Analysis of Global Life Expectancy and Related Factors

Echo Chen, Andrew Kroening, Pooja Kabber, Dingkun Yang

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Report: Your report will be an 8-10 page self-contained document describing your analysis. It should be written as a professional document that can be understood by someone with limited statistics background (e.g., a client). You are also required to submit an RMD file that includes your code for the EDA and analysis. The report should be organized as follows:

Abstract

This analysis is conducted to understand which factors influence life expectancy and the development status of countries around the world. The dataset used for this research consists of national disease, economic, and social factors and was compiled by the World Health Organization (WHO). [Need to link to the dataset from Kaggle] To conduct the analysis, two research objectives are formulated: one prediction question and one inference question. Unique models are fit to each approach and the results are analyzed for utility. [Add a concluding punchline]

Introduction

Provide more background on the data and research questions. Be sure to cite the data and background information appropriately (APA style is fine)

This analysis uses data from the WHO to better understand the drivers of life expectancy around the globe. We also attempt to find inferential value from the data for determining the developmental status of a given country. From the two research questions we aim to improve insights into factors that drive a country's developmental status, and the population health indicators that lead to improved life expectancy.

The particular dataset for this analysis contains national-level observations of variables related to life expectancy around the globe for a period spanning the early portion of the 21st century. The complete dataset includes observations beginning in the year 2000 and ending in the year 2015. As a full dataset, there are 2,938 observations for 22 variables. Practically, each country has approximately one observation each year, averaging 183 for each of the 16 years encompassed by the data. The dataset effectively contains 20 variables for each country and year combination, covering significant disease, economic, and social factors. Below are the questions we aim to answer in this analysis:

Question #1 (Prediction)

"How did major disease, economic, and social factors impact life expectancy around the globe in 2014?"

Question #2 (Inference)

"How did disease and mortality rates, along with national economic factors, contribute to a country's development status in 2014?"

Methods

Describe the process you used to conduct analysis. This includes EDA and any relevant data cleaning information (e.g., did you exclude missing values? If so, how many? Did you collapse categories for any variables?) Then describe the models you fit, and any changes you made to improve model fit (e.g., did you exclude any influential points? Did you do have to address multicollinearity issues? Did you transform any variables?). Also describe model diagnostics. The organization of this section may depend on your particular dataset/analysis, but you may want to break it into subsections such as "Data," "Models," and "Model assessment." Note that you do not present any results in this section.

The general methodology of our analysis centered around the ability to draw insights from the dataset without significant transformations or imputations. To accomplish this objective, the team began with exploratory data analysis (EDA) to examine the distributions of key variables. From the EDA, missing data points were identified, and decisions made for courses of action to cope with those non-values. At conclusion of data preparation, we subset for the year 2014, our focal point for this analysis, and the year 2013 as a testing validation dataset used in our second research question.

We then proceed to model fitting. [High-level how we do this.] Finally, we obtain diagnostic information about the performance of our models.

Data

[Data introduction: address missing, factors, cleanliness, subsetting, and eda]

During the course of this initial rouund of EDA, the team identified a number of missing values from the dataset. These missing values included: 41x Population, 10x Hepatitis B, and 10x Schooling observations, with the large number of missing population values the most concerning. The team considered several approaches for mitigating the problems posed by this data, as it precludes a number of potentially influential countries from being included in this analysis. We considered multiple imputation as well as scholastic imputation for ways to mitigate these issues.

An alternative approach for missing data was identified as theoretically feasible early in the analysis process. Because of the national-level of our dataset, it is possible that we could find suitable replacement values from another source with high integrity in these areas, such as the World Bank, the International Monetary Fund, or the CIA World Factbook. While those sources had existing data for some of our missing values, we opt to not use them for replacement. Most replacement candidates we found did not match the surrounding data points (i.e. GDP figures for the country/year in question were not close enough to consider a match), and thus we have low-confidence that those values would be consistent with the WHO's data collection methods.

