

Derive string $w = abaabaa$ from production rules

$$S \rightarrow a \quad (1)$$

$$S \rightarrow aAS \quad (2)$$

$$A \rightarrow bs \quad (3)$$

Given variables (Non-terminals) are $\{S, A\}$

Terminals are $\{a, b\}$

Production rules are

$$\begin{aligned} S &\rightarrow a \\ S &\rightarrow aAS \\ A &\rightarrow bs \end{aligned}$$

Consider production rule (2)

$$\begin{aligned} S &\rightarrow aAS && \text{from} \\ S &\rightarrow abss && \rightarrow (3) \\ S &\rightarrow abaaAS && \rightarrow 1 \& 2 \\ S &\rightarrow abaabss && \rightarrow 3 \\ S &\rightarrow abaabaa && \rightarrow 1 \end{aligned}$$

Finally $w = abaabaa$ string is derived

Derive LDT and RDT for the following $aabaa$ string,

$$S \rightarrow aAS / ass / \epsilon$$

$$A \rightarrow sbA / ba$$

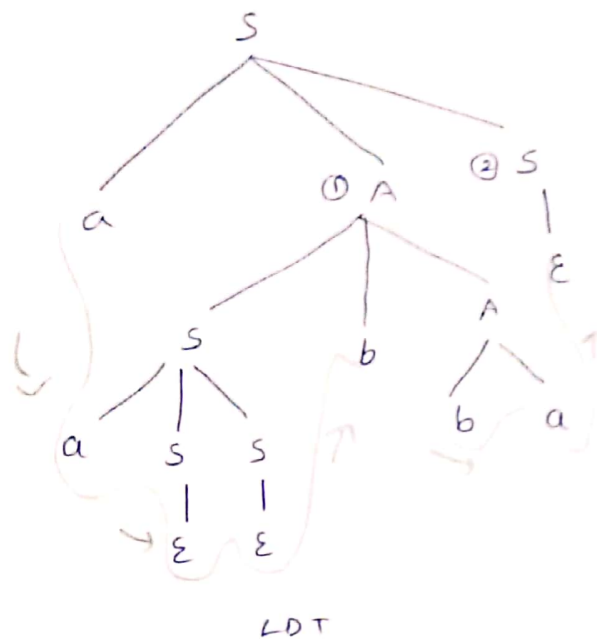
Given: Variables are $\{S, A\}$

Non Terminals are $\{a, b\}$

Production rules are

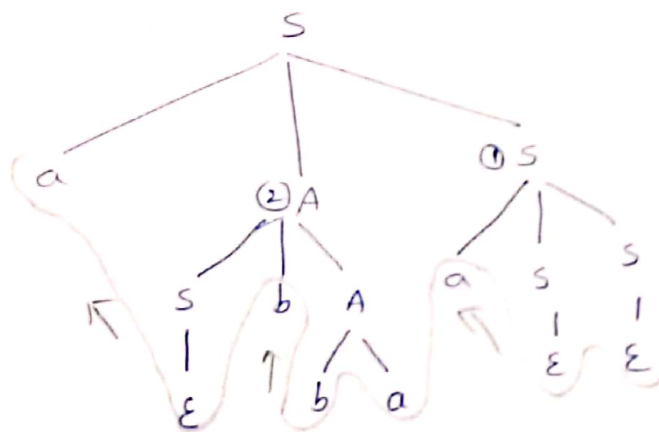
$$\begin{aligned} S &\rightarrow aAS \\ S &\rightarrow ass \\ S &\rightarrow \epsilon \\ A &\rightarrow sbA \\ A &\rightarrow ba \end{aligned}$$

Left Derivation Tree (LDT) is obtained by applying production rules to left most variable in each step



Final string is
aabba

Right Derivation Tree (RDT) is obtained by applying productions to right most variable in each step.



