## Filtering not properly fitted countries using MSSE

01월 04일



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생물정보통계 연구실

**박사과정** 구태완 **석사과정** 한결희, 이도은 **학부과정** 고영현, 김학용, 김태현, 정혜원

#### MSE vs MAPE

Mean Squared Error (MSE) vs Mean Absolute Percentage Error (MAPE)

- 
$$MSE = \frac{1}{N} \sum_{t=1}^{N} (Y_t - \widehat{Y}_t)^2$$
 -> Scale을 반영하지 못함.

- 
$$MAPE = \frac{100}{N} \sum_{t=1}^{N} |\frac{Y_t - \widehat{Y}_t}{Y_{t+1}}|$$
 ->  $Y_t$  (일일 확진자 수)가 작으면 과대추정.

where  $\mathbf{Y_t}$  is the number of daily cases ,  $\widehat{\mathbf{Y_t}}$  is the predicted value for  $Y_t$  ,

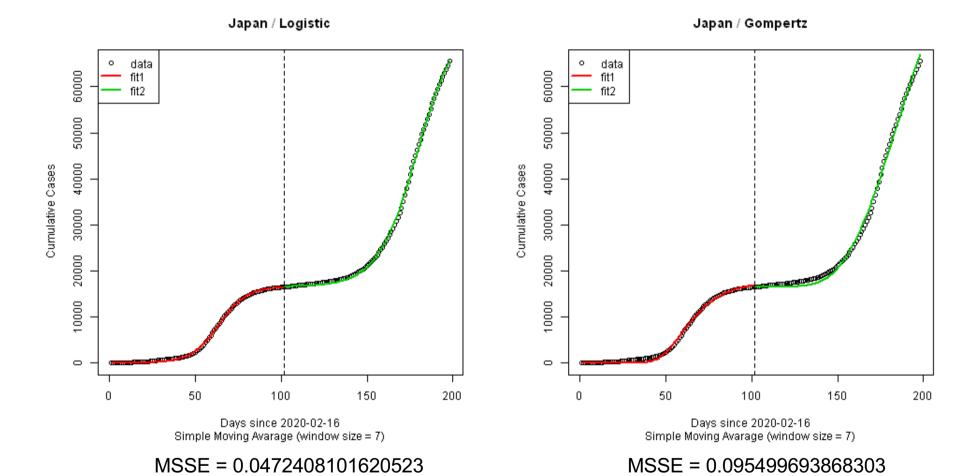
### **MSSE**

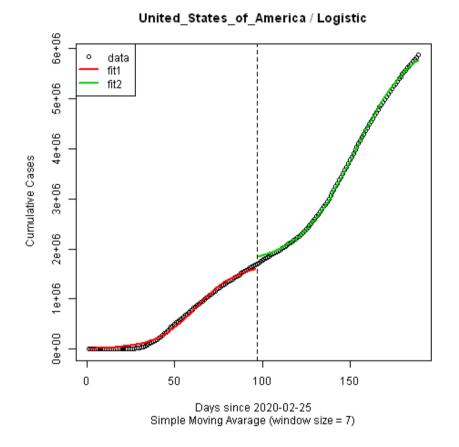
#### **Mean Squared Scaled Error (MSSE)**

$$-MSSE = \frac{1}{N} \sum_{t=1}^{N} \left( \frac{Y_t - \widehat{Y}_t}{\overline{Y}} \right)^2$$

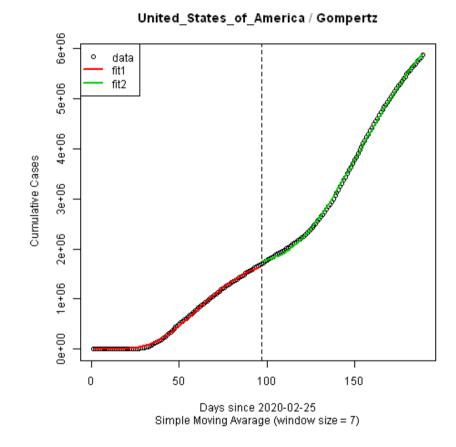
where  $\mathbf{Y}_t$  is the number of daily cases ,  $\widehat{\mathbf{Y}_t}$  is the predicted value for  $Y_t$  ,

