

Deuteron Electro-Disintegration At Very High Missing Momenta

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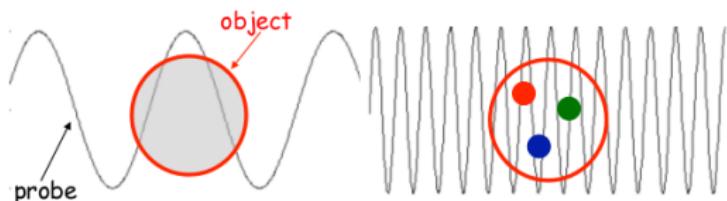


Motivation

- Study Deuteron at short ranges ($\lesssim 1\text{fm}$).

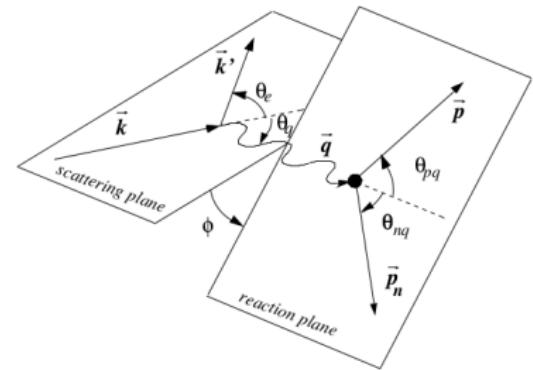
High momentum transfers (Q^2) \implies probe the Deuteron at smaller distances. Smaller internucleon distances enables one to access the high momentum components of nucleons

- Extract D(e,e'p)n cross-section beyond 500 MeV/c missing momentum at high Q^2
- Extract momentum distributions(not an observable) from cross sections



Theoretical Framework of D(e,e'p)n

- E.M. Interaction is well understood from Q.E.D.
- One Photon-Exchange (Born) Approximation is valid
- Virtual photon coherently interacts with Deuteron through a variety of processes (MEC, FSI, IC)
- Most direct way to probe internal structure of deuteron



$$k^\mu = (E, \mathbf{k}) \quad k'^\mu = (E', \mathbf{k}')$$

$$q^\mu = (\omega, \mathbf{q})$$

$$\omega = E - E', \mathbf{q} = \mathbf{k} - \mathbf{k}'$$

$$P_D^\mu = (M_D, \mathbf{P}_D)$$

$$\mathbf{P}_D = \mathbf{p}_{i,p} + \mathbf{p}_{i,n} = 0$$

$$Q^2 \equiv -q_\mu q^\mu = 4EE' \sin^2 \left(\frac{\theta_e}{2} \right)$$

General Unpolarized $(e, e'p)$ Cross-Section

$$\frac{d^6\sigma}{d\omega d\Omega_e dT_p d\Omega_p} = \sigma_{MOTT} (v_L R_L + v_T R_T + v_{LT} R_{LT} \cos \phi + v_{TT} R_{TT} \cos 2\phi)$$

Mott Cross Section

Electron-scattering off an infinitely massive, spinless point-like object

v_i, v_{ij} - Leptonic Kinematic Factors

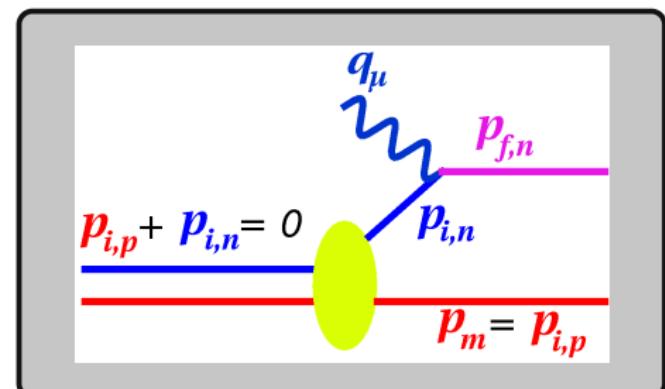
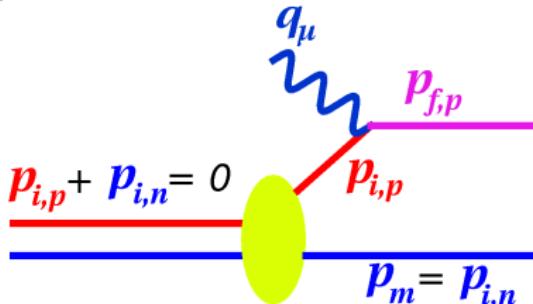
Quantities obtained from the leptonic tensor, $L_{\mu\nu}$, are dependent on electron kinematics ($\mathbf{q}, \omega, \theta_e$), and describe the longitudinal and transverse polarization of the virtual photon

