

Energy Efficiency Analysis for Building Design

Final project for Machine Learning for Business

TEAM 2

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Dataset overview

Dataset Description

- Buildings vary in terms of **glazing area**, **glazing area distribution**, **orientation**, and other structural parameters.
- The objective is to utilize the **eight features** to accurately predict the response variables.



VARIABLE	DATA	DATA TYPE
X1	Relative Compactness	Continuous
X2	Surface Area	Continuous
X3	Wall Area	Continuous
X4	Roof Area	Continuous
X5	Overall Height	Continuous
X6	Orientation	Categorical and Discrete
X7	Glazing Area	Continuous
X8	Glazing Area Distribution	Categorical and Discrete
Y1	Heating Load	Continuous
Y2	Cooling Load	Continuous

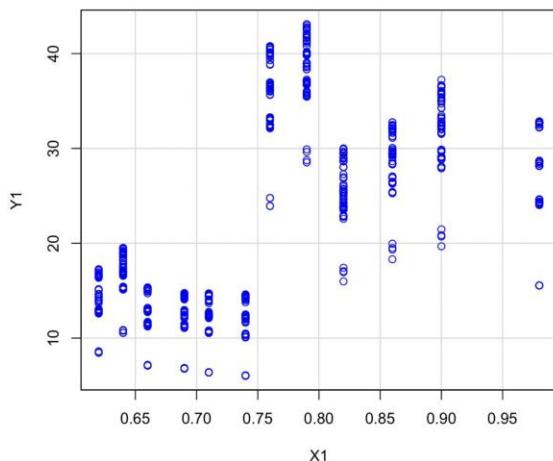
Data cleaning

- **Handling X6: Orientation**
 - The original variable had four categories:
 $2 = North, 3 = East, 4 = South, 5 = West.$
 - Following the rule for dummy variable creation (n categories $\rightarrow n-1$ dummies), I excluded **West (5)** as the base category and created dummy variables for **North, East, and South using Excel.**
- **Handling X8: Glazing Area Distribution**
 - The original variable had six categories:
 $0 = Unknown, 1 = Uniform, 2 = North, 3 = East, 4 = South, 5 = West.$
 - Similarly, I chose **Unknown (0)** as the base category and created dummy variables for **Uniform, North, East, South, and West.**

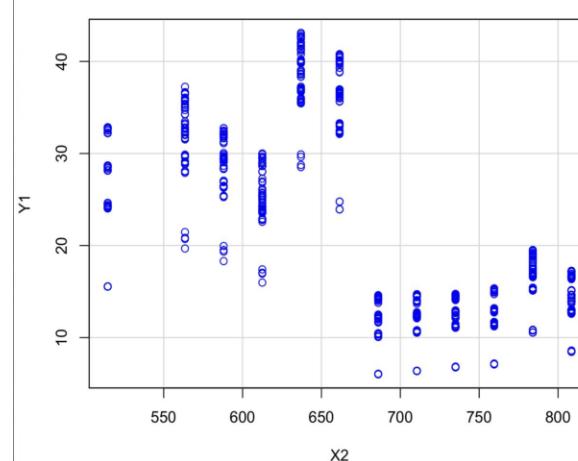


1. Visualization

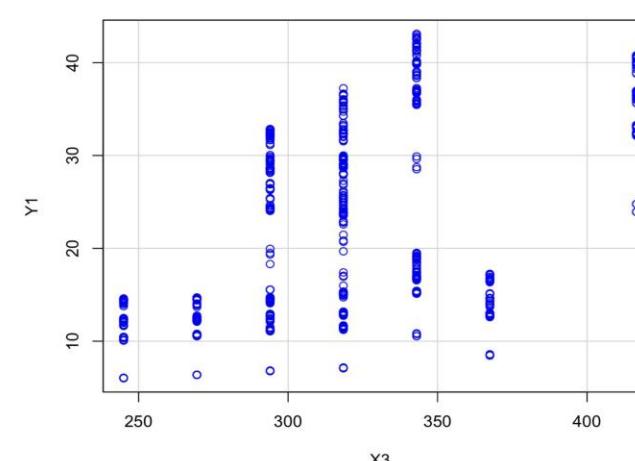
Scatter Plot relationships between the predictors (X1–X8) vs Heating Pad(y1)



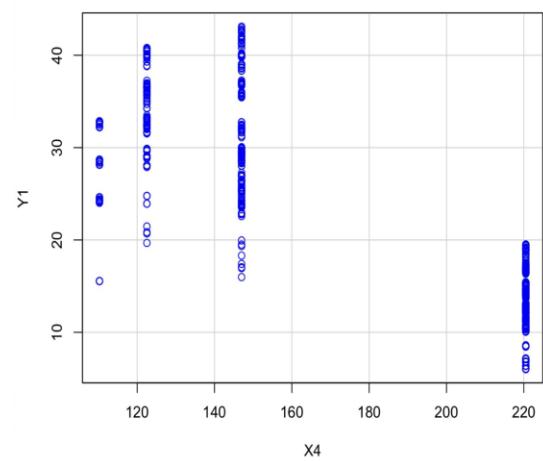
We observe an upward trend



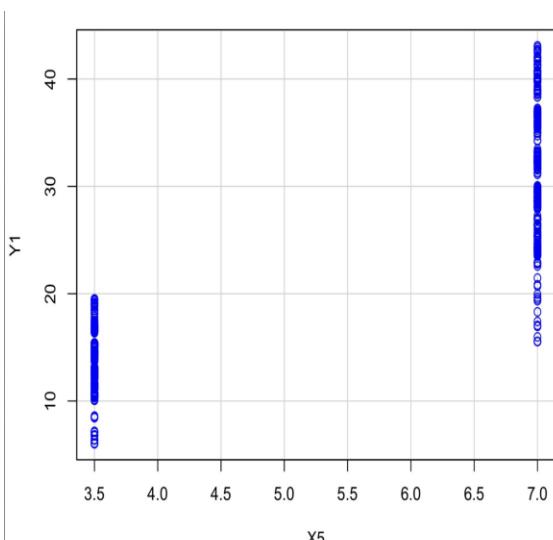
We observe a downward trend



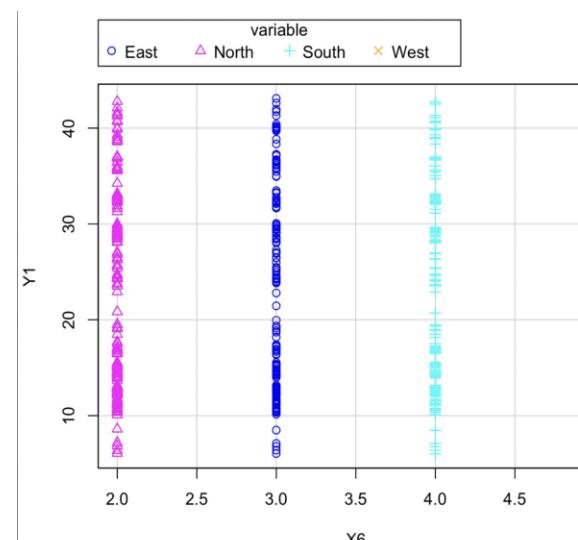
We observe an upward trend



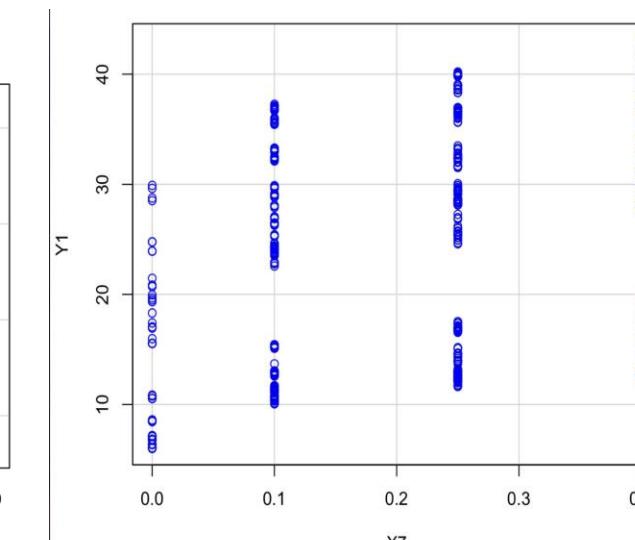
We observe a downward trend



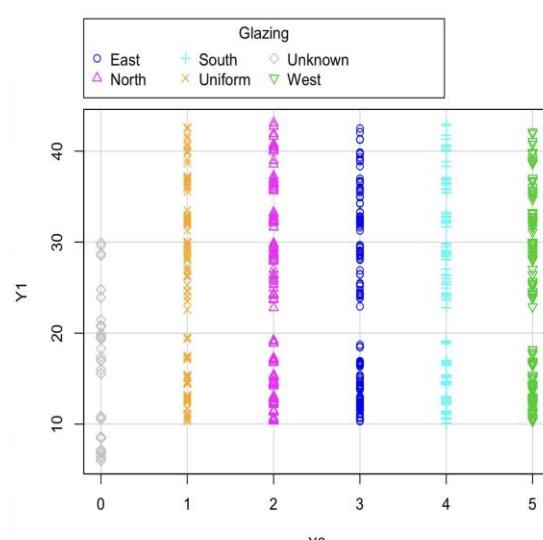
We observe an upward trend



Change in y does not affect x for each of the variable

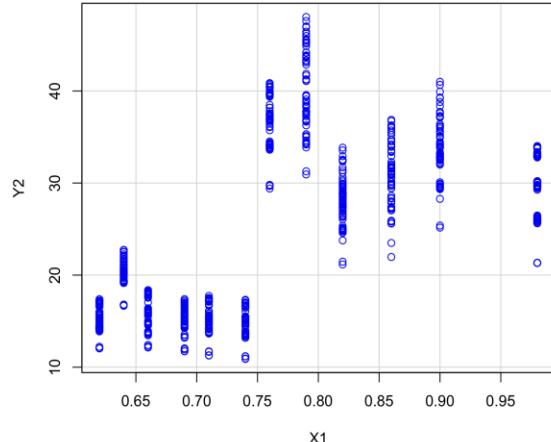


We observe an upward trend

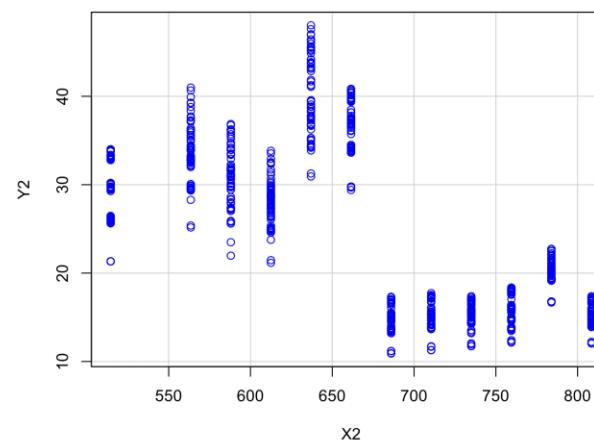


Change in y does not affect x for each of the variable

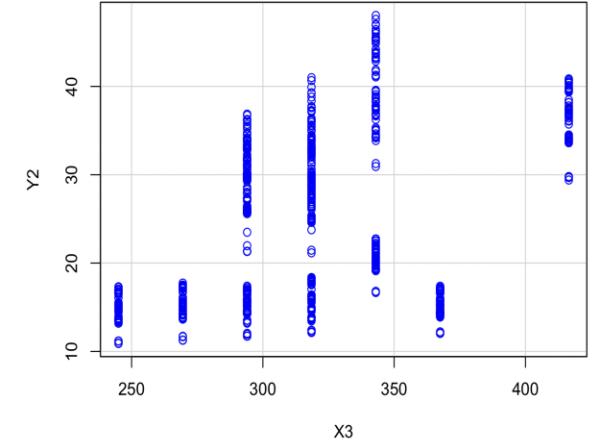
Scatter Plot relationships between the predictors (X1–X8) vs Cooling Pad(y2)