 $\overline{\mathbf{Y}}$  is the mean of  $\{Y_t\}$  for t = 1, ..., N

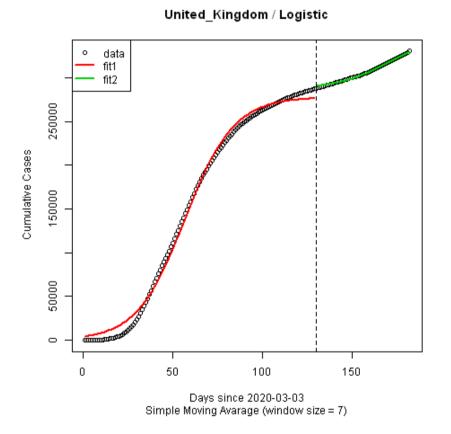




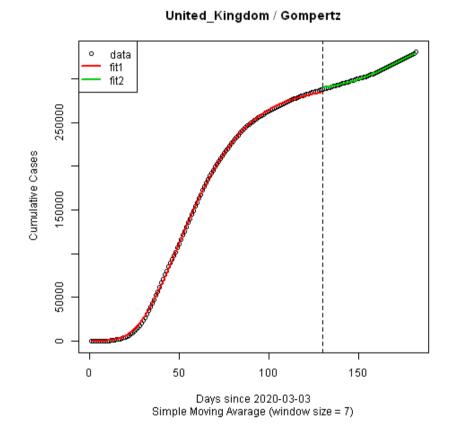




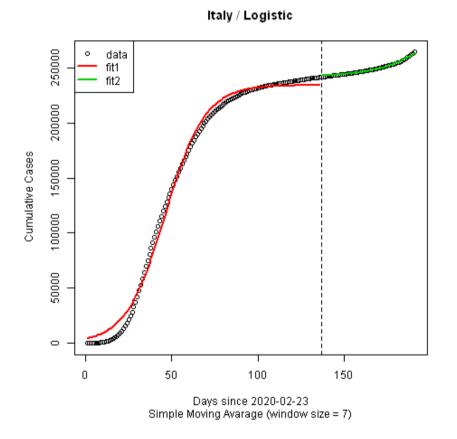
MSSE = 0.0230935353651733



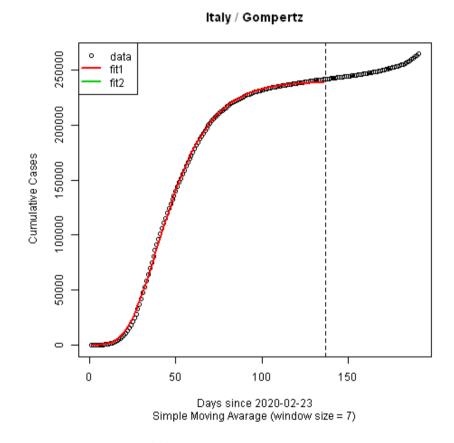




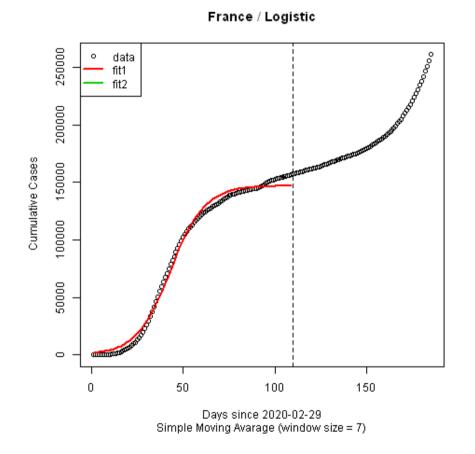
MSSE = 0.0251241604433823



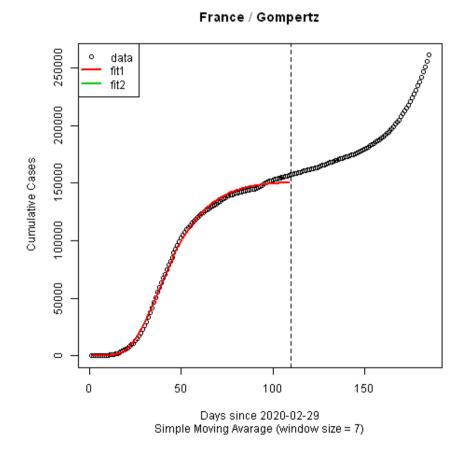
MSSE = 0.1474903497915



