

## 96. Boruvka's Algorithm

Program:

```
def boruvka(graph):
    mst = []
    subsets = [[i] for i in range(len(graph))]

    while len(mst) < len(graph) - 1:
        cheapest = [None] * len(graph)

        for i in range(len(graph)):
            for j in range(len(graph[i])):
                if i != j:
                    root_i = find(subsets, i)
                    root_j = find(subsets, j)

                    if root_i != root_j:
                        if cheapest[root_i] is None or graph[i][j] < graph[cheapest[root_i]][root_i]:
                            cheapest[root_i] = j
                        if cheapest[root_j] is None or graph[i][j] < graph[cheapest[root_j]][root_j]:
                            cheapest[root_j] = i

        for i in range(len(graph)):
            if cheapest[i] is not None:
                root_i = find(subsets, i)
                root_j = find(subsets, cheapest[i])

                if root_i != root_j:
                    mst.append([i, cheapest[i], graph[i][cheapest[i]]])
                    union(subsets, root_i, root_j)

    return mst

def find(subsets, node):
    for i in range(len(subsets)):
        if node in subsets[i]:
            return i

def union(subsets, a, b):
    subsets[a] += subsets[b]
    subsets.pop(b)

# Example Usage
graph = [
    [0, 2, 0, 6, 0],
    [2, 0, 3, 8, 5],
    [0, 3, 0, 0, 7],
    [6, 8, 0, 0, 9],
    [0, 5, 7, 9, 0]
]

minimum_spanning_tree = boruvka(graph)
print(minimum_spanning_tree)
Output:
```

```
[[0, 2, 0], [1, 0, 2], [3, 2, 0], [4, 0, 0]]
```

```
=== Code Execution Successful ===
```

Time complexity:

$O(\log V)$