

2. Paired Permutation Test

- Logistic, Gompertz 모델에 대해 segment 별로 Paired Permutation t-test 시행

- Logistic :

$$f(t) = \sum_{i=1}^n \left(\frac{\alpha_i}{1 + e^{\beta_i - \gamma_i t}} + q_i \right) I_{seg_i}(t)$$

$$= \frac{\alpha_1}{1 + e^{\beta_1 - \gamma_1 t}} I_{seg_1}(t) + \left(\frac{\alpha_2}{1 + e^{\beta_2 - \gamma_2 t}} + q_2 \right) I_{seg_2}(t)$$

where q_i is number of cumulative cases at breakpoint i ($q_1 = 0$).

$$I_{seg_i}(t) = \begin{cases} 1, & t \in seg_i \\ 0, & t \notin seg_i \end{cases} \text{ is indicator function,}$$

seg_i is set of index which is in i th wave.

- Gompertz :

$$f(t) = \sum_{i=1}^n (\alpha_i e^{-\beta_i e^{-\gamma_i t}} + q_i) I_{seg_i}(t)$$

$$= (\alpha_1 e^{-\beta_1 e^{-\gamma_1 t}} + q_1) I_{seg_1}(t) + (\alpha_2 e^{-\beta_2 e^{-\gamma_2 t}} + q_2) I_{seg_2}(t)$$

where q_i is number of cumulative cases at breakpoint i ($q_1 = 0$).

$$I_{seg_i}(t) = \begin{cases} 1, & t \in seg_i \\ 0, & t \notin seg_i \end{cases} \text{ is indicator function,}$$

seg_i is set of index which is in i th wave.



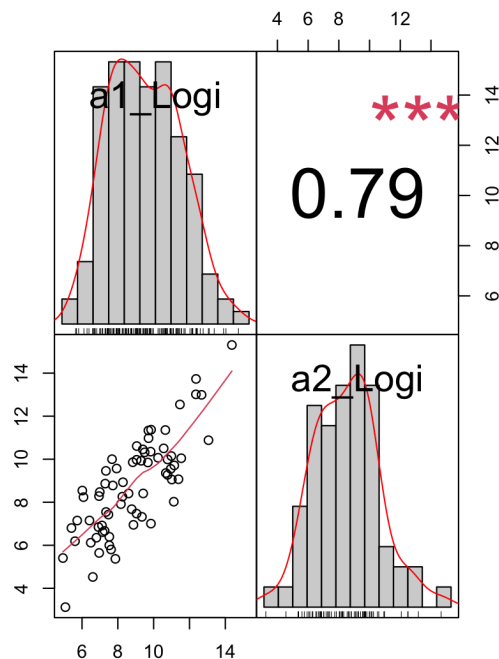
2. Paired Permutation Test

- 하나의 국가에서의 시점(segment)에 따른 평균 차이 검정이므로 등분산 검정은 필요 없음.
- 1000번을 복원추출한 t-test statistic을 검정
(이때의 permutation test의 t-statistic은 paired t-value)
- **Empirical p-value**((paired t-value) 오른쪽에 있는 개수들의 평균)로 귀무가설 기각 여부 결정
- **귀무가설 (H0)**
: COVID-19 재확산에 따른 Segment별 Growth Curve Model의 계수는 유의미한 차이가 없다.

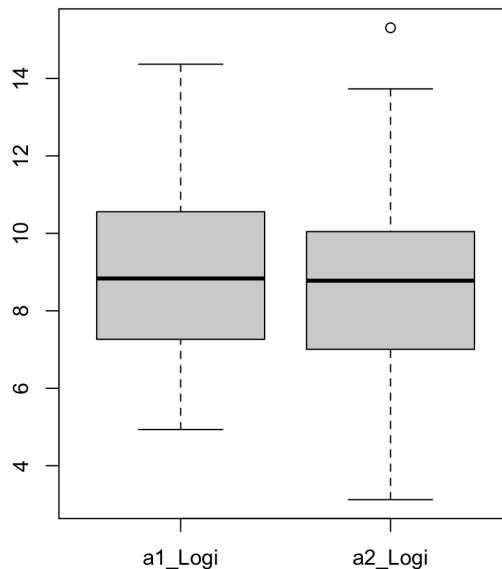
Result Analysis

2-1. Logistic Coefficient “a”

