

PolSAR Undeveloped Speckle Suppression Using Clutter Decomposition and Dual-domain Filtering

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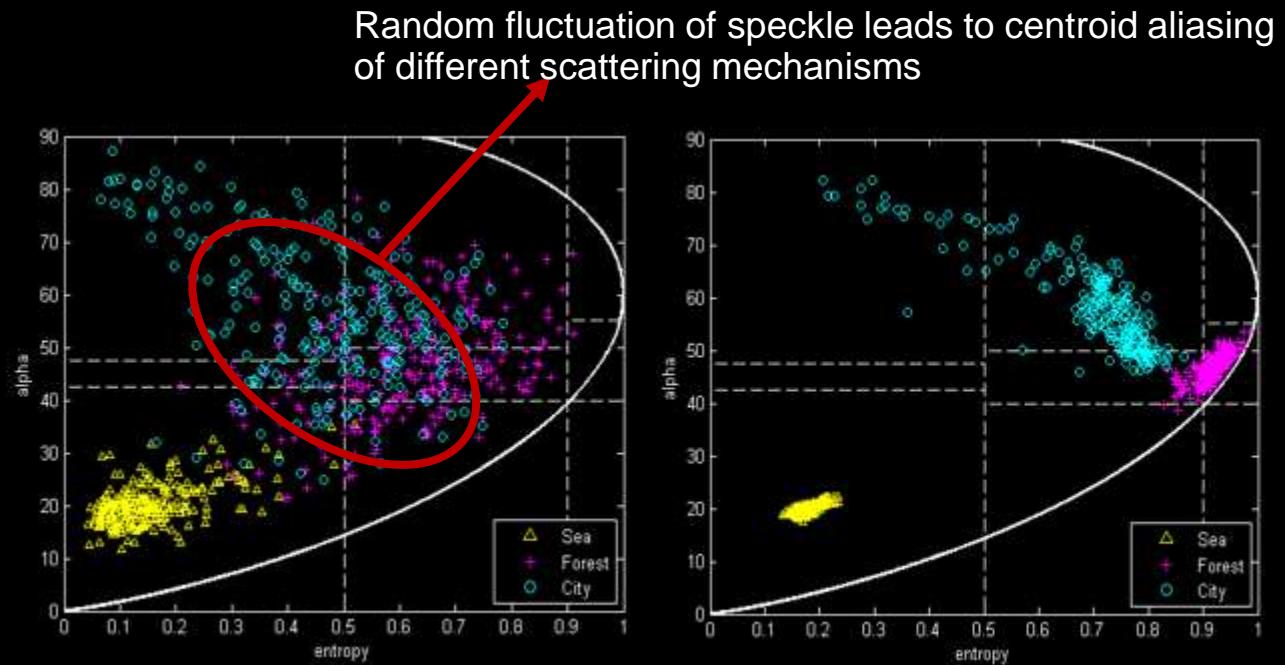
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Speckle Suppression

- An important topic in SAR remote sensing
 - Estimating physical/polarization parameters;
 - Detection, classification and terrain interpretation...



AIRSAR L-band
San Francisco



Original 4-look PolSAR image

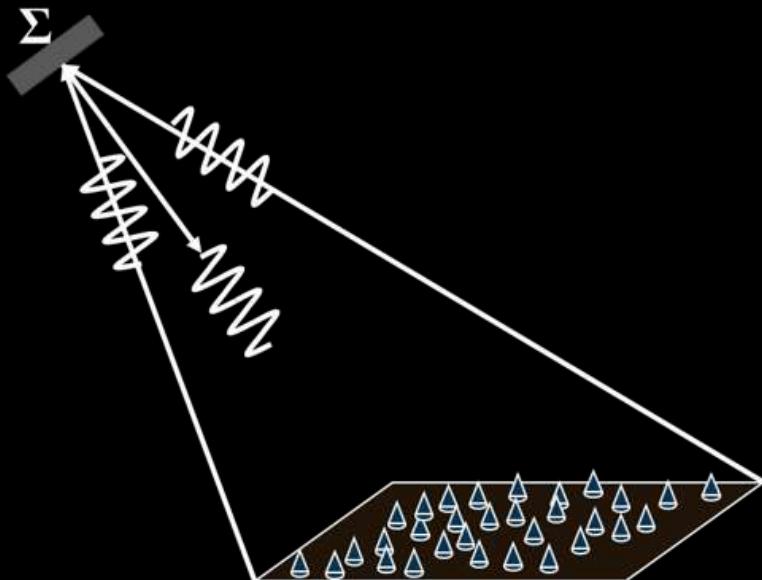
After 7*7 Refined Lee filter

Related Work

- PolSAR speckle filter
 - Nonlocal [Chen et al. 2011, Deledalle et al. 2015]
 - Meanshift [Lang et al. 2014]
 - Adaptive size window [Lang et al. 2015]
 - Extended Sigma [Lee et al. 2016]
 - POSSC [Xu et al. 2016]
 - CV-deSpeckNet [Mullissa et al. 2022]
 - RIRSN [Lin et al. 2023]
 - SDAN [Vasile et al. 2010]
 - ACM [Yang et al. 2016]
 - GMM [Wang et al. 2017]
 -
- 
- Developed speckle assumption
- Undeveloped speckle assumption