R_i, R_{ij} - Nuclear Response Functions

Consist of combinations of matrix elements from the hadronic tensor,
 $W^{\mu\nu} \propto \langle \mathbf{p}_n; \mathbf{p}_p | J^\mu | \mathbf{P}_D \rangle^* \langle \mathbf{p}_n; \mathbf{p}_p | J^\nu | \mathbf{P}_D \rangle$

Plane Wave Impulse Approximation (PWIA)

- virtual photon couples to proton
- the other nucleon is a spectator
- final state particles treated as plane waves (free particles)
- direct access to the deuteron momentum distribution (factorization)
- The PWBA diagram suppressed for $p_m \sim$ few hundred MeV/c, and $p_p \sim$ few GeV/c



Deuteron Momentum Distribution

$$\sigma_{exp} \equiv \frac{d^6\sigma}{d\omega d\Omega_e dT_p d\Omega_p} = K \cdot \sigma_{ep} \cdot S(E_m, p_m)$$

$$S(p_m) \approx \sigma_{red} \equiv \frac{\sigma_{exp}}{K\sigma_{ep}}$$

ep off-shell cross section

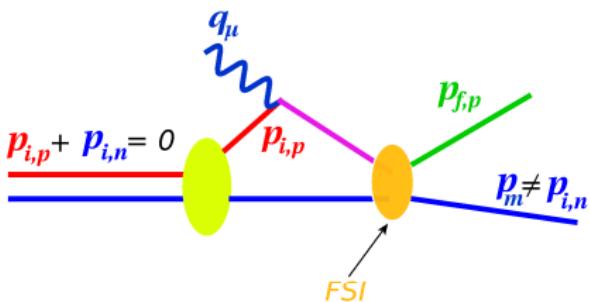
electron scatters off a bound proton within the nucleus; usually,
de Forest σ_{cc1} or σ_{cc2} is prescribed

Spectral Function, $S(p_m)$

the momentum distribution inside the deuteron is interpreted as
the probability density of finding a bound proton with
momentum p_i

Final State Interactions (FSI)

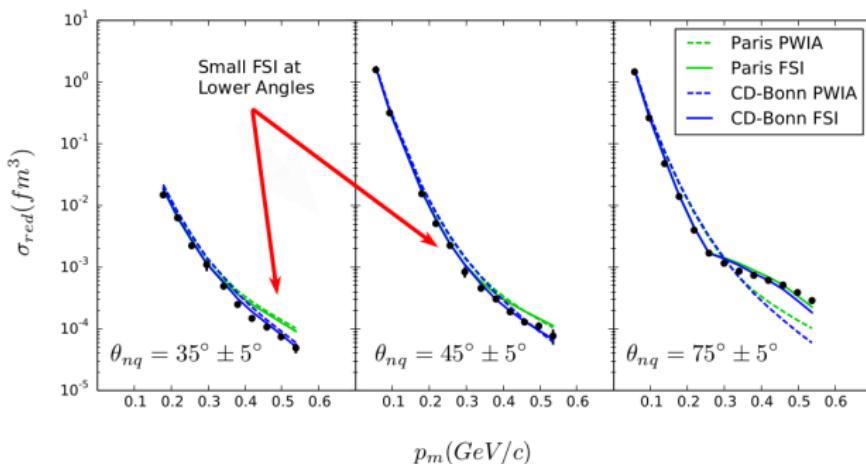
- in final state, the nucleons are at short enough distances (~ 2 fm) and continue to interact
- neutron re-scatters with a final momentum different than inside the deuteron
- generalized eikonal approximation: potentially infinite NN interactions are represented by an effective NN interaction amplitude obtained from NN scattering experiments



Experimental Support for D(e,e'p)n at Hall C

Previous D(e,e'p)n data from Hall A at $Q^2=3.25 \text{ GeV}^2$

W.U.Boeglin
et. al
 Phys.Rev.Let
 89, 6 (2002)