Final string is
aabba

3. Derive string ab from production rules $S \rightarrow AB$

Given:- Non terminals are $\{S, A, B\}$

Terminals are $\{a, b\}$

Production rules are $S \rightarrow AB \rightarrow (1)$

$A \rightarrow a \rightarrow (2)$

$B \rightarrow b \rightarrow (3)$

$$S \rightarrow AB$$

$$S \rightarrow aB \rightarrow (2)$$

$$S \rightarrow ab \rightarrow (3)$$

string ab is derived

Derive $a^m b^n$ from production rules $S \rightarrow AB$

$$A \rightarrow aA/a$$

$$B \rightarrow bB/b$$

In grammar

Given: Nonterminals are $\{S, A, B\}$

Terminals are $\{a, b\}$

Production rules are $S \rightarrow AB \rightarrow (1)$

$$A \rightarrow aA \rightarrow (2)$$

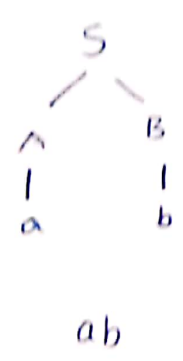
$$A \rightarrow a \rightarrow (3)$$

$$B \rightarrow bB \rightarrow (4)$$

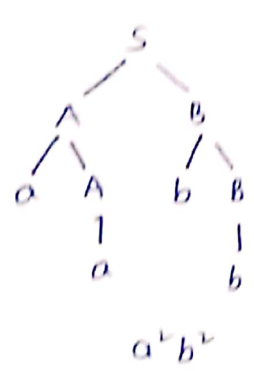
$$B \rightarrow b \rightarrow (5)$$

case-1

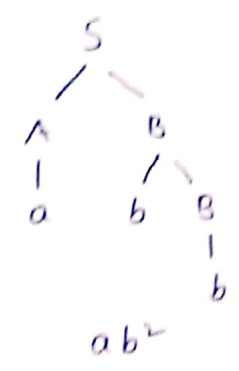
consider



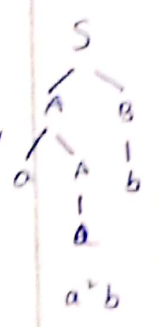
case: 2



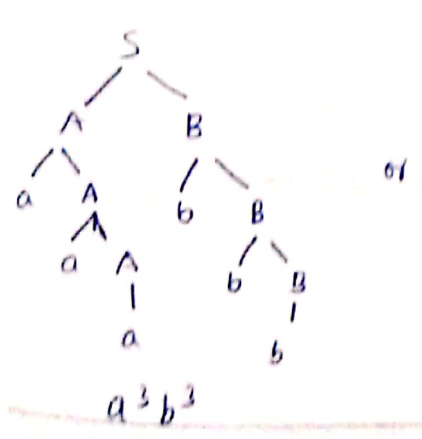
or



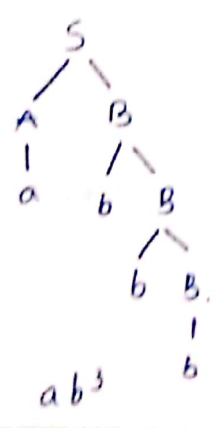
or



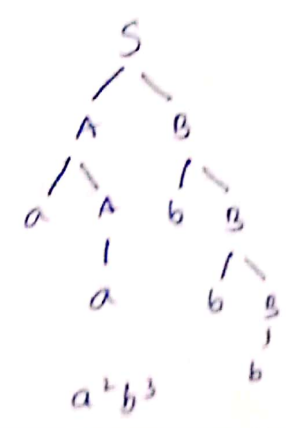
case: 3



or



or



Similarly we can derive multiple strings

General form will be $a^m b^n$ when $m, n \geq 0$

5 Show that context free grammar $S \rightarrow SS/a/b$ is ambiguous

Given grammar consists

Non terminals are $\{S\}$

Terminals are $\{a, b\}$

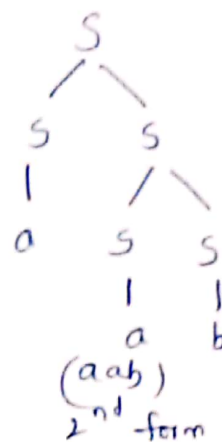
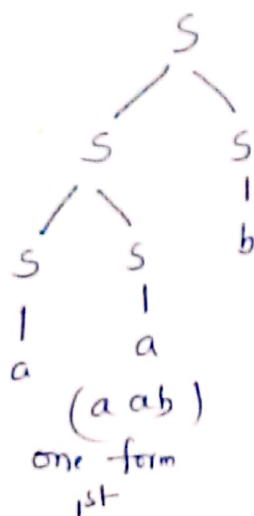
Production rules are $S \rightarrow SS \rightarrow 1$

$S \rightarrow a \rightarrow 2$

$S \rightarrow b \rightarrow 3$

Ambiguous grammar: A grammar is said to be ambiguous if it is having more than one form

To show: Given grammar is ambiguous



\therefore String aab can be expressed in 2 forms so given grammar is ambiguous

Hence showed.

Find whether given grammar is ambiguous or not

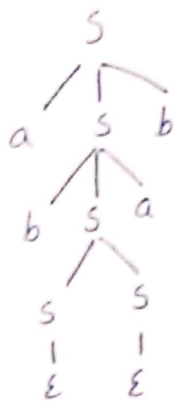
1) $S \rightarrow \epsilon$
 $S \rightarrow asb$
 $S \rightarrow bsa$
 $S \rightarrow SS$

2) $S \rightarrow AA$
 $A \rightarrow AAA$
 $A \rightarrow bA$
 $A \rightarrow AB$
 $A \rightarrow a$

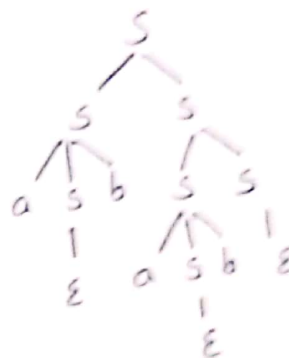
3) $S \rightarrow A$
 $S \rightarrow ASB$
 $S \rightarrow BS$
 $A \rightarrow AC$
 $A \rightarrow a$

① Given grammar contains
 Non terminals $\{S\}$
 Terminals $\{a, b\}$

Production rules are
 $S \rightarrow \epsilon$
 $S \rightarrow asb$
 $S \rightarrow bsa$
 $S \rightarrow SS$



String is abab
 1st form

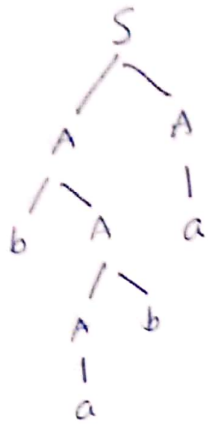


String is abab
 2nd form

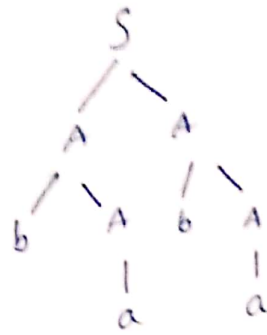
Hence given grammar is ambiguous.

② Given grammar contains
 Non terminals are $\{S, A\}$
 Terminals are $\{a, b\}$

Production rules are
 $S \rightarrow AA$
 $A \rightarrow AAA$
 $A \rightarrow bA$
 $A \rightarrow Ab$
 $A \rightarrow a$



string is baba
1st form



string is baba
2nd form

∴ Given grammar is ambiguous

Ⓒ Given grammar contains

$$S \rightarrow A$$

Non terminals are $\{S, A\}$

Terminals are $\{a, b\}$

Production rules are

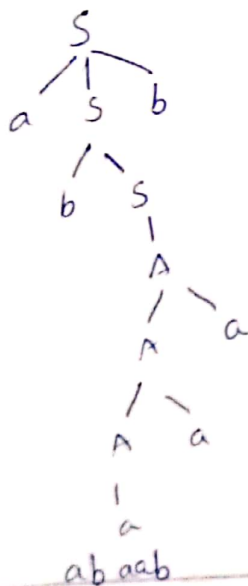
$$S \rightarrow A$$

$$S \rightarrow asb$$

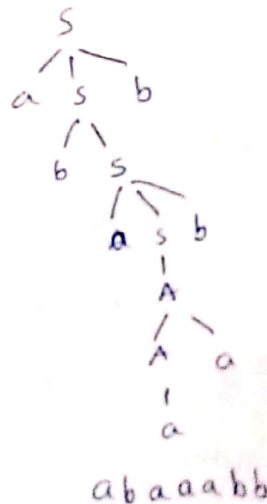
$$S \rightarrow bs$$

$$A \rightarrow Aa$$

$$A \rightarrow a$$



abaaab



abaaabb

Hence string grammar is unambiguous.

