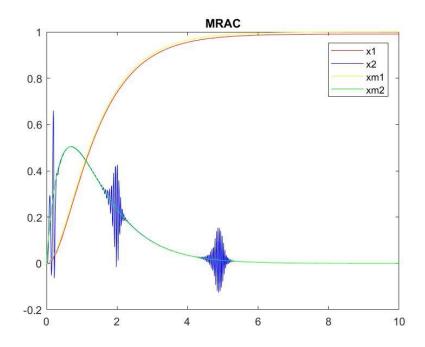


(2) Y ₀越大, x1 穩態誤差越糟, x1,x2 震盪情形持續較久。



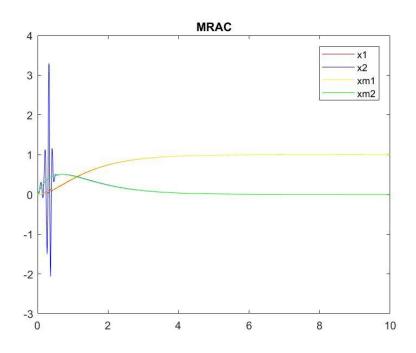
(3) γ :=越小,x2 震盪越久。貌似越大越好,也不會發散,但是往上調至定值後看起來效果都一樣。

降低 Y 1(Y 0=0.025 Y 1=0.005 Y 2=0.005 Q22=1000)



(4) γ 2 越大, x1、x2 的振幅都會變大也會振比較久, 其中 x2 影響非常嚴重。

增加 Y 2 (Y 0=0.025 Y 1=0.5 Y 2=0.5 Q22=1000)

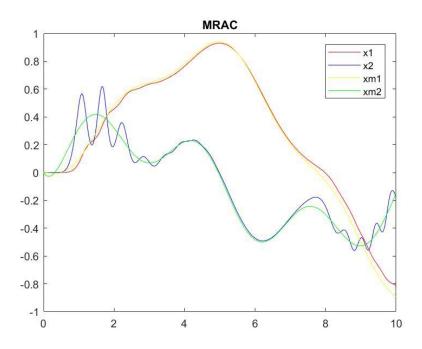


經多次測試結論:

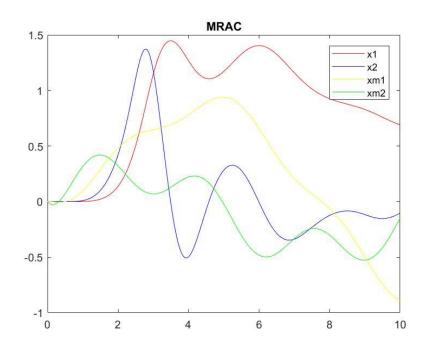
Q22要大、 γ 。要小 γ 1可大 γ 2盡量小,但這些參數太小系統都容易發散。 在三個 γ 中 γ 2最為敏感也最重要。