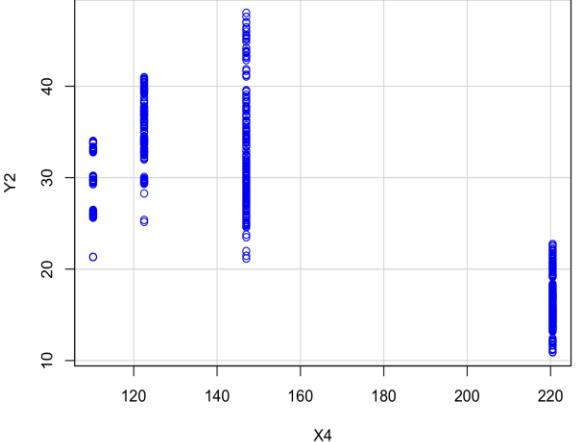
We observe an upward trend



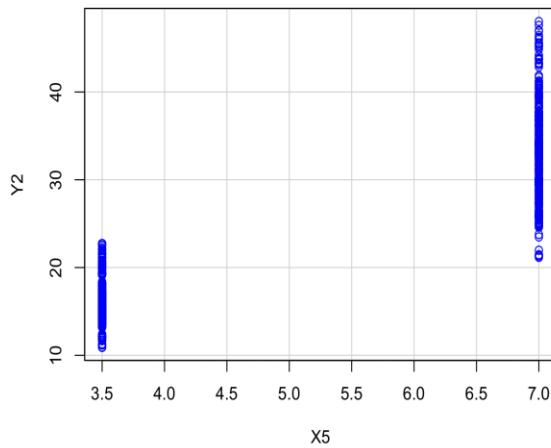
We observe a downward trend



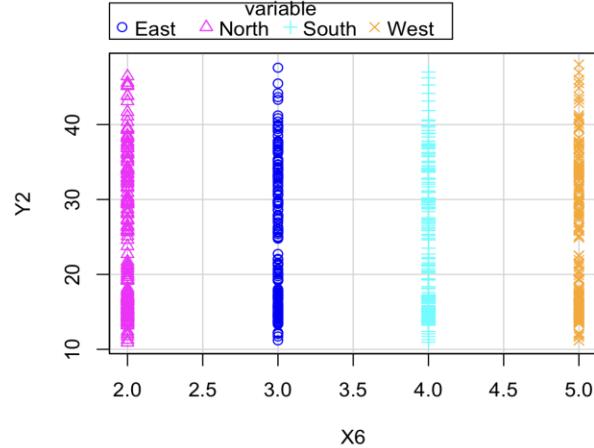
We observe an upward trend



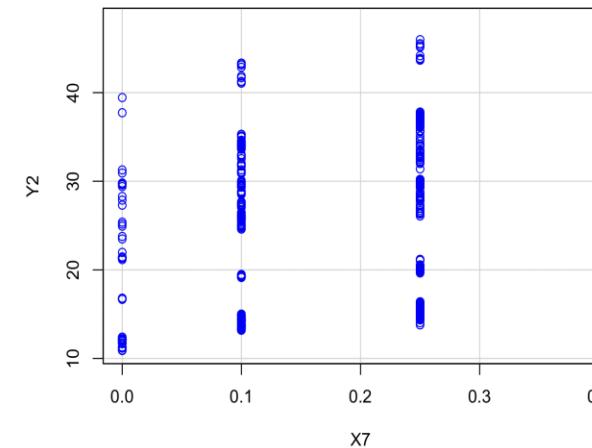
We observe a downward trend



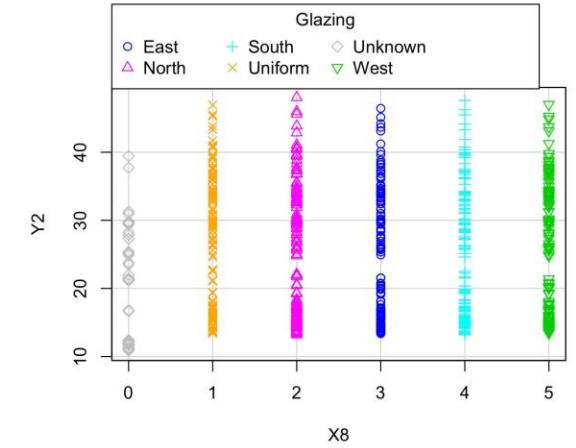
We observe an upward trend



Change in y does not affect x for each of the variable

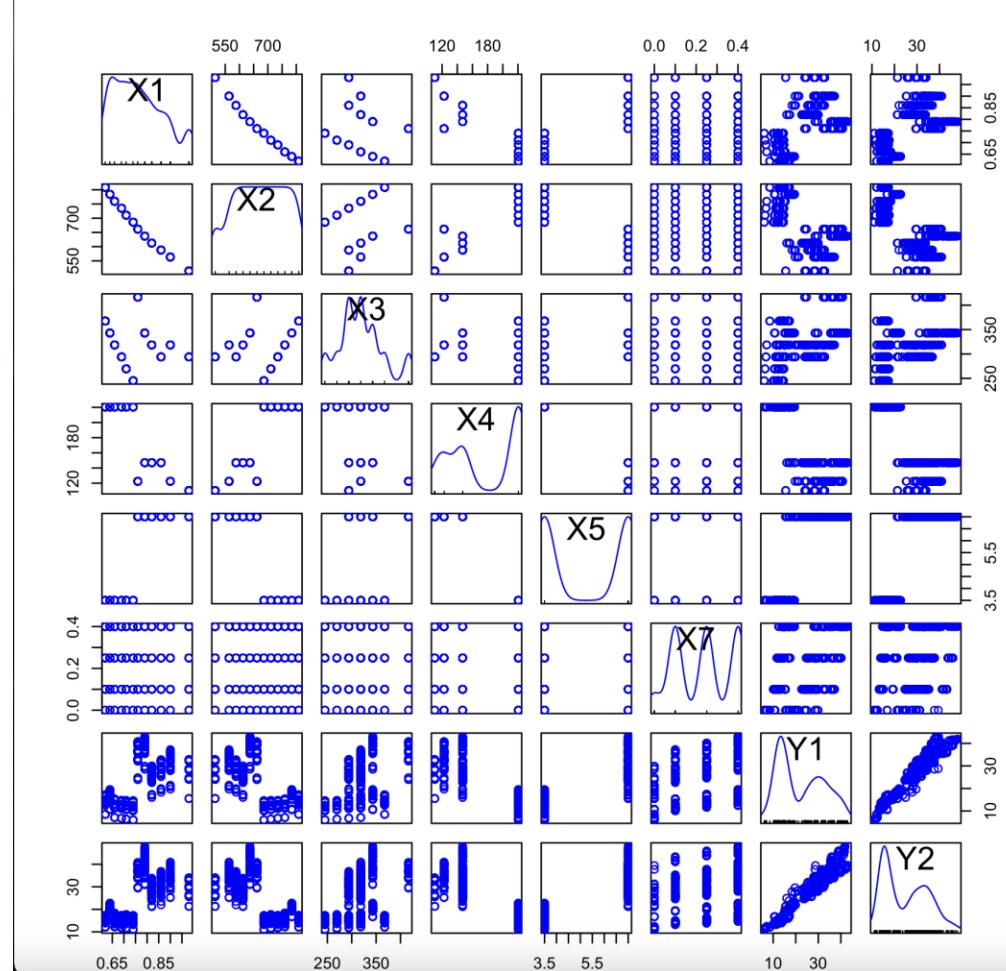


We observe an upward trend



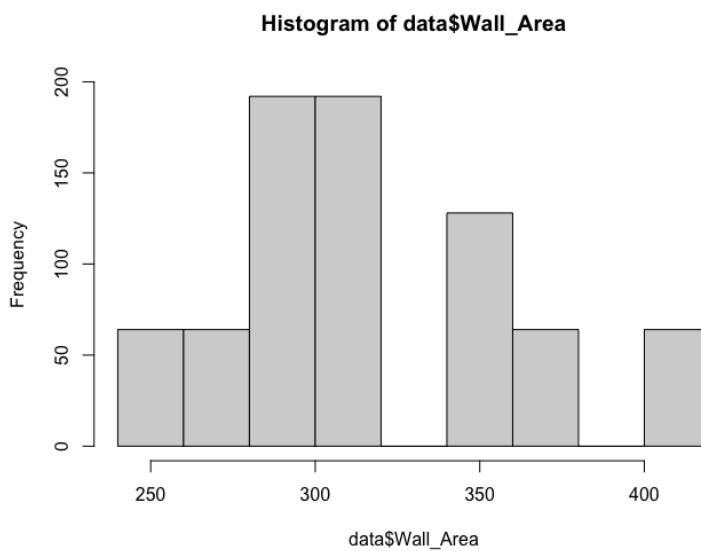
Change in y does not affect x for each of the variable

Scatter Plot Matrix

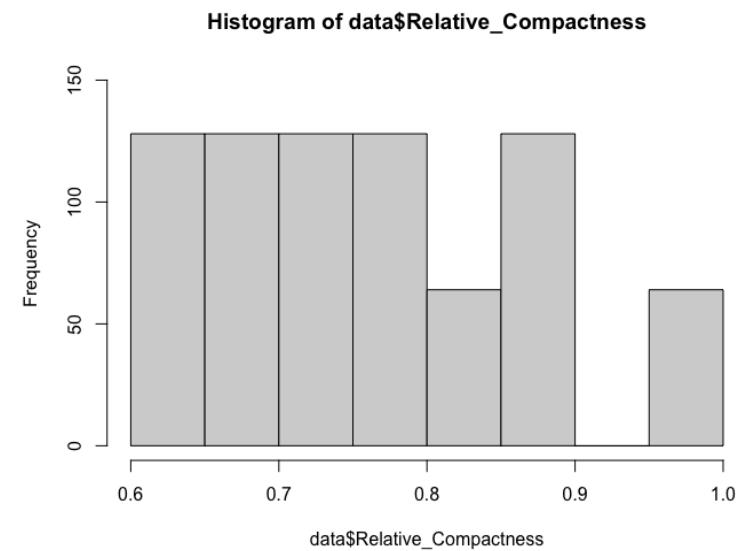


Scatter Plot matrix
for variables
x1,x2,x3,x4,x5,x7,x8
and y1 and y2

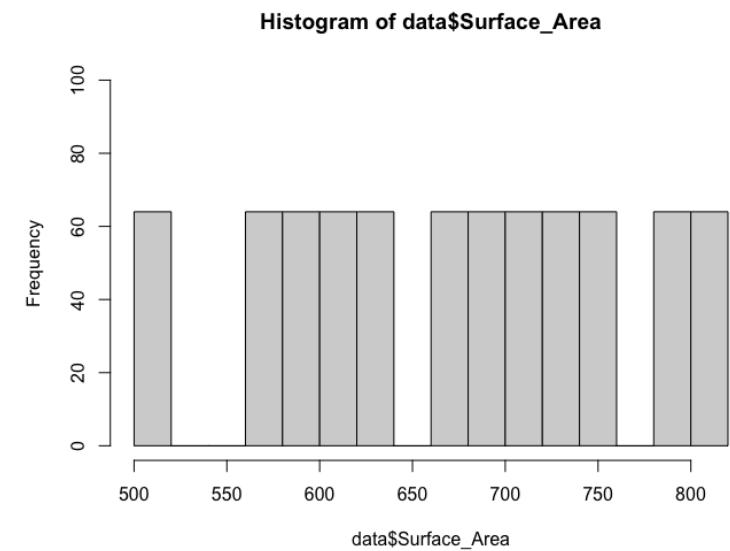
Histograms



Majority of the values are concentrated around 300-350 freq units

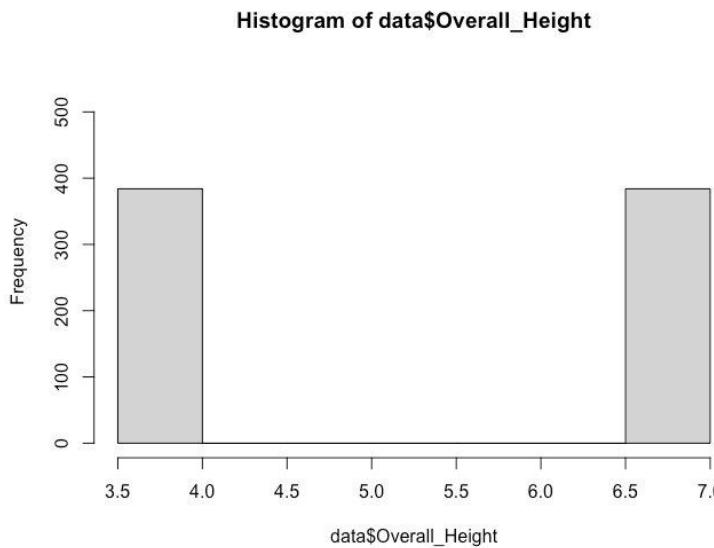


Most values are at 125 freq units

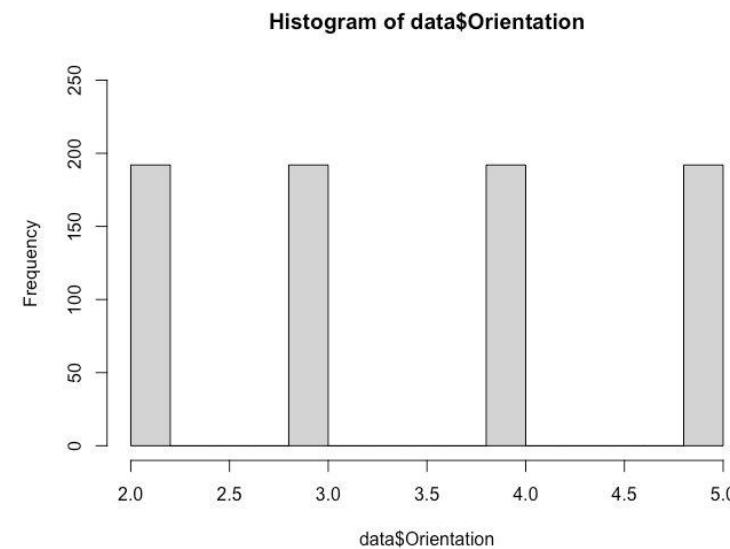


All values are slightly above 60 freq units

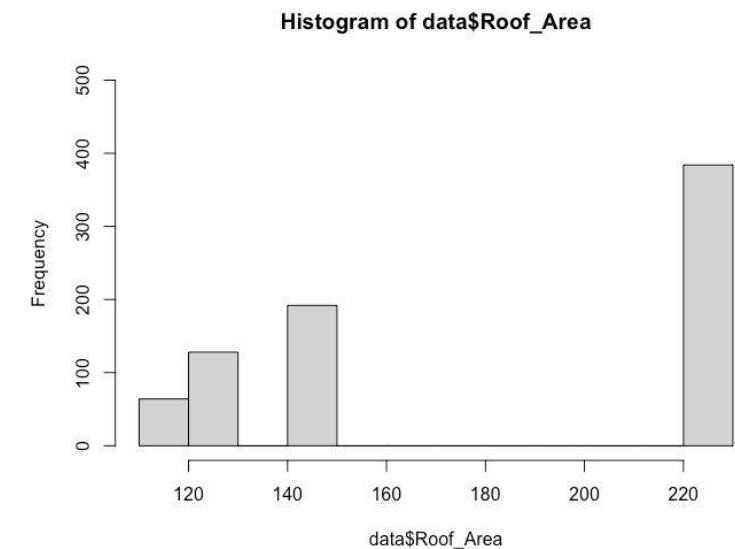
Histograms



Both values are at around
400 freq units



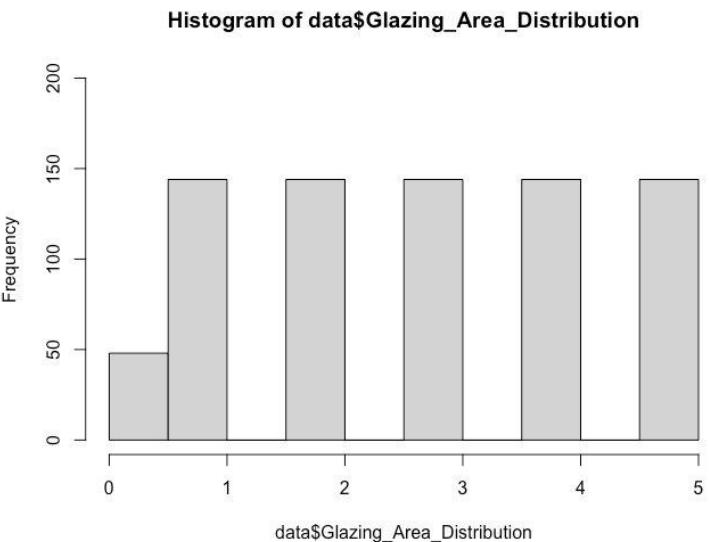
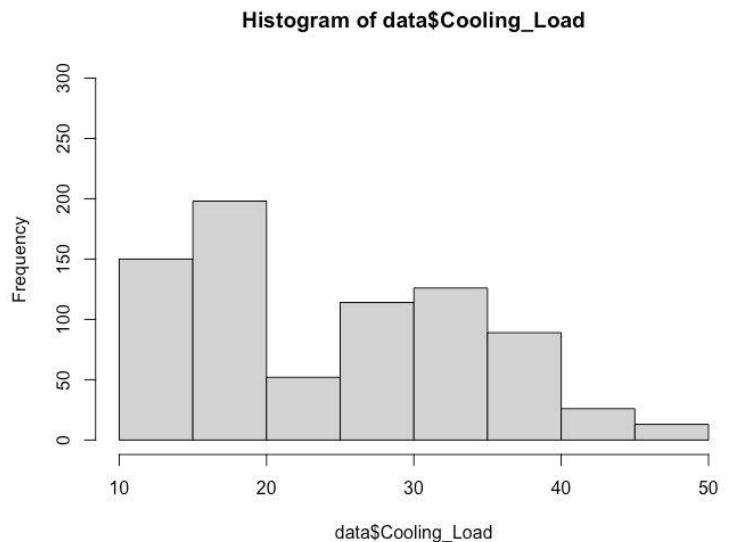
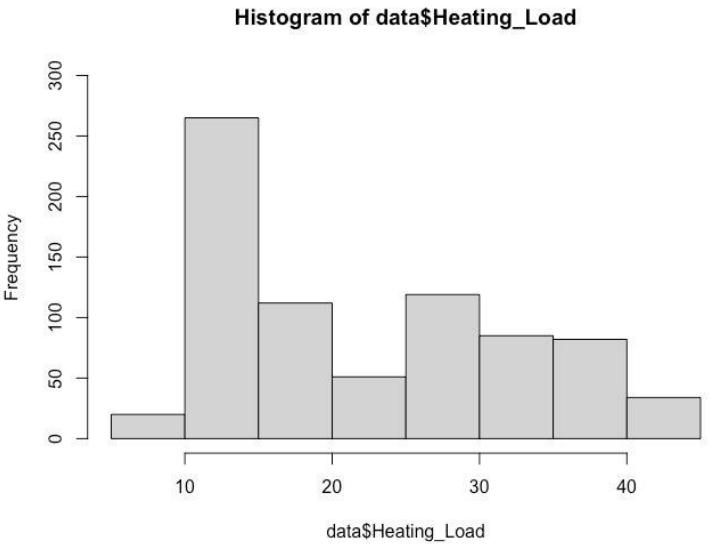
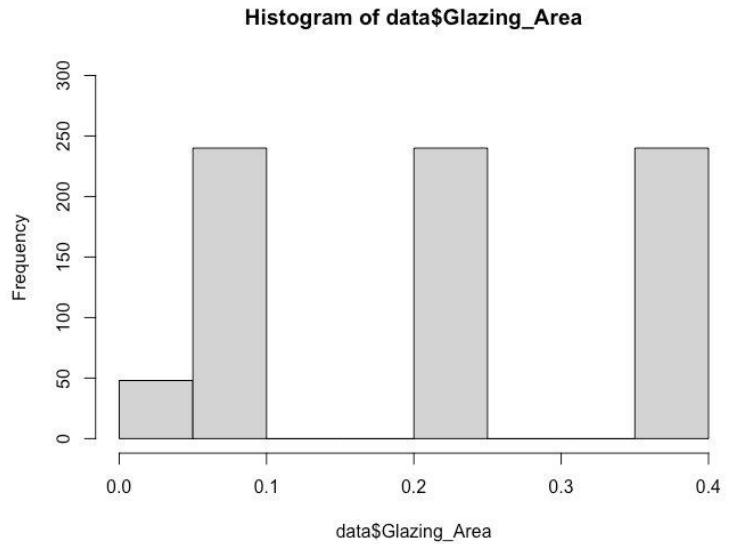
All values are around 400
freq units