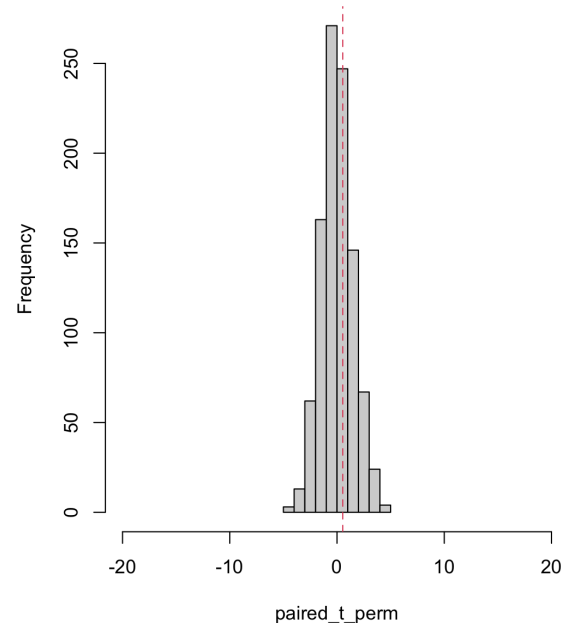
- Logistic Model의 a coefficient (empirical p-value : 0.692)



Boxplots for Logistic coef. a between two segments



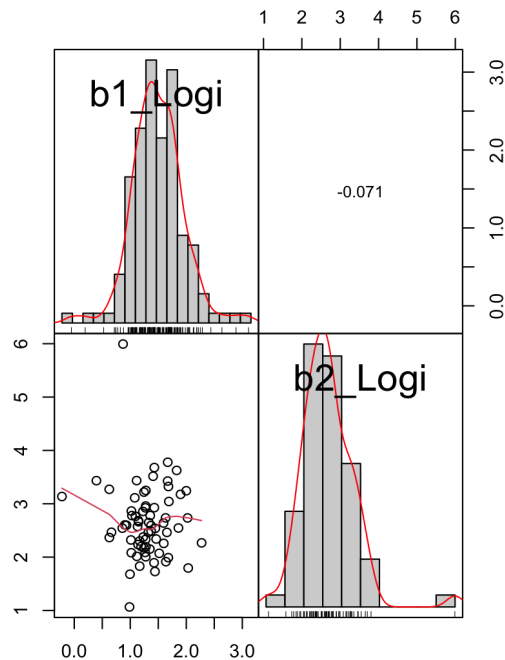
Paired Permutation Test for $a1_Logi$ & $a2_Logi$



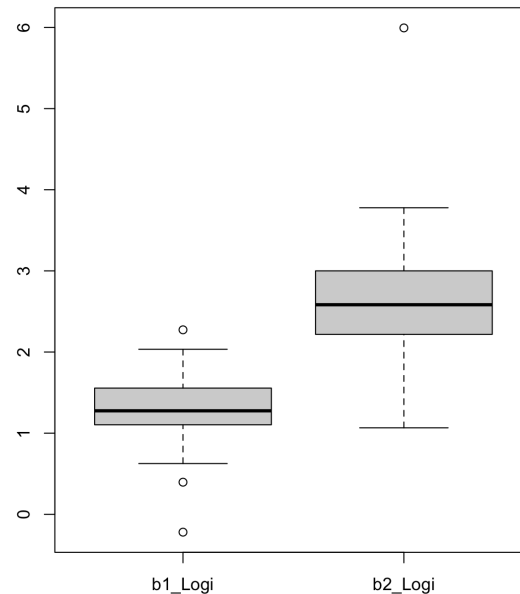
Result Analysis

2-1. Logistic Coefficient “b”

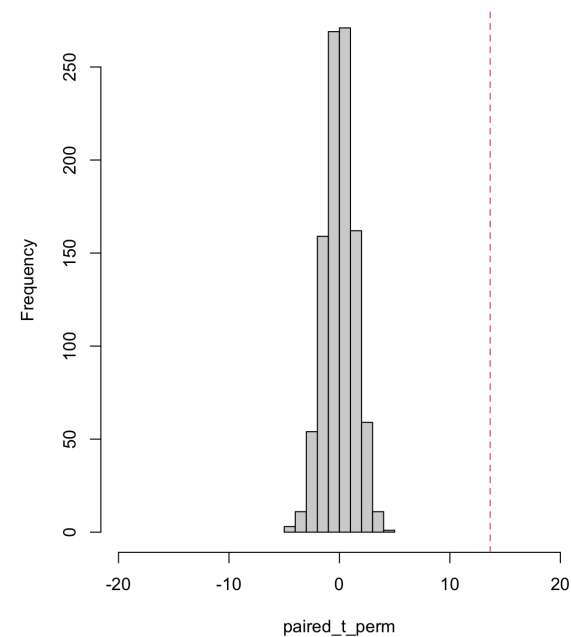
- Logistic Model의 b coefficient (empirical p-value : 0)