Eliminate ϵ -production rules if any

$$1) S \rightarrow Abac$$

$$A \rightarrow Bc$$

$$B \rightarrow b/\epsilon$$

$$C \rightarrow D/\epsilon$$

$$D \rightarrow d$$

Given grammar contains

Non terminals are $\{S, A, B, C, D\}$

Terminals are $\{a, b, c, d\}$

Production rules are $S \rightarrow Abac \rightarrow 1$

$$A \rightarrow Bc \rightarrow 2$$

$$B \rightarrow b \rightarrow 3$$

$$B \rightarrow \epsilon \rightarrow 4$$

$$C \rightarrow D \rightarrow 5$$

$$C \rightarrow \epsilon \rightarrow 6$$

$$D \rightarrow d \rightarrow 7$$

Steps:-

1) Identify Nullable variables

Nullable variables are A, B, C

2) Create two versions one with nullable variables and other without nullable variable

with

$$A \rightarrow Bc$$

$$B \rightarrow \epsilon$$

$$C \rightarrow \epsilon$$

without

$$S \rightarrow Abac$$

$$B \rightarrow b$$

$$C \rightarrow D$$

$$D \rightarrow d$$

$$A \rightarrow Bc$$

3) Remove ϵ production then we get

$$S \rightarrow bac$$

$$A \rightarrow B \cancel{c} / Bc \quad A \rightarrow Bc / c / B$$

$$B \rightarrow b$$

$$c \rightarrow \emptyset$$

$$D \rightarrow d$$

$$2) S \rightarrow as / bs / \epsilon$$

Given grammar contains

Non terminals are S

Terminals are a, b

Production rules are $S \rightarrow as$

$$S \rightarrow bs$$

$$S \rightarrow \epsilon$$

Steps:

1) Identify Nullable variables S

2) Two versions one with Nullable variable and other without
Nullable variables are

with	without
$S \rightarrow \epsilon$	$S \rightarrow as$
	$S \rightarrow bs$

3) Eliminate ϵ production we get

$$S \rightarrow a/b$$

$$3) S \rightarrow ABAC$$

$$A \rightarrow aA / \epsilon$$

$$B \rightarrow bB / \epsilon$$

$$C \rightarrow c$$

Given grammar contains

Non-terminals are $\{S, A, B, C\}$

Terminals are $\{a, b, c\}$

Production rules are

$$S \rightarrow ABAC$$

$$A \rightarrow aA/\epsilon$$

$$B \rightarrow bB/\epsilon$$

$$C \rightarrow c$$

Steps:-

1) Identify Nullable variables $\{A, B\}$

2) Two versions one with Nullable variables and other without nullable variable on RHS side

with	without
$A \rightarrow \epsilon$	$C \rightarrow c$
$B \rightarrow bB$	
$S \rightarrow ABAC$	

3) ϵ eliminate ϵ -production we get

$S \rightarrow C$
 $A \rightarrow a$
 $B \rightarrow b$
 $C \rightarrow c$

4) $S \rightarrow bEd$

$E \rightarrow bEc$

$E \rightarrow GGe$

$G \rightarrow b$

$G \rightarrow kL$

$k \rightarrow ckd$

$k \rightarrow \epsilon$

$L \rightarrow dLe$

$L \rightarrow \epsilon$

Given grammar contains

Non terminals are $\{S, E, G, K, L\}$

Terminals are $\{b, c, d, e, f\}$

Production rules are $S \rightarrow bef$

$E \rightarrow bEc$

$E \rightarrow G G c$

$G \rightarrow b$

$G \rightarrow KL$

$K \rightarrow ckd$

$K \rightarrow \epsilon$

$L \rightarrow dLe$

$L \rightarrow \epsilon$

Steps:-

1) Identify Nullable variables $\{G, K, L\}$

2) Two versions with Nullable variables and without Nullable variables on right side

with	without
$G \rightarrow KL$	$S \rightarrow bef$
$K \rightarrow ckd$	$E \rightarrow bEc$
$L \rightarrow dLe$	$E \rightarrow G G c$
	$E \rightarrow b$

3) Eliminate ϵ - productions we get

$S \rightarrow bef / bf$

$E \rightarrow bEc / bc$

$E \rightarrow G G c / c / bc / bbc$

$E \rightarrow b$

$K \rightarrow cd$

$L \rightarrow de$

$$S \rightarrow eSc$$

$$S \rightarrow GH$$

$$G \rightarrow cGb$$

$$G \rightarrow \epsilon$$

$$H \rightarrow JHd$$

$$H \rightarrow \epsilon$$

$$J \rightarrow bJ$$

$$J \rightarrow f$$

Given grammar contains

Non terminals are $\{S, G, H, J\}$

Terminals are $\{e, b, c, d, f\}$

Production rules are

$$S \rightarrow eSc$$

$$S \rightarrow GH$$

$$G \rightarrow cGb$$

$$G \rightarrow \epsilon$$

$$H \rightarrow JHd$$

$$H \rightarrow \epsilon$$

$$J \rightarrow bJ$$

$$J \rightarrow f$$

Steps:

1) Identifying Nullable variables

$\{S, G, H\}$

2) Two versions one with Nullable variables and other without nullable variables on right side

with	without
$S \rightarrow GH$	$J \rightarrow bJ$
$G \rightarrow cGb$	$J \rightarrow f$
$H \rightarrow JHd$	
$S \rightarrow eSc$	