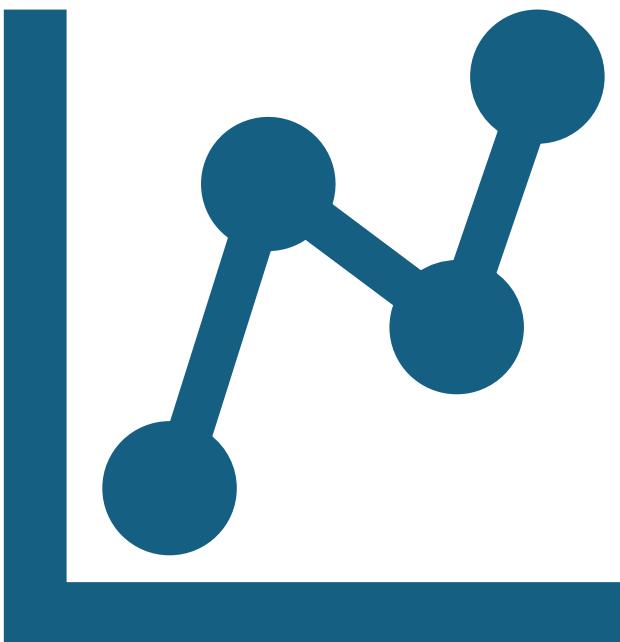


The freq increases
gradually



Histograms





2. Statistical Analysis

Descriptive Statistics

- Let's interpret some of the key variables:
- **Relative Compactness:** Ranges from **0.62 to 0.98**, with a mean of approximately **0.76**.
 - Indicates variability in building compactness.
- **Surface Area:** Varies from **514.5 to 808.5** with a mean of approximately **671.7**
 - Highlights diverse building sizes.
- **Cooling Load:** The dependent variable of interest, ranging from **10.90 to 48.03** with a mean of about **24.59**
 - Reflects variability in energy requirements for heating across buildings.

```
> library(readxl)
> EnergyEfficiencyfinal <- read_excel("Desktop/Humana /EnergyEfficiencyfinal.xlsx")
> View(EnergyEfficiencyfinal)
> summary(EnergyEfficiencyfinal)

Relative_Compactness    Surface_Area      Wall_Area      Roof_Area      Overall_Height   Orientation
Min.   :0.6200          Min.   :514.5        Min.   :245.0      Min.   :110.2       Min.   :3.50        Min.   :2.00
1st Qu.:0.6825          1st Qu.:606.4        1st Qu.:294.0      1st Qu.:140.9       1st Qu.:3.50        1st Qu.:2.75
Median :0.7500          Median :673.8        Median :318.5      Median :183.8       Median :5.25        Median :3.50
Mean   :0.7642          Mean   :671.7        Mean   :318.5      Mean   :176.6       Mean   :5.25        Mean   :3.50
3rd Qu.:0.8300          3rd Qu.:741.1        3rd Qu.:343.0      3rd Qu.:220.5       3rd Qu.:7.00        3rd Qu.:4.25
Max.   :0.9800          Max.   :808.5        Max.   :416.5      Max.   :220.5       Max.   :7.00        Max.   :5.00

North_Or     East_Or      South_Or      Glazing_Area    Glazing_Area_Distribution
Min.   :0.00          Min.   :0.00        Min.   :0.0000    Min.   :0.0000        Min.   :0.0000
1st Qu.:0.00          1st Qu.:0.00        1st Qu.:0.0000    1st Qu.:0.1000        1st Qu.:1.750
Median :0.00          Median :0.00        Median :0.0000    Median :0.2500        Median :3.000
Mean   :0.25          Mean   :0.25        Mean   :0.2500    Mean   :0.2344        Mean   :2.812
3rd Qu.:0.25          3rd Qu.:0.25        3rd Qu.:0.2500    3rd Qu.:0.4000        3rd Qu.:4.000
Max.   :1.00          Max.   :1.00        Max.   :1.0000    Max.   :0.4000        Max.   :5.000

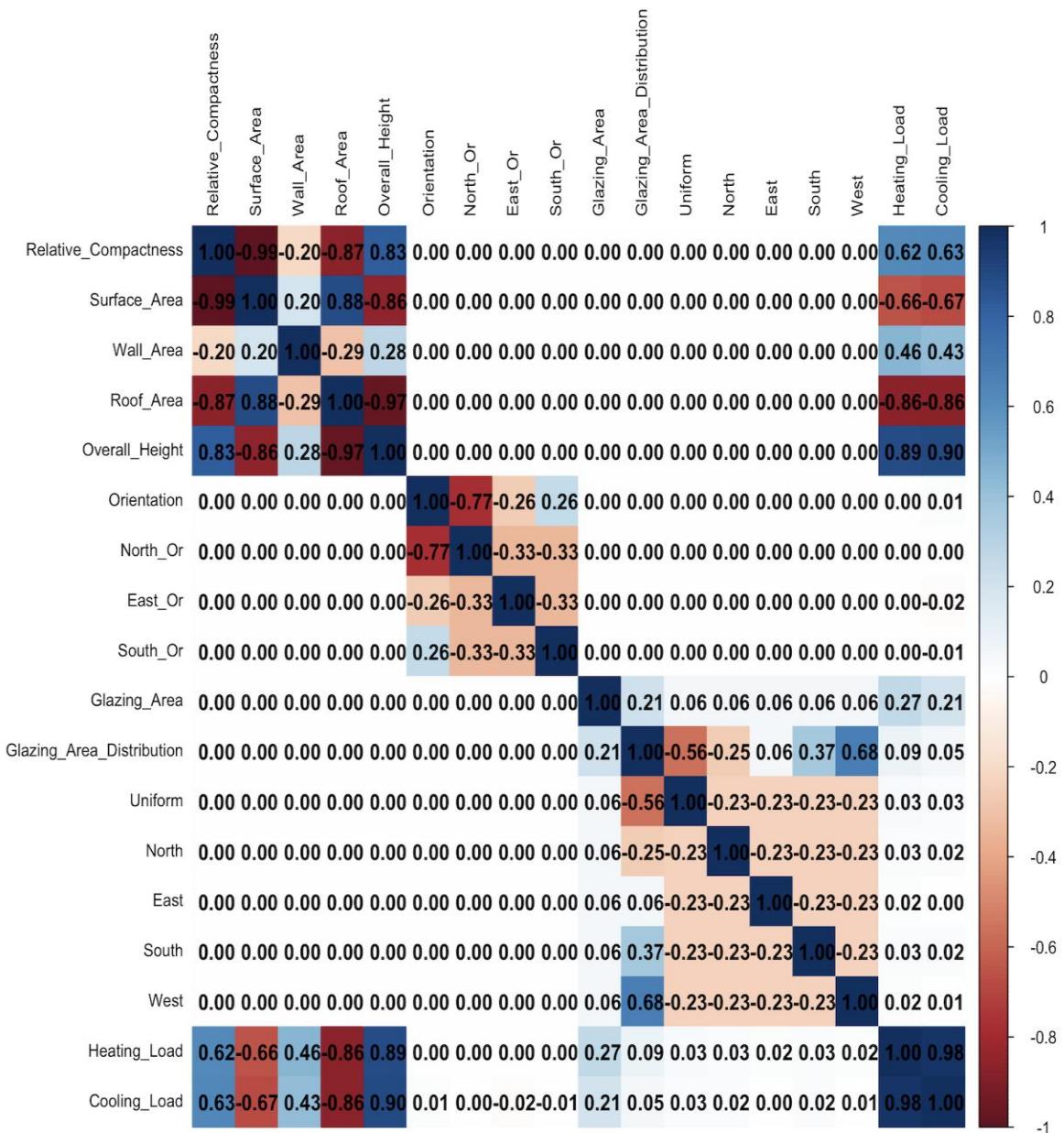
Uniform      North        East         South        West        Heating_Load
Min.   :0.0000    Min.   :0.0000    Min.   :0.0000    Min.   :0.0000    Min.   :0.0000    Min.   : 6.01
1st Qu.:0.0000  1st Qu.:0.0000  1st Qu.:0.0000  1st Qu.:0.0000  1st Qu.:0.0000  1st Qu.:12.99
Median :0.0000  Median :0.0000  Median :0.0000  Median :0.0000  Median :0.0000  Median :18.95
Mean   :0.1875  Mean   :0.1875  Mean   :0.1875  Mean   :0.1875  Mean   :0.1875  Mean   :22.31
3rd Qu.:0.0000  3rd Qu.:0.0000  3rd Qu.:0.0000  3rd Qu.:0.0000  3rd Qu.:0.0000  3rd Qu.:31.67
Max.   :1.0000  Max.   :1.0000  Max.   :1.0000  Max.   :1.0000  Max.   :1.0000  Max.   :43.10

Cooling_Load
Min.   :10.90
1st Qu.:15.62
Median :22.08
Mean   :24.59
3rd Qu.:33.13
Max.   :48.03
>
```



2(b) Correlation

Correlation Heatmap



- Relative_Compactness and Surface_Area:**
 - Strong negative correlation** (-0.99): As the relative compactness of a building increases, its surface area decreases, and vice versa.
- Overall_Height and Roof_Area:**
 - Very strong negative correlation** (-0.97): Taller buildings generally have less roof area.
- Heating_Load:**
 - Strong positive correlation** with Relative_Compactness (0.62): Buildings with higher relative compactness are associated with higher heating loads.
 - Very Strong positive correlation** with Overall_Height (0.89): Taller buildings tend to have higher heating loads.
 - Strong negative correlation** with Surface_Area (-0.66): Buildings with larger surface areas tend to have lower heating loads.
- Cooling_Load:**
 - Strong positive correlation** with Relative_Compactness (0.63): More compact buildings are linked to higher cooling loads.
 - Moderate positive correlation** with Wall_Area (0.43): A larger wall area contributes to higher cooling loads.
 - Very strong positive correlation** with Overall_Height (0.90): Taller buildings have significantly higher cooling loads.
 - Strong negative correlation** with Surface_Area (-0.67): Larger surface areas correspond to lower cooling loads.

Linear Regression

Heating_Load

- **R-Squared: 0.9228**
- Indicates that approximately **92.28%** of the variance in the Heating load can be explained by the model's predictors.

Positive Correlation

- East, North, South , West
- Glazing Area
- Overall Height
- Uniform

As these variables increases, heating load also increases.

Example: Larger glazing areas lead to higher heating loads.

Negative Correlation

- Relative Compactness
- Roof Area
- Surface Area

As the variable increases, heating load decreases.

Example: Higher relative compactness reduces the heating load due to better energy efficiency.

```
> summary(RegModel.2)
```

Call:

```
lm(formula = Heating_Load ~ East + East_Or + Glazing_Area + North +  
North_Or + Overall_Height + Relative_Compactness + Roof_Area +  
South + South_Or + Surface_Area + Uniform + Wall_Area + West,  
data = EnergyEfficiencyfinal)
```

Residuals:

Min	1Q	Median	3Q	Max
-7.1237	-1.4299	-0.2555	1.2972	7.4342

Coefficients: (1 not defined because of singularities) **Significant Predictors:**

	Estimate	Std. Error	t value	Pr(> t)
(Intercept)	81.12397	18.18928	4.460	9.44e-06 ***
East	4.18300	0.51372	8.143	1.60e-15 ***
East_Or	0.10531	0.28618	0.368	0.7130
Glazing_Area	16.84833	0.85324	19.746	< 2e-16 ***
North	4.43599	0.51372	8.635	< 2e-16 ***
North_Or	0.03750	0.28618	0.131	0.8958
Overall_Height	4.16995	0.32298	12.911	< 2e-16 ***
Relative_Compactness	-64.77343	9.83256	-6.588	8.38e-11 ***
Roof_Area	-0.12163	0.01271	-9.573	< 2e-16 ***
South	4.38821	0.51372	8.542	< 2e-16 ***
South_Or	-0.01549	0.28618	-0.054	0.9569
Surface_Area	-0.02648	0.01221	-2.169	0.0304 *
Uniform	4.52765	0.51372	8.814	< 2e-16 ***
Wall_Area	NA	NA	NA	NA
West	4.18244	0.51372	8.142	1.61e-15 ***

Signif. codes: 0 ‘***’ 0.001 ‘**’ 0.01 ‘*’ 0.05 ‘.’ 0.1 ‘ ’ 1

Residual standard error: 2.804 on 754 degrees of freedom

Multiple R-squared: 0.9241, Adjusted R-squared: 0.9228

F-statistic: 706 on 13 and 754 DF, p-value: < 2.2e-16

Linear Regression

Cooling_Load

- **R-Squared: 0.8885** Indicates that approximately **88.85%** of the variance in the cooling load can be explained by the model's predictors.

Positive Correlation

- East, North, South , West
- Glazing Area
- Overall Height
- Uniform

As the variable increases, cooling load also increases.

Example: Larger glazing areas lead to higher cooling loads.

Negative Correlation

- Relative Compactness
- East_Or
- Roof Area
- Surface Area

As the variable increases, cooling load decreases.

Example: Higher relative compactness reduces the cooling load due to better energy efficiency.

```
> summary(RegModel.3)
```

Call:

```
lm(formula = Cooling_Load ~ East + East_Or + Glazing_Area + North +  
    North_Or + Overall_Height + Relative_Compactness + Roof_Area +  
    South + South_Or + Surface_Area + Uniform + Wall_Area + West,  
    data = EnergyEfficiencyfinal)
```

Residuals:

Min	1Q	Median	3Q	Max
-7.7082	-1.6996	-0.2814	1.4302	11.0365

Coefficients: (1 not defined because of singularities) Significant Predictors:

	Estimate	Std. Error	t value	Pr(> t)
(Intercept)	96.71918	20.60428	4.694	3.18e-06 ***
East	1.63997	0.58192	2.818	0.004956 **
East_Or	-0.64109	0.32418	-1.978	0.048340 *
Glazing_Area	13.25292	0.96652	13.712	< 2e-16 ***
North	1.97740	0.58192	3.398	0.000714 ***
North_Or	-0.34911	0.32418	-1.077	0.281865
Overall_Height	4.28384	0.36586	11.709	< 2e-16 ***
Relative_Compactness	-70.78771	11.13804	-6.355	3.59e-10 ***
Roof_Area	-0.08936	0.01439	-6.209	8.80e-10 ***
South	1.99566	0.58192	3.429	0.000638 ***
South_Or	-0.47333	0.32418	-1.460	0.144683
Surface_Area	-0.04356	0.01383	-3.151	0.001694 **
Uniform	2.16003	0.58192	3.712	0.000221 ***
Wall_Area		NA	NA	NA
West	1.69552	0.58192	2.914	0.003678 **

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 3.176 on 754 degrees of freedom

Multiple R-squared: 0.8904, Adjusted R-squared: 0.8885

F-statistic: 471.3 on 13 and 754 DF, p-value: < 2.2e-16

VIF Analysis

➤ High Multicollinearity:

- **Roof Area:** VIF = **32.12**.
- **Overall Height:** VIF = **31.20**.
- **Surface Area:** VIF = **112.77**.
- **Relative Compactness:** VIF = **105.5**.
- all have VIF values above **10** Indicates strong multicollinearity, requiring attention during model adjustment.

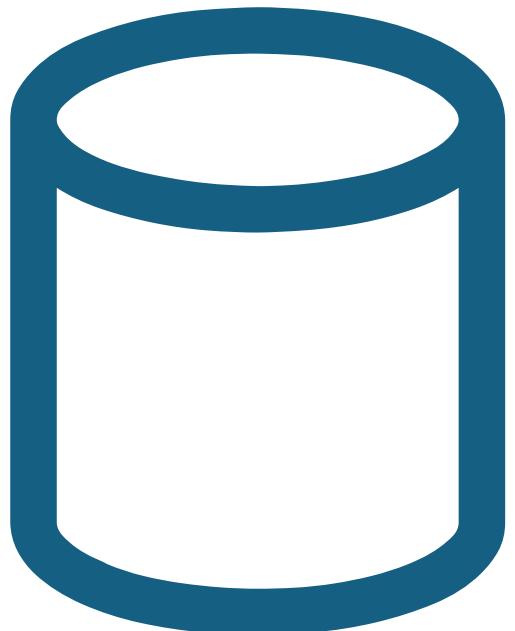
➤ Low Multicollinearity:

- Directional variables (**East**, **South**, **West**, and **North**) and **Glazing Area** all have VIF values below **5**, indicating minimal concern for multicollinearity.

```
> library(car)
> vif_values <- vif(RegModel.2_updated)
> print(vif_values)
```

	East	Glazing_Area	North	Overall_Height
Relative_Compactness	1.456897	1.043103	1.456897	31.205474
	105.524054	Roof_Area	South	Surface_Area
		32.124528	1.456897	112.774196
	West			
	1.456897			

```
>
>
```



3. Modeling Analysis

Assign categories for each Y-variable

A for highest quartile, B for second highest quartile, C for third highest quartile, D for lowest quartile

Assigning Categories for Heating Load

```
> data$HeatingLoadCategory <- cut(  
+   data$Y1,  
+   breaks = quantile(data$Y1, probs = seq(0, 1, 0.25), na.rm = TRUE),  
+   labels = c("D", "C", "B", "A"),  
+   include.lowest = TRUE  
)  
>
```

Assigning Categories for Cooling Load

```
> data$CoolingLoadCategory <- cut(  
+   data$Y2,  
+   breaks = quantile(data$Y2, probs = seq(0, 1, 0.25), na.rm = TRUE),  
+   labels = c("D", "C", "B", "A"),  
+   include.lowest = TRUE  
)  
>
```

Perceptrons

```
# Define the perceptron algorithm
perceptron <- function(X, y, numEpochs) {
  w <- runif(ncol(X), -10, 10) # Initialize weights
  for (epoch in 1:numEpochs) {
    for (i in 1:length(y)) {
      xi <- as.numeric(unlist(X[i, ]))
      if (sign(w %*% xi) != y[i]) {
        w <- w + y[i] * xi
      }
    }
  }
  return(w)
}

# Run the process 5 times for both heating and cooling
set.seed(42) # For reproducibility
numRuns <- 5
numEpochs <- 10
heating_accuracies <- numeric(numRuns)
cooling_accuracies <- numeric(numRuns)

for (run in 1:numRuns) {
  # Split data into training (70%) and testing (30%)
  train_indices <- sample(nrow(data), 0.7 * nrow(data))
  train_data <- data[train_indices, ]
  test_data <- data[-train_indices, ]

  # For Heating
  X_heating <- train_data[, c("Relative_Compactness", "Surface_Area", "Wall_Area",
                               "Roof_Area", "Overall_Height", "North_Or", "East_Or",
                               "South_Or", "Glazing_Area", "Uniform", "North",
                               "East", "South", "West")]
  y_heating <- train_data$Heating_Class

  w_heating <- perceptron(X_heating, y_heating, numEpochs)

  X_heating_test <- test_data[, c("Relative_Compactness", "Surface_Area", "Wall_Area",
                                   "Roof_Area", "Overall_Height", "North_Or", "East_Or",
                                   "South_Or", "Glazing_Area", "Uniform", "North",
                                   "East", "South", "West")]
  y_heating_test <- test_data$Heating_Class
  y_heating_pred <- sign(as.matrix(X_heating_test) %*% w_heating)

  heating_accuracies[run] <- mean(y_heating_pred == y_heating_test)

  # For Cooling
  X_cooling <- train_data[, c("Relative_Compactness", "Surface_Area", "Wall_Area",
                               "Roof_Area", "Overall_Height", "North_Or", "East_Or",
                               "South_Or", "Glazing_Area", "Uniform", "North",
                               "East", "South", "West")]
  y_cooling <- train_data$Cooling_Class

  w_cooling <- perceptron(X_cooling, y_cooling, numEpochs)

  X_cooling_test <- test_data[, c("Relative_Compactness", "Surface_Area", "Wall_Area",
                                   "Roof_Area", "Overall_Height", "North_Or", "East_Or",
                                   "South_Or", "Glazing_Area", "Uniform", "North",
                                   "East", "South", "West")]
  y_cooling_test <- test_data$Cooling_Class
  y_cooling_pred <- sign(as.matrix(X_cooling_test) %*% w_cooling)

  cooling_accuracies[run] <- mean(y_cooling_pred == y_cooling_test)
}

# Print accuracies
cat("Heating Accuracies over 5 runs:\n", heating_accuracies, "\n")
cat("Cooling Accuracies over 5 runs:\n", cooling_accuracies, "\n")
```

```

+ }

>
> # Print accuracies
> cat("Heating Accuracies over 5 runs:\n", heating_accuracies, "\n")
Heating Accuracies over 5 runs:
0.978355 0.965368 0.969697 0.974026 0.982684
> cat("Cooling Accuracies over 5 runs:\n", cooling_accuracies, "\n")
Cooling Accuracies over 5 runs:
0.982684 0.974026 0.969697 0.982684 0.987013