Resolution: Medium/low VS High

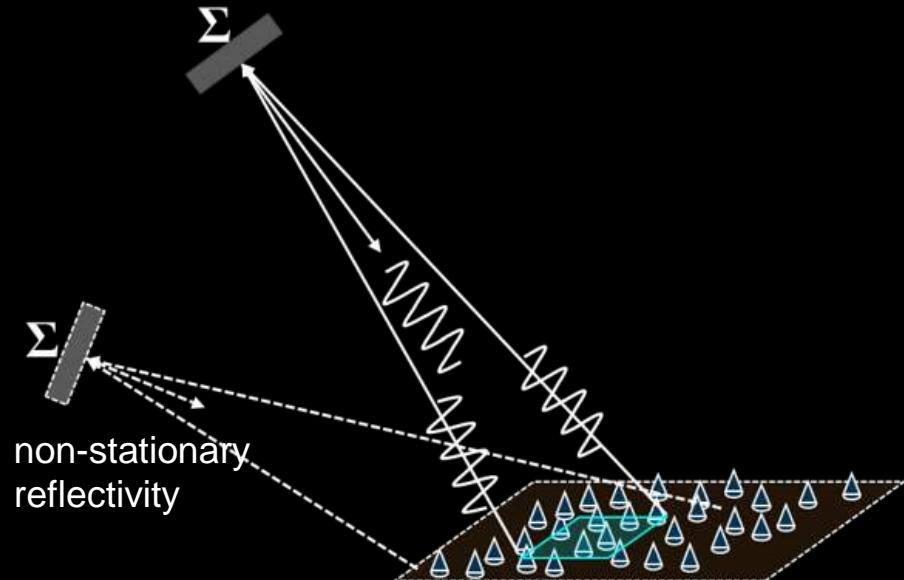
- HR inevitably leads to heterogeneous clutter



Central limit theorem (CLT)

→ SLC Gaussian Vectors

→ Rayleigh, Wishart...

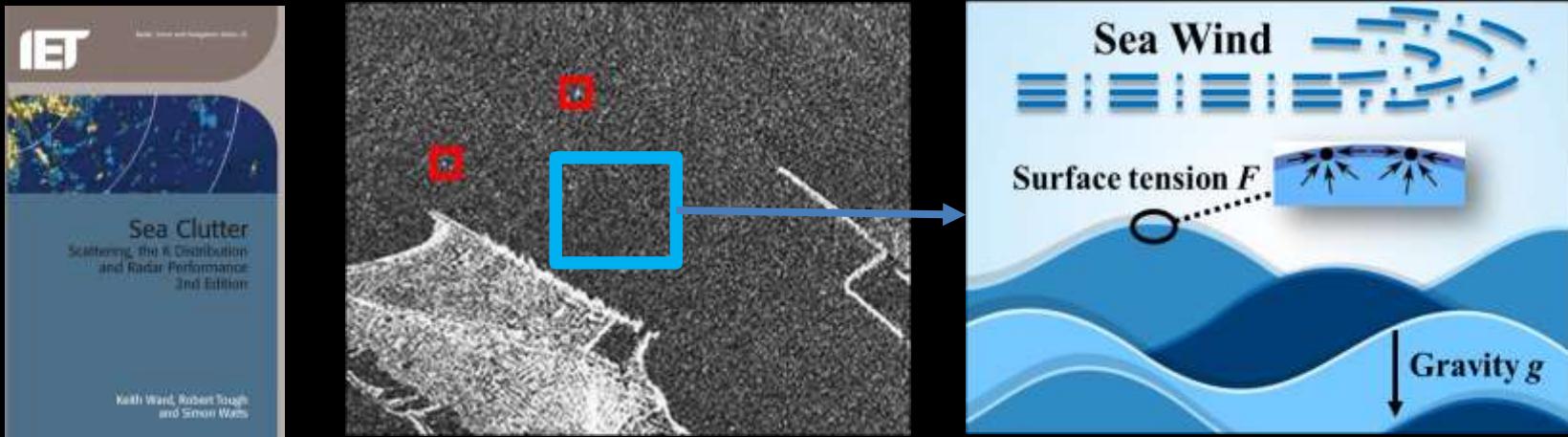


CLT: Insufficient

→ SLC non-Gaussian Vectors

→ Heterogeneous clutter

An Interesting Viewpoint about Heterogeneous Sea Clutter



- Sea surface waves can be decomposed into **dual** parts:
 - Surface tension wave
 - *micro scale*, fast-changing (millisecond order), i.e. *speckle*.
 - Gravity wave
 - *macro scale*, slow-changing (second order), i. e. *texture/modulation*.
- Heterogeneous sea clutter is amplitude modulation of tension wave signal by gravity wave signal.

Understanding of HR PolSAR Image



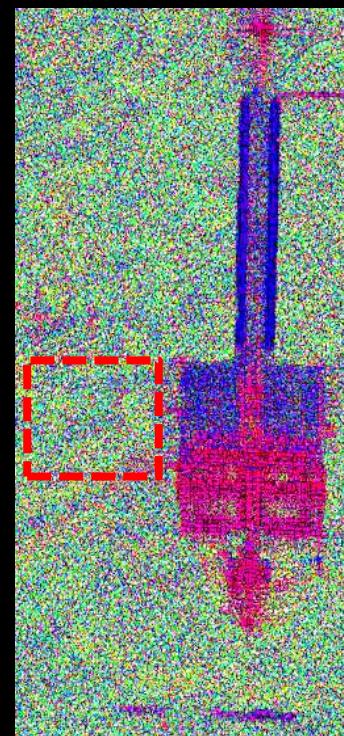
Complex Scattering Vectors

=



Texture
(RCS)

×



Complex Random Vectors
(Speckle)

$$k = \sqrt{\tau} z$$



Texture

Assumptions

- Sparse (visual-pleasing)
- Smooth (slow-changing)



Normalized Vectors

Assumptions

- Gaussian (easy to solve)
- Depolarization (relatively high)

SIRV Model

$$p(\mathbf{k}) = \frac{1}{(\pi\tau)^m |\mathbf{M}|} \exp\left(-\frac{\mathbf{k}^H \mathbf{M}^{-1} \mathbf{k}}{\tau}\right) \times p(\tau) d\tau$$