2-B.弦波輸入測試

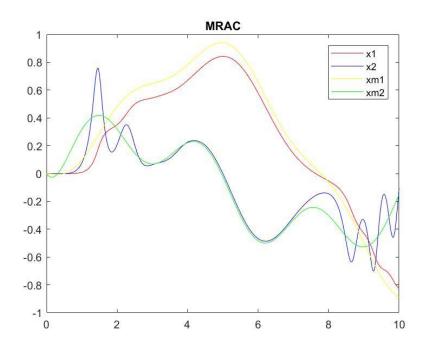
(1)弦波對照組 Y ₀=1 Y ₁=0.5 Y ₂=0.4 Q₂₂=1000



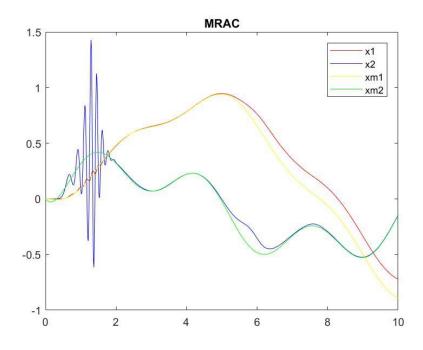
(2)同樣 Q22 越大越穩定



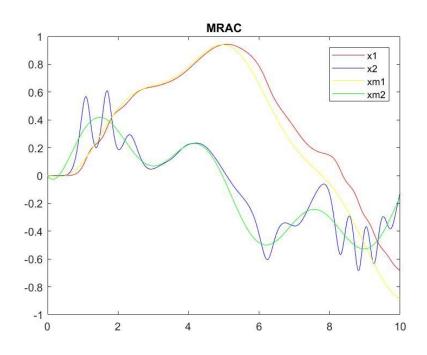
增加γ ο=(γ ο=10γ 1=0.5γ 2=0.4 Q22=1000),誤差變大



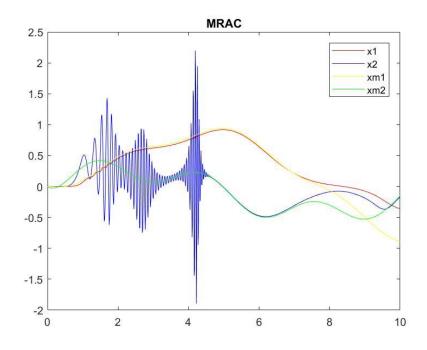
降低 γ \circ =(γ \circ =0.05 γ 1=0.5 γ 2=0.4 Q22=1000),暫態響應的震盪變嚴重。



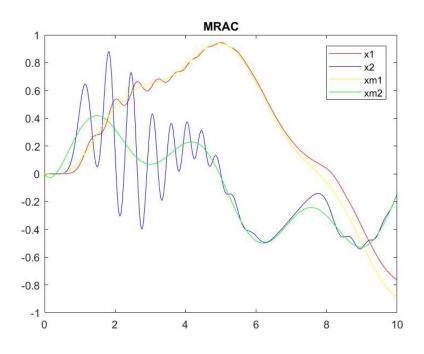
增加 γ 1 (γ 0=1 γ 1=5 γ 2=0.4 Q22=1000),誤差變大。



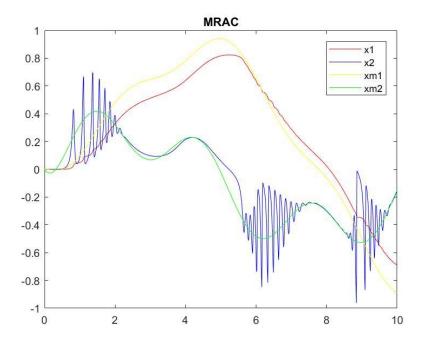
降低 γ ı (γ 0=1 γ 1=0.005 γ 2=0.4 Q22=1000),震盪情形持續較久。



增加 γ 2(γ □=1 γ □=0.5 γ 2=4 Q22=1000), X 要花更多時間追上 Xm。



降低 γ 2(γ 0=1 γ 1=0.5 γ 2=0.005 Q22=1000),後期震盪變明顯。



經多次測試結論:

 Q_{22} 要大,三個 γ 都有其較適當的範圍,不能太大或太小。

附錄(程式碼)