```

Mode Type	Accuracy-Model 1	Accuracy-Model 2	Accuracy-Model 3	Accuracy-Model 4	Accuracy-Model 5	NIR	P-value
Heating Load	0.978355	0.965368	0.969697	0.974026	0.982684	0.5368	0.00
Cooling Load	0.982684	0.974026	0.969697	0.982684	0.987013	0.5368	0.00

Support Vector Machines

DV: Cooling

```
#Run the svm for Cooling_Class
Cooling_Class_datasvm <- svm(Cooling_Class ~ Relative_Compactness + Surface_Area + Wall_Area
+ Roof_Area + Overall_Height + North_Or + East_Or + South_Or +
Glazing_Area + Uniform + North + East + South + West,
data = data_train)

#Print Cooling_Class_datasvm
print(Cooling_Class_datasvm)

# Plot the SVM model for Cooling_Class
plot(Cooling_Class_datasvm,
      data_train,
      Surface_Area ~ Roof_Area,
      slice = list(Relative_Compactness = 0.8,
                  Wall_Area = 500,
                  Overall_Height = 2,
                  North_Or = 1,
                  East_Or = 0,
                  Glazing_Area = 0.03,
                  Uniform = 1,
                  North = 1,
                  East = 0,
                  South = 1,
                  West = 1
))

# Predict Cooling_Class on the test dataset
cooling_predictions <- predict(Cooling_Class_datasvm, newdata = data_test[,c("Relative_Compactness",
cooling_predictions
predicttable <- table(data_test$Cooling_Class == 'AB', cooling_predictions =='AB')
predicttable
sum(diag(predicttable))/sum(predicttable)
library(caret)
confusionMatrix(cooling_predictions,data_test$Cooling_Class)
```

Parameters:
SVM-Type: C-classification
SVM-Kernel: radial
cost: 1
Number of Support Vectors: 113

```
> predicttable <- table(data_test$Cooling_Class == 'AB', cooling_predictions =='AB')
> predicttable
   FALSE TRUE
FALSE 104   4
TRUE    5 118
> sum(diag(predicttable))/sum(predicttable)
[1] 0.961039
> library(caret)
> confusionMatrix(cooling_predictions,data_test$Cooling_Class)
Confusion Matrix and Statistics

Reference
Prediction CD AB
      CD 104   5
      AB   4 118

Accuracy : 0.961
95% CI : (0.9273, 0.982)
No Information Rate : 0.5325
P-Value [Acc > NIR] : <2e-16

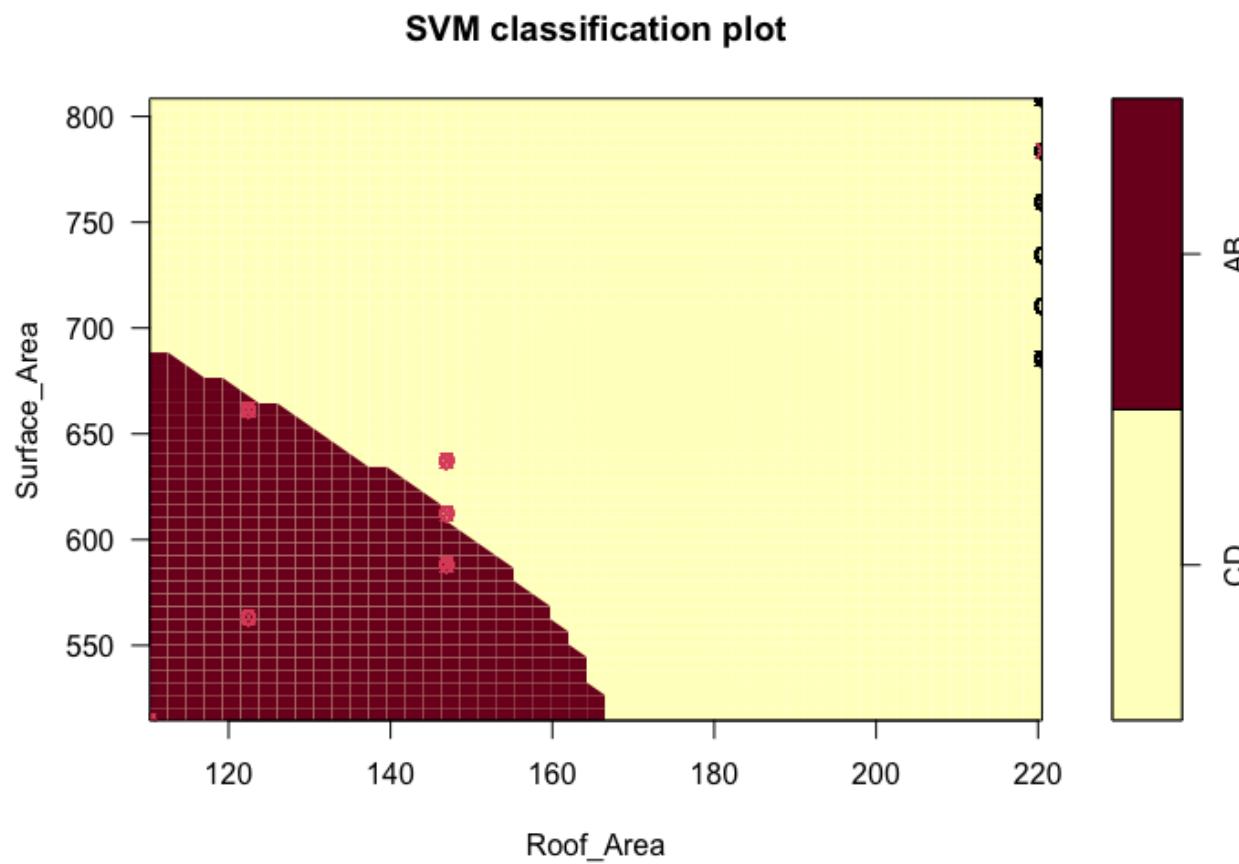
Kappa : 0.9218

McNemar's Test P-Value : 1

Sensitivity : 0.9630
Specificity : 0.9593
Pos Pred Value : 0.9541
Neg Pred Value : 0.9672
Prevalence : 0.4675
Detection Rate : 0.4502
Detection Prevalence : 0.4719
Balanced Accuracy : 0.9612

'Positive' Class : CD
```

DV: Cooling



DV: Heating

```
#Run the svm for Heating_Class
Heating_Class_datasvm <- svm(Heating_Class ~ Relative_Compactness + Surface_Area + Wall_Area +
  Roof_Area + Overall_Height + North_Or + East_Or + South_Or +
  Glazing_Area + Uniform + North + East + South + West,
  data = data_train)

#Print Heating_Class_datasvm
print(Heating_Class_datasvm)

# plot heating svm
plot(Heating_Class_datasvm,
  data_train,
  Surface_Area ~ Roof_Area,
  slice = list(Relative_Compactness = 1,
    Wall_Area = 400,
    Overall_Height = 2,
    North_Or = 1,
    East_Or = 0,
    South_Or = 1,
    Glazing_Area = 0.00,
    Uniform = 1,
    North = 1,
    East = 0,
    South = 0,
    West = 0
  ))
  # Predict Cooling_Class on the test dataset
heating_predictions <- predict(Heating_Class_datasvm, newdata = data_test[,c("Relative_Compactness",
heating_predictions
predicttable2 <- table(data_test$Heating_Class == 'AB', heating_predictions =='AB')
predicttable2
sum(diag(predicttable2))/sum(predicttable2)
library(caret)
confusionMatrix(heating_predictions,data_test$Heating_Class)
```

Parameters:
SVM-Type: C-classification
SVM-Kernel: radial
cost: 1

Number of Support Vectors: 127

```
> predicttable2 <- table(data_test$Heating_Class == 'AB', heating_predictions =='AB')
> predicttable2
  FALSE TRUE
FALSE 104 4
TRUE 5 118
> sum(diag(predicttable2))/sum(predicttable2)
[1] 0.961039
> library(caret)
> confusionMatrix(heating_predictions,data_test$Heating_Class)
Confusion Matrix and Statistics

Reference
Prediction CD AB
  CD 104 5
  AB 4 118

Accuracy : 0.961
95% CI : (0.9273, 0.982)
No Information Rate : 0.5325
P-Value [Acc > NIR] : <2e-16

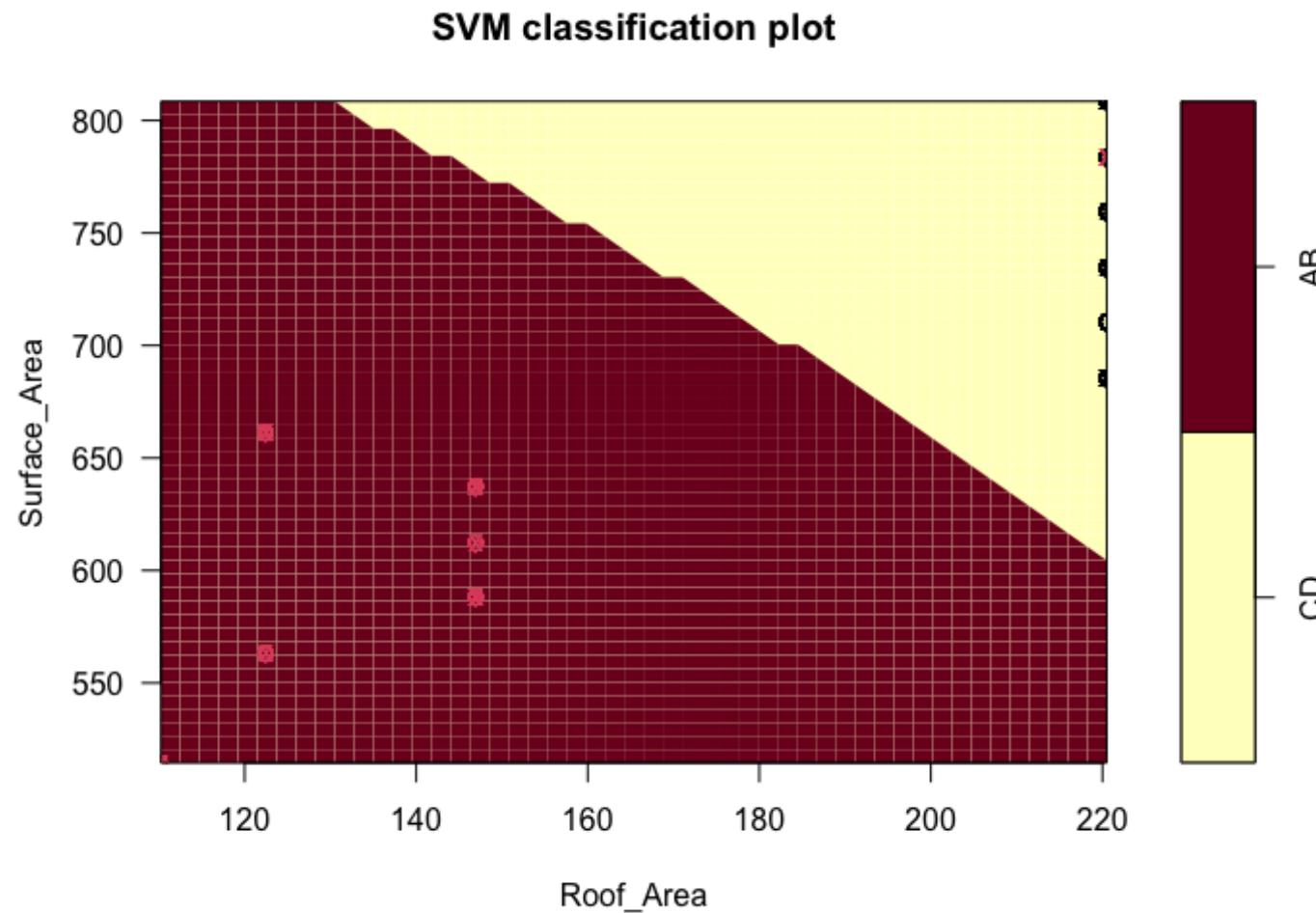
Kappa : 0.9218

McNemar's Test P-Value : 1

Sensitivity : 0.9630
Specificity : 0.9593
Pos Pred Value : 0.9541
Neg Pred Value : 0.9672
Prevalence : 0.4675
Detection Rate : 0.4502
Detection Prevalence : 0.4719
Balanced Accuracy : 0.9612

'Positive' Class : CD
```

DV: Heating



Neural Networks

Using a loop for 1 to 5 hidden nodes, create a neural network for each Y-variable cooling load and heating load) (use actual numeric values for loads, continuous output neural network). Report the accuracies for all ten (10) models (5 cooling and 5 heating)

```
install.packages("neuralnet", dependencies = TRUE)

# Load necessary libraries
library(neuralnet)
library(readxl)

data <- read_excel("/Users/bhvvnnaa/Downloads/EnergyEfficiency_final (1).xlsx")

cooling_net <- neuralnet(Cooling_Load ~ Relative_Compactness + Surface_Area + Wall_Area + Roof_Area +
                           Overall_Height + North_Or + East_Or + South_Or + Glazing_Area + Uniform + North + East + South + West, data, hidden=5,
                           lifesign="minimal", linear.output=TRUE, threshold=0.01)

normalize <- function(x) {return((x-min(x))/(max(x)-min(x)))}
denormalize <- function(y,x){return(y*(max(x)-min(x))+min(x))}

cooling_norm <- as.data.frame(lapply(data,normalize))

set.seed(123) # For reproducibility
data_index <- sample(nrow(cooling_norm), 0.7 * nrow(cooling_norm), replace = FALSE)
cooling_train <- cooling_norm[data_index, ]
cooling_test <- cooling_norm[-data_index, ]

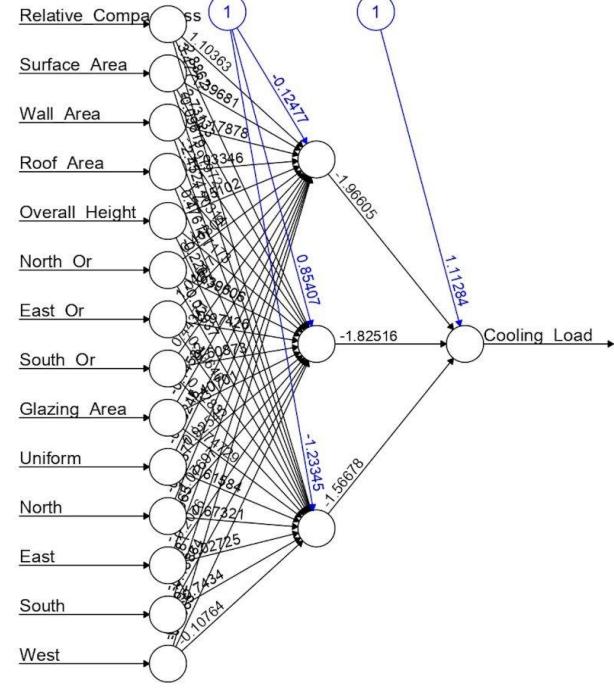
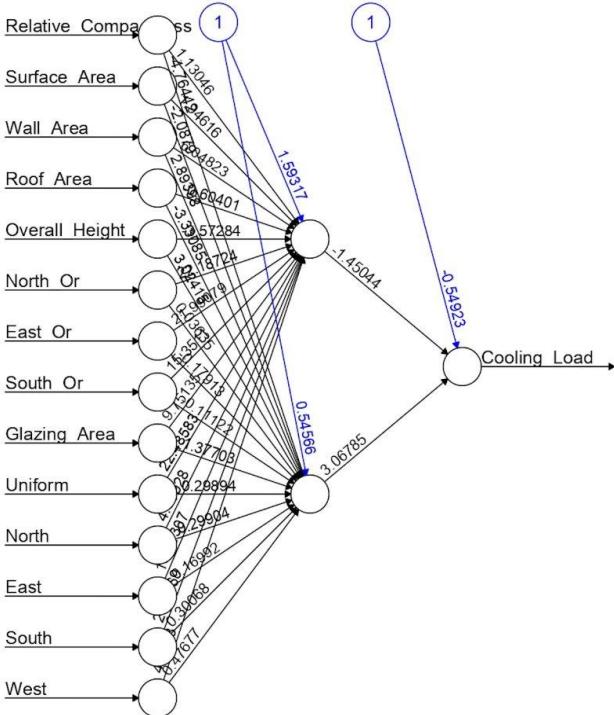
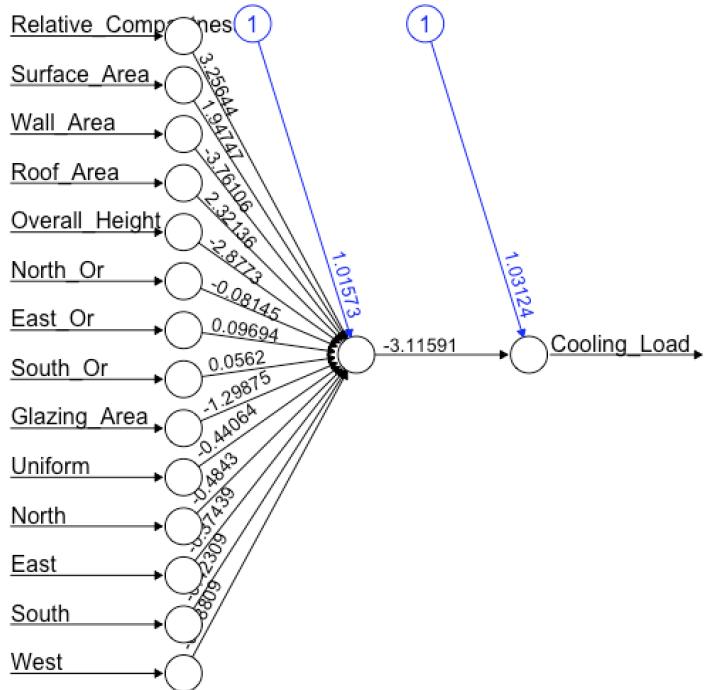
head(data)
head(cooling_norm)
```