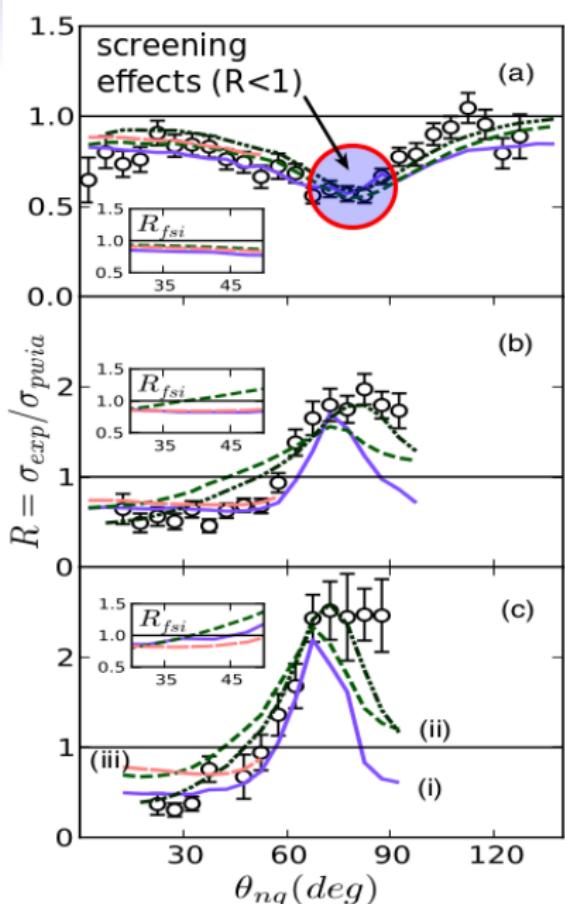
- New Hall C will focus at $\theta_{nq} \sim 40^\circ$ and $p_m \geq 500 \text{ MeV}/c$ at $Q^2=4.25 \text{ GeV}^2$
- greater sensitivity of deuteron momentum distribution to different NN potential models (e.g. CD-Bonn, Paris, etc.)

- Data (JLAB HallA)
- - - JML (FSI+MEC+IC)
- - - JML (FSI)
- MS using CD-Bonn potential
- - - JVO

$$Q^2 = 3.5 \text{ (GeV/c)}^2$$

- (a) $p_m = 0.2 \text{ GeV/c}$
 (b) $p_m = 0.4 \text{ GeV/c}$
 (c) $p_m = 0.5 \text{ GeV/c}$

W.U. Boeglin et. al
 PRL 107(2011) 262501

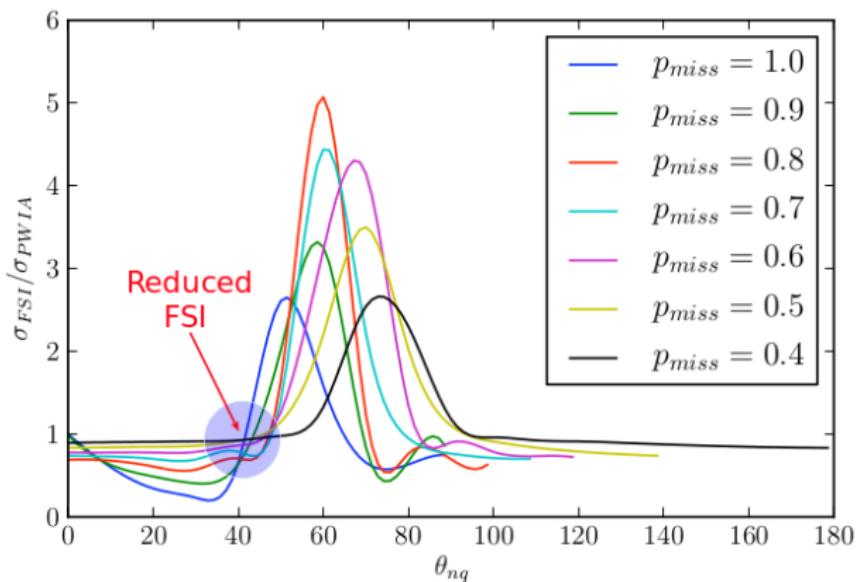


GEA: Theoretical Prediction

D(e,e'p)n Kinematics

$E_e = 11 \text{ GeV}$
 $Q^2 = 4.25 (\text{GeV}/c)^2$
 $x_{Bj} = 1.35$
 $p_m = 0.5 - 1.0 \text{ GeV}/c$
 $\theta_{nq} = 35^\circ - 40^\circ$