Boxplots for Logistic coefficient b between two segments



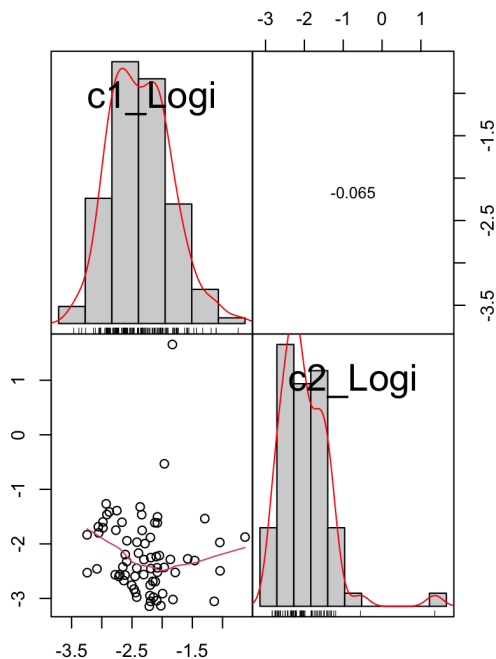
Paired Permutation Test for b1_Logi & b2_Logi



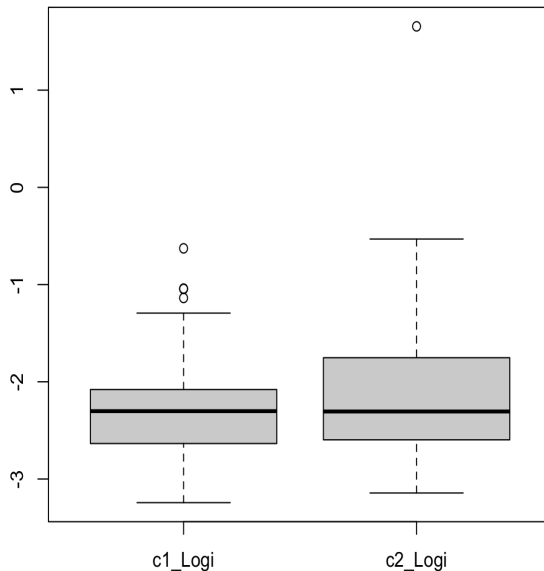
Result Analysis

2-1. Logistic Coefficient “c”

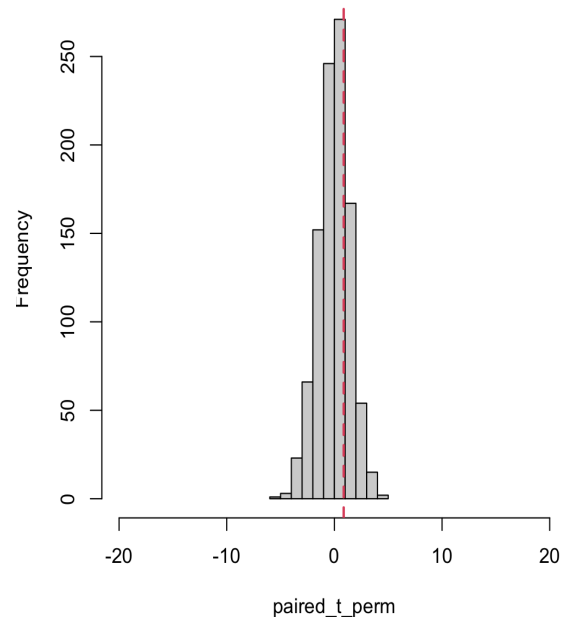
- Logistic Model의 c coefficient (empirical p-value : 0.541)