After the initial treatments to factor variables, our dataset is reduced to complete cases only and subset for the two years of interest in our analysis. We ultimately decide to preserve the original integrity of the data and bypass any available imputation methods. While there are certainly options available, the team assesses that the potential gain from the inclusion of the additional countries does not offset the possible bias or skew introduced from imputation. At the conclusion of these steps and decisions, we subset the data to make two sub-datasets: one for the year 2014 and one for the year 2013 which we will use in our second research question. These two datasets are nearly ideintical in size, with the 2014 dataset consisting of 131 observations, and the 2013 dataset having 130.

After some simple steps to prepare the data, the team began its EDA. [EDA plots and findings - need to truncate this and decide what's actually important to what we are trying to say]

[Does Table 1 have everything we want in it????]

[Describe Table 1 - feels like we should add more variables]

Models

The model used for the first research question, the prediction question, is linear regression

Table 1: Summary of Variables

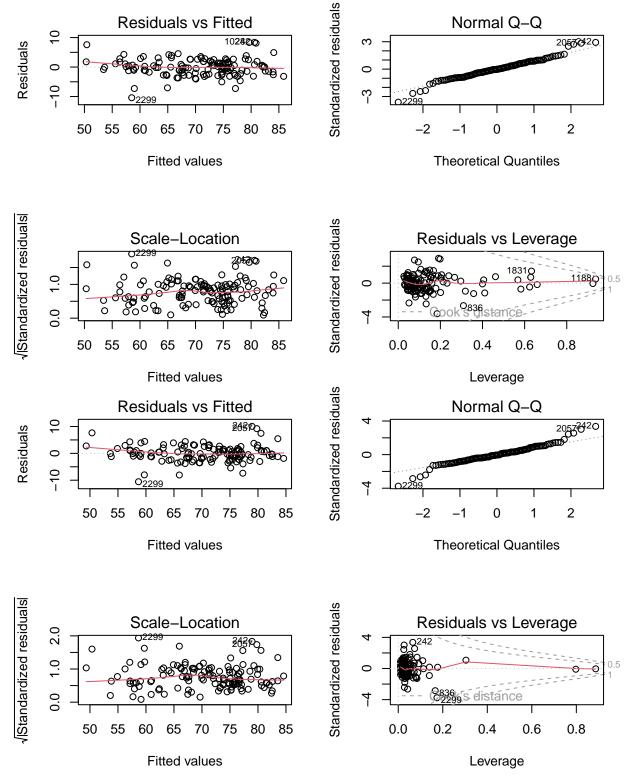
| Statistic | N | Mean | St. Dev. | Min | Max |
|---------------------------------|-----|----------------|-----------------|--------|-------------------|
| Population | 131 | 22,269,096.000 | 116,699,866.000 | 41.000 | 1,293,859,294.000 |
| Life.expectancy | 131 | 70.520 | 8.605 | 48.100 | 89.000 |
| percentage.expenditure | 131 | 850.874 | 2,071.444 | 0.443 | 16,255.160 |
| Measles | 131 | 2,042.863 | 9,842.341 | 0 | 79,563 |
| Polio | 131 | 83.496 | 20.966 | 8 | 99 |
| HIV.AIDS | 131 | 0.810 | 1.562 | 0.100 | 9.400 |
| GDP | 131 | 7,256.847 | 14,741.400 | 12.277 | 119,172.700 |
| Schooling | 131 | 12.676 | 2.750 | 5.300 | 20.400 |
| Income.composition.of.resources | 131 | 0.670 | 0.151 | 0.345 | 0.936 |
| BMI | 131 | 40.476 | 20.734 | 2.000 | 77.100 |
| Total.expenditure | 131 | 6.107 | 2.533 | 1.210 | 13.730 |

[Describe how we fit the model and the process]