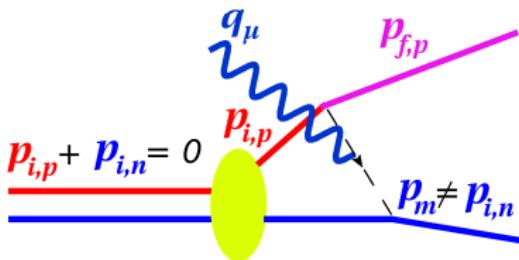
W.U. Boeglin *et. al*
Int.J.Mod.Phys. E24
(2015) no.03, 1530003



Theoretical Calculation by: M. Sargsian

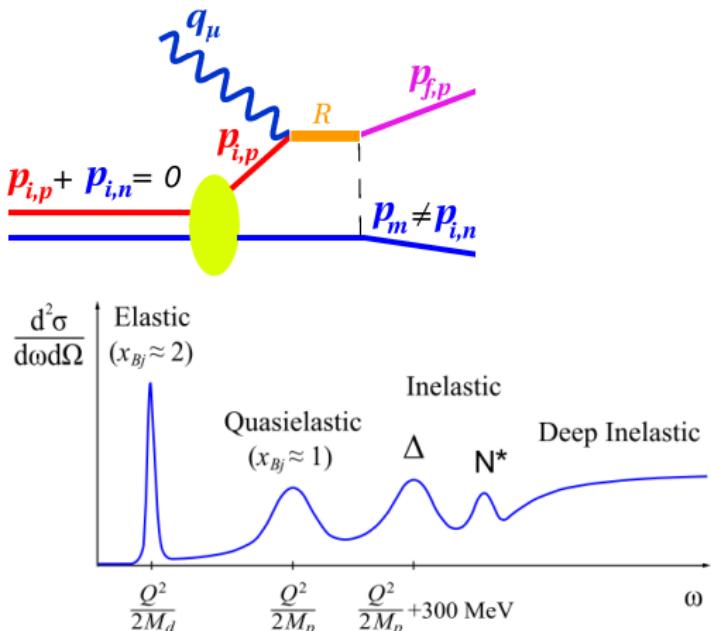
Meson Exchange Currents (MEC)

- virtual photon couples with exchange meson between nucleons
- virtual meson may become real after photon absorption
- meson exchange propagator is proportional to $(1 + \frac{Q^2}{m_{meson}^2})^{-1}$
 \Rightarrow MEC suppressed for $Q^2 \gg m_{meson}^2$

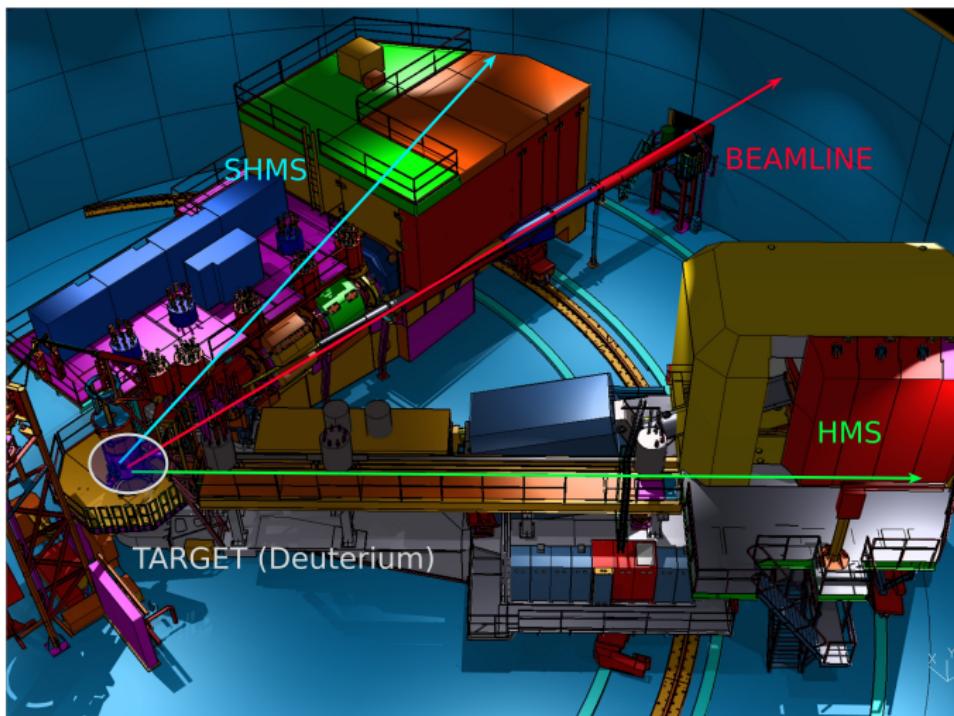


Isobar Configuration Currents (IC)