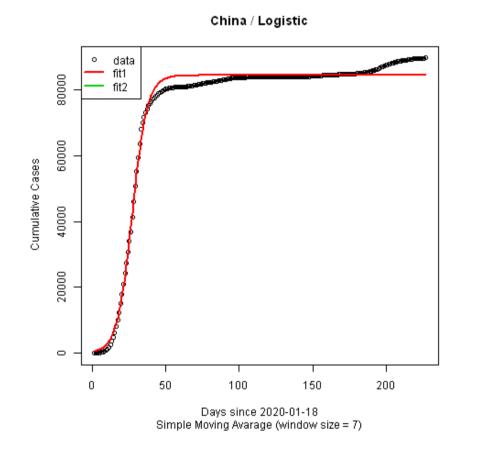
MSSE = 0.0219116461768186

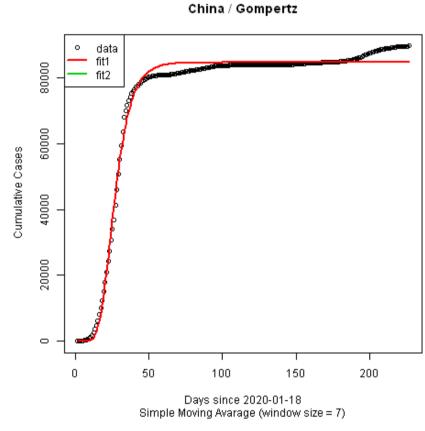


MSSE = 0.126514391218183



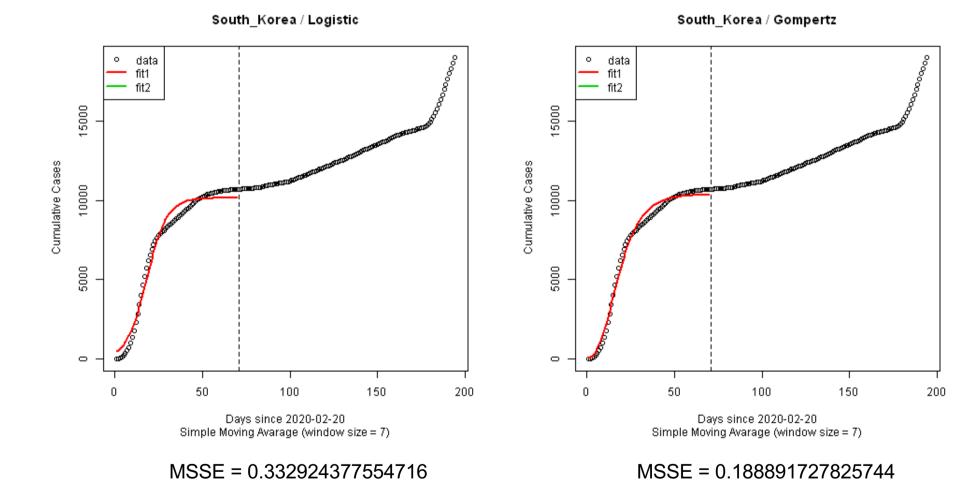
MSSE = 0.0523266231286347

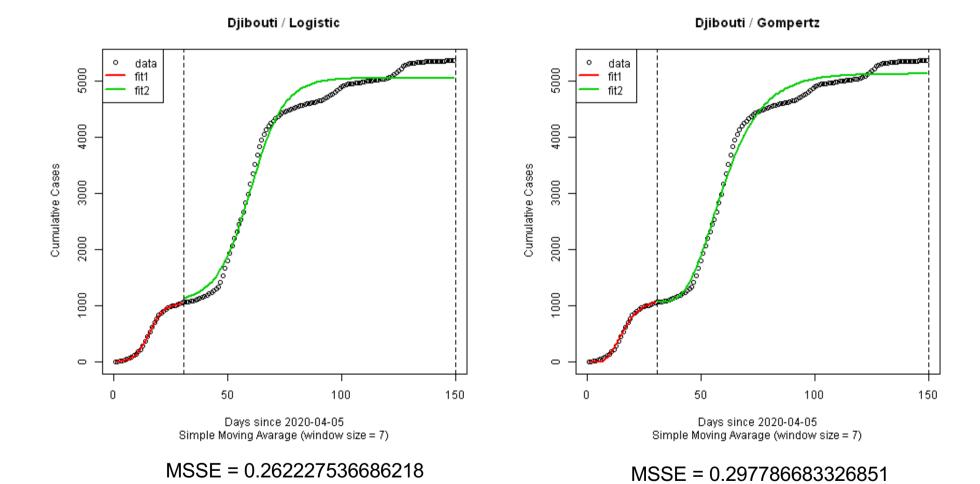


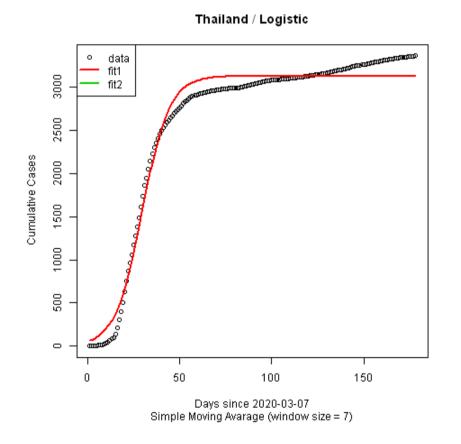


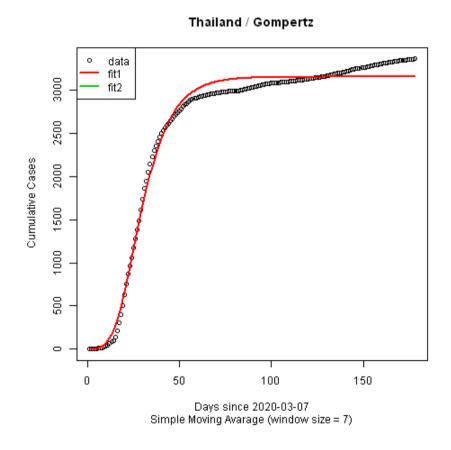
MSSE = 0.325181978417923

MSSE = 0.582192867942544



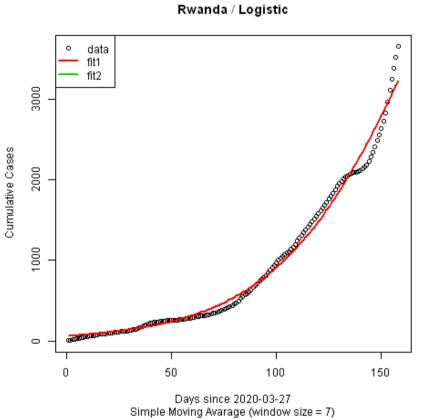