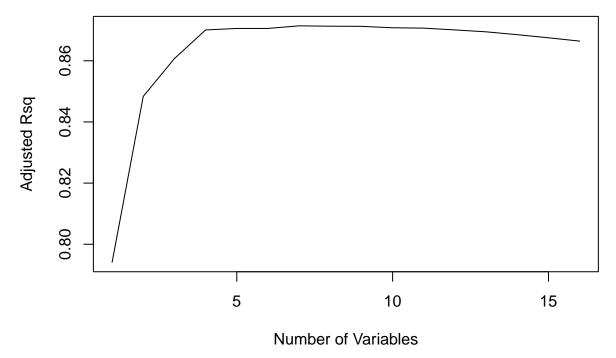
```
## Warning in model.matrix.default(mt, mf, contrasts): the response appeared on the
## right-hand side and was dropped
## Warning in model.matrix.default(mt, mf, contrasts): problem with term 3 in
## model.matrix: no columns are assigned
##
## Call:
## lm(formula = Life.expectancy ~ Status + Population + Life.expectancy +
      percentage.expenditure + Measles + Polio + HIV.AIDS + GDP +
##
      Schooling + Income.composition.of.resources + BMI + Total.expenditure,
      data = df_life_expectancy_2014)
##
##
## Residuals:
##
      Min
               1Q Median
                               3Q
                                      Max
                   0.186
                            1.848
                                    8.598
## -13.910 -1.885
##
## Coefficients:
##
                                    Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                                   4.262e+01 2.751e+00 15.492 < 2e-16 ***
## StatusDeveloping
                                  -9.977e-01 1.070e+00 -0.932
                                                                  0.3531
                                                         0.393
## Population
                                   1.394e-09 3.545e-09
                                                                  0.6949
## percentage.expenditure
                                   5.012e-04 4.793e-04
                                                         1.046
                                                                  0.2978
## Measles
                                                                  0.4846
                                  -2.977e-05 4.247e-05 -0.701
## Polio
                                   1.008e-02 1.605e-02
                                                         0.628
                                                                  0.5310
## HIV.AIDS
                                                         -6.020 1.99e-08 ***
                                  -1.365e+00 2.267e-01
## GDP
                                  -6.893e-05 6.930e-05
                                                         -0.995
                                                                  0.3219
                                                         -0.774
## Schooling
                                  -2.175e-01 2.811e-01
                                                                  0.4407
## Income.composition.of.resources 4.547e+01 5.906e+00
                                                         7.699 4.47e-12 ***
                                  -5.827e-03 1.941e-02 -0.300
                                                                  0.7645
                                   2.722e-01 1.329e-01
                                                                  0.0428 *
## Total.expenditure
                                                          2.047
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 3.404 on 119 degrees of freedom
## Multiple R-squared: 0.8567, Adjusted R-squared: 0.8435
## F-statistic: 64.69 on 11 and 119 DF, p-value: < 2.2e-16
```