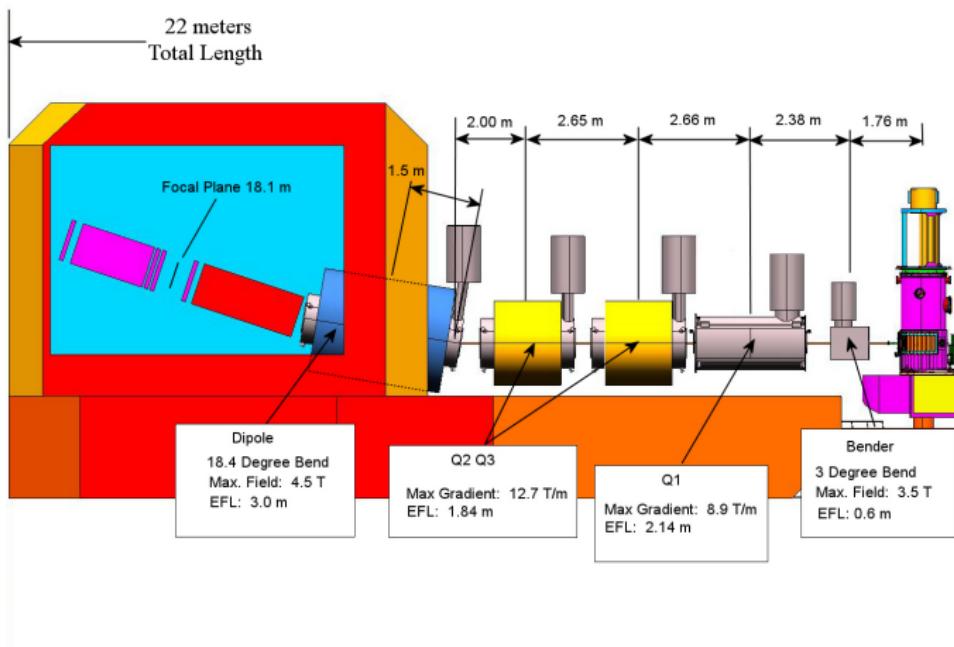
- virtual photon excites nucleon into resonance
- resonance de-excites through meson exchange with spectator nucleon
- for high Q^2 , and $x_{B_j} > 1$ ($x_{B_j} \equiv \frac{Q^2}{2M_p\omega}$) one is able to probe the lower ω region of the quasi-elastic peak to suppress Δ or N^* resonance production