3) Eliminate ϵ production we get

$$S \rightarrow ec$$

$$G \rightarrow cb$$

$$H \rightarrow \cancel{f}d$$

$$J \rightarrow bf$$

$$J \rightarrow f$$

Removal of Unit production.

$$1) S \rightarrow Aa/B$$

$$B \rightarrow A/bb$$

$$A \rightarrow a/bc/B$$

Given grammar contains

Non terminals are $\{S, A, B\}$

Terminals are $\{a, b, c\}$

Production rules are $S \rightarrow Aa/B$

$$B \rightarrow A/bb$$

$$A \rightarrow a/bc/B$$

Unit production

$$S \rightarrow B$$

$$B \rightarrow A$$

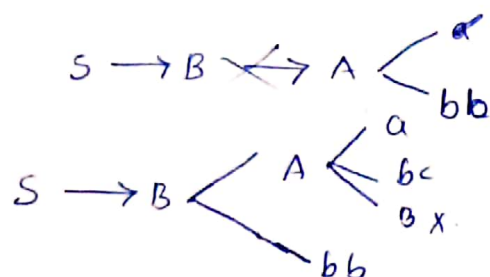
$$A \rightarrow B$$

Non unit production

$$S \rightarrow Aa$$

$$B \rightarrow bb$$

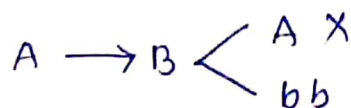
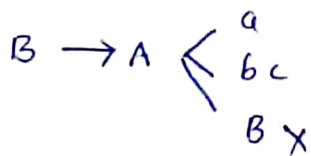
$$A \rightarrow a/bc$$



$$S \rightarrow Aa/bb/a/bc$$

$$B \rightarrow bb/a/bc$$

$$A \rightarrow a/bc/bb$$



$$\therefore S \rightarrow Aa/bb/a/bc$$

$$B \rightarrow bb/a/bc$$

$$A \rightarrow a/bc/bb$$

$$a) S \rightarrow CBA$$

$$S \rightarrow B$$

$$A \rightarrow CB$$

$$A \rightarrow Abbs$$

$$B \rightarrow aaa$$

Given grammar contains

Variables (Non-terminals) are $\{S, A, B, c\}$

Terminals are $\{a, b\}$

Production rules are

$$S \rightarrow CBA$$

$$S \rightarrow B$$

$$A \rightarrow CB$$

$$A \rightarrow Abbs$$

$$B \rightarrow aaa$$

Unit production

$$S \rightarrow B$$

Non unit production

$$S \rightarrow CBA$$

$$A \rightarrow CB$$

$$A \rightarrow Abbs$$

$$B \rightarrow aaa$$

$$S \rightarrow B \rightarrow aaa$$

$$S \rightarrow CBA$$

$$S \rightarrow aaa$$

$$A \rightarrow CB$$

$$A \rightarrow Abbs$$

$$B \rightarrow aaa$$

$$37 \quad S \rightarrow AB$$

$$A \rightarrow a$$

$$B \rightarrow C/b$$

$$C \rightarrow D$$

$$D \rightarrow E/bc$$

$$E \rightarrow d/Ab$$

Given grammar contains

Non terminals are $\{S, A, B, C, D, E\}$

Terminals are $\{a, b, c, d\}$

Production rules are

$$S \rightarrow AB$$

$$A \rightarrow a$$

$$B \rightarrow C/b$$

$$C \rightarrow D$$

$$D \rightarrow E/bc$$

$$E \rightarrow d/Ab$$

Unit production

$$B \rightarrow C$$

$$C \rightarrow D$$

$$D \rightarrow E$$

Non unit production

$$S \rightarrow AB$$

$$A \rightarrow a$$

$$B \rightarrow b/d/Ab$$

$$D \rightarrow bc$$

$$E \rightarrow d/Ab$$

$$B \rightarrow C \rightarrow D \leftarrow E \begin{cases} d \\ Ab \end{cases}$$

$$C \rightarrow D \rightarrow E \begin{cases} d \\ Ab \end{cases}$$

$$D \rightarrow E \begin{cases} d \\ Ab \end{cases}$$

So final productions are

$$S \rightarrow AB$$

$$A \rightarrow a$$

$$B \rightarrow b/d/Ab$$

$$C \rightarrow d/Ab$$

$$D \rightarrow bc/d/Ab$$

$$E \rightarrow d/Ab$$

Removal of useless symbols:-

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$$1) S \rightarrow ABC / BaB$$

$$A \rightarrow aA / Bac / aaa$$

$$B \rightarrow bBb / a$$

$$C \rightarrow cA / Ac$$

Given grammar contains

Non terminals are $\{S, A, B, C\}$

Terminals are $\{a, b\}$

Production rules are $S \rightarrow ABC / BaB$

$$A \rightarrow aA / Bac / aaa$$

$$B \rightarrow bBb / a$$

$$C \rightarrow cA / Ac$$

rules:-

1) Remove symbols not deriving terminal string

2) Remove symbols non reachable from S.

useless symbols are $\{C, SA\}$ as C can't derive any terminal string and $S \rightarrow ABC$ as it contains C.
 $A \rightarrow Bac$

After removing useless symbols production rules are:-

$$S \rightarrow BaB$$

$$A \rightarrow aA / ~~Bac~~ / aaa$$

$$B \rightarrow bBb / a$$

$$2) S \rightarrow Sa / A / c$$

$$A \rightarrow a$$

$$B \rightarrow bb$$

$$C \rightarrow ac$$

Ans) Given grammar contains

Non terminals are $\{S, A, B, C\}$

Terminals are $\{a, b\}$

Production rules are $S \rightarrow Sa / A / c$

$$A \rightarrow a$$

$$B \rightarrow bb$$

$$C \rightarrow ac$$

Useless symbols are $\{S, C\}$

After removing useless symbols we get

$$S \rightarrow Sa / A$$

$$A \rightarrow a$$

Use 3 rules to simplify given grammar

$$S \rightarrow aA / bB / a$$

$$A \rightarrow aB / B / \epsilon$$

$$B \rightarrow b / \epsilon$$

Given grammar contains

Non terminals are $\{S, A, B\}$

Terminals are $\{a, b\}$

Production rules are

$$S \rightarrow aA / bB / a$$

$$A \rightarrow aB / B / \epsilon$$

$$B \rightarrow b / \epsilon$$

Rule 1:

→ Removal of ϵ rules.

a) Nullable variables are $\{A, B\}$

b) 2 versions with & without Nullable variables on R.H.

with	without
$A \rightarrow B$	$S \rightarrow a$
$A \rightarrow aB$	$A \rightarrow B$
$S \rightarrow aA$	$S \rightarrow aA$
$S \rightarrow bB$	$S \rightarrow bB$
	$A \rightarrow aB$

c) Removal of ϵ productions we get $S \rightarrow a / b / a$

$$A \rightarrow a$$

$$B \rightarrow b$$

Rule 2 :-

→ And there is no need of using other two second rule

Since there are no unit production

Rule 3: Removal of useless symbols

Since the production 'S' is not having variables A, B we can eliminate them. After eliminating we get production rules

$$S \rightarrow a / b$$

Normal forms:-

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Find CNF and GNF equivalent to following grammar

$$1) S \rightarrow SAS$$

$$S \rightarrow SVS$$

$$S \rightarrow TS$$

$$S \rightarrow (S)$$

$$S \rightarrow P$$

$$S \rightarrow Q$$

$$2) E \rightarrow E + E$$

$$E \rightarrow E * E$$

$$E \rightarrow (E)$$

$$E \rightarrow a$$

1) Given grammar contains Non-terminals are $\{S\}$

Terminals are $\{A, V, T, (,), P, Q\}$

To find CNF we make of assigning new variables to terminals

let $x_1 = A, x_2 = V, x_3 = T, x_4 = (, x_5 =)$

Then production rules are

$$S \rightarrow SX_1S \rightarrow \text{Not in CNF} \textcircled{1}$$

$$S \rightarrow SX_2S \rightarrow \text{Not in CNF} \textcircled{2} \text{ Rule (a) Conditions for GNF}$$

$$S \rightarrow x_3S \quad \checkmark \quad \textcircled{3} \quad 1) A \rightarrow BC$$

$$S \rightarrow x_4Sx_5 \rightarrow \text{Not in CNF} \textcircled{4} \quad 2) A \rightarrow a$$

$$S \rightarrow P \quad \checkmark \quad \textcircled{5}$$

$$S \rightarrow Q \quad \checkmark \quad \textcircled{6}$$

Production rules 1, 2, 4 are not in CNF we convert them into CNF

$$S \rightarrow SX_1S \rightarrow X_6S$$

$$X_6 \rightarrow SX_1$$

$$S \rightarrow SX_2S \rightarrow X_7S$$

$$X_7 \rightarrow SX_2$$

$$S \rightarrow x_4Sx_5 \rightarrow X_8X_5$$

$$X_8 \rightarrow x_4S$$

∴ Finally CNF is

$$S \rightarrow X_6 S$$

$$S \rightarrow X_7 S$$

$$X_6 \rightarrow S X_1$$

$$X_7 \rightarrow S X_2$$

$$S \rightarrow X_8 X_5$$

$$X_8 \rightarrow X_4 S$$

$$X_1 \rightarrow \wedge$$

$$X_2 \rightarrow \vee$$

$$X_3 \rightarrow \neg$$

$$X_4 \rightarrow ($$

$$X_5 \rightarrow)$$

ϵ

$$S \rightarrow X_3 S$$

ϵ

$$S \rightarrow P$$

$$S \rightarrow \neg$$

Converting to GNF

The given grammar is in CNF
and there is no left recursion

Condition

$$A \rightarrow \alpha$$

$$\alpha \in N^*$$

$$S \rightarrow \epsilon$$

$$S \rightarrow X_6 S / X_7 S / X_8 X_5 / X_3 S$$

$$X_6 \rightarrow S X_1$$

$$X_7 \rightarrow S X_2$$

$$X_8 \rightarrow X_4 S$$

are not in GNF

Substitute $X_4 \rightarrow ($, $X_3 \rightarrow \neg$ so we get $X_8 \rightarrow (S$, $S \rightarrow \neg S$

Substitute $X_8 \rightarrow (S$ in $S \rightarrow X_8 X_5$ we get

$$S \rightarrow X_6 S / X_7 S / (S X_5 / \neg S$$

$$X_8 \rightarrow (S$$

$$X_6 \rightarrow S X_1$$

$$X_7 \rightarrow S X_2$$

Now $S \rightarrow X_6 S / X_7 S$

$X_6 \rightarrow S X_1$

$X_7 \rightarrow S X_2$

Now $X_6 \rightarrow X_6 S X_1 / X_7 S X_1$

$X_7 \rightarrow 7 S X_2 / (S X_5 X_2$

$S \rightarrow 7 S X_2 S / (S X_5 X_2 S / 7 S X_1 S / (S X_5 S_1$

$X_6 \rightarrow 7 S X_1 / (S X_5 S_1$

GNF is
 $S \rightarrow 7 S X_2 S / (S X_5 X_1 S / 7 S X_1 S / (S X_5 S_1 S$

$X_1 \rightarrow \wedge, X_2 \rightarrow \vee, X_3 \rightarrow 7,$

$X_4 \rightarrow (, X_5 \rightarrow), S \rightarrow P,$

$S \rightarrow Q, S \rightarrow (S X_5 / 7 S$

$X_7 \rightarrow 7 S X_2 / (S X_5 X_2$

$X_6 \rightarrow 7 S X_1 / (S X_5 S_1$

3. $E \rightarrow E + E$

$E \rightarrow E * E$

$E \rightarrow (E)$

$E \rightarrow a$

Given grammar contains Non terminal $\{E\}$

Terminals are $\{+, *, (,), a\}$

To convert CNF

$E \rightarrow E + E$

$E \rightarrow E * E$

$E \rightarrow (E)$

} are not in CNF

So, to convert substitute terminals with new variable,

as

$X_1 \rightarrow +$

$X_2 \rightarrow *$

$X_3 \rightarrow ($

$X_4 \rightarrow)$

we get

$E \rightarrow E X_1 E$

$E \rightarrow E X_2 E$

$E \rightarrow X_3 E X_4$

$X_1 \rightarrow +$

$X_2 \rightarrow *$

$X_3 \rightarrow ($

$X_4 \rightarrow)$

$E \rightarrow a$

$$E \rightarrow E X_1 E \begin{cases} X_5 E \\ X_5 \rightarrow E X_1 \end{cases}$$