Boxplots for Logistic coefficient c between two segments

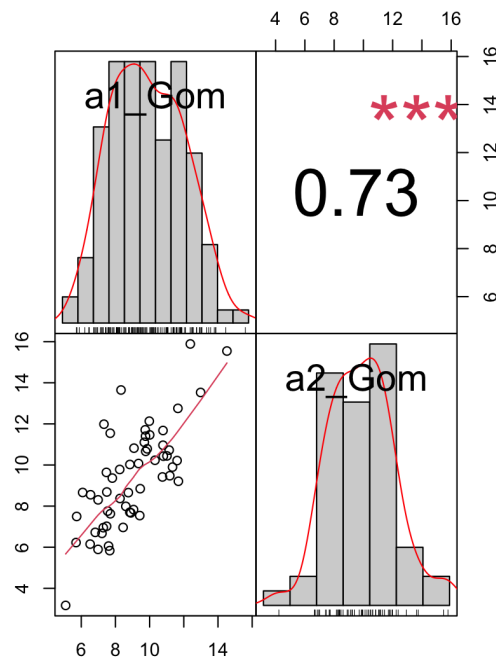


Paired Permutation Test for c1_Logi & c2_Logi

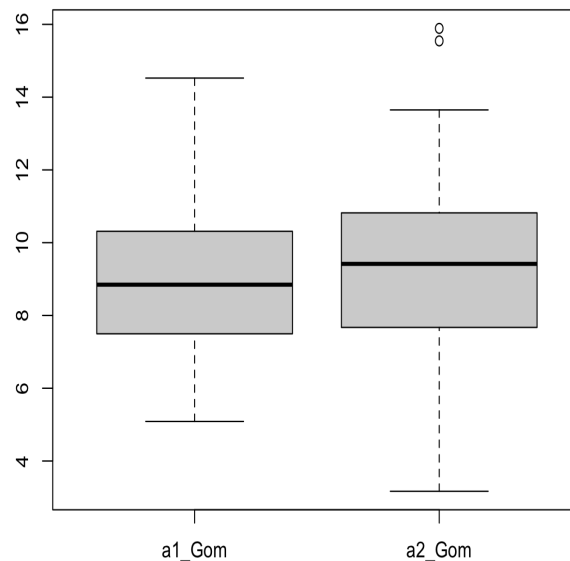


Result Analysis 2-2. Gompertz Coefficient “a”

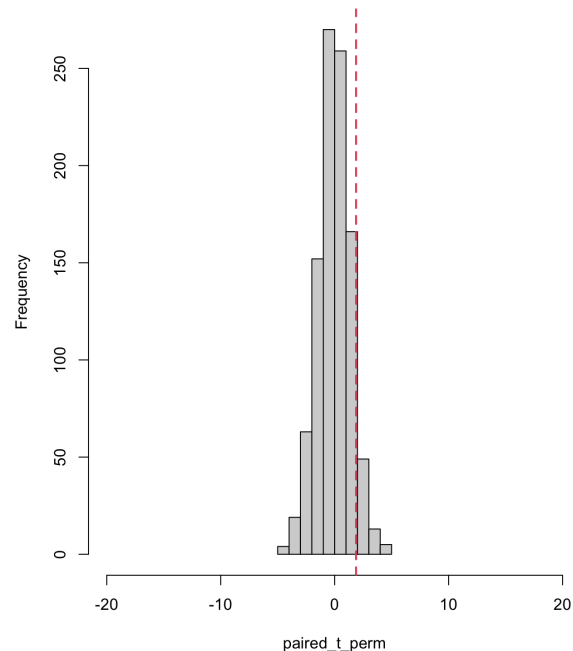
- Gompertz Model의 a coefficient (empirical p-value : 0.177)



Boxplots for Gompertz coefficient a between two segments



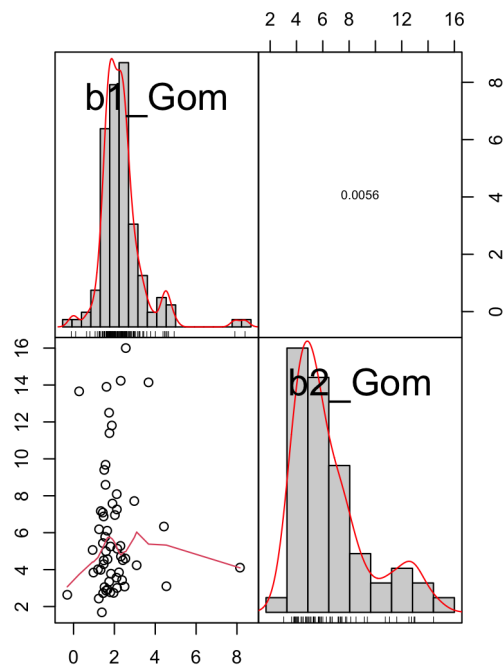
Paired Permutation Test for a1_Gom & a2_Gom