(1)閉迴路控制器

```
%close loop control
%result same as using equivalent open loop transfer func.
clear; clc;
totalStep=1000;
a1=0.3;a2=-0.88;b1=0.9;b2=0.6;%system
for k=1:totalStep
   d(k) = 0.01* (rand-0.5);
end
poly=conv([1,-0.82],conv([1,-0.5+0.5i],[1,-0.5-0.5i]));%pole
assignment
A=[1 b1 0;a1 b2 b1;a2 0 b2];
b=[poly(2)-a1;poly(3)-a2;poly(4)];
x=inv(A)*b;
alpha1=x(1);beta0=x(2);beta1=x(3);
y=[1:totalStep]*0;
u=[1:totalStep]*0;
r=[1:totalStep]*0;
e=[1:totalStep]*0;
r(1) = 0;
r(2) = 1;
r(3)=1;
for k=1:totalStep-2
 r(k+1)=1;
 e(k+1)=r(k+1)-y(k+1);
  u(k+1) = (-alpha1*u(k)+beta0*e(k+1)+beta1*e(k));
  y(k+2) = -a1*y(k+1) - a2*y(k) + b1*u(k+1) + b2*u(k) + d(k+2);
end
figure(1)
plot(y,'b');hold on;plot(u,'g');hold on;plot(r,'y');plot(e,'r');
xlabel("k");
legend('y','u','r','e');
title("3á3á3ú°µ¥X-t¦^±Â¤F (r=unit step)");
```

```
y=[1:totalStep]*0;
u=[1:totalStep]*0;
r=[1:totalStep]*0;
e=[1:totalStep]*0;
r(1) = \sin(6*1/20) + 0.5*\cos(6*1/15+3.2) + 0.2*\sin(2.57*1/13+1.36);
r(2) = sin(6*2/20) + 0.5*cos(6*2/15+3.2) + 0.2*sin(2.57*2/13+1.36);
r(3) = \sin(6*3/20) + 0.5*\cos(6*3/15+3.2) + 0.2*\sin(2.57*3/13+1.36);
for k=1:totalStep-2
r(k+1)=\sin(6*(k+1)/20)+0.5*\cos(6*(k+1)/15+3.2)+0.2*\sin(2.57*(k+1)/13+
1.36);
  e(k+1)=r(k+1)-y(k+1);
   u(k+1) = (-alpha1*u(k) + beta0*e(k+1) + beta1*e(k));
  y(k+2) = -a1*y(k+1) -a2*y(k) +b1*u(k+1) +b2*u(k) +d(k+2);
end
figure(2)
plot(y,'b');hold on;plot(u,'g');hold on;plot(r,'y');plot(e,'r');
xlabel("k");
legend('y','u','r','e');
title("^3á^3á^3á^5Ú^\circµ^4X^-t^+^\pmÂ^xF (r=^\odot¶^ai)");
```

(2)閉迴路控制器使用等效開環轉移函數

```
%design C(z) and using equivalent open loop transfer func.
clear; clc;
totalStep=1000;
a1=0.3;a2=-0.88;b1=0.9;b2=0.6;%system
for k=1:totalStep
  d(k) = 0.01* (rand-0.5);
end
poly=conv([1,-0.82],conv([1,-0.5+0.5i],[1,-0.5-0.5i]));%pole
assignment
A=[1 b1 0;a1 b2 b1;a2 0 b2];
b=[poly(2)-a1;poly(3)-a2;poly(4)];
x=inv(A)*b;
alpha1=x(1); beta0=x(2); beta1=x(3);
fprintf("alpha1=%f;beta0=%f;beta1=%f;\n",alpha1,beta0,beta1);
num=conv([b1,b2],[beta0,beta1]); %C(z)*G(z)
den=conv([1,a1,a2],[1,alpha1]);%C(z)*G(z)
fb num=num; %equivalent open loop sys.
fb den=[0,num]+den; %equivalent open loop sys.
y=[1:totalStep]*0;
u=[1:totalStep]*0;
r=[1:totalStep]*0;
y(1) = 0; y(2) = 0; y(3) = 0;
u(1) = 0; u(2) = 1; u(3) = 1;
for k=1:totalStep-3
 u(k+3)=1;
y(k+3) = -fb den(2)*y(k+2)-fb den(3)*y(k+1)-fb den(4)*y(k)+fb num(1)*u(
k+2)+fb num(2)*u(k+1)+fb num(3)*u(k)+d(k+3);
end
figure(1);
plot(y);hold on;plot(u);
legend('y','u=unit step');
title("design C(z) and using equivalent open loop transfer func.");
```

```
y=[1:totalStep]*0;
u=[1:totalStep]*0;
r=[1:totalStep]*0;
y(1) = 0; y(2) = 0; y(3) = 0;
u(1) = \sin(6*1/20) + 0.5*\cos(6*1/15+3.2) + 0.2*\sin(2.57*1/13+1.36);
u(2) = \sin(6*2/20) + 0.5*\cos(6*2/15+3.2) + 0.2*\sin(2.57*2/13+1.36);
u(3) = \sin(6*3/20) + 0.5*\cos(6*3/15+3.2) + 0.2*\sin(2.57*3/13+1.36);
for k=1:totalStep-3
u(k+3) = \sin(6*(k+2)/20) + 0.5*\cos(6*(k+2)/15+3.2) + 0.2*\sin(2.57*(k+2)/13+
1.36);
y(k+3) = -fb den(2)*y(k+2) - fb den(3)*y(k+1) - fb den(4)*y(k) + fb num(1)*u(
k+2)+fb num(2)*u(k+1)+fb num(3)*u(k)+d(k+3);
end
figure(2);
plot(y);hold on;plot(u);
legend('y','u=©¶ai');
title("design C(z) and using equivalent open loop transfer func.");
```