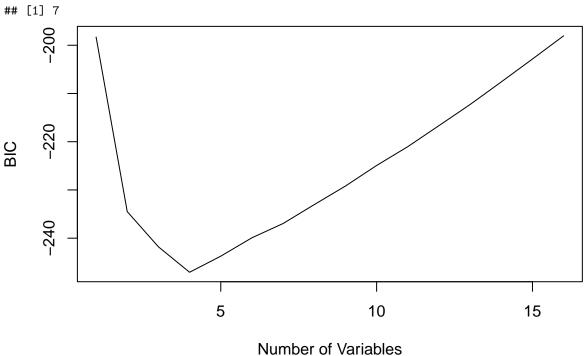
```
##
## Call:
## lm(formula = Life.expectancy ~ ., data = subset(df_life_expectancy_cc_2014,
      select = -c(Country, Year)))
## Residuals:
                      Median
                 10
                                   30
                                           Max
                                        8.3880
## -10.4098 -1.7264 -0.0392
                               1.7715
## Coefficients: (1 not defined because of singularities)
                                    Estimate Std. Error t value Pr(>|t|)
                                   5.122e+01 3.314e+00 15.457 < 2e-16 ***
## (Intercept)
                                                         -1.130 0.261006
## StatusDeveloping
                                  -1.170e+00 1.035e+00
## Adult.Mortality
                                  -1.724e-02 4.148e-03 -4.157 6.36e-05 ***
## infant.deaths
                                   8.287e-02 5.619e-02
                                                         1.475 0.143057
## Alcohol
                                   5.674e-03 9.749e-02
                                                          0.058 0.953689
                                   4.627e-04 4.639e-04
                                                          0.997 0.320716
## percentage.expenditure
## Hepatitis.B
                                   1.205e-02 2.808e-02
                                                          0.429 0.668582
## Measles
                                  -3.361e-05 4.823e-05 -0.697 0.487345
## BMT
                                  -7.576e-03 2.000e-02 -0.379 0.705531
## under.five.deaths
                                  -6.014e-02 3.838e-02 -1.567 0.119989
## Polio
                                  -8.746e-03 2.117e-02 -0.413 0.680327
## Total.expenditure
                                  2.878e-01 1.274e-01
                                                          2.259 0.025833 *
## Diphtheria
                                   7.644e-03 3.445e-02
                                                         0.222 0.824805
## HIV.AIDS
                                  -8.363e-01 2.470e-01 -3.385 0.000984 ***
## GDP
                                  -5.980e-05 6.656e-05 -0.898 0.370911
## Population
                                  -1.729e-09 6.804e-09
                                                         -0.254 0.799816
                                                         -0.574 0.567462
## thinness..1.19.years
                                  -1.300e-01 2.267e-01
                                                         0.025 0.980489
## thinness.5.9.years
                                   5.458e-03 2.227e-01
## Income.composition.of.resources 3.597e+01 6.228e+00
                                                         5.775 7.11e-08 ***
## Schooling
                                   -1.617e-01
                                              2.740e-01
                                                         -0.590 0.556279
## Status_num
                                          NΑ
                                                     NA
                                                             NA
                                                                      NA
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 3.186 on 111 degrees of freedom
## Multiple R-squared: 0.8829, Adjusted R-squared: 0.8629
## F-statistic: 44.06 on 19 and 111 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = Life.expectancy ~ Adult.Mortality + infant.deaths +
      under.five.deaths + Total.expenditure + HIV.AIDS + Income.composition.of.resources,
##
##
      data = subset(df_life_expectancy_cc_2014, select = -c(Country,
##
          Year)))
##
## Residuals:
      Min
               10 Median
                               3Q
                                      Max
## -10.568 -1.569 -0.127
                           1.561 10.060
##
## Coefficients:
##
                                   Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                                              2.066580 23.159 < 2e-16 ***
                                  47.860575
## Adult.Mortality
                                              0.003866 -4.502 1.53e-05 ***
                                  -0.017405
```

```
## infant.deaths
                                       0.042287
                                                    0.029527
                                                                1.432 0.154625
## under.five.deaths
                                      -0.033561
                                                    0.022614
                                                               -1.484 0.140331
  Total.expenditure
                                                                3.119 0.002258 **
                                       0.349095
                                                    0.111930
                                      -0.809261
## HIV.AIDS
                                                    0.231621
                                                               -3.494 0.000661 ***
##
   Income.composition.of.resources 35.911609
                                                    2.502726
                                                               14.349
                                                                       < 2e-16 ***
##
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 3.096 on 124 degrees of freedom
## Multiple R-squared: 0.8765, Adjusted R-squared: 0.8705
## F-statistic: 146.7 on 6 and 124 DF, p-value: < 2.2e-16
## Warning in model.matrix.default(object, data = structure(list(Life.expectancy =
## c(59.9, : the response appeared on the right-hand side and was dropped
## Warning in model.matrix.default(object, data = structure(list(Life.expectancy =
## c(59.9, : problem with term 3 in model.matrix: no columns are assigned
                                                  Standardized residuals
                Residuals vs Fitted
                                                                     Normal Q-Q
                                                                                      <u>86570</u>
     10
                                   205700
Residuals
            0
     0
                                                       0
                                                              -15
                                                                                  1
                                                                                       2
               55
                        65
                            70
                                75
                                     80
                                         85
                                                                -2
                                                                            0
           50
                    60
                     Fitted values
                                                                   Theoretical Quantiles
(Standardized residuals)
                                                  Standardized residuals
                                                                Residuals vs Leverage
                  Scale-Location
     2.0
                      O50
                                   205700
                                                                          05628310
            0
                                                                                              0.5
     1.0
                                                                              00
                                                                       Ö
     0.0
                                                                  Gook's distance
                                                                  0.2
                   60
                        65
                            70
                                 75
                                     80
                                                           0.0
                                                                         0.4
                                                                               0.6
                                                                                      8.0
           50
               55
                     Fitted values
                                                                        Leverage
```