Hall C Overview

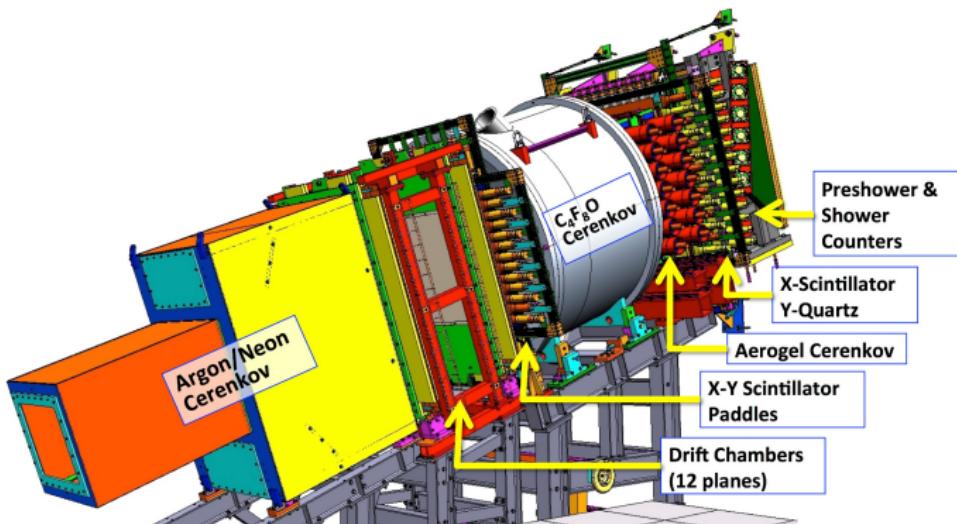


SHMS Carriage: Side View



SHMS Detector Stack

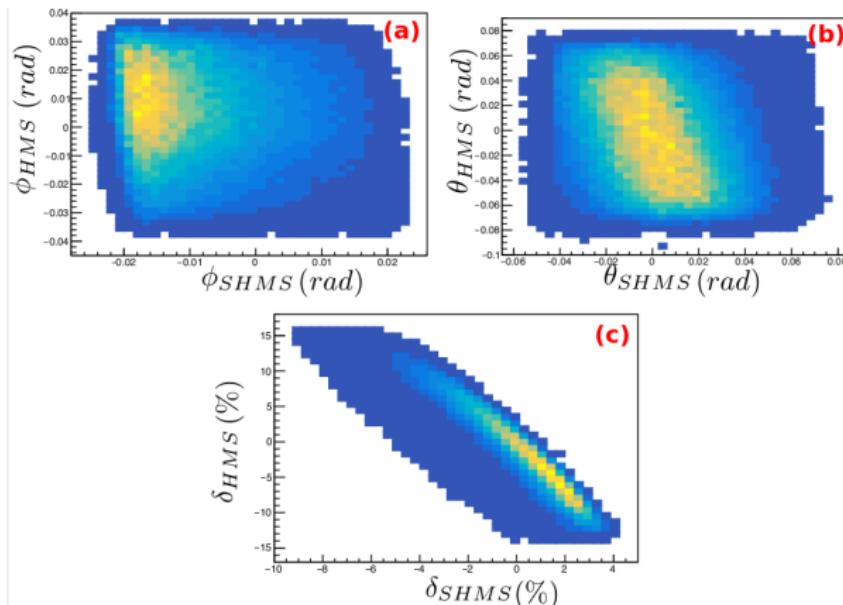
Particle Detectors inside the SHMS



E12-10-003: D(e,e'p)n Commissioning at Hall C

Spectrometer Acceptance Requirements During D($e,e'p$)n Commissioning

- D($e,e'p$)n will **NOT** require SHMS full acceptance
- SIMC kinematic setting, $p_m = 500$ MeV/c



D(e,e'p)n Kinematics and Simulation Results

Beam:

Energy:10.6 GeV

Current:70 μ A

Target:

LD₂ (10 cm)

electron arm (SHMS) *fixed* at:

$p_{cen} = 8.92 \text{ GeV}/c$

$$\theta_c \equiv 12.17^\circ, Q^2 \equiv 4.25 \text{ (GeV/c)}^2$$

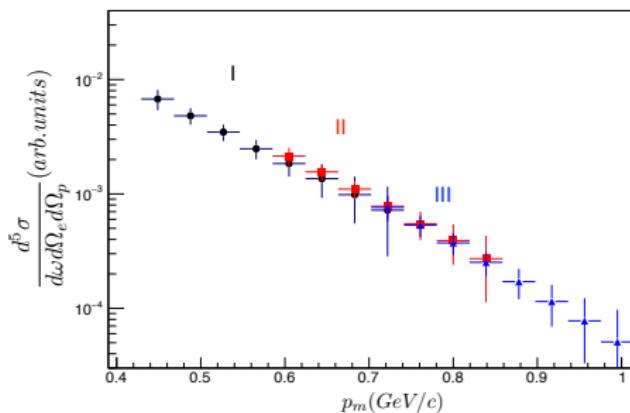
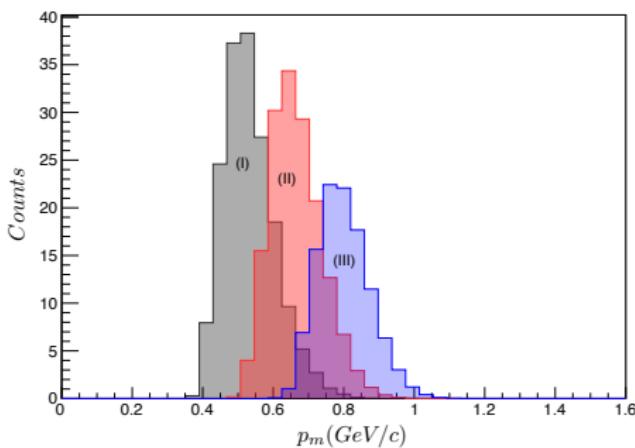
$$x_{B,i} \equiv 1.35 \quad \theta_{p,q} \approx 40^\circ$$