Gaussian Term **Non-Gaussian Term**
(Necessary conditions for solving inverse problems)

- \mathbf{M} : Second-order statistics of speckle
 - Complex correlation between channels
- τ : Non-negative scalar
 - Diverse and uncertain distributions

Likelihood 

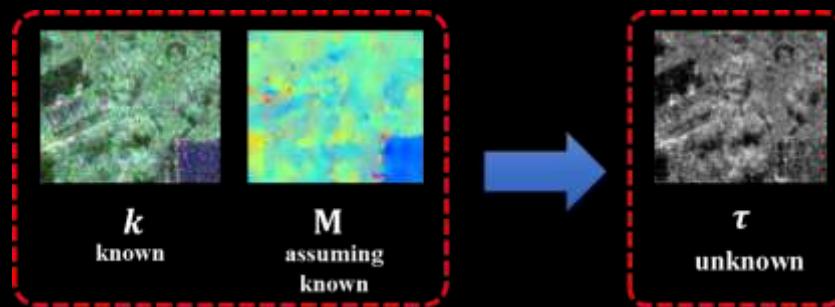
$$\begin{aligned} L(\mathbf{k}_1, \mathbf{k}_2, \dots, \mathbf{k}_N; \mathbf{M}) &= \prod_{i=1}^N p(\mathbf{k}_i; \mathbf{M}) \\ &= \prod_{i=1}^N \int_0^{+\infty} \frac{1}{(\pi\tau)^m |\mathbf{M}|} \exp\left(-\frac{\mathbf{k}_i^H \mathbf{M}^{-1} \mathbf{k}_i}{\tau}\right) \times p(\tau) d\tau \end{aligned}$$

$\tau - \mathbf{M}$ Iteration

- Fix \mathbf{M} , update τ :

- Likelihood

$$\ln L(\mathbf{k}_1, \mathbf{k}_2, \dots, \mathbf{k}_N; \tau_i | \mathbf{M}) = -N \cdot \ln |\mathbf{M}| - m \sum_{i=1}^N \ln(\pi \tau_i) - \sum_{i=1}^N \frac{\mathbf{k}_i^H \mathbf{M}^{-1} \mathbf{k}_i}{\tau_i}$$



- Estimation

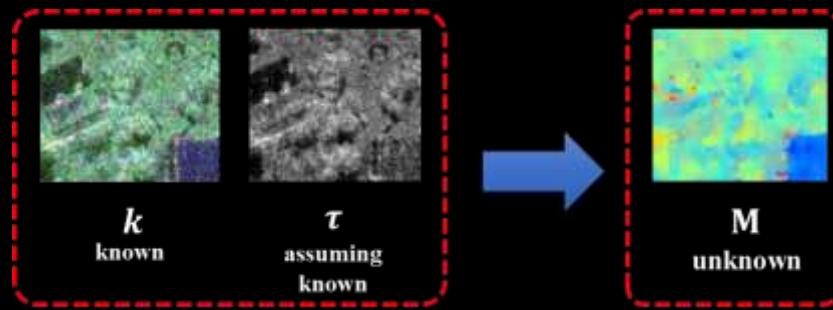
$$\begin{aligned} \frac{\partial \ln L(\mathbf{k}_1, \mathbf{k}_2, \dots, \mathbf{k}_N; \tau_i | \mathbf{M})}{\partial \tau_i} &= 0 \quad \longrightarrow \quad -m \sum_{i=1}^N \frac{1}{\tau_i} + \sum_{i=1}^N \frac{\mathbf{k}_i^H \mathbf{M}^{-1} \mathbf{k}_i}{\tau_i^2} = 0 \\ &\longrightarrow \quad \hat{\tau}_i = \frac{\mathbf{k}_i^H \mathbf{M}^{-1} \mathbf{k}_i}{m} \end{aligned}$$

$\tau - \mathbf{M}$ Iteration

- Fix τ , update \mathbf{M} :

- Likelihood

$$\ln L(\mathbf{k}_1, \mathbf{k}_2, \dots, \mathbf{k}_N; \mathbf{M} | \tau_1, \tau_2, \dots, \tau_N) = -N \cdot \ln |\mathbf{M}| - m \sum_{i=1}^N \ln(\pi \tau_i) - \sum_{i=1}^N \frac{\mathbf{k}_i^H \mathbf{M}^{-1} \mathbf{k}_i}{\tau_i}$$



- Estimation

$$\frac{\partial \ln L(\mathbf{k}_1, \mathbf{k}_2, \dots, \mathbf{k}_N; \mathbf{M} | \tau_1, \tau_2, \dots, \tau_N)}{\partial \mathbf{M}} = 0 \quad \xrightarrow{\hspace{1cm}} \quad -N \cdot \mathbf{M}^{-1} - \sum_{i=1}^N \frac{-\mathbf{k}_i \mathbf{k}_i^H \mathbf{M}^{-2}}{\tau_i} = 0$$

$$\xrightarrow{\hspace{1cm}} \quad \widehat{\mathbf{M}} = \frac{1}{N} \sum_{i=1}^N \frac{\mathbf{k}_i \mathbf{k}_i^H}{\tau_i}$$