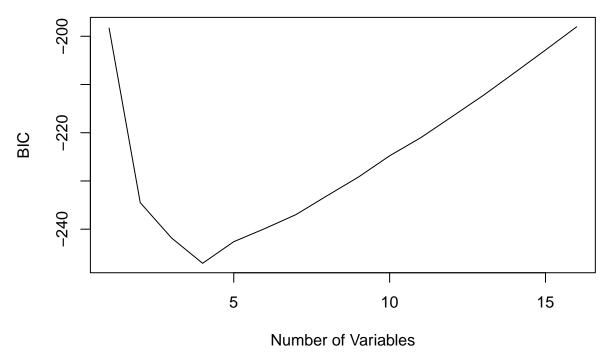


Warning in leaps.setup(x, y, wt = wt, nbest = nbest, nvmax = nvmax, force.in =
force.in, : 1 linear dependencies found





[1] 4
Warning in leaps.setup(x, y, wt = wt, nbest = nbest, nvmax = nvmax, force.in =
force.in, : 1 linear dependencies found



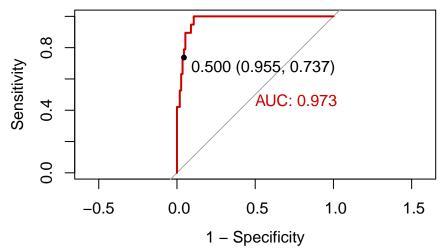
[1] 4

[The second question, the inferential one, will be approached with a logistic regression model]

[Dingkun, what is all of this]

[Multicolinearity concerns]

Percentage expenditure and GDP are the ones have higher VIF being over 10, WE NEED TO DECIDE WHICH ONE TO INCLUDE IN THE MODEL



Income composition of resources VIF is near 5, with p-value less than 0.05 (CANNOT DELETE, but maybe delete total expenditure)

Table 2: Logistic Regression Model

| | Dependent variable: |
|---------------------------------|-----------------------------|
| | Status_num |
| Life.expectancy | -0.07 (0.12) |
| | p = 0.57 |
| percentage.expenditure | $-0.0002 \ (0.0005)$ |
| | p = 0.62 |
| BMI | -0.04 (0.03) |
| | p = 0.14 |
| Total.expenditure | 0.22(0.18) |
| | p = 0.22 |
| HIV.AIDS | -152.86 (23,893.84) |
| | p = 1.00 |
| GDP | $0.0000 \ (0.0001)$ |
| | p = 0.84 |
| Income.composition.of.resources | 41.25 (15.60) |
| | $p = 0.01^{***}$ |
| Schooling | -0.06(0.39) |
| | p = 0.89 |
| Constant | -12.15(2,389.40) |
| | p = 1.00 |
| Observations | 131 |
| Log Likelihood | -20.18 |
| Akaike Inf. Crit. | 58.36 |
| Note: | *p<0.1; **p<0.05; ***p<0.01 |

Table 3: Variance Inflation Factors

| Life.expectancy | percentage.expenditure | BMI | Total.expenditure | HIV.AIDS | GDP | Income.composition.of.resources | Scho |
|-----------------|------------------------|------|-------------------|----------|-------|---------------------------------|------|
| 2.04 | 10.61 | 1.29 | 1.20 | 1.00 | 10.56 | 4.23 | 2. |

Table 4: Confusion Matrix for Full Model

| | True Developed | True Developing |
|----------------------|----------------|-----------------|
| Predicted Developed | 14 | 5 |
| Predicted Developing | 5 | 107 |