vary proton arm (HMS) to

$$p_m = 0.5, 0.65, 0.8 \text{ GeV/c}$$

HMS: $2.12 < p_{cen} < 2.3$ GeV/c

Angles: $59.6^\circ > \theta_p > 53.1^\circ$



SIMC Results

- I. $p_m = 0.5$ GeV/c, beam time 8 hours
 - II. $p_m = 0.65$ GeV/c, beam time 18 hours
 - III. $p_m = 0.8$ GeV/c, beam time 36 hours

Statistical Uncertainties

16.1%

17.0%

20.9%

Calibration Run Setting

Beam:

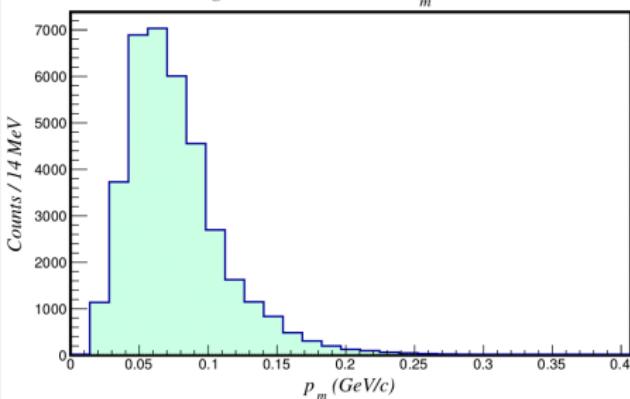
Energy: 10.6 GeV

Current: 70 μ A

Target:

LD₂ (10 cm)

Missing Momentum Yield, $P_{\perp} = 0.08 \text{ GeV}$



electron arm (SHMS) fixed at:

SHMS $p_{cen} = 8.44$ GeV/c

$$\theta_e \equiv 12.51^\circ \quad Q^2 \equiv 4.25 \text{ (GeV/c)}^2$$

$$x_{B,i} \equiv 1.05 \theta_{B,i} \approx 59^\circ$$

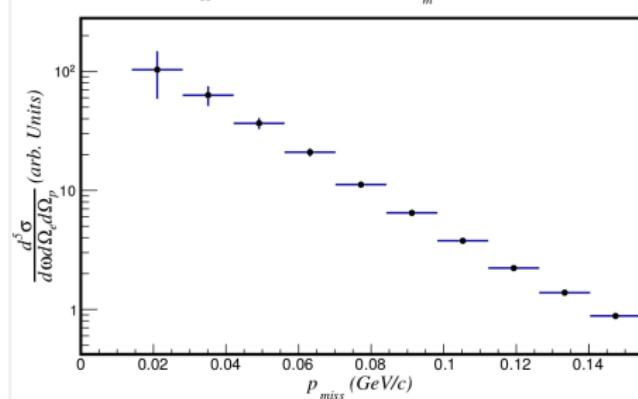
proton arm (HMS) to measure:

proton arm (HR)