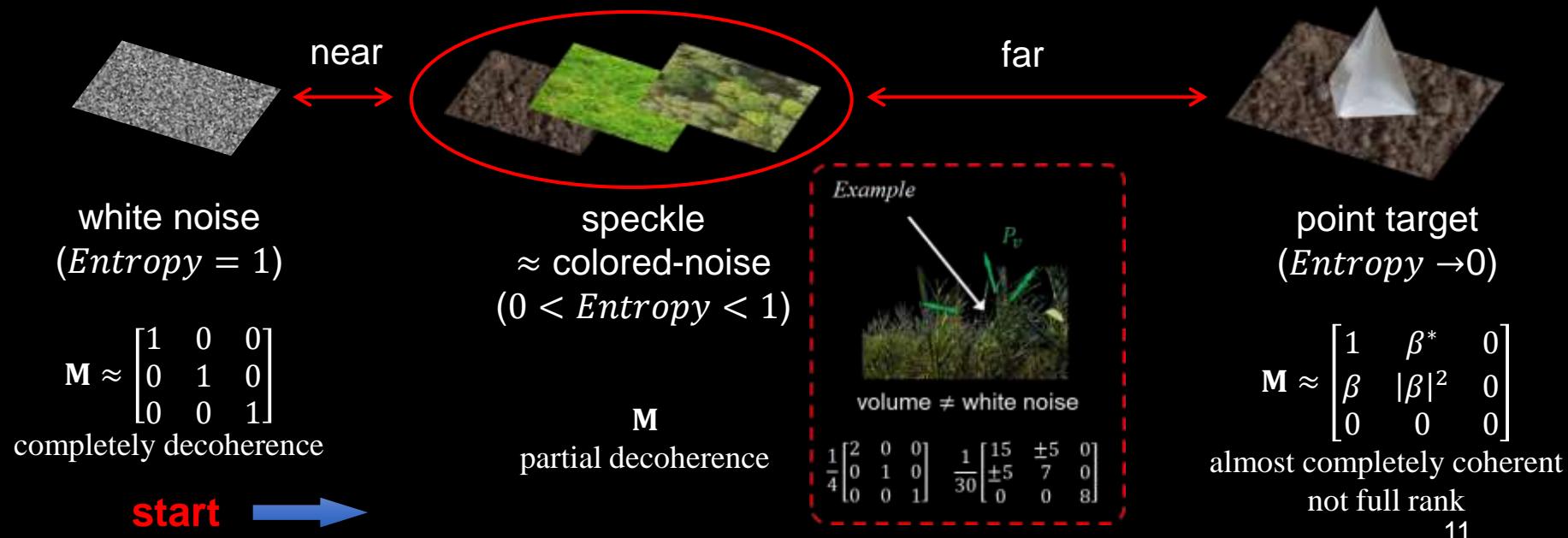
$\tau - \mathbf{M}$ Iteration

- Fixed point iteration (SIRV estimator)

$$\widehat{\mathbf{M}}(j+1) = \frac{m}{N} \sum_{i=1}^N \frac{\mathbf{k}_i \mathbf{k}_i^H}{\mathbf{k}_i^H \widehat{\mathbf{M}}^{-1}(j) \mathbf{k}_i} \xrightarrow{\text{Generalization}} \widehat{\mathbf{M}}(j+1) = \frac{m}{N} \sum_{i=1}^N \frac{\mathbf{T}_i}{\text{Tr}(\widehat{\mathbf{M}}^{-1}(j) \mathbf{T}_i)}$$

L-look case: \mathbf{T}

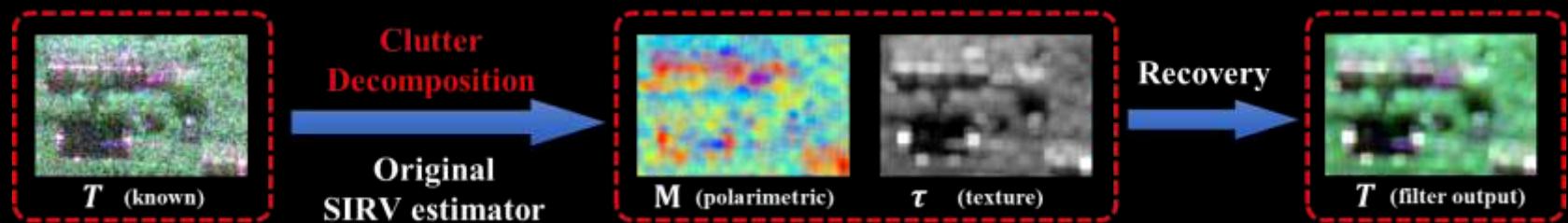
- Iteration initialization



Clutter Decomposition Problem

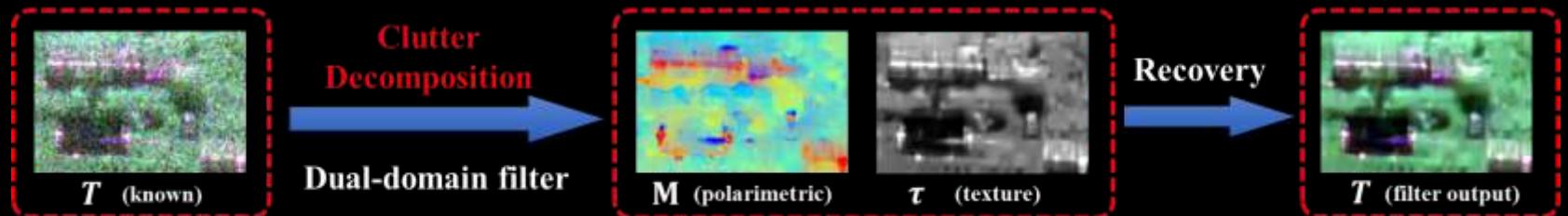
- Using original SIRV estimator
 - Showing poor performance