Table 5: Logistic Regression Model

| | Dependent variable: |
|---------------------------------|-----------------------------|
| | Status_num |
| Life.expectancy | -0.07 (0.12) |
| | p = 0.53 |
| BMI | -0.04 (0.03) |
| | p = 0.14 |
| Total.expenditure | 0.20(0.17) |
| | p = 0.24 |
| HIV.AIDS | -153.11 (23,950.77) |
| | p = 1.00 |
| GDP | -0.0000 (0.0000) |
| | p = 0.52 |
| Income.composition.of.resources | 40.86 (15.68) |
| | $p = 0.01^{***}$ |
| Schooling | -0.03 (0.40) |
| | p = 0.95 |
| Constant | -11.67 (2,395.09) |
| | p = 1.00 |
| Observations | 131 |
| Log Likelihood | -20.32 |
| Akaike Inf. Crit. | 56.64 |
| Note: | *p<0.1; **p<0.05; ***p<0.01 |
| | |

Table 6: Variance Inflation Factors

| Life.expectancy | BMI | Total.expenditure | HIV.AIDS | GDP | Income.composition.of.resources | Schooling |
|-----------------|------|-------------------|----------|----------------------|---------------------------------|-----------|
| 2.03 | 1.28 | 1.09 | 1.00 | 1.62 | 4.34 | 2.07 |

Table 7: Confusion Matrix for Model 1

| | True Developed | True Developing |
|----------------------|----------------|-----------------|
| Predicted Developed | 14 | 4 |
| Predicted Developing | 5 | 108 |

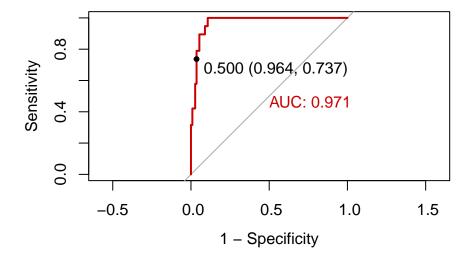


Table 8: Analysis of Deviance: Full Model vs Model 1

| | Resid. Df | Resid. Dev | Df | Deviance | Pr(>Chi) |
|---|-----------|------------|----|----------|----------|
| 1 | 122 | 40.36 | | | |
| 2 | 123 | 40.64 | -1 | -0.28 | 0.59 |

Without GDP

$\bf Model~2$

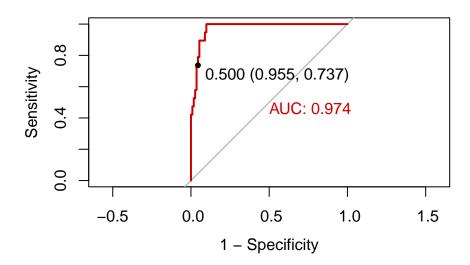
Table 9: Logistic Regression Model

| | $Dependent\ variable:$ |
|---------------------------------|-----------------------------|
| | Status_num |
| Life.expectancy | -0.07 (0.12) |
| | p = 0.55 |
| BMI | -0.04 (0.03) |
| | p = 0.13 |
| percentage.expenditure | $-0.0001 \ (0.0002)$ |
| | p = 0.41 |
| Total.expenditure | 0.22(0.17) |
| | p = 0.22 |
| HIV.AIDS | -153.15 (23,916.24) |
| | p = 1.00 |
| Income.composition.of.resources | $41.73\ (15.53)$ |
| | $p = 0.01^{***}$ |
| Schooling | -0.05 (0.39) |
| | p = 0.89 |
| Constant | -12.26 (2,391.64) |
| | p = 1.00 |
| Observations | 131 |
| Log Likelihood | -20.20 |
| Akaike Inf. Crit. | 56.40 |
| Note: | *p<0.1; **p<0.05; ***p<0.01 |

% Error: Unrecognized object type.