$$E \rightarrow E X_2 E \begin{cases} X_6 E \\ X_6 \rightarrow E X_2 \end{cases}$$

$$E \rightarrow X_3 E X_4 \begin{cases} X_7 X_4 \\ X_7 \rightarrow X_3 E \end{cases}$$

Final production rules in CNF are

$$E \rightarrow X_5 E$$

$$X_5 \rightarrow E X_1$$

$$X_1 \rightarrow +$$

$$E \rightarrow X_6 E$$

$$X_6 \rightarrow E X_2$$

$$X_2 \rightarrow *$$

$$E \rightarrow X_7 X_4$$

$$X_7 \rightarrow X_3 E$$

$$X_3 \rightarrow ($$

$$X_4 \rightarrow)$$

$$E \rightarrow a$$

GNF

$$E \rightarrow E + E$$

$$E \rightarrow E * E$$

$$E \rightarrow (E)$$

$$E \rightarrow a$$

} Not in GNF. but converted present

$$E \rightarrow X_5 E$$

$$X_5 \rightarrow E X_1$$

$$X_1 \rightarrow +$$

$$E \rightarrow X_6 E$$

$$X_6 \rightarrow E X_2$$

$$E \rightarrow X_7 X_4$$

$$X_7 \rightarrow X_3 E$$

$$X_3 \rightarrow ($$

$$X_4 \rightarrow)$$

$$E \rightarrow a$$

So we get GNF as

$$X_1 \rightarrow +$$

$$X_4 \rightarrow)$$

$$E \rightarrow a$$

$$X_3 \rightarrow ($$

$$X_7 \rightarrow (E$$

$$X_6 \rightarrow a X_2$$

$$E \rightarrow a X_2 E$$

$$X_5 \rightarrow a X_1$$

$$E \rightarrow a X_1 E$$

$$E \rightarrow (E)$$

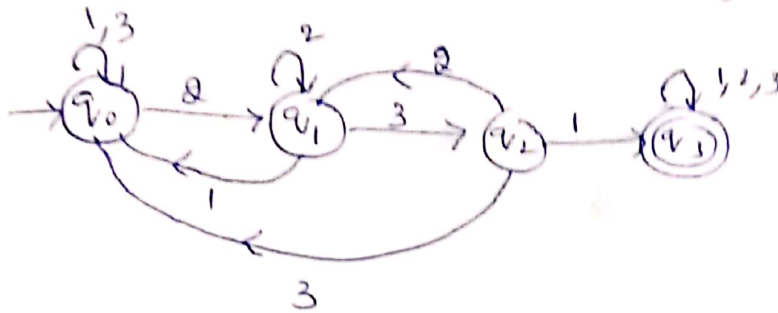
Finite Automata:

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1)

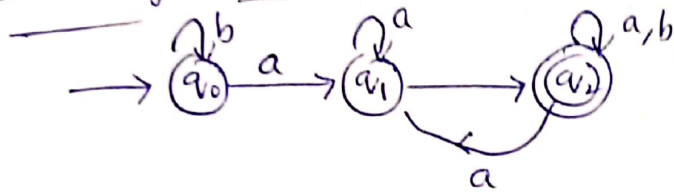
1) construct DFA which accepts set of strings in $\{1,2,3\}^*$ containing $\{2,3,1\}$ as substring

$$L = \{231, 1231, 2231, 3231, 2311, \dots\}$$



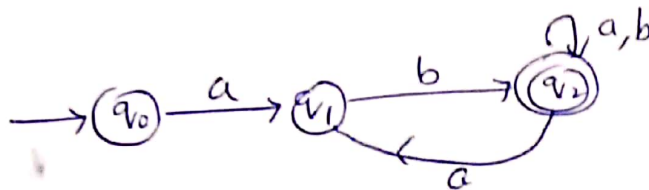
2) DFA which accepts set of strings containing $\{ab\}$ as substring, containing $\{2,3,1\}$ as substring.

substring ab



starting with ab

$$L = \{ab, abaa, abb, \dots\}$$



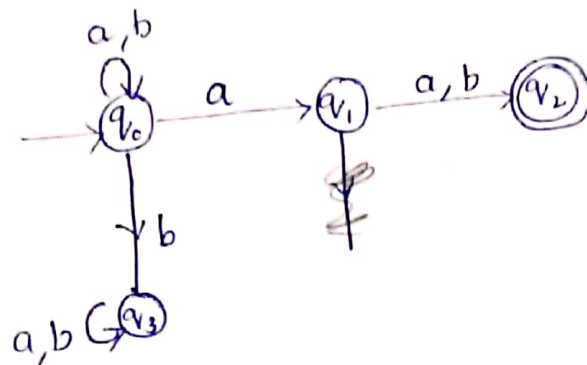
Ending with ab

$$L = \{ab, bab, bbab, abab, aabab, \dots\}$$

DFA and NFA

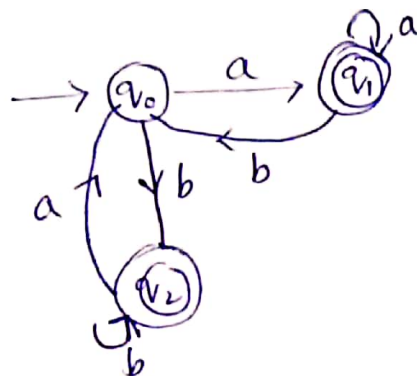
Construct DFA whose string accepts ^{Second third symbol} from RHS is 'a'.