(3)1-a,b,c 總程式碼

```
clear; clc;
totalStep=200;
a1=0.3;a2=-0.88;b1=0.9;b2=0.6;%system
for k=1:totalStep
  d(k) = 0.1* (rand-0.5);
응응응응
%just run with unit step input
y1A=[1:totalStep]*0;
u1A=[1:totalStep]*0;
y1A(1)=0;y1A(2)=0;u1A(1)=0;u1A(2)=1;
for k=1:totalStep-2
 u1A(k+2)=1;
   y1A(k+2) = -a1*y1A(k+1) - a2*y1A(k) + b1*u1A(k+1) + b2*u1A(k) + d(k+2);
end
figure(1);
plot(y1A);hold on;plot(u1A);
xlabel("k");
ylabel("y(k)");
title("1-a-A (x_W^{a_3}G(z), u=1)");
응응응응
%just run with the given input
y1B=[1:totalStep]*0;
u1B=[1:totalStep]*0;
y1B(1) = 0; y1B(2) = 0;
u1B(1) = sin(6*1/20) + 0.5*cos(6*1/15+3.2) + 0.2*sin(2.57*1/13+1.36);
u1B(2) = sin(6*2/20) + 0.5*cos(6*2/15+3.2) + 0.2*sin(2.57*2/13+1.36);
for k=1:totalStep-2
u1B(k+2) = sin(6*(k+2)/20) + 0.5*cos(6*(k+2)/15+3.2) + 0.2*sin(2.57*(k+2)/1
3+1.36);
   y1B(k+2) = -a1*y1B(k+1) - a2*y1B(k) + b1*u1B(k+1) + b2*u1B(k) + d(k+2);
end
figure(2);
```

```
plot(y1B);hold on;plot(u1B);
xlabel("k");
ylabel("y(k)");
title("1-a-B (¤w<sup>a</sup>¾G(z),u¦pÃD¥Ø«ü©w)");
응응응응응
%use the optimal method to find the system parameter whit dataA
for k=3:length(y1A)+1
 phiA(k-1,1)=y1A(k-1);
phiA(k-1,2)=y1A(k-2);
 phiA(k-1,3)=u1A(k-1);
  phiA(k-1,4)=u1A(k-2);
end
tmp1A=[0 0 0 0;0 0 0 0;0 0 0 0;0 0 0];
tmp2A = [0 \ 0 \ 0 \ 0];
for k=3:totalStep
  for i=1:4
    for j=1:4
       tmp1A(i,j) = tmp1A(i,j) + phiA(k-1,j) * phiA(k-1,i);
    end
    tmp2A(i) = tmp2A(i) + y1A(k) * phiA(k-1, i);
 end
end
thetaA=inv(tmp1A)*tmp2A';
a1A=-thetaA(1);
a2A=-thetaA(2);
b1A=thetaA(3);
b2A=thetaA(4);
응응응응응
%use the optimal method to find the system parameter whit dataB
for k=3:length(y1B)+1
```

```
phiB(k-1,1) = y1B(k-1);
 phiB(k-1,2)=y1B(k-2);
  phiB(k-1,3)=u1B(k-1);
 phiB(k-1,4)=u1B(k-2);
end
tmp1B=[0 0 0 0;0 0 0;0 0 0;0 0 0;0 0 0];
tmp2B=[0 0 0 0];
for k=3:totalStep
  for i=1:4
     for j=1:4