HMS $p_{cen} \equiv 2.94$ GeV/c

Angle: 39.14°

Differential Cross Section, $P_{\perp} = 0.08 \text{ GeV}$



SIMC Results

$p_m=0.08$ GeV/c, beam time 1 hour

Statistical Uncertainties

1.29%

Uncertainty in Kinematic Variables

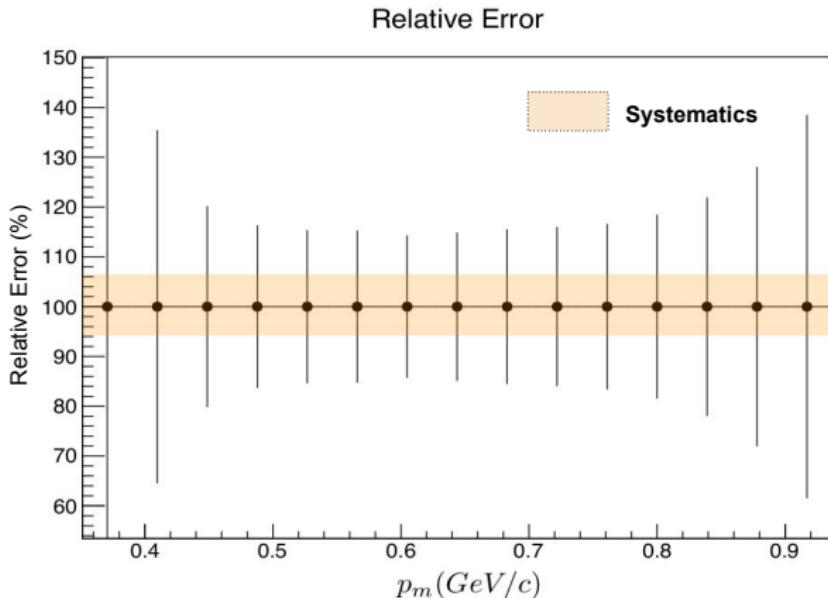
- Study sensitivity of cross-section due to small variations in kinematic variables

Kinematic Variable	Symbol	Conservative Kinematic Uncertainty	Optimum Kinematic Uncertainty
Beam Energy, E_B	$\Delta E_B/E_B$	1×10^{-3}	5×10^{-4}
Electron Final Momentum, \mathbf{k}_f	$\Delta k_f/k_f$	1×10^{-3}	5×10^{-4}
Proton Final Momentum, \mathbf{p}_f	$\Delta p_f/p_f$	1×10^{-3}	5×10^{-4}
Electron Scatt. Angle, θ_e	$\Delta\theta_e$	$\pm 1\text{mrad}$	$\pm 0.2\text{mrad}$
Proton Scatt. Angle, θ_p	$\Delta\theta_p$	$\pm 1\text{mrad}$	$\pm 0.2\text{mrad}$

Systematic Uncertainty Estimates on D($e,e'p$)n Cross Section

p_{miss} (GeV/c)	Total Error in $d\sigma/d\Omega$ (%)	δE_B (%)	δk_f (%)	$\delta\theta_e$ (%)	$\delta\theta_p$ (%)
0.69	7.4	1.1	0.6	7.0	2.2
0.72	7.6	1.2	0.7	7.1	2.3
0.76	7.8	1.2	0.8	7.2	2.5
0.80	8.1	1.3	0.9	7.5	2.7
0.84	8.5	1.3	1.0	7.8	2.9
0.88	9.0	1.4	1.1	8.2	3.1
0.91	9.5	1.5	1.2	8.6	3.4
0.95	10.2	1.6	1.3	9.2	3.7
0.99	11.2	1.8	1.4	10.0	4.1

Relative Systematic and Statistical Errors on the D($e,e'p$)n Cross Section



Conclusion and Future Outlook

- First meaningful data at very high missing momenta obtainable during commissioning period
- Systematic errors on the cross section are consistently smaller than statistical errors for the range of missing momentum studied
- Requirements on initial spectrometer performance are realistic
- 3 days of beam time required
- Good opportunity to obtain new early physics results

SHMS Detector Stack Photo



Acknowledgments

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BACKUP SLIDES

Cuts Applied to Extract Yield

Kinematic Cuts:

$$-10 \text{ MeV} \leq E_{miss} \leq 25 \text{ MeV}$$

$$35^\circ \leq \theta_{nq} \leq 45^\circ$$

$$1.30 \leq x_{Bj} \leq 1.40$$

$$3.1 \leq Q^2 \leq 5.2$$

Solid Angle Cuts:

e-arm: $|\frac{dx}{dz}|_{tgt} = |\theta|_{tgt} \leq 0.05 \text{ rad}$

(SHMS) $|\frac{dy}{dz}|_{tgt} = |\phi|_{tgt} \leq 0.025 \text{ rad}$

p-arm: $|\frac{dx}{dz}|_{tgt} = |\theta|_{tgt} \leq 0.08 \text{ rad}$

(HMS) $|\frac{dy}{dz}|_{tgt} = |\phi|_{tgt} \leq 0.035 \text{ rad}$

Momentum Acceptance Cuts:

e-arm: $-8 \leq \delta_e \leq 4$

(SHMS)

p-arm: $-15 \leq \delta_p \leq 15$

(HMS)

where $\delta \equiv \frac{p - p_{cen}}{p_{cen}}$