

1. 134. Given an array of integers nums, sort the array in ascending order and return it. You must solve the problem without using any built-in functions in  $O(n \log(n))$  time complexity and with the smallest space complexity possible.

PROGRAM:-

```
def merge_sort(nums):  
    # Base case: If the array is empty or has one element, it is already sorted  
    if len(nums) <= 1:  
        return nums  
  
    # Divide the array into two halves  
    mid = len(nums) // 2  
    left_half = nums[:mid]  
    right_half = nums[mid:]  
  
    # Recursively sort each half  
    left_sorted = merge_sort(left_half)  
    right_sorted = merge_sort(right_half)  
  
    # Merge the sorted halves  
    return merge(left_sorted, right_sorted)  
  
def merge(left, right):  
    merged = []  
    i = j = 0  
  
    # Merge the two sorted lists into one sorted list  
    while i < len(left) and j < len(right):
```

```
if left[i] <= right[j]:  
    merged.append(left[i])  
    i += 1  
else:  
    merged.append(right[j])  
    j += 1
```

# Append any remaining elements

```
while i < len(left):  
    merged.append(left[i])  
    i += 1  
while j < len(right):  
    merged.append(right[j])  
    j += 1
```

```
return merged
```

# Test Case

```
nums = [3, 1, 4, 1, 5, 9, 2, 6, 5, 3, 5]  
sorted_nums = merge_sort(nums)  
print(f"Original Array: {nums}")  
print(f"Sorted Array: {sorted_nums}")
```

OUTPUT:-

```
Original Array: [3, 1, 4, 1, 5, 9, 2, 6, 5, 3, 5]  
Sorted Array: [1, 1, 2, 3, 3, 4, 5, 5, 5, 6, 9]  
  
=== Code Execution Successful ===
```

TIME COMPLEXITY:- $O(n \log n)$