Problem is not solved

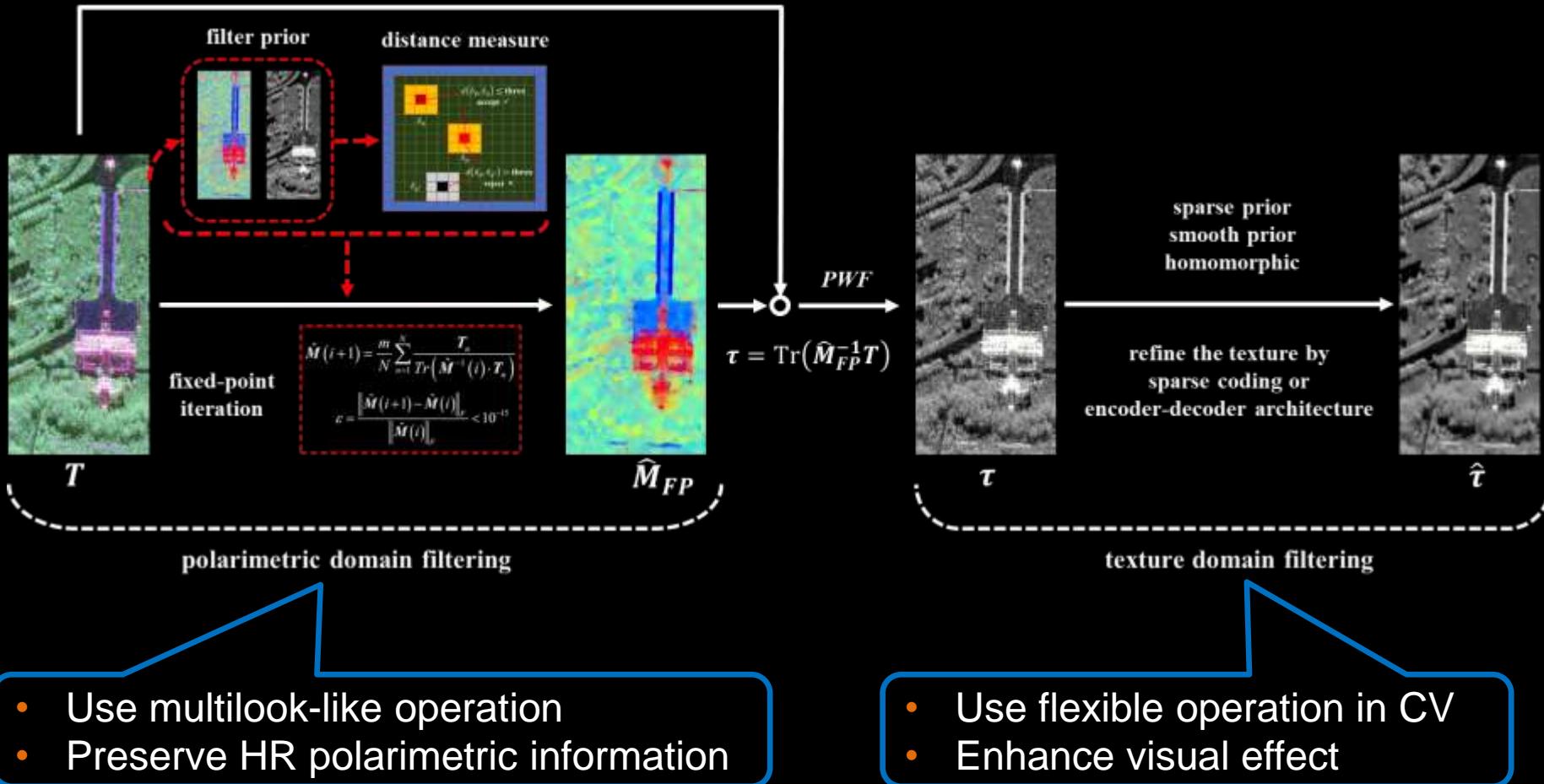


- Using dual-domain filter
 - Showing technical superiority

Problem is largely solved

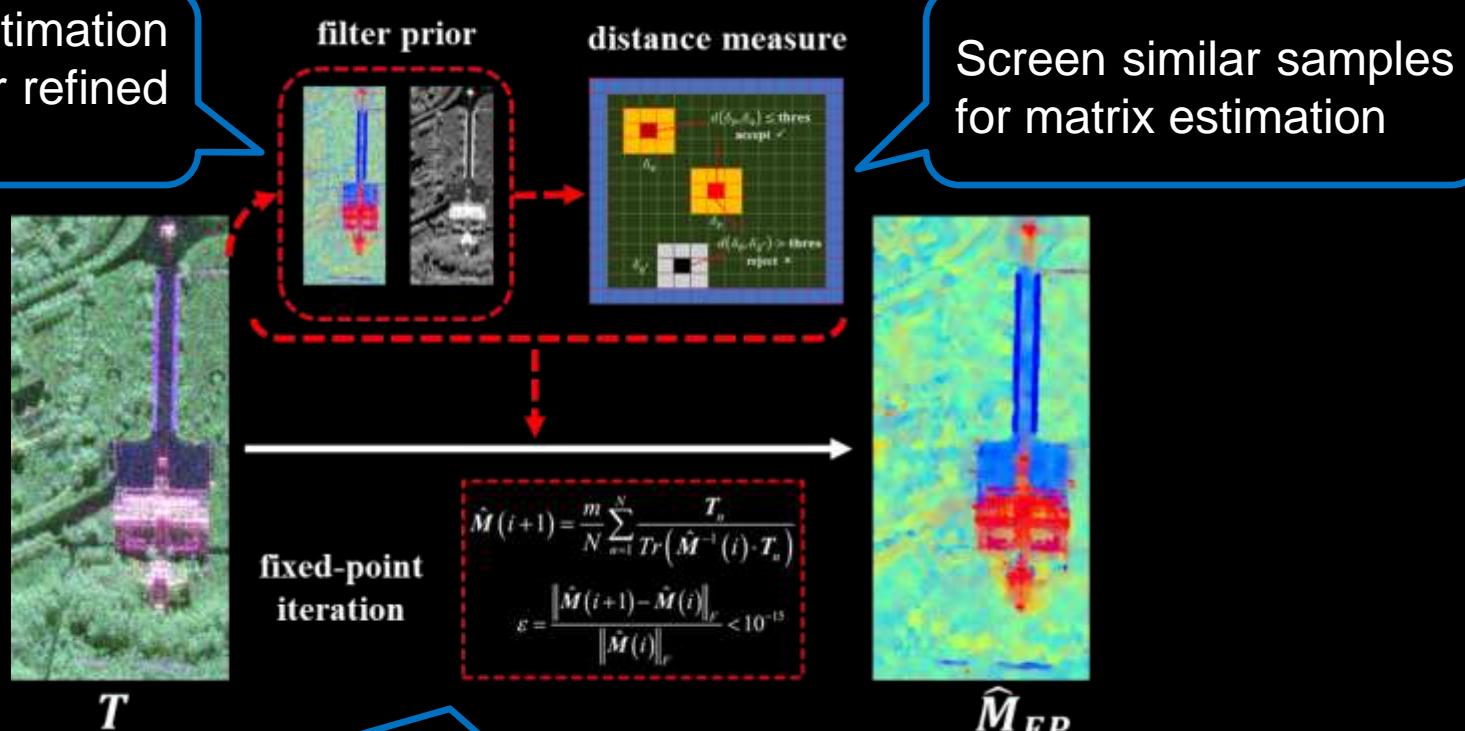


Clutter Decomposition and Dual-domain Filtering



Polarimetric Domain Filtering

Using rough estimation
as filter prior for refined
estimation

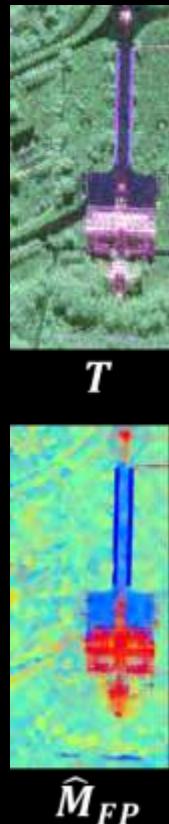


Screen similar samples
for matrix estimation

Eliminating data scale/level caused by texture fluctuations in