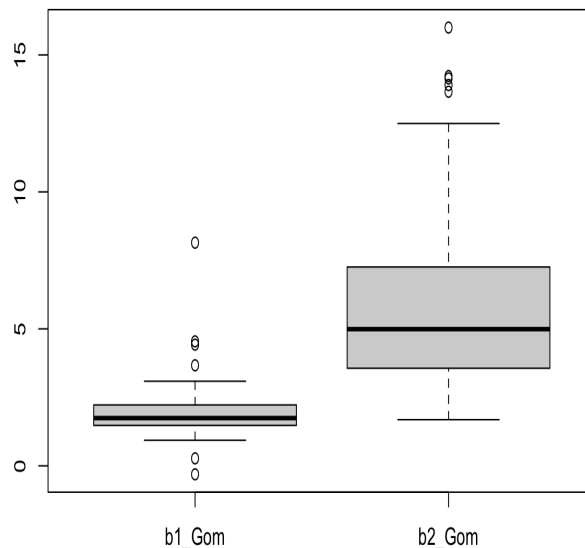
Result Analysis

2-2. Gompertz Coefficient “b”

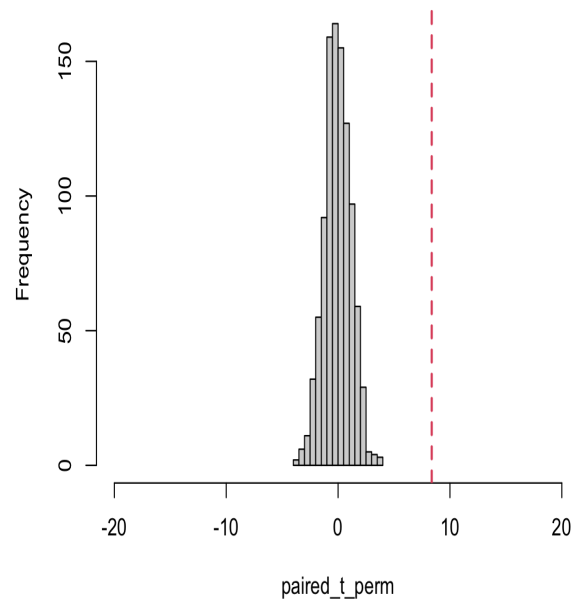
- Gompertz Model의 b coefficient (empirical p-value : 0)



Boxplots for Gompertz coefficient b between two segments



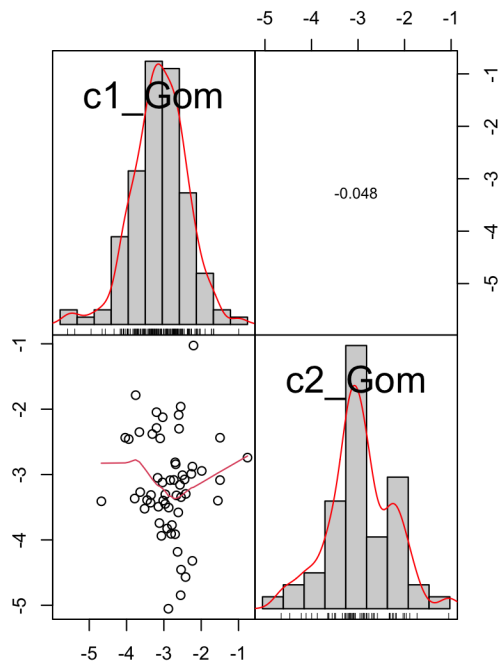
Paired Permutation Test for $b1_Gom$ & $b2_Gom$



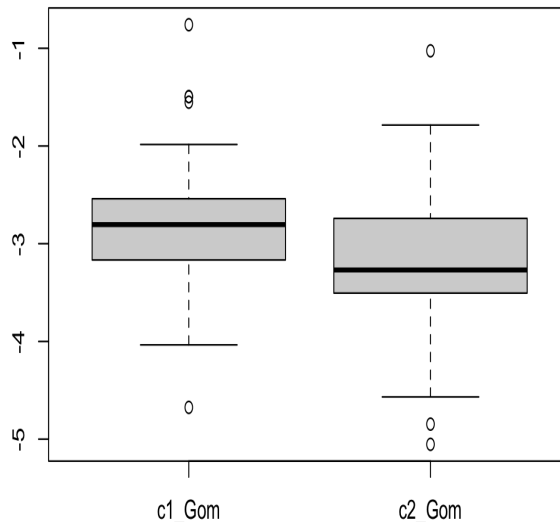
Result Analysis

2-2. Gompertz Coefficient “c”

- Gompertz Model의 c coefficient (empirical p-value : 0.087)



Boxplots for Gompertz coefficient c between two segments



Paired Permutation Test for c_1_Gom & c_2_Gom

