

## 3887 - Slim Span

#### Asia - Tokyo - 2007/2008

Given an undirected weighted graph G, you should find one of spanning trees specified as follows.

The graph G is an ordered pair (V, E), where V is a set of vertices  $\{v_1, v_2, ..., v_n\}$  and E is a set of undirected edges  $\{e_1, e_2, ..., e_m\}$ . Each edge  $e \in E$  has its weight w(e).

A spanning tree T is a tree (a connected subgraph without cycles) which connects all the n vertices with n - 1 edges. The slimness of a spanning tree T is defined as the difference between the largest weight and the smallest weight among the n - 1 edges of T.

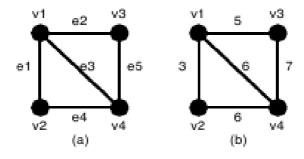


Figure 5: A graph G and the weights of the edges

For example, a graph G in Figure 5(a) has four vertices  $\{v_1, v_2, v_3, v_4\}$  and five undirected edges  $\{e_1, e_2, e_3, e_4, e_5\}$ . The weights of the edges are  $w(e_1) = 3$ ,  $w(e_2) = 5$ ,  $w(e_3) = 6$ ,  $w(e_4) = 6$ ,  $w(e_5) = 7$  as shown in Figure 5(b).

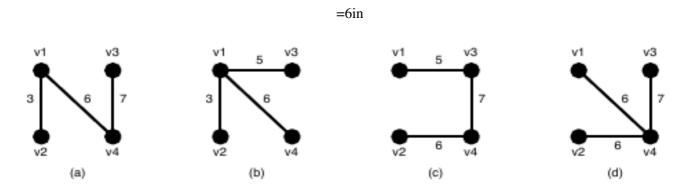


Figure 6: Examples of the spanning trees of G

There are several spanning trees for G. Four of them are depicted in Figure 6(a) a 4(d). The spanning tree  $T_a$  in Figure 6(a) has three edges whose weights are 3, 6 and 7. The largest weight is 7 and the smallest weight is

3 so that the slimness of the tree  $T_{\rm a}$  is 4. The slimnesses of spanning trees  $T_{\rm b}$ ,  $T_{\rm c}$  and  $T_{\rm d}$  shown in Figure 6(b), (c) and (d) are 3, 2 and 1, respectively. You can easily see the slimness of any other spanning tree is greater than or equal to 1, thus the spanning tree  $T_{\rm d}$  in Figure 6(d) is one of the slimnest spanning trees whose slimness is 1.

Your job is to write a program that computes the smallest slimness.

#### Input

The input consists of multiple datasets, followed by a line containing two zeros separated by a space. Each dataset has the following format.

```
n m 
 a_1 b_1 w_1 
 \vdots 
 a_m b_m w_m
```

Every input item in a dataset is a non-negative integer. Items in a line are separated by a space.

*n* is the number of the vertices and *m* the number of the edges. You can assume  $2 \le n \le 100$  and  $0 \le m \le n(n - 100)$ 

1)/2 .  $a_k$  and  $b_k$  (k = 1,..., m) are positive integers less than or equal to n, which represent the two vertices  $v_{a_k}$  and  $v_{b_k}$  connected by the k-th edge  $e_k$ .  $w_k$  is a positive integer less than or equal to 10000, which indicates the weight of  $e_k$ . You can assume that the graph G = (V, E) is simple, that is, there are no self-loops (that connect the same vertex) nor parallel edges (that are two or more edges whose both ends are the same two vertices).

### **Output**

For each dataset, if the graph has spanning trees, the smallest slimness among them should be printed. Otherwise, `-1' should be printed. An output should not contain extra characters.

## Sample Input

```
4 5
1 2 3
1 3 5
1 4 6
2 4 6
3 4 7
4 6
1 2 10
1 3 100
1 4 90
2 3 20
2 4 80
3 4 40
2 1
1 2 1
3 0
3 1
1 2 1
3 3
1 2 2
```

```
2 3 5
1 3 6
5 10
1 2 110
1 3 120
1 4 130
1 5 120
2 3 110
2 4 120
2 5 130
3 4 120
3 5 110
4 5 120
5 10
1 2 9384
1 3 887
1 4 2778
1 5 6916
2 3 7794
2 4 8336
2 5 5387
3 4 493
3 5 6650
4 5 1422
5 8
1 2 1
2 3 100
3 4 100
4 5 100
1 5 50
2 5 50
3 5 50
4 1 150
0 0
```

# **Sample Output**

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