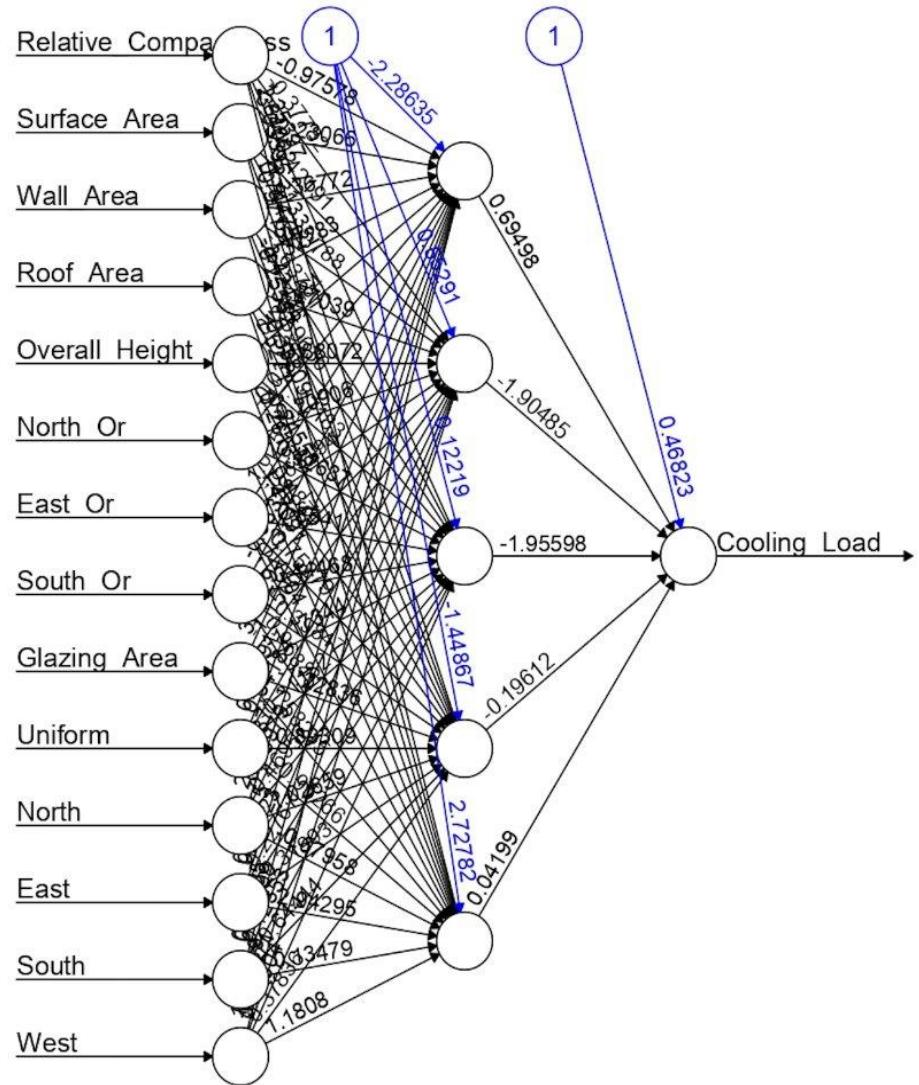
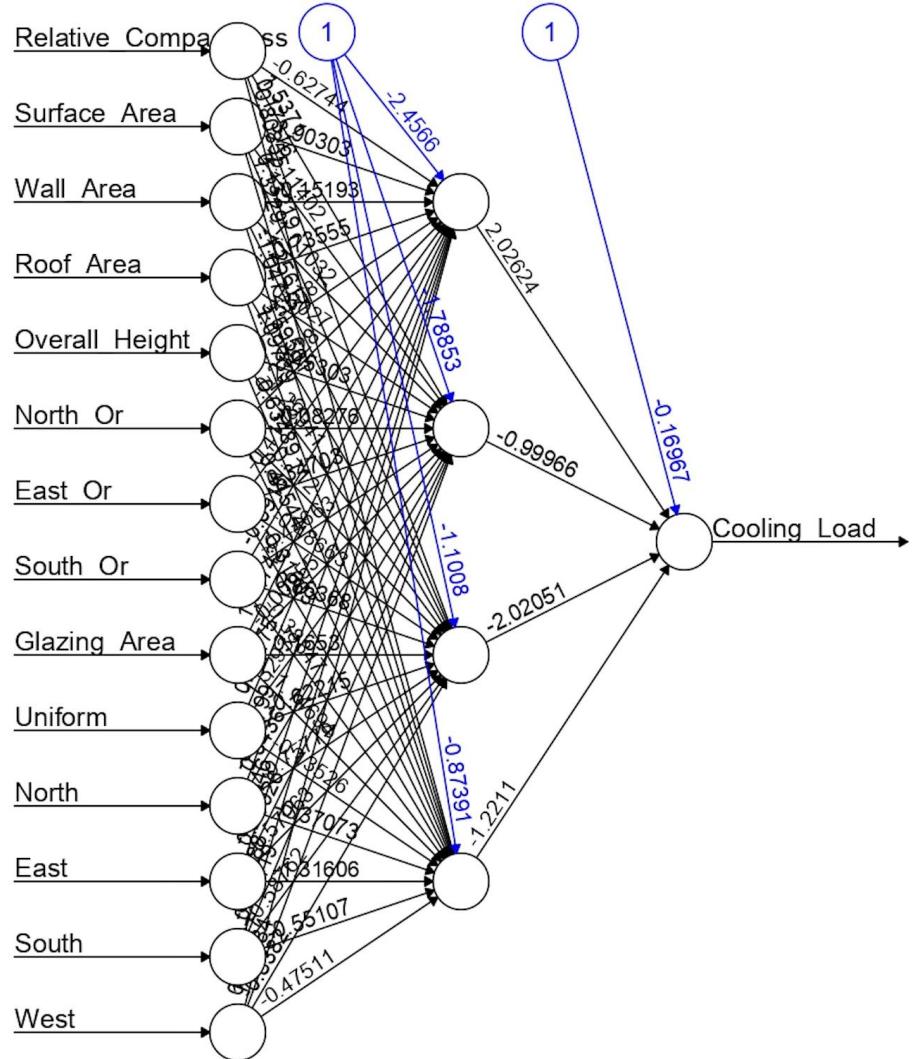
	Relative_Compactness	Surface_Area	Wall_Area	Roof_Area	Overall_Height	Orientation	North_Or	East_Or	South_Or	Glazing_Area	Glazing_Area_Distribution	Uniform	North
1	1.0000000	0.0000000	0.2857143	0.0000000	1	0.0000000	1	0	0	0	0	0	0
2	1.0000000	0.0000000	0.2857143	0.0000000	1	0.3333333	0	1	0	0	0	0	0
3	1.0000000	0.0000000	0.2857143	0.0000000	1	0.6666667	0	0	1	0	0	0	0
4	1.0000000	0.0000000	0.2857143	0.0000000	1	1.0000000	0	0	0	0	0	0	0
5	0.7777778	0.1666667	0.4285714	0.1111111	1	0.0000000	1	0	0	0	0	0	0
6	0.7777778	0.1666667	0.4285714	0.1111111	1	0.3333333	0	1	0	0	0	0	0
	East	South	West	Heating_Load	Cooling_Load								
1	0	0	0	0.2572122	0.2809049								
2	0	0	0	0.2572122	0.2809049								
3	0	0	0	0.2572122	0.2809049								
4	0	0	0	0.2572122	0.2809049								
5	0	0	0	0.3998382	0.4680851								
6	0	0	0	0.4165543	0.3899811								

DV: Cooling

```
corr_max_list <- list()
# Loop through 1 to 5 hidden nodes
for (hidden_nodes in 1:5){
  # Cooling_Load Model
  cooling_model <- neuralnet(Cooling_Load ~ Relative_Compactness + Surface_Area + Wall_Area + Roof_Area +
                                Overall_Height + North_Or + East_Or + South_Or + Glazing_Area + Uniform + North + East + South + West,
                                data = cooling_train, hidden = hidden_nodes, lifesign = "minimal", linear.output = FALSE, threshold = 0.1, stepmax = 1e7)
  cooling_results <- compute(cooling_model, cooling_test[, c("Relative_Compactness", "Surface_Area", "Wall_Area", "Roof_Area",
                                                               "Overall_Height", "North_Or", "East_Or", "South_Or", "Glazing_Area", "Uniform", "North", "East", "South", "")]
  cooling_denorm <- denormalize(cooling_results$net.result,data$Cooling_Load[data_index])
  cooling_correlation <- cor(cooling_denorm, actualCooling)
  print(cooling_correlation)
  corr_max_list[paste(hidden_nodes)] <- cooling_correlation
  plot(cooling_model)
}
corr_max_list[which.max(sapply(corr_max_list,max))]
```

```
hidden: 1 thresh: 0.1 rep: 1/1 steps: 159 error: 2.11538 time: 0.01 secs
[,1]
[1,] 0.9421985
hidden: 2 thresh: 0.1 rep: 1/1 steps: 70 error: 2.11147 time: 0.01 secs
[,1]
[1,] 0.942914
hidden: 3 thresh: 0.1 rep: 1/1 steps: 48 error: 1.9949 time: 0 secs
[,1]
[1,] 0.9470624
hidden: 4 thresh: 0.1 rep: 1/1 steps: 45 error: 1.97789 time: 0.03 secs
[,1]
[1,] 0.947677
hidden: 5 thresh: 0.1 rep: 1/1 steps: 72 error: 1.76572 time: 0.01 secs
[,1]
[1,] 0.9447179
> corr_max_list[which.max(sapply(corr_max_list,max))]
$`4`
[1] 0.947677
```





Method		Cooling			
		Accuracy	NIR	P-value	Significant?
Neural network	Hidden = 1	0.7662	0.2771	<2.2e-16	YES
	Hidden = 2	0.7576	0.2771	<2.2e-16	YES
	Hidden = 3	0.7403	0.2771	<2.2e-16	YES
	Hidden = 4	0.7403	0.2771	<2.2e-16	YES
	Hidden = 5	0.7835	0.2771	<2.2e-16	YES

```

heating_net <- neuralnet(Heating_Load ~ Relative_Compactness + Surface_Area + Wall_Area + Roof_Area +
                         Overall_Height + North_Or + East_Or + South_Or + Glazing_Area + Uniform + North + East + South + West, data, hidden=5,
                         lifesign="minimal", linear.output=TRUE, threshold=0.01)

normalize <- function(x) {return((x-min(x))/(max(x)-min(x)))}
denormalize <- function(y,x){return(y*(max(x)-min(x))+min(x))}

heating_norm <- as.data.frame(lapply(data,normalize))

set.seed(123) # For reproducibility
data_index <- sample(nrow(heating_norm), 0.7 * nrow(heating_norm), replace = FALSE)
heating_train <- heating_norm[data_index, ]
heating_test <- heating_norm[-data_index, ]

head(data)
head(heating_norm)
actualHeating <- data$Heating_Load[-data_index]

corr_max_list2 <- list()
# Loop through 1 to 5 hidden nodes
for (hidden_nodes in 1:5){
  # Cooling_Load Model
  heating_model <- neuralnet(Heating_Load ~ Relative_Compactness + Surface_Area + Wall_Area + Roof_Area +
                             Overall_Height + North_Or + East_Or + South_Or + Glazing_Area + Uniform + North + East + South + West,
                             data = heating_train, hidden = hidden_nodes, lifesign = "minimal", linear.output = FALSE, threshold = 0.1, stepmax = 1e7)
  heating_results <- compute(heating_model, heating_test[, c("Relative_Compactness", "Surface_Area", "Wall_Area", "Roof_Area",
                                                             "Overall_Height", "North_Or", "East_Or", "South_Or", "Glazing_Area", "Uniform", "North", "East", "South", "West")])
  heating_denorm <- denormalize(heating_results$net.result, data$Heating_Load[data_index])
  heating_correlation <- cor(heating_denorm, actualHeating)
  print(heating_correlation)
  corr_max_list2[paste(hidden_nodes)] <- heating_correlation
  plot(heating_model)
}

corr_max_list2[which.max(sapply(corr_max_list2,max))]

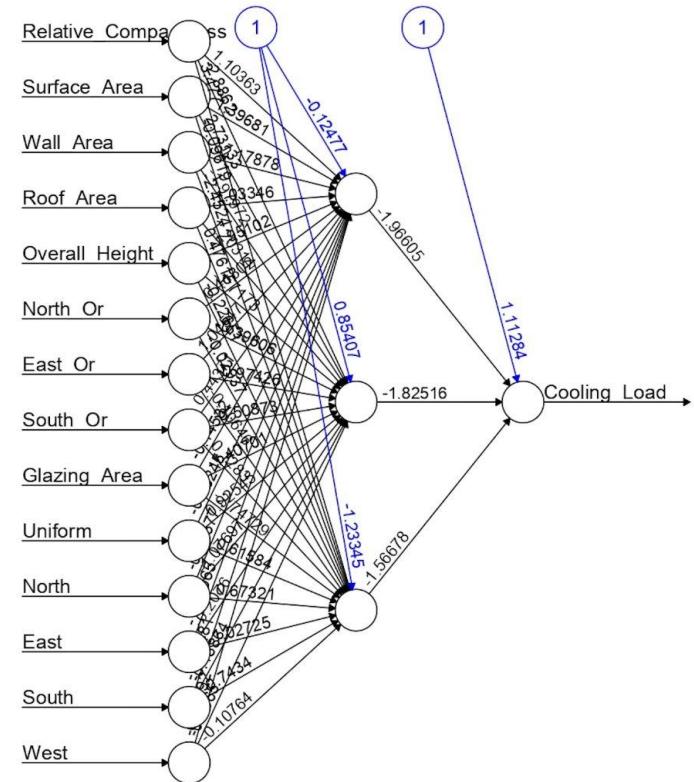
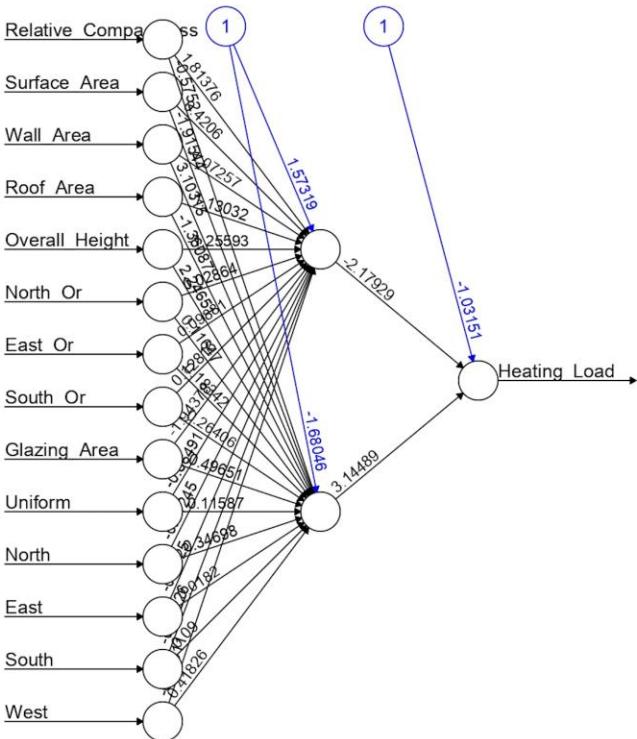
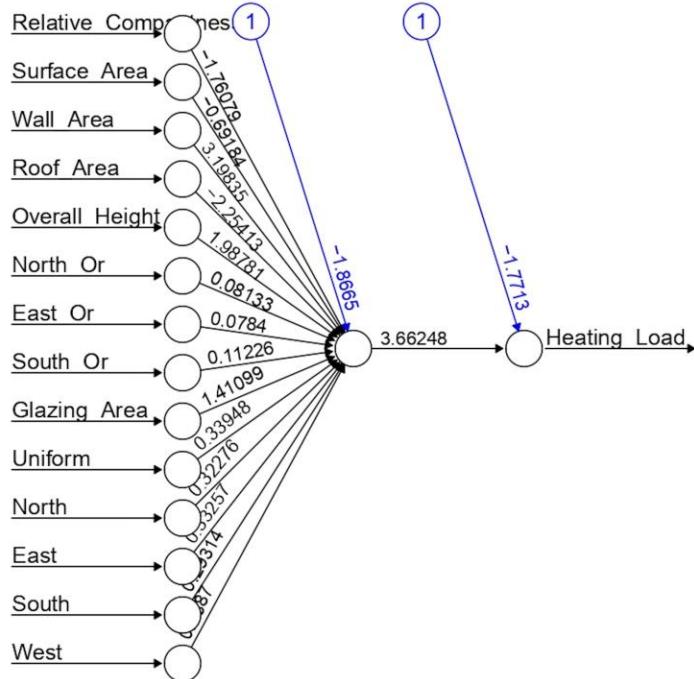
```