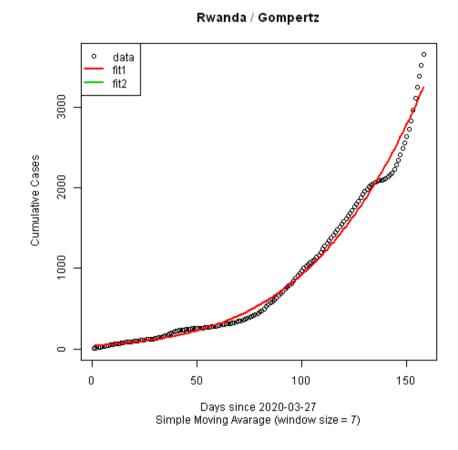


MSSE = 0.409838367855645

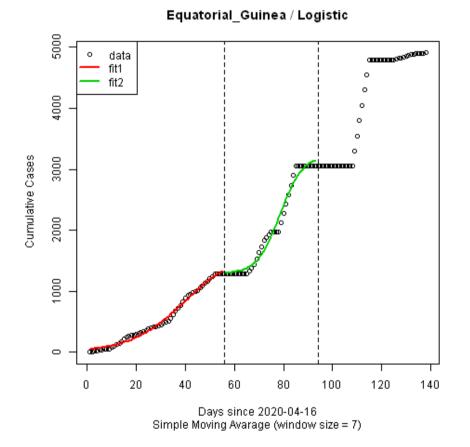
MSSE = 0.220907456275208



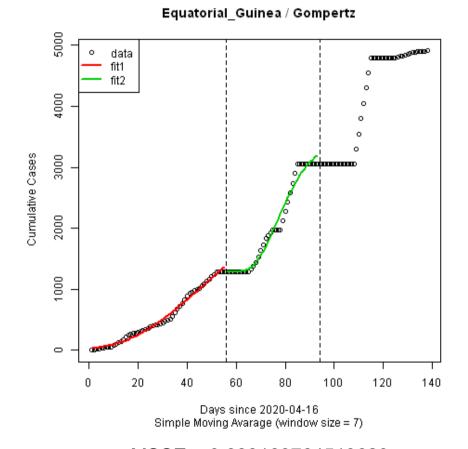
MSSE = 0.707876818681935



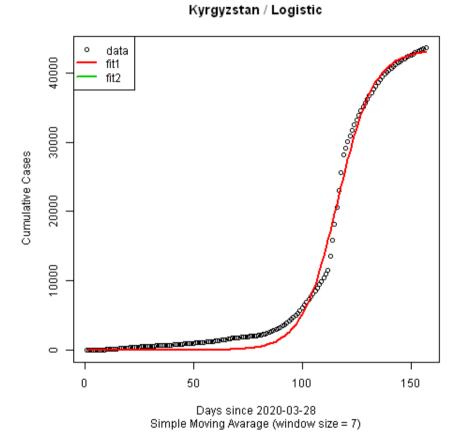
MSSE = 0.651178020925684



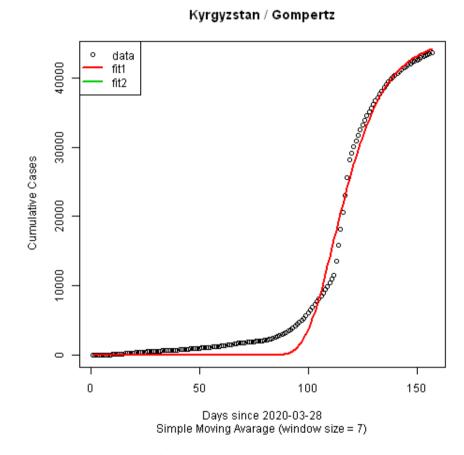
MSSE = 0.63867981951264



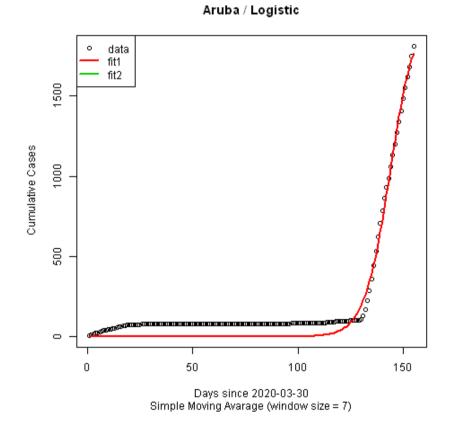
MSSE = 0.688163764513623



MSSE = 1.02293143702645



MSSE = 1.27271534445623



data fit1 fit2 1500 0 0 Cumulative Cases 1000 200 0 50 100 150 0 Days since 2020-03-30 Simple Moving Avarage (window size = 7)

Aruba / Gompertz

MSSE = 0.41355852911879

Not fitted

# 결론

- $MMSE = \frac{1}{N} \sum_{t=1}^{N} (\frac{Y_t \hat{Y}_t}{\bar{Y}})^2$  기준 0.4 이상인 국가들 제외
- Logistic: Aruba / Equatorial\_Guinea / Kyrgyzstan / Rwanda / Thailand
- Gompertz: China / Equatorial\_Guinea / Kyrgyzstan / Rwanda / Zambia