Coherency Estimation.

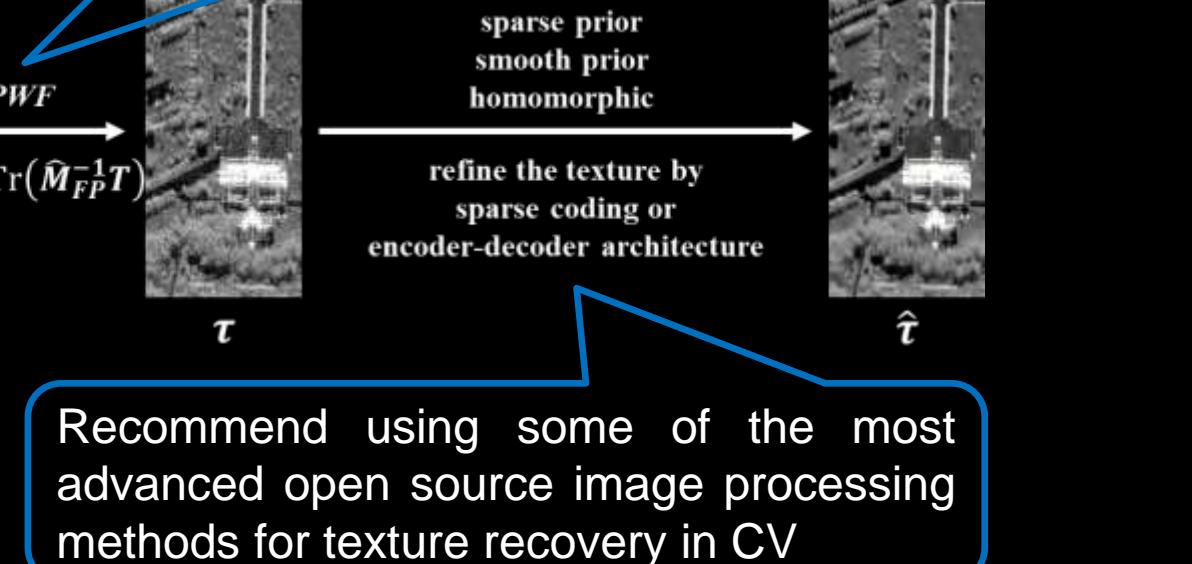
Remark: Each iteration **strictly** obeys Lee's three filtering principles to preserve polarimetric scattering information, especially consistency of correlation and phase difference.

Texture Domain Filtering



PWF: key connection between two filters

- separate polarimetric information
- **speckle decorrelation** (meaningless pure noise)
- improve SCR without loss of resolution (2.7 dB gain)