        tmp1B(i,j) = tmp1B(i,j) + phiB(k-1,j) * phiB(k-1,i);
     end
     tmp2B(i) = tmp2B(i) + y1B(k) * phiB(k-1, i);
  end
end
thetaB=inv(tmp1B)*tmp2B';
a1B=-thetaB(1);
a2B=-thetaB(2);
b1B=thetaB(3);
b2B=thetaB(4);
응응응응응
%compare the ans
fprintf("Ans from A:\n");
fprintf("a1=%f (error=%2f )\n",a1A,(a1A-a1));
fprintf("a2=%f (error=%2f )\n",a2A,(a2A-a2));
fprintf("b1=%f (error=%2f ) \n", b1A, (b1A-b1));
fprintf("b2=%f (error=%2f )\n",b2A,(b2A-b2));
fprintf("Ans from B:\n");
fprintf("a1=%f (error=%2f ) \n",a1B,(a1B-a1));
fprintf("a2=%f (error=%2f )\n",a2B,(a2B-a2));
fprintf("b1=%f (error=%2f )\n",b1B,(b1B-b1));
fprintf("b2=%f (error=%2f )\n",b2B,(b2B-b2));
응응응응
```

```
%pole assignment
poly=conv([1,-0.82],conv([1,-0.5+0.5i],[1,-0.5-0.5i]));%characteristi
c poly.
const=[1 b1A 0;a1A b2A b1A;a2A 0 b2A];
b=[poly(2)-a1A;poly(3)-a2A;poly(4)];
x=inv(const)*b;
alpha1A=x(1);beta0A=x(2);beta1A=x(3);
응응응응
%pole assignment
poly=conv([1,-0.82],conv([1,-0.5+0.5i],[1,-0.5-0.5i]));%characteristi
c poly.
const=[1 b1B 0;a1B b2B b1B;a2B 0 b2B];
b = [poly(2) - a1B; poly(3) - a2B; poly(4)];
x=inv(const)*b;
alpha1B=x(1);beta0B=x(2);beta1B=x(3);
%compare the control design from dataA and dataB
%controller A
numA=conv([b1,b2],[beta0A,beta1A]);%C(z)*G(z)
denA=conv([1,a1,a2],[1,alpha1A]); %C(z)*G(z)
fb numA=numA; %equivalent open loop sys.
fb denA=[0,numA]+denA; %equivalent open loop sys.
%controller B
numB=conv([b1,b2], [beta0B,beta1B]); %C(z) *G(z)
denB=conv([1,a1,a2],[1,alpha1B]);%C(z)*G(z)
fb numB=numB; %equivalent open loop sys.
fb denB=[0,numB]+denB; %equivalent open loop sys.
%controller A with unit step input
y3A=[1:totalStep]*0;
u3A=[1:totalStep]*0;
y3A(1)=0; y3A(2)=0; y3A(3)=0;
u3A(1)=1;u3A(2)=1;u3A(3)=1;
for k=1:totalStep-3
```

```
u3A(k+3)=1;
y3A(k+3) = -fb denA(2)*y3A(k+2)-fb denA(3)*y3A(k+1)-fb denA(4)*y3A(k)+f