Table 10: Variance Inflation Factors

| Life.expectancy | BMI | percentage.expenditure | Total.expenditure | HIV.AIDS | Income.composition.of.resources | Schooling |
|-----------------|------|------------------------|-------------------|----------|---------------------------------|-----------|
| 2.02 | 1.31 | 1.63 | 1.14 | 1.00 | 4.21 | 2.08 |



Model 1 vs Model 2

Table 11: Analysis of Deviance: Model 1 (W/O percentage expenditure) vs Model 2 (W/O GDP)

| | Resid. Df | Resid. Dev | Df | Deviance | Pr(>Chi) |
|---|-----------|------------|----|----------|----------|
| 1 | 123 | 40.64 | | | |
| 2 | 123 | 40.40 | 0 | 0.24 | |

Full Model vs Model 2

Table 12: Analysis of Deviance: Full Model vs Model 2

| | Resid. Df | Resid. Dev | Df | Deviance | Pr(>Chi) |
|---|-----------|------------|----|----------|----------|
| 1 | 122 | 40.36 | | | |
| 2 | 123 | 40.40 | -1 | -0.04 | 0.83 |

Using Model 1 (w/o percentage expenditure) to predict out-of-sample (Year 2013) probabilities

Table 13: Confusion Matrix 4

| | True Developed | True Developing |
|----------------------|----------------|-----------------|
| Predicted Developed | 14 | 6 |
| Predicted Developing | 5 | 105 |

Using Model 2 (w/o GDP) to predict out-of-sampl e(Year 2013) probabilities

Table 14: Confusion Matrix 5

| | True Developed | True Developing |
|----------------------|----------------|-----------------|
| Predicted Developed | 14 | 5 |
| Predicted Developing | 5 | 106 |

Model 2 is slightly better, numerical wise. But not statistically different than Model 1 $\,$

Tested, not good

Without Total Expenditure and percentage expenditure.

Model 3

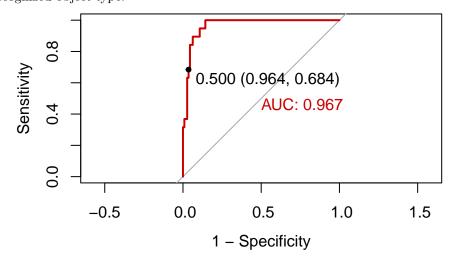
Table 15: Logistic Regression Model

| | $Dependent\ variable:$ |
|---------------------------------|-----------------------------|
| | Status_num |
| Life.expectancy | -0.04 (0.11) |
| | p = 0.74 |
| BMI | -0.03 (0.03) |
| | p = 0.19 |
| HIV.AIDS | -152.18 (24,634.34) |
| | p = 1.00 |
| Income.composition.of.resources | $35.30\ (13.99)$ |
| | $p = 0.02^{**}$ |
| Schooling | 0.01 (0.39) |
| | p = 0.98 |
| Constant | -9.94(2,463.44) |
| | p = 1.00 |
| Observations | 131 |
| Log Likelihood | -21.27 |
| Akaike Inf. Crit. | 54.54 |
| Note: | *p<0.1; **p<0.05; ***p<0.01 |

Table 16: Variance Inflation Factors

| Life.expectancy | BMI | HIV.AIDS | Income.composition.of.resources | Schooling |
|-----------------|------|----------|---------------------------------|-----------|
| 2.01 | 1.19 | 1.00 | 3.62 | 2.13 |

% Error: Unrecognized object type.



Model 1 vs Model 3

Table 17: Analysis of Deviance: Model 1 vs Model 3

| | Resid. Df | Resid. Dev | Df | Deviance | Pr(>Chi) |
|---|-----------|------------|----|----------|----------|
| 1 | 123 | 40.64 | | | |
| 2 | 125 | 42.54 | -2 | -1.90 | 0.39 |

Full Model vs Model 3

Table 18: Analysis of Deviance: Full Model vs Model 3

| | Resid. Df | Resid. Dev | Df | Deviance | Pr(>Chi) |
|---|-----------|------------|----|----------|----------|
| 1 | 122 | 40.36 | | | |
| 2 | 125 | 42.54 | -3 | -2.18 | 0.54 |

Model Assessment

[How did we assess the linear model and its assumptions? Plots, four key assumptions, etc.] [How did we assess the validity of the logistic model?]

Results:

Here you should present results for all aspects of the analysis. The structure of this section should mirror the structure of the methods section. For example, you can start with a few key EDA results (e.g., a table of descriptive statistics), then present model results, then address assessment. This is the section where you will primarily refer to tables and figures. You should have at least 1 figure for each research question that illustrates a key result of the analysis.