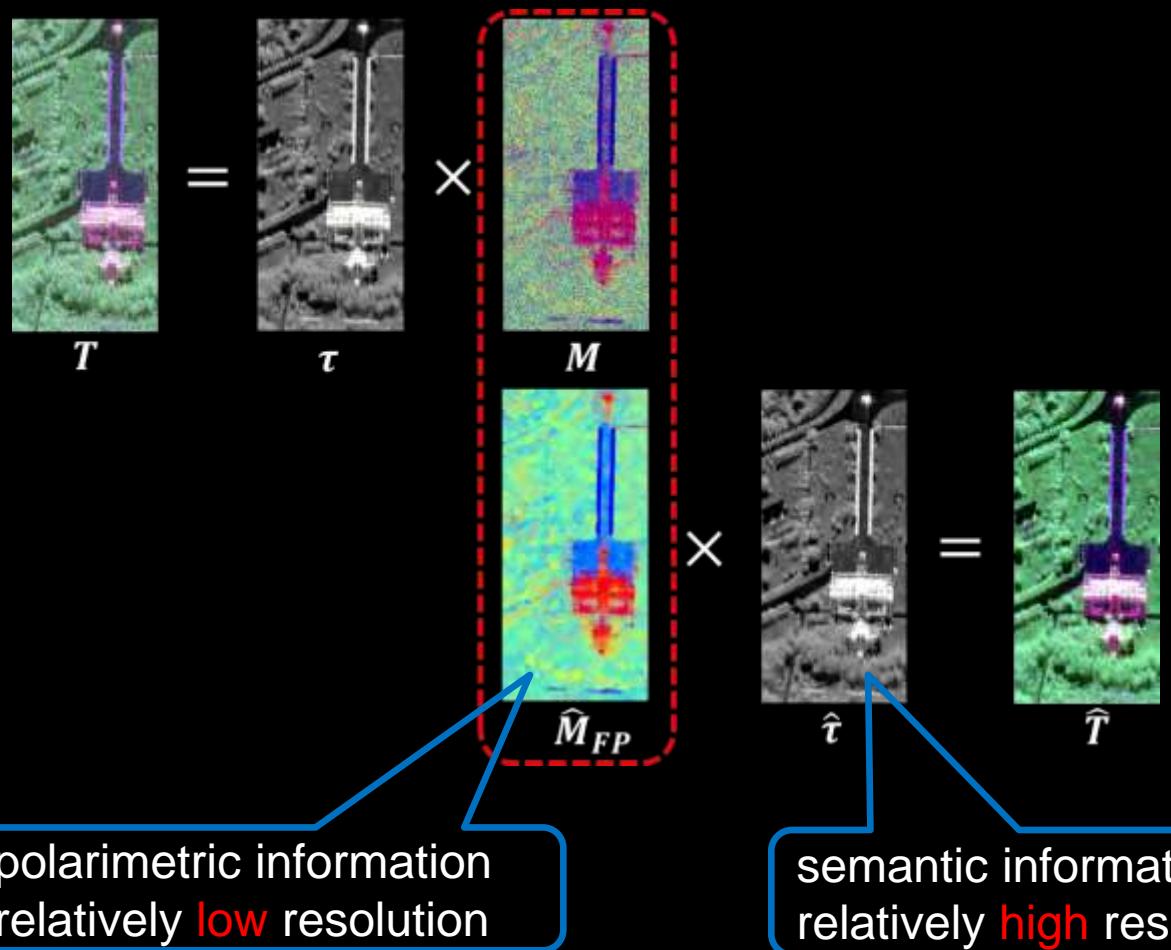


Recommend using some of the most advanced open source image processing methods for texture recovery in CV

Remark: SOTA methods in CV can be **flexibly** applied for texture image processing, including sparse coding and NN-based encoder -decoder methods.

Dual-domain Fusion

- HR PolSAR recovery is an image fusion problem



Mixed Distance Measure

- Integrating texture and polarization information

$$d_m = \frac{1}{K} \sum_k^K \left[(1 - \alpha) \left[\frac{1}{2} \left(\frac{\tilde{\tau}_{\delta_p(k)}}{\tilde{\tau}_{\delta_q(k)}} + \frac{\tilde{\tau}_{\delta_q(k)}}{\tilde{\tau}_{\delta_p(k)}} \right) - 1 \right] + \alpha \left[1 - \frac{\text{Tr}(\tilde{\mathbf{M}}_{\delta_p(k)} \tilde{\mathbf{M}}_{\delta_q(k)})}{\sqrt{\text{Tr}(\tilde{\mathbf{M}}_{\delta_p(k)} \tilde{\mathbf{M}}_{\delta_p(k)}) \text{Tr}(\tilde{\mathbf{M}}_{\delta_q(k)} \tilde{\mathbf{M}}_{\delta_q(k)})}} \right] \right]$$

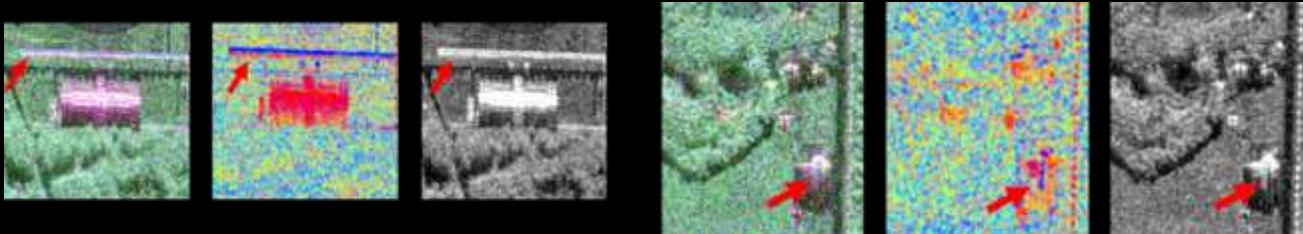
texture info.

multiplicative noise (ratio)

polarimetric info.