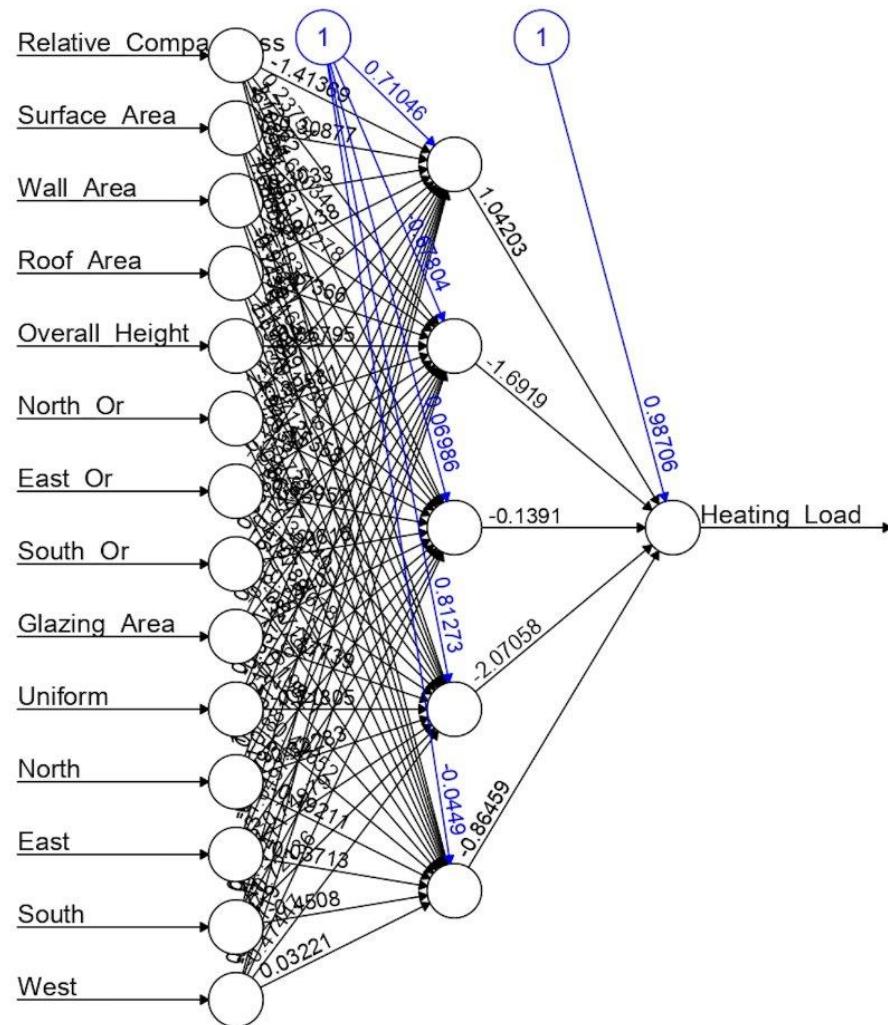
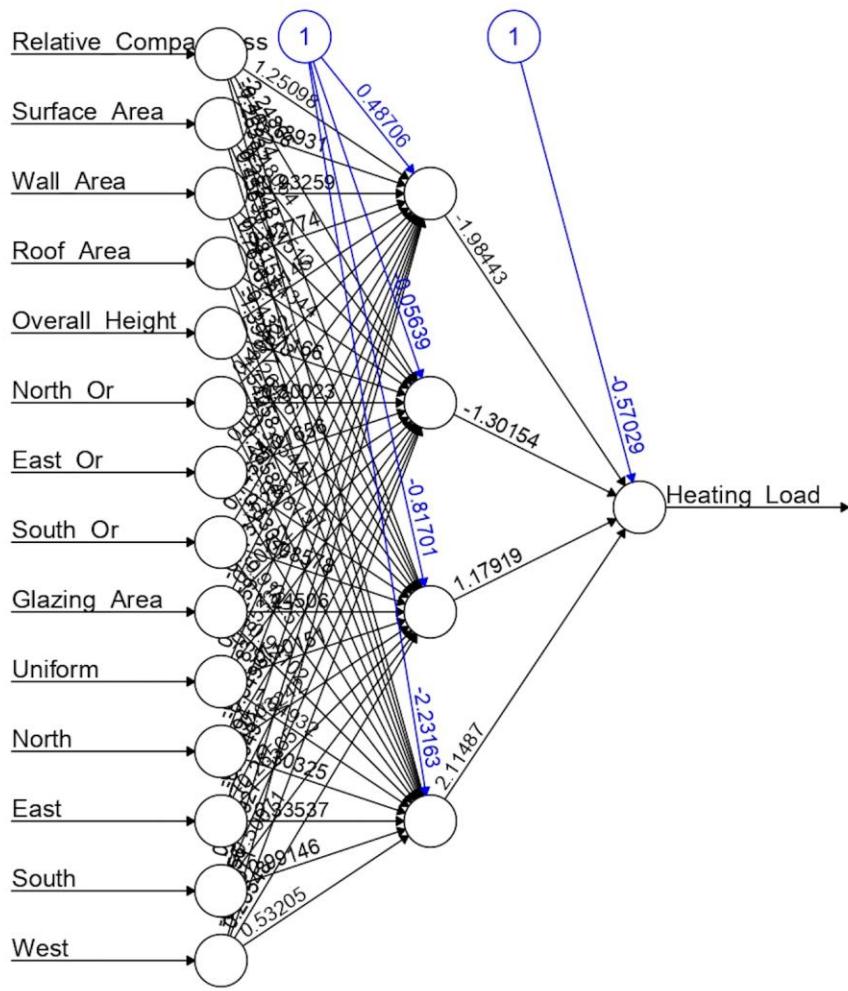
DV: Heating

```

hidden: 1    thresh: 0.1    rep: 1/1    steps:      133  error: 1.72166  time: 0.01 secs
[1,]
[1,] 0.9559848
hidden: 2    thresh: 0.1    rep: 1/1    steps:      107  error: 1.35973  time: 0.01 secs
[1,]
[1,] 0.9645049
hidden: 3    thresh: 0.1    rep: 1/1    steps:       56  error: 1.53629  time: 0.01 secs
[1,]
[1,] 0.963374
hidden: 4    thresh: 0.1    rep: 1/1    steps:       55  error: 1.49456  time: 0.01 secs
[1,]
[1,] 0.9639266
hidden: 5    thresh: 0.1    rep: 1/1    steps:       60  error: 1.53034  time: 0.01 secs
[1,]
[1,] 0.9609335
> corr_max_list2[which.max(sapply(corr_max_list2,max))]
$`2`
[1] 0.9645049

```





Method		Heating			
		Accuracy	NIR	P-value	Significant?
Neural network	Hidden = 1	0.7835	0.2684	<2.2e-16	YES
	Hidden = 2	0.7835	0.2684	<2.2e-16	YES
	Hidden = 3	0.8268	0.2684	<2.2e-16	YES
	Hidden = 4	0.8095	0.2684	<2.2e-16	YES
	Hidden = 5	0.7965	0.2684	<2.2e-16	YES

3 (e) K-nearest neighbor

3(e) DV: cooling; k=5

```

> set.seed(7)
> energy_index <- sample(nrow(energy_norm), 0.7 * nrow(energy_norm))
> energy_train <- energy_norm[energy_index, ]
> energy_test <- energy_norm[-energy_index, ]
> energy_train_labels <- energy[energy_index, 17, drop=TRUE]
> energy_test_labels <- energy[-energy_index, 17, drop=TRUE]
> library(class)
> energy_test_pred <- knn(train = energy_train, test = energy_test,
+                           cl=energy_train_labels, k=5)
> library(gmodels)
> energytable <- CrossTable(x=energy_test_labels, y=energy_test_pred,
+                             prop.chisq=FALSE)

```

Cell Contents	
	N
N / Row Total	
N / Col Total	
N / Table Total	

Total Observations in Table: 231

energy_test_labels	energy_test_pred				Row Total
	A	B	C	D	
A	36	33	0	0	69
	0.522	0.478	0.000	0.000	0.299
	0.692	0.452	0.000	0.000	
	0.156	0.143	0.000	0.000	
B	16	40	1	0	57
	0.281	0.702	0.018	0.000	0.247
	0.308	0.548	0.017	0.000	
	0.069	0.173	0.004	0.000	
C	0	0	41	13	54
	0.000	0.000	0.759	0.241	0.234
	0.000	0.000	0.695	0.277	
	0.000	0.000	0.177	0.056	
D	0	0	17	34	51
	0.000	0.000	0.333	0.667	0.221
	0.000	0.000	0.288	0.723	
	0.000	0.000	0.074	0.147	
Column Total	52	73	59	47	231
	0.225	0.316	0.255	0.203	

```

> sum(diag(energytable$prop.tb1))
[1] 0.6536797
> confusionMatrix(energy_test_pred, energy_test_labels)
Confusion Matrix and Statistics

Reference
Prediction   A   B   C   D
          A 36  16  0   0
          B 33  40  0   0
          C  0   1 41 17
          D  0   0 13 34

Overall Statistics

Accuracy : 0.6537
95% CI : (0.5885, 0.7149)
No Information Rate : 0.2987
P-Value [Acc > NIR] : < 2.2e-16

Kappa : 0.5383

McNemar's Test P-Value : NA

Statistics by Class:

Class: A Class: B Class: C Class: D
Sensitivity      0.5217  0.7018  0.7593  0.6667
Specificity       0.9012  0.8103  0.8983  0.9278
Pos Pred Value    0.6923  0.5479  0.6949  0.7234
Neg Pred Value    0.8156  0.8924  0.9244  0.9076
Prevalence        0.2987  0.2468  0.2338  0.2208
Detection Rate    0.1558  0.1732  0.1775  0.1472
Detection Prevalence 0.2251  0.3160  0.2554  0.2035
Balanced Accuracy 0.7115  0.7560  0.8288  0.7972

```

Accuracy: 0.6537

3(e) DV: cooling; k=7

```
> energy_test_pred <- knn(train = energy_train, test = energy_test,
+                           cl=energy_train_labels, k=7)
> library(gmodels)
> energhtable <- CrossTable(x=energy_test_labels, y=energy_test_pred,
+                             prop.chisq=FALSE)
```

Cell Contents	
N	
N / Row Total	
N / Col Total	
N / Table Total	

Total Observations in Table: 231

energy_test_labels	energy_test_pred				Row Total
	A	B	C	D	
A	35	34	0	0	69
	0.507	0.493	0.000	0.000	0.299
	0.673	0.466	0.000	0.000	
	0.152	0.147	0.000	0.000	
B	17	39	1	0	57
	0.298	0.684	0.018	0.000	0.247
	0.327	0.534	0.017	0.000	
	0.074	0.169	0.004	0.000	
C	0	0	42	12	54
	0.000	0.000	0.778	0.222	0.234
	0.000	0.000	0.700	0.261	
	0.000	0.000	0.182	0.052	
D	0	0	17	34	51
	0.000	0.000	0.333	0.667	0.221
	0.000	0.000	0.283	0.739	
	0.000	0.000	0.074	0.147	
Column Total	52	73	60	46	231
	0.225	0.316	0.260	0.199	

```
> confusionMatrix(energy_test_pred,energy_test_labels)
Confusion Matrix and Statistics
```

Prediction	Reference			
	A	B	C	D
A	35	17	0	0
B	34	39	0	0
C	0	1	42	17
D	0	0	12	34

Overall Statistics

Accuracy : 0.6494
 95% CI : (0.584, 0.7108)
 No Information Rate : 0.2987
 P-Value [Acc > NIR] : < 2.2e-16

Kappa : 0.5325

Mcnemar's Test P-Value : NA

Statistics by Class:

	Class: A	Class: B	Class: C	Class: D
Sensitivity	0.5072	0.6842	0.7778	0.6667
Specificity	0.8951	0.8046	0.8983	0.9333
Pos Pred Value	0.6731	0.5342	0.7000	0.7391
Neg Pred Value	0.8101	0.8861	0.9298	0.9081
Prevalence	0.2987	0.2468	0.2338	0.2208
Detection Rate	0.1515	0.1688	0.1818	0.1472
Detection Prevalence	0.2251	0.3160	0.2597	0.1991
Balanced Accuracy	0.7012	0.7444	0.8380	0.8000

Accuracy: 0.6494

3(e) DV: heating; k=5

```

> set.seed(7)
> energy_index <- sample(nrow(energy_norm), 0.7 * nrow(energy_norm))
> energy_train <- energy_norm[energy_index, ]
> energy_test <- energy_norm[-energy_index, ]
> energy_train_labels <- energy[energy_index, 18, drop=TRUE]
> energy_test_labels <- energy[-energy_index, 18, drop=TRUE]
> library(class)
> energy_test_pred <- knn(train = energy_train, test = energy_test,
+                             cl=energy_train_labels, k=5)
> library(gmodels)
> energytable <- CrossTable(x=energy_test_labels, y=energy_test_pred,
+                             prop.chisq=FALSE)

```

Cell Contents

	N
N / Row Total	
N / Col Total	
N / Table Total	

Total Observations in Table: 231

energy_test_labels	energy_test_pred					Row Total
	D	C	B	A		
D	42	11	0	0		53
	0.792	0.208	0.000	0.000		0.229
	0.764	0.212	0.000	0.000		
	0.182	0.048	0.000	0.000		
C	13	37	1	0		51
	0.255	0.725	0.020	0.000		0.221
	0.236	0.712	0.012	0.000		
	0.056	0.160	0.004	0.000		
B	0	4	45	8		57
	0.000	0.070	0.789	0.140		0.247
	0.000	0.077	0.536	0.200		
	0.000	0.017	0.195	0.035		
A	0	0	38	32		70
	0.000	0.000	0.543	0.457		0.303
	0.000	0.000	0.452	0.800		
	0.000	0.000	0.165	0.139		
Column Total	55	52	84	40		231
	0.238	0.225	0.364	0.173		

```

> confusionMatrix(energy_test_pred, energy_test_labels)
Confusion Matrix and Statistics

```

		Reference				
		Prediction	D	C	B	A
		D	42	13	0	0
		C	11	37	4	0
		B	0	1	45	38
		A	0	0	8	32

Overall Statistics

Accuracy : 0.6753
95% CI : (0.6108, 0.7353)

No Information Rate : 0.303
P-Value [Acc > NIR] : < 2.2e-16

Kappa : 0.5691

McNemar's Test P-Value : NA

Statistics by Class:

	Class: D	Class: C	Class: B	Class: A
Sensitivity	0.7925	0.7255	0.7895	0.4571
Specificity	0.9270	0.9167	0.7759	0.9503
Pos Pred Value	0.7636	0.7115	0.5357	0.8000
Neg Pred Value	0.9375	0.9218	0.9184	0.8010
Prevalence	0.2294	0.2208	0.2468	0.3030
Detection Rate	0.1818	0.1602	0.1948	0.1385
Detection Prevalence	0.2381	0.2251	0.3636	0.1732
Balanced Accuracy	0.8597	0.8211	0.7827	0.7037

Accuracy: 0.6753

3(e) DV: heating; k=7

```
> energy_test_pred <- knn(train = energy_train, test = energy_test,
+                           cl=energy_train_labels, k=7)
> library(gmodels)
> energytable <- CrossTable(x=energy_test_labels, y=energy_test_pred,
+                             prop.chisq=FALSE)
```

Cell Contents			
N			
N / Row Total			
N / Col Total			
N / Table Total			

Total Observations in Table: 231

energy_test_labels	energy_test_pred				Row Total
	D	C	B	A	
D	42	11	0	0	53
	0.792	0.208	0.000	0.000	0.229
	0.764	0.208	0.000	0.000	
	0.182	0.048	0.000	0.000	
C	13	38	0	0	51
	0.255	0.745	0.000	0.000	0.221
	0.236	0.717	0.000	0.000	
	0.056	0.165	0.000	0.000	
B	0	4	41	12	57
	0.000	0.070	0.719	0.211	0.247
	0.000	0.075	0.539	0.255	
	0.000	0.017	0.177	0.052	
A	0	0	35	35	70
	0.000	0.000	0.500	0.500	0.303
	0.000	0.000	0.461	0.745	
	0.000	0.000	0.152	0.152	
Column Total	55	53	76	47	231
	0.238	0.229	0.329	0.203	

```
> confusionMatrix(energy_test_pred, energy_test_labels)
Confusion Matrix and Statistics
```

Reference				
Prediction	D	C	B	A
D	42	13	0	0
C	11	38	4	0
B	0	0	41	35
A	0	0	12	35

Overall Statistics

```
Accuracy : 0.6753
95% CI : (0.6108, 0.7353)
No Information Rate : 0.303
P-Value [Acc > NIR] : < 2.2e-16
```

Kappa : 0.5682

McNemar's Test P-Value : NA

Statistics by Class:

	Class: D	Class: C	Class: B	Class: A
Sensitivity	0.7925	0.7451	0.7193	0.5000
Specificity	0.9270	0.9167	0.7989	0.9255
Pos Pred Value	0.7636	0.7170	0.5395	0.7447
Neg Pred Value	0.9375	0.9270	0.8968	0.8098
Prevalence	0.2294	0.2208	0.2468	0.3030
Detection Rate	0.1818	0.1645	0.1775	0.1515
Detection Prevalence	0.2381	0.2294	0.3290	0.2035
Balanced Accuracy	0.8597	0.8309	0.7591	0.7127