b numA(1)*u3A(k+2)+fb numA(2)*u3A(k+1)+fb numA(3)*u3A(k)+d(k+3);
end
%controller B with unit step input
y3B=[1:totalStep]*0;
u3B=[1:totalStep]*0;
y3B(1)=0; y3B(2)=0; y3B(3)=0;
u3B(1)=1;u3B(2)=1;u3B(3)=1;
for k=1:totalStep-3
 u3B(k+3)=1;
y3B(k+3)=-fb denB(2)*y3B(k+2)-fb denB(3)*y3B(k+1)-fb denB(4)*y3B(k)+f
b numB(1)*u3B(k+2)+fb numB(2)*u3B(k+1)+fb numB(3)*u3B(k)+d(k+3);
end
figure(3);
plot(y3A);hold on;plot(y3B);hold on;plot(u3B);
xlabel("k");
ylabel("y(k)");
legend('controllerA','controllerB','u=step input');
title("1-c-C (¤ñ ûA,B3]-p\X\ao±±"î¾1,u=1)");
%controller A with given input
y3A=[1:totalStep]*0;
u3A=[1:totalStep]*0;
y3A(1)=0; y3A(2)=0; y3A(3)=0;
u3A(1) = sin(6*1/20) + 0.5*cos(6*1/15+3.2) + 0.2*sin(2.57*1/13+1.36);
u3A(2)=sin(6*2/20)+0.5*cos(6*2/15+3.2)+0.2*sin(2.57*2/13+1.36);
u3A(3) = sin(6*3/20) + 0.5*cos(6*3/15+3.2) + 0.2*sin(2.57*3/13+1.36);
for k=1:totalStep-3
u3A(k+3) = sin(6*(k+3)/20) + 0.5*cos(6*(k+3)/15+3.2) + 0.2*sin(2.57*(k+3)/1
3+1.36);
y3A(k+3)=-fb_denA(2)*y3A(k+2)-fb_denA(3)*y3A(k+1)-fb denA(4)*y3A(k)+f
b numA(1)*u3A(k+2)+fb numA(2)*u3A(k+1)+fb numA(3)*u3A(k)+d(k+3);
end
```

```
%controller B with given input
y3B=[1:totalStep]*0;
u3B=[1:totalStep]*0;
y3B(1)=0; y3B(2)=0; y3B(3)=0;
u3B(1) = sin(6*1/20) + 0.5*cos(6*1/15+3.2) + 0.2*sin(2.57*1/13+1.36);
u3B(2) = sin(6*2/20) + 0.5*cos(6*2/15+3.2) + 0.2*sin(2.57*2/13+1.36);
u3B(3) = sin(6*3/20) + 0.5*cos(6*3/15+3.2) + 0.2*sin(2.57*3/13+1.36);
for k=1:totalStep-3
u3B(k+3) = sin(6*(k+3)/20) + 0.5*cos(6*(k+3)/15+3.2) + 0.2*sin(2.57*(k+3)/1
3+1.36);
y3B(k+3)=-fb denB(2)*y3B(k+2)-fb denB(3)*y3B(k+1)-fb denB(4)*y3B(k)+f
b_numB(1)*u3B(k+2)+fb_numB(2)*u3B(k+1)+fb_numB(3)*u3B(k)+d(k+3);
end
figure(4);
plot(y3A);hold on;plot(y3B);hold on;plot(u3B);
xlabel("k");
ylabel("y(k)");
legend('controllerA','controllerB','u');
title("1-c-C (¤ñ ûA,B3]-p\XXao±±"î¾1)");
```

