

**153.** You are given a list of cities represented by their coordinates. Develop a program that utilizes exhaustive search to solve the TSP. The program should:

1. Define a function `distance(city1, city2)` to calculate the distance between two cities (e.g., Euclidean distance).
2. Implement a function `tsp(cities)` that takes a list of cities as input and performs the following:
  - Generate all possible permutations of the cities (excluding the starting city) using `itertools.permutations`.
  - For each permutation (representing a potential route):
    - Calculate the total distance traveled by iterating through the path and summing the distances between consecutive cities.
    - Keep track of the shortest distance encountered and the corresponding path.
  - Return the minimum distance and the shortest path (including the starting city at the beginning and end).

**Program:-**

```
import itertools
```

```
import math
```

```
def distance(city1, city2):
```

```
    """ Calculate the Euclidean distance between two cities """
```

```
    x1, y1 = city1
```

```
    x2, y2 = city2
```

```
    return math.sqrt((x2 - x1)*2 + (y2 - y1)*2)
```

```
def tsp(cities):
```

```
    """ Solve the TSP using exhaustive search """
```

```
    n = len(cities)
```

```
    if n < 2:
```

```
        return 0, []
```

```
    # Generate all permutations of cities (excluding starting city)
```

```
    perm = itertools.permutations(cities[1:])
```

```
    min_distance = float('inf')
```

```
shortest_path = None
```

```
for route in perm:
```

```
    # Construct the full path including starting and ending at the first city
```

```
    full_route = [cities[0]] + list(route) + [cities[0]]
```

```
    # Calculate total distance for this route
```

```
    total_distance = 0
```

```
    for i in range(n):
```

```
        total_distance += distance(full_route[i], full_route[i+1])
```

```
if total_distance < min_distance:
```

```
    min_distance = total_distance
```

```
    shortest_path = full_route
```

```
return min_distance, shortest_path
```

input:-

```
cities1 = [(1, 2), (4, 5), (7, 1), (3, 6)]
```

```
cities2 = [(2, 4), (8, 1), (1, 7), (6, 3), (5, 9)]
```

output:-

```
Output
Test Case 1:
Shortest Distance: 16.969112047670894
Shortest Path: [(1, 2), (7, 1), (4, 5), (3, 6), (1, 2)]

Test Case 2:
Shortest Distance: 23.12995011084934
Shortest Path: [(2, 4), (6, 3), (8, 1), (5, 9), (1, 7), (2, 4)]

=== Code Execution Successful ===
```

**TIME COMPLEXITY:- $O(n-1)!$**