Accuracy: 0.6753

3(f) Naïve bayes

3(f) DV: cooling

```

> ##Naive bayes -- for cooling
> #install.packages("e1071",dependencies=TRUE)
> library(e1071) ## in SVM
> energy <- read_xlsx("energy.xlsx")
> convert_to_quartile_categories <- function(x) {
+   quartiles <- quantile(x, probs = c(0, 0.25, 0.5, 0.75, 1))
+   categories <- cut(x,
+                      breaks = quartiles,
+                      labels = c("D", "C", "B", "A"),
+                      include.lowest = TRUE)
+   return(categories)
+ }
> energy$cooling_category <- convert_to_quartile_categories(energy$Cooling_Load)
> energy$heating_category <- convert_to_quartile_categories(energy$Heating_Load)
> energy <- subset(energy, select = -c(Orientation, Glazing_Area_Distribution, heating_category, Heating_Load, Cooling_Load ))
> set.seed(7)
> energy_index <- sample(nrow(energy), 0.7 * nrow(energy))
> energy_train <- energy[energy_index, ]
> energy_test <- energy[-energy_index, ]
> #Run the Naïve Bayes classifier
> energy_model <- naiveBayes(cooling_category ~ ., data=energy_train, laplace=1)
> #Print the results of the Naïve Bayes
> energy_model

```

```

> energy_pred <- predict(energy_model, energy_test, type="class")
> energy_pred_table <- table(energy_test$cooling_category, energy_pred)
> energy_pred_table
  energy_pred
    D C B A
  D 51 0 0 0
  C 54 0 0 0
  B 1 0 0 56
  A 0 0 0 69

```

Naive Bayes Classifier for Discrete Predictors				
Y	Overall_Height		Uniform	
	[,1]	[,2]	[,1]	[,2]
	D 3.500000	0.0000000	D 0.1347518	0.3426756
	C 3.677536	0.7708198	C 0.1811594	0.3865533
A-priori probabilities:		B 6.844444	0.7239678	
		A 7.000000	0.0000000	
Y	North_Or		North	
	[,1]	[,2]	[,1]	[,2]
	D 0.2765957	0.4489095	D 0.1560284	0.3641759
	C 0.2246377	0.4188639	C 0.2028986	0.4036227
Conditional probabilities:		B 0.2666667	0.4438636	
Relative_Compactness		A 0.2357724	0.4262167	
Y	East_Or		East	
	[,1]	[,2]	[,1]	[,2]
	D 0.2695035	0.4452837	D 0.1985816	0.4003545
	C 0.2681159	0.4445921	C 0.1594203	0.3674011
Surface_Area		B 0.2888889	0.4549343	
Y	South_Or		South	
	[,1]	[,2]	[,1]	[,2]
	D 734.3050	43.13106	D 0.1985816	0.4003545
	C 747.6051	59.73703	C 0.2608696	0.4407086
Wall_Area		B 0.2222222	0.4172881	
Y	Roof_Area		West	
	[,1]	[,2]	[,1]	[,2]
	D 293.3050	43.13106	D 0.1514184	0.09616639
	C 316.1920	38.01149	C 0.2916667	0.13202291
Glazing_Area		B 0.2096296	0.13008268	
Y			[,1]	[,2]
			D 0.2894309	0.12318386
			C 0.1666667	0.3740357
			B 0.1481481	0.3565699
		A 0.2357724	0.4262167	

3(f) DV: heating

```

> library(e1071) ## in SVM
> energy <- read_xlsx("energy.xlsx")
> convert_to_quartile_categories <- function(x) {
+   quartiles <- quantile(x, probs = c(0, 0.25, 0.5, 0.75, 1))
+   categories <- cut(x,
+                      breaks = quartiles,
+                      labels = c("D", "C", "B", "A"),
+                      include.lowest = TRUE)
+   return(categories)
+ }
> energy$cooling_category <- convert_to_quartile_categories(energy$Cooling_Load)
> energy$heating_category <- convert_to_quartile_categories(energy$Heating_Load)
> energy <- subset(energy, select = -c(Orientation, Glazing_Area_Distribution, cooling_category, Heating_Load, Cooling_Load ))
> set.seed(7)
> energy_index <- sample(nrow(energy), 0.7 * nrow(energy))
> energy_train <- energy[energy_index, ]
> energy_test <- energy[-energy_index, ]
> #Run the Naïve Bayes classifier
> energy_model <- naiveBayes(heating_category ~ ., data=energy_train, laplace=1)
> #Print the results of the Naïve Bayes
> energy_model

```

```

> energy_pred <- predict(energy_model, energy_test, type="class")
> energy_pred_table <- table(energy_test$heating_category, energy_pred)
> energy_pred_table
  energy_pred
  D C B A
  D 53 0 0 0
  C 50 0 0 1
  B 3 0 0 54
  A 0 0 0 70

```

Naive Bayes Classifier for Discrete Predictors

Call:
naiveBayes.default(x = X, y = Y, laplace = laplace)

A-priori probabilities:

	D	C	B	A
Y	0.2588454	0.2625698	0.2513966	0.2271881

Conditional probabilities:

	Relative_Compactness	
	[,1]	[,2]
Y	D 0.6957554	0.03593429
	C 0.6736879	0.07059352
	B 0.8635556	0.07934872
	A 0.8327869	0.07617143

	Surface_Area	
	[,1]	[,2]
Y	D 727.7734	35.81531
	C 753.0709	62.64431
	B 588.9074	57.60611
	A 610.0902	51.21854

	Wall_Area	
	[,1]	[,2]
Y	D 286.7734	35.81531
	C 322.4965	40.43021
	B 310.6963	21.71878
	A 349.6270	46.72358

	Roof_Area	
	[,1]	[,2]
Y	D 220.5000	0.00000
	C 215.2872	21.77775
	B 139.1056	23.49513
	A 130.2316	13.65745

	Overall_Height	
	[,1]	[,2]
Y	D 3.500000	0.0000000
	C 3.698582	0.8125784
	B 6.844444	0.7239678
	A 7.000000	0.0000000

	North_Or	
	[,1]	[,2]
Y	D 0.2661871	0.4435617
	C 0.2340426	0.4249084
	B 0.2814815	0.4513967
	A 0.2213115	0.4168416

	East_Or	
	[,1]	[,2]
Y	D 0.2589928	0.4396660
	C 0.2624113	0.4415135
	B 0.2814815	0.4513967
	A 0.2622951	0.4416962

	South_Or	
	[,1]	[,2]
Y	D 0.2158273	0.4128829
	C 0.2482270	0.4335242
	B 0.2000000	0.4014898
	A 0.2540984	0.4371484

	Glazing_Area	
	[,1]	[,2]
Y	D 0.1500000	0.09724465
	C 0.2890071	0.13216497
	B 0.2040741	0.12623300
	A 0.2979508	0.12084372

	Uniform	
	[,1]	[,2]
Y	D 0.1366906	0.3447629
	C 0.1773050	0.3832882
	B 0.2000000	0.4014898
	A 0.1639344	0.3717427

	North	
	[,1]	[,2]
Y	D 0.1654676	0.3729460
	C 0.1914894	0.3948760
	B 0.1851852	0.3898945
	A 0.1885246	0.3927434

	East	
	[,1]	[,2]
Y	D 0.1942446	0.3970489
	C 0.1631206	0.3707928
	B 0.1777778	0.3837495
	A 0.2295082	0.4222507

	South	
	[,1]	[,2]
Y	D 0.1726619	0.3793216
	C 0.2269504	0.4203535
	B 0.1851852	0.3898945
	A 0.2049180	0.4053062

	West	
	[,1]	[,2]
Y	D 0.1942446	0.3970489
	C 0.1843972	0.3891903
	B 0.1703704	0.3773581
	A 0.2131148	0.4111968

3(f) comparison

DV: heating

DV: cooling

```
> confusionMatrix(energy_pred,energy_test$heating_category)
Confusion Matrix and Statistics
```

```
Reference
Prediction D C B A
D 53 50 3 0
C 0 0 0 0
B 0 0 0 0
A 0 1 54 70
```

Overall Statistics

```
Accuracy : 0.5325
95% CI : (0.4659, 0.5982)
No Information Rate : 0.303
P-Value [Acc > NIR] : 3.474e-13
```

Kappa : 0.3602

Mcnemar's Test P-Value : NA

Statistics by Class:

	Class: D	Class: C	Class: B	Class: A
Sensitivity	1.0000	0.0000	0.0000	1.0000
Specificity	0.6944	1.0000	1.0000	0.6543
Pos Pred Value	0.4811	NaN	NaN	0.5520
Neg Pred Value	1.0000	0.7662	0.7532	1.0000
Prevalence	0.2208	0.2338	0.2468	0.2987
Detection Rate	0.2208	0.0000	0.0000	0.2987
Detection Prevalence	0.4589	0.0000	0.0000	0.5411
Balanced Accuracy	0.8472	0.5000	0.5000	0.8272

Accuracy: 0.5195

```
> confusionMatrix(energy_pred,energy_test$heating_category)
Confusion Matrix and Statistics
```

Prediction	D	C	B	A
D	53	50	3	0
C	0	0	0	0
B	0	0	0	0
A	0	1	54	70

Overall Statistics

```
Accuracy : 0.5325
95% CI : (0.4659, 0.5982)
No Information Rate : 0.303
P-Value [Acc > NIR] : 3.474e-13
```

Kappa : 0.3602

Mcnemar's Test P-Value : NA

Statistics by Class:

	Class: D	Class: C	Class: B	Class: A
Sensitivity	1.0000	0.0000	0.0000	1.0000
Specificity	0.7022	1.0000	1.0000	0.7532
Pos Pred Value	0.5000	NaN	NaN	0.7792
Neg Pred Value	1.0000	0.2294	0.2208	0.2468
Prevalence	0.2294	0.2208	0.2468	0.0000
Detection Rate	0.2294	0.0000	0.0000	0.0000
Detection Prevalence	0.4589	0.0000	0.0000	0.5411
Balanced Accuracy	0.8511	0.5000	0.5000	0.5000

	Class: A
Sensitivity	1.0000
Specificity	0.6584
Pos Pred Value	0.5600
Neg Pred Value	1.0000
Prevalence	0.3030
Detection Rate	0.3030
Detection Prevalence	0.5411
Balanced Accuracy	0.8292

Accuracy: 0.5325

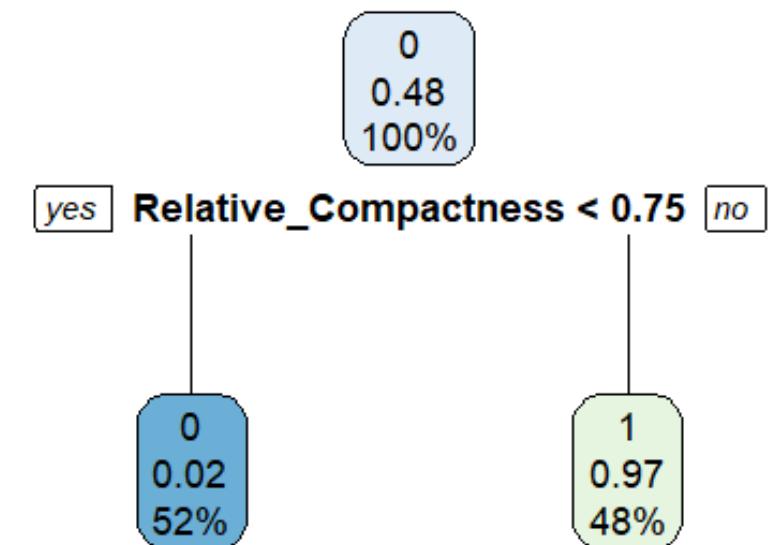
3(g) Decision tree

3(g) cooling

```
> energy <- read_xlsx("energy.xlsx")
> convert_to_quartile_categories <- function(x) {
+   quartiles <- quantile(x, probs = c(0, 0.25, 0.5, 0.75, 1))
+   categories <- cut(x,
+                       breaks = quartiles,
+                       labels = c("D", "C", "B", "A"),
+                       include.lowest = TRUE)
+   return(categories)
+ }
> energy$cooling_category <- convert_to_quartile_categories(energy$Cooling_Load)
> energy$heating_category <- convert_to_quartile_categories(energy$Heating_Load)
> energy$cooling_binary <- ifelse(energy$cooling_category %in% c("A", "B"), 1, 0)
> energy$heating_binary <- ifelse(energy$heating_category %in% c("A", "B"), 1, 0)
> energy$heating_binary <- factor(energy$heating_binary,
+                                   levels = c(0, 1),
+                                   labels = c("Low", "High"))
> energy$cooling_binary <- factor(energy$cooling_binary,
+                                   levels = c(0, 1),
+                                   labels = c("Low", "High"))
> energy <- subset(energy, select = -c(Orientation, Glazing_Area_Distribution, heating_category, Heating_Load, Cooling_Load, heating_binary, cooling_category ))
> set.seed(7)
> energy_index <- sample(nrow(energy), 0.7 * nrow(energy))
> energy_train <- energy[energy_index, ]
> energy_test <- energy[-energy_index, ]
> prop.table(table(energy_train$cooling_binary))
```

	Low	High
0.5195531	0.4804469	

```
> library(rpart)
> library(rpart.plot)
> energytree <- rpart(cooling_binary~ ., data = energy_train, method = 'class')
> rpart.plot(energytree)
```

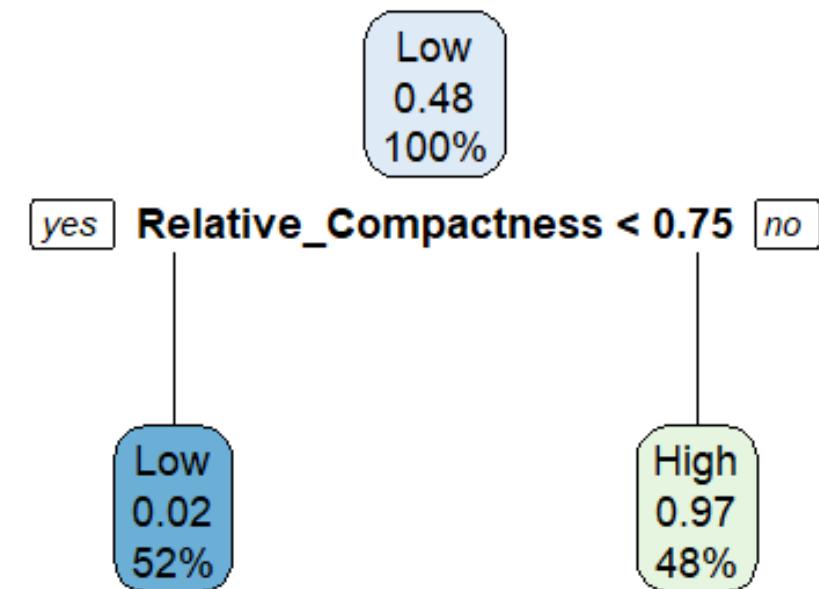


3(g) heating

```
> energy <- read_xlsx("energy.xlsx")
> convert_to_quartile_categories <- function(x) {
+   quartiles <- quantile(x, probs = c(0, 0.25, 0.5, 0.75, 1))
+   categories <- cut(x,
+                       breaks = quartiles,
+                       labels = c("D", "C", "B", "A"),
+                       include.lowest = TRUE)
+   return(categories)
+ }
> energy$cooling_category <- convert_to_quartile_categories(energy$Cooling_Load)
> energy$heating_category <- convert_to_quartile_categories(energy$Heating_Load)
> energy$cooling_binary <- ifelse(energy$cooling_category %in% c("A", "B"), 1, 0)
> energy$heating_binary <- ifelse(energy$heating_category %in% c("A", "B"), 1, 0)
> energy$heating_binary <- factor(energy$heating_binary,
+                                   levels = c(0, 1),
+                                   labels = c("Low", "High"))
> energy$cooling_binary <- factor(energy$cooling_binary,
+                                   levels = c(0, 1),
+                                   labels = c("Low", "High"))
> energy <- subset(energy, select = -c(Orientation, Glazing_Area_Distribution, heating_category, Heating_Load, Cooling_Load, cooling_binary, cooling_category ))
> set.seed(7)
> energy_index <- sample(nrow(energy), 0.7 * nrow(energy))
> energy_train <- energy[energy_index, ]
> energy_test <- energy[-energy_index, ]
> prop.table(table(energy_train$heating_binary))
```

	Low	High
0.5214153	0.4785847	

```
> library(rpart)
> library(rpart.plot)
> energytree <- rpart(heating_binary~ ., data = energy_train, method = 'class')
> rpart.plot(energytree)
```



3(g) comparison

DV: cooling

```
> energypredict <- predict(energytree, energy_test[,1:14],  
+                               type = 'class')  
> #install.packages("caret")  
> library("caret")  
> confusionMatrix(energypredict, energy_test$cooling_binary)  
Confusion Matrix and Statistics  
  
Reference  
Prediction Low High  
    Low   105     1  
    High    0   125  
  
Accuracy : 0.9957  
95% CI : (0.9761, 0.9999)  
No Information Rate : 0.5455  
P-Value [Acc > NIR] : <2e-16  
  
Kappa : 0.9913  
  
Mcnemar's Test P-Value : 1  
  
Sensitivity : 1.0000  
Specificity : 0.9921  
Pos Pred Value : 0.9906  
Neg Pred Value : 1.0000  
Prevalence : 0.4545  
Detection Rate : 0.4545  
Detection Prevalence : 0.4589  
Balanced Accuracy : 0.9960  
  
'Positive' Class : Low
```