$$L = \{ aa, ab, aab, bab, \overset{a \text{ (2nd)}}{\underset{\text{initial}}{a}} \dots \}$$



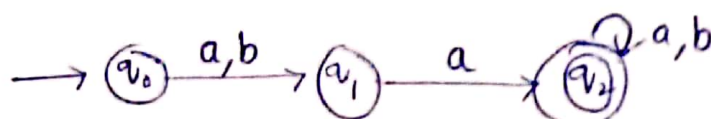
Construct DFA which accepts set of strings which start and ends with same symbols.

$$L = \{ a, b, aa, bb, aba, bab, aaa, bbb, \dots \}$$



Construct NFA and convert it to DFA for language whose strings contains second symbol from LHS is 'a'.

$$L = \{ aa, ba, baa, aaa, \dots \}$$



1) Construct state transition table for NFA

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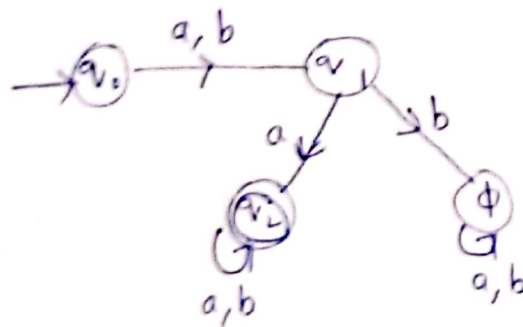
18001A0545

	a	b
$\rightarrow q_0$	q_1	q_1
q_1	q_2	ϕ
$* q_2$	q_2	q_2

2) State transition table for DFA

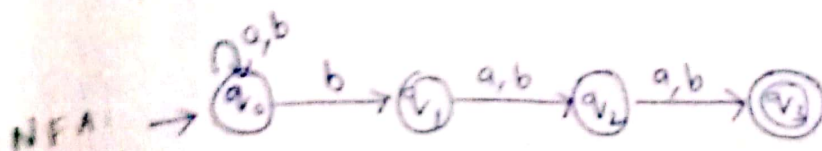
	a	b
$\rightarrow q_0$	q_1	q_1
q_1	q_2	ϕ
$* q_2$	q_2	q_2
	D	D

3) Draw DFSA



Construct NFA and convert it to DFA for the language whose strings accepts 3rd symbol from RHS is b

$$L = \{ baa, bbb, abaa, bbab, \dots \}$$



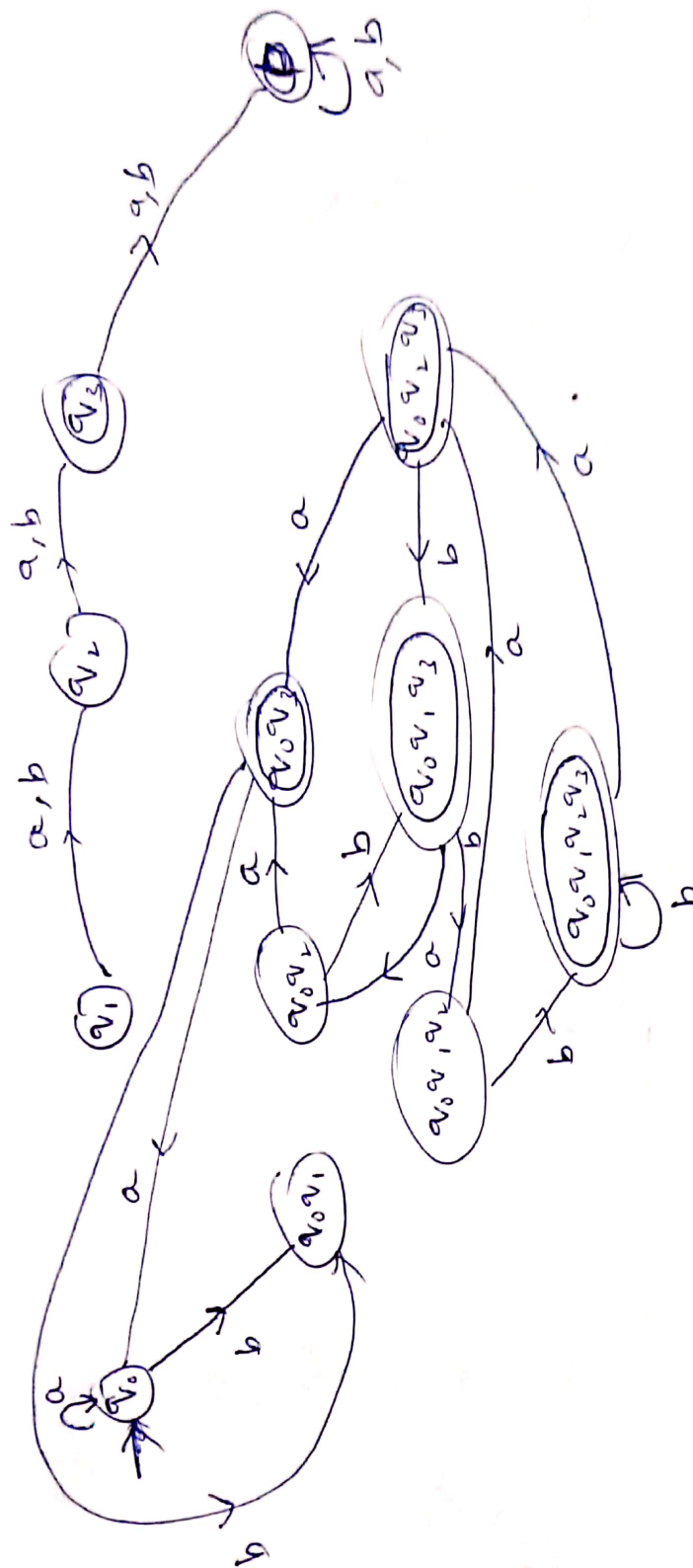
State transition table for NFA:

