#### **3621 - Power Calculus**

#### Asia - Yokohama - 2006/2007

Starting with x and repeatedly multiplying by x, we can compute  $x^{31}$  with thirty multiplications:

$$x^2 = x \times x$$
,  $x^3 = x^2 \times x$ ,  $x^4 = x^3 \times x$ , ...,  $x^{31} = x^{30} \times x$ .

The operation of squaring can appreciably shorten the sequence of multiplications. The following is a way to compute  $x^{31}$  with eight multiplications:

$$x^2 = x \times x$$
,  $x^3 = x^2 \times x$ ,  $x^6 = x^3 \times x^3$ ,  $x^7 = x^6 \times x$ ,  $x^{14} = x^7 \times x^7$ ,  $x^{15} = x^{14} \times x$ ,  $x^{30} = x^{15} \times x^{15}$ ,  $x^{31} = x^{30} \times x$ .

This is not the shortest sequence of multiplications to compute  $x^{31}$ . There are many ways with only seven multiplications. The following is one of them:

$$x^2 = x \times x$$
,  $x^4 = x^2 \times x^2$ ,  $x^8 = x^4 \times x^4$ ,  $x^{10} = x^8 \times x^2$ ,  $x^{20} = x^{10} \times x^{10}$ ,  $x^{30} = x^{20} \times x^{10}$ ,  $x^{31} = x^{30} \times x$ .

There however is no way to compute  $x^{31}$  with fewer multiplications. Thus this is one of the most efficient ways to compute  $x^{31}$  only by multiplications.

If division is also available, we can find a shorter sequence of operations. It is possible to compute  $x^{31}$  with six operations (five multiplications and one division):

$$x^2 = x \times x$$
,  $x^4 = x^2 \times x^2$ ,  $x^8 = x^4 \times x^4$ ,  $x^{16} = x^8 \times x^8$ ,  $x^{32} = x^{16} \times x^{16}$ ,  $x^{31} = x^{32} \div x$ .

This is one of the most efficient ways to compute  $x^{31}$  if a division is as fast as a multiplication.

Your mission is to write a program to find the least number of operations to compute  $x^n$  by multiplication and division starting with x for the given positive integer n. Products and quotients appearing in the sequence of operations should be x to a positive integer's power. In other words,  $x^3$ , for example, should never appear.

### Input

The input is a sequence of one or more lines each containing a single integer n. n is positive and less than or equal to 1000. The end of the input is indicated by a zero.

## **Output**

Your program should print the least total number of multiplications and divisions required to compute  $x^n$  starting with x for the integer n. The numbers should be written each in a separate line without any superfluous characters such as leading or trailing spaces.

### **Sample Input**

# **Sample Output**

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