Accuracy: 0.9957

DV: heating

```
> energypredict <- predict(energytree, energy_test[,1:14],  
+                               type = 'class')  
> #install.packages("caret")  
> library("caret")  
> confusionMatrix(energypredict, energy_test$heating_binary)  
Confusion Matrix and Statistics  
  
Reference  
Prediction Low High  
    Low   103     3  
    High    1   124  
  
Accuracy : 0.9827  
95% CI : (0.9563, 0.9953)  
No Information Rate : 0.5498  
P-Value [Acc > NIR] : <2e-16  
  
Kappa : 0.9651  
  
Mcnemar's Test P-Value : 0.6171  
  
Sensitivity : 0.9904  
Specificity : 0.9764  
Pos Pred Value : 0.9717  
Neg Pred Value : 0.9920  
Prevalence : 0.4502  
Detection Rate : 0.4459  
Detection Prevalence : 0.4589  
Balanced Accuracy : 0.9834  
  
'Positive' Class : Low
```

Accuracy: 0.9827

3(h) Random forest

```

> library("randomForest")
> energy <- read_xlsx("energy.xlsx")
> convert_to_quartile_categories <- function(x) {
+   quartiles <- quantile(x, probs = c(0, 0.25, 0.5, 0.75, 1))
+   categories <- cut(x,
+                      breaks = quartiles,
+                      labels = c("D", "C", "B", "A"),
+                      include.lowest = TRUE)
+   return(categories)
+ }
> energy$cooling_category <- convert_to_quartile_categories(energy$Cooling_Load)
> energy$heating_category <- convert_to_quartile_categories(energy$Heating_Load)
> energy$cooling_binary <- ifelse(energy$cooling_category %in% c("A", "B"), 1, 0)
> energy$heating_binary <- ifelse(energy$heating_category %in% c("A", "B"), 1, 0)
> energy$heating_binary <- factor(energy$heating_binary,
+                                   levels = c(0, 1),
+                                   labels = c("Low", "High"))
> energy$cooling_binary <- factor(energy$cooling_binary,
+                                   levels = c(0, 1),
+                                   labels = c("Low", "High"))
> energy <- subset(energy, select = -c(Orientation, Glazing_Area_Distribution, heating_category, Heating_Load, Cooling_Load, heating_binary, cooling_category ))
> set.seed(7)
> energy_index <- sample(nrow(energy), 0.7 * nrow(energy))
> energy_train <- energy[energy_index, ]
> energy_test <- energy[-energy_index, ]
> energyforest <- randomForest(cooling_binary ~ ., data = energy_train, ntree=500,
+                                proximity=TRUE, importance=TRUE)
> energyforest

```

Call:

```
randomForest(formula = cooling_binary ~ ., data = energy_train,
ntree = 500, proximity = TRUE, importance = TRUE)
```

Type of random forest: classification

Number of trees: 500

No. of variables tried at each split: 3

OOB estimate of error rate: 1.86%

Confusion matrix:

	Low	High	class.error
Low	275	4	0.01433692
High	6	252	0.02325581

3(h) DV: cooling

```

> energypredict <- predict(energyforest, newdata = energy_test[,1:14], type = 'class')
> confusionMatrix(energypredict, energy_test$cooling_binary)
Confusion Matrix and Statistics

Reference
Prediction Low High
      Low    105     1
      High     0    125

Accuracy : 0.9957
95% CI : (0.9761, 0.9999)
No Information Rate : 0.5455
P-Value [Acc > NIR] : <2e-16

Kappa : 0.9913

McNemar's Test P-Value : 1

Sensitivity : 1.0000
Specificity : 0.9921
Pos Pred Value : 0.9906
Neg Pred Value : 1.0000
Prevalence : 0.4545
Detection Rate : 0.4545
Detection Prevalence : 0.4589
Balanced Accuracy : 0.9960

'Positive' Class : Low

```

```
> ##0.9957
```

3(h) DV: heating

```
> library("randomForest")
> energy <- read_xlsx("energy.xlsx")
> convert_to_quartile_categories <- function(x) {
+   quartiles <- quantile(x, probs = c(0, 0.25, 0.5, 0.75, 1))
+   categories <- cut(x,
+                      breaks = quartiles,
+                      labels = c("D", "C", "B", "A"),
+                      include.lowest = TRUE)
+   return(categories)
+ }
> energy$cooling_category <- convert_to_quartile_categories(energy$Cooling_Load)
> energy$heating_category <- convert_to_quartile_categories(energy$Heating_Load)
> energy$cooling_binary <- ifelse(energy$cooling_category %in% c("A", "B"), 1, 0)
> energy$heating_binary <- ifelse(energy$heating_category %in% c("A", "B"), 1, 0)
> energy$heating_binary <- factor(energy$heating_binary,
+                                   levels = c(0, 1),
+                                   labels = c("Low", "High"))
> energy$cooling_binary <- factor(energy$cooling_binary,
+                                   levels = c(0, 1),
+                                   labels = c("Low", "High"))
> energy <- subset(energy, select = -c(Orientation, Glazing_Area_Distribution, heating_category, Heating_Load, Cooling_Load, cooling_binary, cooling_category ))
> set.seed(7)
> energy_index <- sample(nrow(energy), 0.7 * nrow(energy))
> energy_train <- energy[energy_index, ]
> energy_test <- energy[-energy_index, ]
> energyforest <- randomForest(heating_binary~ ., data = energy_train, ntree=500,
+                               proximity=TRUE, importance=TRUE)
> energyforest

Call:
randomForest(formula = heating_binary ~ ., data = energy_train,      ntree = 50
0, proximity = TRUE, importance = TRUE)
      Type of random forest: classification
                  Number of trees: 500
No. of variables tried at each split: 3

      OOB estimate of error rate: 1.68%
Confusion matrix:
             Low High class.error
Low    277    3   0.01071429
High     6   251   0.02334630
```

```
> energypredict <- predict(energyforest, newdata = energy_test[,1:14],
+ type = 'class')
> confusionMatrix(energypredict, energy_test$heating_binary)
Confusion Matrix and Statistics

                                         Reference
Prediction          Low       High
      Low        103        3
      High        1       124

                                Accuracy : 0.9827
                                95% CI : (0.9563, 0.9953)
No Information Rate : 0.5498
P-Value [Acc > NIR] : <2e-16

                                Kappa : 0.9651

Mcnemar's Test P-Value : 0.6171

                                Sensitivity : 0.9904
                                Specificity : 0.9764
Pos Pred Value : 0.9717
Neg Pred Value : 0.9920
Prevalence : 0.4502
Detection Rate : 0.4459
Detection Prevalence : 0.4589
Balanced Accuracy : 0.9834

'Positive' Class : Low

> ##0.0.9827
```

3(i) Boosting

3(i) DV: cooling

```
> library("randomForest")
> energy <- read_xlsx("energy.xlsx")
> convert_to_quartile_categories <- function(x) {
+   quartiles <- quantile(x, probs = c(0, 0.25, 0.5, 0.75, 1))
+   categories <- cut(x,
+                       breaks = quartiles,
+                       labels = c("D", "C", "B", "A"),
+                       include.lowest = TRUE)
+   return(categories)
+ }
> energy$cooling_category <- convert_to_quartile_categories(energy$Cooling_Load)
> energy$heating_category <- convert_to_quartile_categories(energy$Heating_Load)
> energy$cooling_binary <- ifelse(energy$cooling_category %in% c("A", "B"), 1, 0)
> energy$heating_binary <- ifelse(energy$heating_category %in% c("A", "B"), 1, 0)
> energy <- subset(energy, select = -c(Orientation, Glazing_Area_Distribution, heating_category, Heating_Load, Cooling_Load, heating_binary, cooling_category ))
> set.seed(7)
> energy_index <- sample(nrow(energy), 0.7 * nrow(energy))
> x_train <- as.matrix(energy[energy_index,1:14])
> y_train <- energy[energy_index,15,drop=TRUE]
> x_test <- as.matrix(energy[-energy_index,1:14])
> y_test <- energy[-energy_index,15,drop=TRUE]
> library(xgboost)
> dtrain <- xgb.DMatrix(data = x_train, label = y_train)
> energyxgb <- xgboost(data = dtrain, max.depth = 5, eta = 1, nthread = 2,
+                         nrounds = 1000,objective = "binary:logistic",verbose = 0)
>
> energypredict <- predict(energyxgb, x_test)
> head(energypredict)
[1] 9.938075e-01 6.822284e-01 9.947772e-01 9.997812e-01 9.932132e-01 1.143190e-09
> energypredict <- as.numeric(energypredict > 0.5)
> head(energypredict)
[1] 1 1 1 1 1 0
```

```
> confusionMatrix(factor(energypredict),factor(y_test))
Confusion Matrix and Statistics

                                         Reference
Prediction          0      1
          0 105  1
          1     0 125

                                Accuracy : 0.9957
                                95% CI : (0.9761, 0.9999)
No Information Rate : 0.5455
P-Value [Acc > NIR] : <2e-16

                                Kappa : 0.9913

McNemar's Test P-Value : 1

                                Sensitivity : 1.0000
                                Specificity  : 0.9921
Pos Pred Value : 0.9906
Neg Pred Value : 1.0000
Prevalence       : 0.4545
Detection Rate  : 0.4545
Detection Prevalence : 0.4589
Balanced Accuracy : 0.9960

'Positive' Class : 0

> ###0.0.9957
```

3(i) DV: heating

```
> library("randomForest")
> energy <- read_xlsx("energy.xlsx")
> convert_to_quartile_categories <- function(x) {
+   quartiles <- quantile(x, probs = c(0, 0.25, 0.5, 0.75, 1))
+   categories <- cut(x,
+                      breaks = quartiles,
+                      labels = c("D", "C", "B", "A"),
+                      include.lowest = TRUE)
+   return(categories)
+ }
> energy$cooling_category <- convert_to_quartile_categories(energy$Cooling_Load)
> energy$heating_category <- convert_to_quartile_categories(energy$Heating_Load)
> energy$cooling_binary <- ifelse(energy$cooling_category %in% c("A", "B"), 1, 0)
> energy$heating_binary <- ifelse(energy$heating_category %in% c("A", "B"), 1, 0)
> energy <- subset(energy, select = -c(Orientation, Glazing_Area_Distribution, heating_category, Heating_Load, Cooling_Load, cooling_binary, cooling_category ))
> set.seed(7)
> energy_index <- sample(nrow(energy), 0.7 * nrow(energy))
> x_train <- as.matrix(energy[energy_index,1:14])
> y_train <- energy[energy_index,15,drop=TRUE]
> x_test <- as.matrix(energy[-energy_index,1:14])
> y_test <- energy[-energy_index,15,drop=TRUE]
> library(xgboost)
> dtrain <- xgb.DMatrix(data = x_train, label = y_train)
> energyxgb <- xgboost(data = dtrain, max.depth = 5, eta = 1, nthread = 2,
+                         nrounds = 1000,objective = "binary:logistic",verbose = 0)
>
> energypredict <- predict(energyxgb, x_test)
> head(energypredict)
[1] 8.769583e-01 8.858487e-01 9.960819e-01 9.960819e-01 9.970587e-01 4.586229e-11
> energypredict <- as.numeric(energypredict > 0.5)
> head(energypredict)
[1] 1 1 1 1 1 0
```

```
> confusionMatrix(factor(energypredict),factor(y_test))
Confusion Matrix and Statistics

Reference
Prediction   0    1
          0 99   3
          1   5 124

Accuracy : 0.9654
95% CI : (0.9329, 0.9849)
No Information Rate : 0.5498
P-Value [Acc > NIR] : <2e-16

Kappa : 0.9299

McNemar's Test P-Value : 0.7237

Sensitivity : 0.9519
Specificity : 0.9764
Pos Pred Value : 0.9706
Neg Pred Value : 0.9612
Prevalence : 0.4502
Detection Rate : 0.4286
Detection Prevalence : 0.4416
Balanced Accuracy : 0.9642

'Positive' Class : 0

> ###0.9654
```

Method		Cooling				Heating			
		Accuracy	NIR	P-value	Significant?	Accuracy	NIR	P-value	Significant?
Perceptrons (best model)		0.9812	0.5368	<2.2e-16	YES	0.9766	0.5368	<2.2e-16	YES
SVM		0.9610	0.5325	<2.2e-16	YES	0.9610	0.5325	<2.2e-16	YES
Neural Network	Node = 1	0.7662	0.2771	<2.2e-16	YES	0.7835	0.2684	<2.2e-16	YES
	Node = 2	0.7576	0.2771	<2.2e-16	YES	0.7835	0.2684	<2.2e-16	YES
	Node = 3	0.7403	0.2771	<2.2e-16	YES	0.8268	0.2684	<2.2e-16	YES
	Node = 4	0.7403	0.2771	<2.2e-16	YES	0.8095	0.2684	<2.2e-16	YES
	Node = 5	0.7835	0.2771	<2.2e-16	YES	0.7965	0.2684	<2.2e-16	YES
K-nearest	K=5	0.6523	0.2987	<2.2e-16	YES	0.6759	0.3030	<2.2e-16	YES
	K=7	0.6494	0.2987	<2.2e-16	YES	0.6753	0.3030	<2.2e-16	YES
Naïve bayes		0.5195	0.2987	2.078e-12	YES	0.5325	0.3030	3.474e-13	YES
Decision tree		0.9957	0.5455	<2e-16	YES	0.9827	0.5498	<2e-16	YES
Random forest		0.9957	0.5455	<2e-16	YES	0.9827	0.5498	<2e-16	YES
Boosting		0.9957	0.5455	<2e-16	YES	0.9654	0.5498	<2e-16	YES

4. Lessons Learned

Which technique worked best? Justify by using the accuracies of your models when possible.

- If only looking at accuracy rate, decision tree, random forest, boosting worked the best. They all have the highest accuracy rate of 0.9957 for predicting cooling categories, and 0.9827 for predicting heating categories. The no information rates are 0.5455 and 0.5498 relatively. The p-values are all equals to 0, which shows that the model is better than random guessing
- However, these methods perform better partially because we reduce the variations of dependent variables for those models. (e.g., from continuous --> 4 --> 2 categories).
 - If we take account into the variation of dependent variables, neural network did a good job too in predicting continuous variables.

What insights do you have for builders of energy efficient buildings? What should they do to reduce cooling loads? What should they do to reduce heating loads?

Heating

	Low	High	MeanDecreaseAccuracy	MeanDecreaseGini
Relative_Compactness	14.62596053	14.545571	14.649960	65.5104663
Surface_Area	13.73628743	13.632912	13.738306	58.5011722
Wall_Area	10.23626977	9.587888	10.773045	8.1961694
Roof_Area	13.39019704	13.374925	13.459355	57.2016905
Overall_Height	13.15143550	13.297356	13.285478	57.1495503
North_Or	-6.75988526	-4.077085	-7.667284	0.4740749
East_Or	-3.72958387	-3.370329	-4.852650	0.5180595
South_Or	-3.90651474	-4.611873	-6.386411	0.4173750
Glazing_Area	25.25637593	18.435475	28.551884	9.1125303
Uniform	0.68833757	5.941626	5.311090	1.1400686
North	-0.07292229	3.136873	2.619627	0.5351335
East	2.69350070	4.910656	5.598635	0.3780917
South	-1.93889218	3.646664	1.558124	0.3221363
West	4.88090809	5.034044	6.731009	0.4660417

Cooling

	Low	High	MeanDecreaseAccuracy	MeanDecreaseGini
Relative_Compactness	14.0498493	13.5749081	13.864109	61.6504884
Surface_Area	13.9696652	13.7566835	13.936819	59.9742842
Wall_Area	9.9960372	9.9904452	11.072411	9.3966730
Roof_Area	13.2103420	13.3501541	13.367688	56.6515229
Overall_Height	13.4038388	13.5535182	13.556726	59.4447912
North_Or	-2.8915394	0.3426788	-2.072015	0.4970665
East_Or	-1.7256062	-3.9433085	-4.036582	0.6374922
South_Or	-5.1823686	-2.0607331	-5.211837	0.5728588
Glazing_Area	21.2868525	13.9867456	23.106493	8.1620201
Uniform	-2.2652941	5.8303410	2.559019	1.1714747
North	-2.1724762	2.5803805	1.014268	0.3659726
East	1.6671445	4.3526616	4.534058	0.3452947
South	-0.4350009	2.5966100	1.974207	0.3347015
West	7.3956345	4.9540937	7.961014	0.4592505

- Glazing area
- Relative compactness
- Surface area
- Roof area
- Overall height

What insights do you have for builders of energy efficient buildings? What should they do to reduce cooling loads? What should they do to reduce heating loads?

- Correlation matrix shows that **relative compactness** has strong negative correlation with cooling/heating load, which is verified in the decision tree.



TAKEAWAY 1:

Larger relative compactness of a building will use less energy for heating and cooling

- Larger surface area

- Linear regression shows that **Overall height** has strong positive correlation with cooling/heating load



TAKEAWAY 2:

Build lower-height structure is better for energy efficiency

**What insights do you have for builders of energy efficient buildings?
What should they do to reduce cooling loads? What should they do to
reduce heating loads?**

Build energy efficient building for both heating & cooling:

- Reduce overall height
- Minimize roof area
- Minimize surface area
- Optimize relative compactness



*International Renewable Energy Agency headquarters
Abu Dhabi*

A wide-angle photograph of a solar farm. Numerous dark blue solar panels are mounted on a metal frame and tilted at an angle, covering a large portion of the left side of the image. The panels are set against a clear, light blue sky. In the background, there's a fence and some greenery, including trees and bushes. The overall scene is bright and sunny.

Thanks!