(4)1-d Online Adaptive Control (A、B 小題大同小異就只附上一個)

```
%online adaptive control
%(unit step input)
clear;clc;
totalStep=1000;step1=50;step2=900;
a1=0.3;a2=-0.88;b1=0.9;b2=0.6;%system
Correctalpha1=4.435315;%C(z) design from the real sys.
Correctbeta0=-7.283683;
Correctbeta1=5.821795;
for k=1:totalStep
  d(k) = 0.01* (rand-0.5);
end
y=[1:totalStep]*0;
u=[1:totalStep]*0;
r=[1:totalStep]*0;
e=[1:totalStep]*0;
응응응응
%just run with unit step input
r(1)=0;r(2)=1;r(3)=1;%unit stpe input
u(1) = 0; u(2) = 1; u(3) = 1;
for k=1:step1
 r(k+2)=1;%unit stpe input
  u(k+2)=r(k+2);
  y(k+2) = -a1*y(k+1) -a2*y(k) +b1*u(k+1) +b2*u(k) +d(k+2);
end
%first time to find the system parameter
for k=3:step1
 phiA(k-1,1)=y(k-1);
 phiA(k-1,2) = y(k-2);
 phiA(k-1,3)=u(k-1);
 phiA(k-1,4)=u(k-2);
end
```

```
tmp1A=[0 0 0 0;0 0 0 0;0 0 0 0;0 0 0 0];
tmp2A=[0 0 0 0];
for k=3:step1
  for i=1:4
     for j=1:4
         tmp1A(i,j) = tmp1A(i,j) + phiA(k-1,j) * phiA(k-1,i);
     end
     tmp2A(i) = tmp2A(i) + y(k) * phiA(k-1,i);
  end
end
thetaA=inv(tmp1A)*tmp2A';
a1A=-thetaA(1);
a2A=-thetaA(2);
b1A=thetaA(3);
b2A=thetaA(4);
fprintf("a1=%f (error=%2f )\n",a1A,(a1A-a1));
fprintf("a2=%f (error=%2f )\n",a2A,(a2A-a2));
fprintf("b1=%f (error=%2f )\n",b1A,(b1A-b1));
fprintf("b2=%f (error=%2f)\n",b2A,(b2A-b2));
%design C(z) with optimal parameter (pole assignment)
poly=conv([1,-0.82],conv([1,-0.5+0.5i],[1,-0.5-0.5i]));%characteristi
c poly.
const=[1 b1A 0;a1A b2A b1A;a2A 0 b2A];
b=[poly(2)-a1A;poly(3)-a2A;poly(4)];
x=inv(const)*b;
alphalA=x(1);beta0A=x(2);beta1A=x(3);%C(z) with optimal parameter
fprintf("alpha1=%f (err=%f) \n",alpha1A,abs(Correctalpha1-alpha1A));
fprintf("beta0=%f (err=%f) \n", beta1A, abs(Correctbeta0-beta0A));
fprintf("betal=%f (err=%f) \n", betalA, abs(Correctbetal-betalA));
응응응응응
%online adaptive
%close loop control & redesign C(z)
for k=step1+1:step2
```

```
fprintf("Now Step:k=%d !!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!\n",k);
r(k+1)=1;
e(k+1) = r(k+1) - y(k+1);
u(k+1) = (-alpha1A*u(k) + beta0A*e(k+1) + beta1A*e(k));
y(k+2) = -a1*y(k+1) -a2*y(k) +b1*u(k+1) +b2*u(k) +d(k+2);
%redesign C(z)
 for i=3:k
   phiA(i-1,1)=y(i-1);
   phiA(i-1,2)=y(i-2);
   phiA(i-1,3)=u(i-1);
   phiA(i-1,4)=u(i-2);
end
tmp1A=[0 0 0 0;0 0 0 0;0 0 0 0;0 0 0];
tmp2A=[0 0 0 0];
 for m=3:k
   for i=1:4
      for j=1:4
          tmp1A(i,j) = tmp1A(i,j) + phiA(m-1,j) * phiA(m-1,i);
      end
       tmp2A(i) = tmp2A(i) + y(m) * phiA(m-1,i);
   end
end
 thetaA=inv(tmp1A)*tmp2A';
a1A=-thetaA(1);
a2A=-thetaA(2);
b1A=thetaA(3);
b2A=thetaA(4);
 fprintf("a1=%f (error=%2f )\n",a1A,(a1A-a1));
fprintf("a2=%f (error=%2f ) \n", a2A, (a2A-a2));
fprintf("b1=%f (error=%2f ) \n", b1A, (b1A-b1));
fprintf("b2=%f (error=%2f )\n",b2A,(b2A-b2));
%design C(z) (pole assignment)
```

```
poly=conv([1,-0.82],conv([1,-0.5+0.5i],[1,-0.5-0.5i]));%characteristi
c poly.
   const=[1 b1A 0;a1A b2A b1A;a2A 0 b2A];
   b=[poly(2)-a1A;poly(3)-a2A;poly(4)];
  x=inv(const)*b;
  alpha1A=x(1);beta0A=x(2);beta1A=x(3);%C(z) with optimal parameter
   fprintf("alpha1=%f (err=%f)
\n",alpha1A,abs(Correctalpha1-alpha1A));
   fprintf("beta0=%f (err=%f) \n", beta1A, abs(Correctbeta0-beta0A));
  fprintf("beta1=%f (err=%f) \n", beta1A, abs(Correctbeta1-beta1A));
end
응응응응응
%close loop control only
for k=step2+1:totalStep-2
 r(k+1)=1;
  e(k+1)=r(k+1)-y(k+1);
  u(k+1) = (-alpha1A*u(k) + beta0A*e(k+1) + beta1A*e(k));
 y(k+2) = -a1*y(k+1) - a2*y(k) + b1*u(k+1) + b2*u(k) + d(k+2);
end
plot(y,'r');hold on;plot(r,'g');
xlabel("k");
legend('y','r=unit step');
title("online adaptive control");
```