	a	b
q_0	q_0	$\{q_0, q_1\}$
q_1	q_2	q_2
q_2	q_3	q_3
q_3	D	D

State transition table for DFA:

	a	b
$\rightarrow q_0$	q_0	$[q_0, q_1]$
q_1	q_2	q_2
q_2	q_3	q_3
* q_3	\emptyset	\emptyset
q_0, q_1	q_0, q_2	$[q_0, q_1, q_2]$
D	\emptyset	\emptyset
q_0, q_2	q_0, q_3	q_0, q_1, q_3
q_0, q_1, q_2	q_0, q_2, q_3	q_0, q_1, q_2, q_3
* q_0, q_3	q_0	q_0, q_1
* q_0, q_1, q_3	q_0, q_2	q_0, q_1, q_2
* q_0, q_2, q_3	q_0, q_3	q_0, q_1, q_3
* q_0, q_1, q_2, q_3	q_0, q_2, q_3	q_0, q_1, q_2, q_3

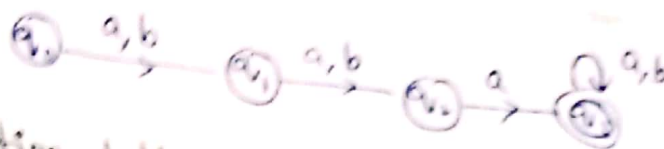
DFSA diagram:-



Construct NFA and convert it to DFA for the language
 whose strings accept 3rd symbol from LHS is a

$$L = \{ aaa, baa, bba, bbab, aaab, \dots \}$$

NFA:



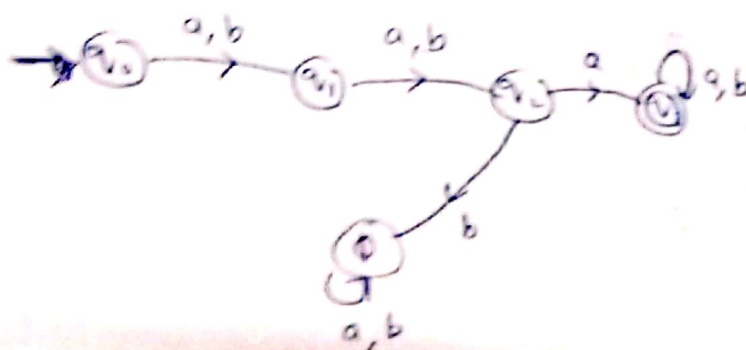
State transition table for NFA:

	a	b
→ q ₀	q ₁	q ₁
q ₁	q ₂	q ₂
q ₂	q ₃	∅
* q ₃	q ₃	q ₃

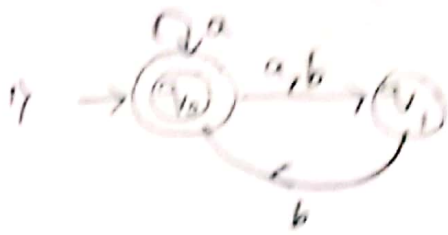
State transition table for DFA:

	a	b
→ q ₀	q ₁	q ₁
q ₁	q ₂	q ₂
q ₂	q ₃	∅
* q ₃	q ₃	q ₃
∅	∅	∅

DFA diagram



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Convert the following NFA into DFA using subset construction method



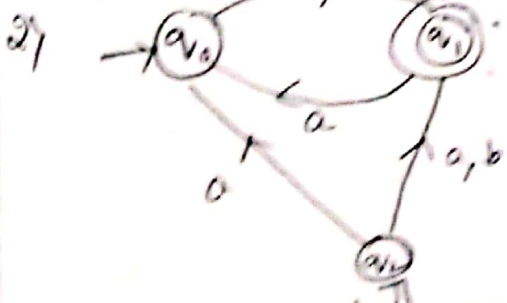
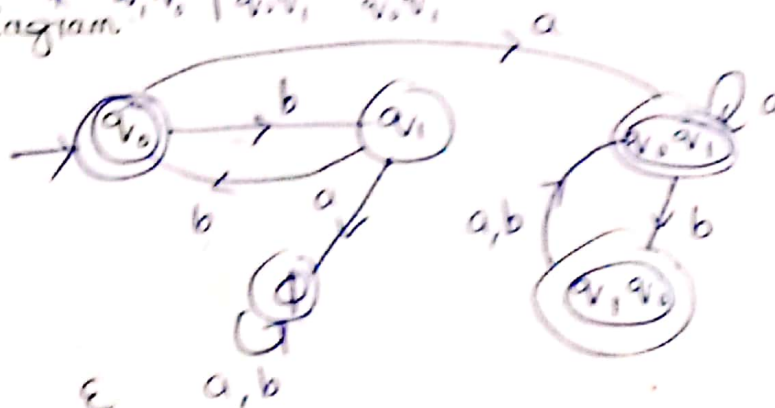
State transition table for NFA:

	a	b
q_0	q_0	q_1
q_1	ϕ	q_0

State transition table for DFA:

	a	b
$\rightarrow * q_0$	$\{q_0, q_1\}$	q_1
q_1	ϕ	q_0
ϕ	ϕ	ϕ
$* q_0, q_1$	q_0, q_1	q_0, q_1
$* q_1, q_0$	q_1, q_0	q_1, q_0

DFA diagram:



State transition table for NFA:-

	a	b	ϵ
$\rightarrow q_0$	ϕ	ϕ	q_1
$* q_1$	q_0	ϕ	ϕ
q_2	$[q_0, q_1]$	$[q_1, q_2]$	ϕ
q_0, q_1			
q_1, q_2			

State transition table for DFA:-

	a	b	ϵ
$\rightarrow q_0$	ϕ	ϕ	q_1
$* q_1$	q_0	ϕ	ϕ
q_2	q_0, q_1	q_1, q_2	ϕ
$* q_0, q_1$	q_0	ϕ	q_1
$* q_1, q_2$	q_0, q_1	q_1, q_2	ϕ
ϕ	ϕ	ϕ	ϕ

DFA diagram:-

