

154. You are given a cost matrix where each element `cost[i][j]` represents the cost of assigning worker `i` to task `j`. Develop a program that utilizes exhaustive search to solve the assignment problem. The program should Define a function `total_cost(assignment, cost_matrix)` that takes an assignment (list representing worker-task pairings) and the cost matrix as input. It iterates through the assignment and calculates the total cost by summing the corresponding costs from the cost matrix Implement a function `assignment_problem(cost_matrix)` that takes the cost matrix as input and performs the following Generate all possible permutations of worker indices (excluding repetitions).

Program:-

```
import numpy as np
```

```
def hungarian_algorithm(cost_matrix):
```

```
    cost_matrix = np.array(cost_matrix)
```

```
    num_workers, num_tasks = cost_matrix.shape
```

```
    # Step 1: Subtract the minimum value of each row from all elements in that row
```

```
    cost_matrix -= np.min(cost_matrix, axis=1)[:, np.newaxis]
```

```
    # Step 2: Subtract the minimum value of each column from all elements in that column
```

```
    cost_matrix -= np.min(cost_matrix, axis=0)
```

```
    # Step 3: Find a complete matching of zeros
```

```
    assignment = [-1] * num_workers
```

```
    task_assigned = [-1] * num_tasks
```

```
    marked_rows = [False] * num_workers
```

```
    marked_cols = [False] * num_tasks
```

```
    num_assigned = 0
```

```
    while num_assigned < num_workers:
```

```
        min_uncovered_value = float('inf')
```

```
            min_row = -1
```

```
            min_col = -1
```

```

# Find the smallest element not covered by any line
for i in range(num_workers):
    if not marked_rows[i]:
        for j in range(num_tasks):
            if not marked_cols[j]:
                if cost_matrix[i, j] < min_uncovered_value:
                    min_uncovered_value = cost_matrix[i, j]
                    min_row = i
                    min_col = j

# Subtract min_uncovered_value from uncovered rows and add it to covered
columns
for j in range(num_tasks):
    if marked_cols[j]:
        cost_matrix[min_row, j] += min_uncovered_value
    else:
        cost_matrix[min_row, j] -= min_uncovered_value

for i in range(num_workers):
    if marked_rows[i]:
        cost_matrix[i, min_col] -= min_uncovered_value
    else:
cost_matrix[i, min_col] += min_uncovered_value

# Assign the worker to the task
assignment[min_row] = min_col
task_assigned[min_col] = min_row
marked_rows[min_row] = True
marked_cols[min_col] = True
num_assigned += 1

```

Calculate total cost based on the optimal assignment

total_cost = 0

for worker in range(num_workers):

total_cost += cost_matrix[worker, assignment[worker]]

Prepare the optimal assignment in the requested format

**optimal_assignment = [(f'worker {worker+1}', f'task {assignment[worker]+1}') for
worker in range(num_workers)]**

return optimal_assignment, total_cost

input:-

cost_matrix1 = [

[3, 10, 7],

[8, 5, 12],

[4, 6, 9]

]

cost_matrix2 = [

[15, 9, 4],

[8, 7, 18],

[6, 12, 11]]

Output:-

Output

Clear

```
Test Case 1:
Optimal Assignment: [('worker 1', 'task 1'), ('worker 2', 'task 2'), ('worker 3',
    'task 3')]
Total Cost: 1

Test Case 2:
Optimal Assignment: [('worker 1', 'task 3'), ('worker 2', 'task 2'), ('worker 3',
    'task 1')]
Total Cost: 0

=== Code Execution Successful ===
```

Time complexity:- $O(n!)$