(5)MRAC

```
%MRAC
clear;clc;
totaltime=10;
delta=0.01;
totalstep=totaltime/delta;
%model
xm1(1) = 0; xm2(1) = 0;
for k=1:totalstep
  r(k) = 1;
  r(k) = sin(0.5*k*delta) + 0.3*cos(2*k*delta+4);
  xm1 dot(k) = xm2(k);
 xm2 dot(k) = -2*xm1(k) - 3*xm2(k) + 2*r(k);
  xm1(k+1)=xm1(k)+xm1 dot(k)*delta;
   xm2(k+1)=xm2(k)+xm2 dot(k)*delta;
end
%select para.
Q=[1 0;0 1000];
Am = [0 1; -2 -3]; bm = 2;
b=1;
P=lyap(Am,Q);
gamma0=1;gamma1=0.5;gamma2=4;
theta0(1)=0; theta1(1)=0; theta2(1)=0;
x1(1)=0; x2(1)=0;
for k=1:totalstep
% r(k)=1;
   r(k) = sin(0.5*k*delta) + 0.3*cos(2*k*delta+4);
   u(k) = theta0(k) *r(k) + theta1(k) *x1(k) + theta2(k) *x2(k);
  x1 dot(k) = x2(k);
   x2 dot(k) = 0.4*x1(k) + 1.8*x2(k) + 1*u(k);
   x1(k+1)=x1(k)+x1 dot(k)*delta;
   x2(k+1)=x2(k)+x2 dot(k)*delta;
```

```
e1(k) = xm1(k) - x1(k);
   e2(k) = xm2(k) - x2(k);
   zeta(k)=0.5*(P(1,2)*e1(k)+P(2,2)*e2(k));
   theta0 dot(k) = zeta(k) *r(k) / (b*gamma0);
   theta1 dot(k) = zeta(k) *x1(k) / (b*gamma1);
   theta2 dot(k) = zeta(k) *x2(k) / (b*gamma2);
   theta0(k+1)=theta0(k)+theta0 dot(k)*delta;
   theta1(k+1) = theta1(k) + theta1 dot(k) * delta;
   theta2(k+1) = theta2(k) + theta2_dot(k) * delta;
end
plot([0:1:totalstep]*delta,x1,'r');hold on;
plot([0:1:totalstep]*delta,x2,'b');hold on;
plot([0:1:totalstep]*delta,xm1,'y');hold on;
plot([0:1:totalstep]*delta,xm2,'g');hold on;
legend('x1','x2','xm1','xm2');
title('MRAC');
```