[General insights. Were the models effective, set the stage for the discussion below]

Question 1: "How did major disease, economic, and social factors impact life expectancy around the globe in 2014?"

Model Results [What does the model output tell us]

Assessment [Assess the validity of the outputs]

Questions 2: "How did disease and mortality rates, along with national economic factors, contribute to a country's development status in 2014?"

Model Results [What does the model output tell us]

Assessment [What kid of accuracy did we find from the model]

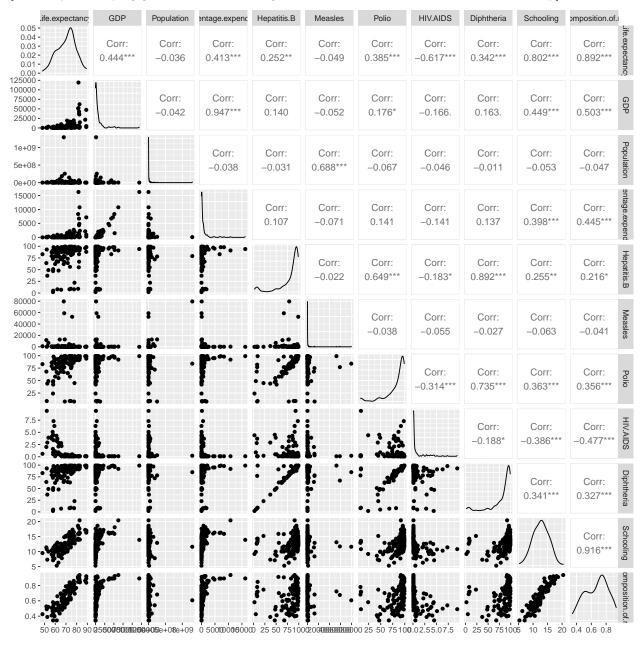
Conclusion

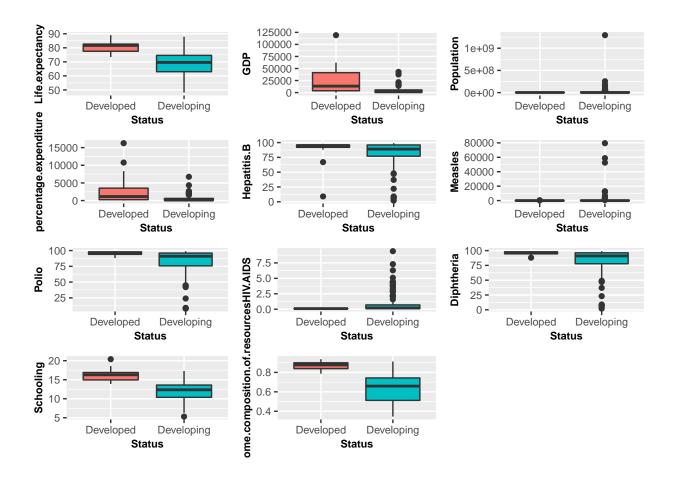
Describe the key takeaways from your analysis, limitations, and future work that can be done to advance knowledge in this area.

[What is the impact of this analysis, do we think it is insightful or not?]

Appendix

[Presently, a dumping ground for all our images and lots until we know what we want to keep]





A few things to keep in mind: • You should never refer to actual variable names in the text, tables, or figures. For example, if a variable for height is called "ht__cm," you should always say "height," and the first time you mention it you should state that it is measured in cm. In plots and tables, it should say "height (cm)" • The report should be produced in R Markdown and knit to PDF. This may mean you need to create tables "manually" with knitr. I recommend this anyway because you can customize the labels and formatting. • Someone should be able to read the abstract and look at the tables and figures and have a pretty good idea of 1) the goals of your analysis, and 2) the key results. • I recommend using colorblind-friendly color palettes in your figures. It can be even better to differentiate with line types or symbols instead of relying on color.

Keep you audience in mind! A non-statistician should be able to read your report and have a good idea of what you did. • You can have an appendix if tables or figures are too large to fit into the main text. For example, if you have several predictors, you may want to put a table of model results in the appendix.