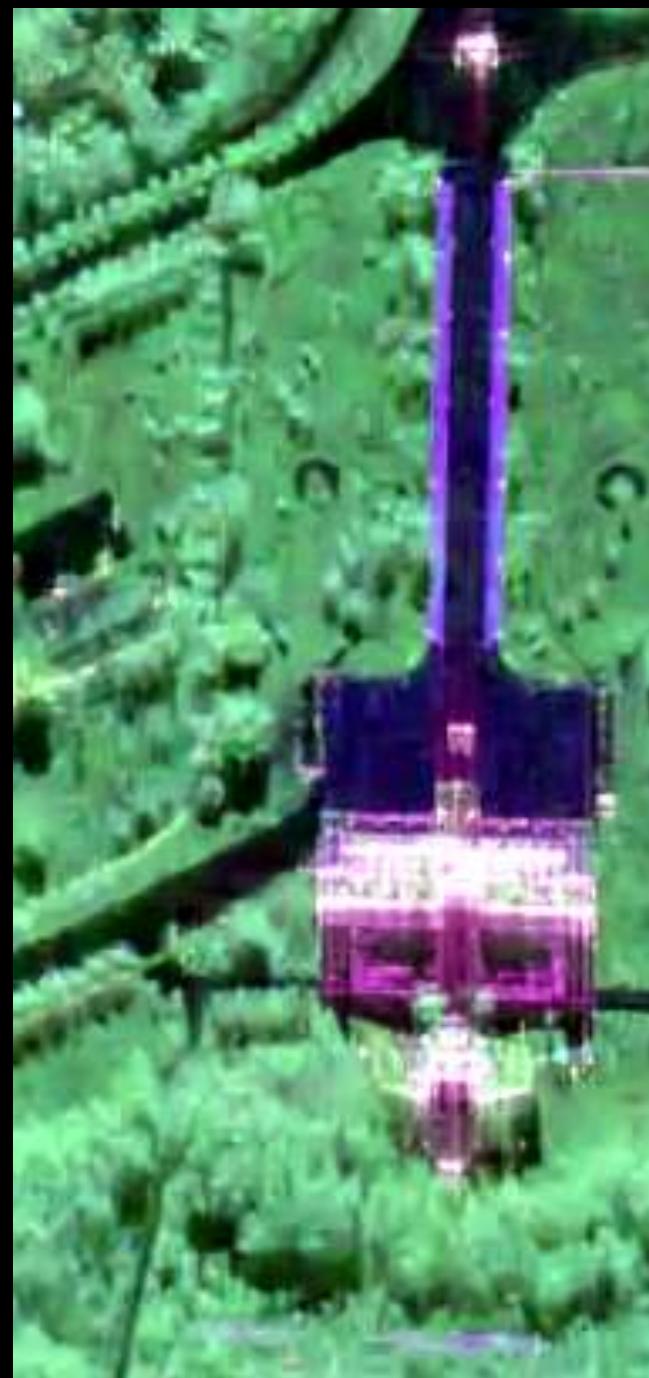
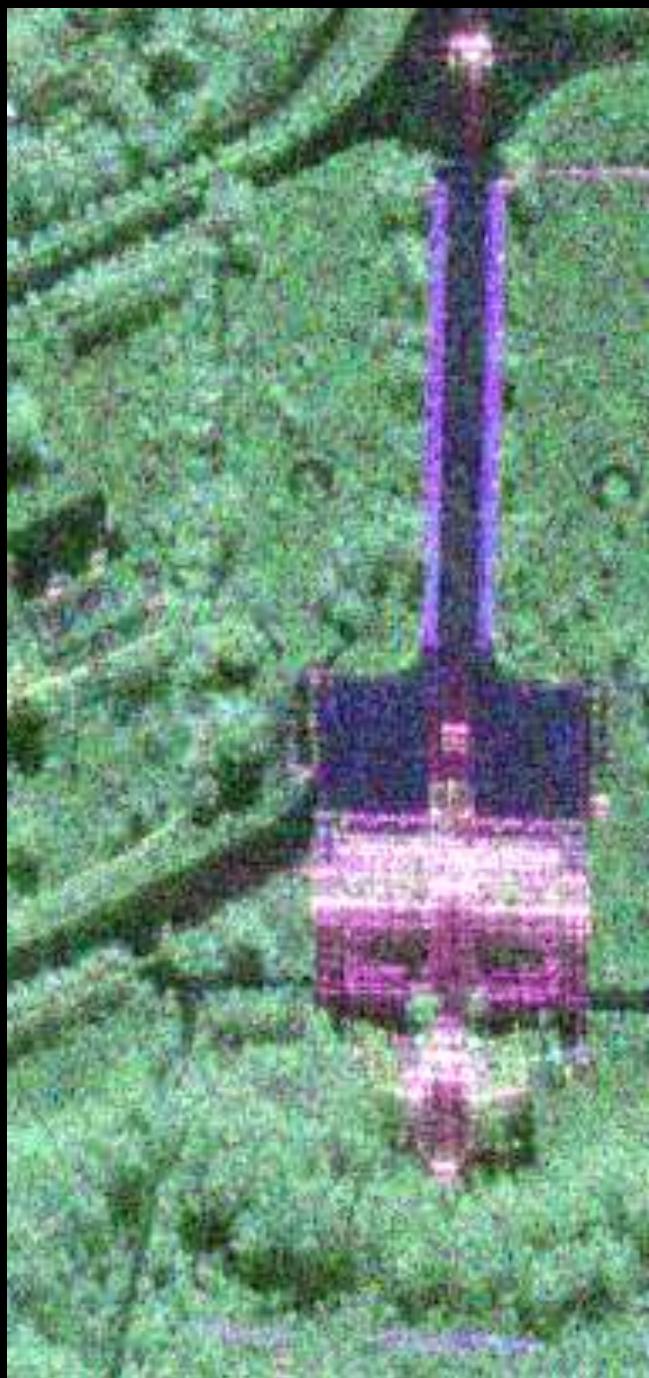
no need for **full rank rotation invariant**

- Phenomenon: targets with the similar texture but different polarimetric properties
 - the coefficient alpha can be slightly larger than 0.5, such as 0.6
 - $\ln Q$ is greatly affected by power/SPAN values
 - d_m use more information in sample screening

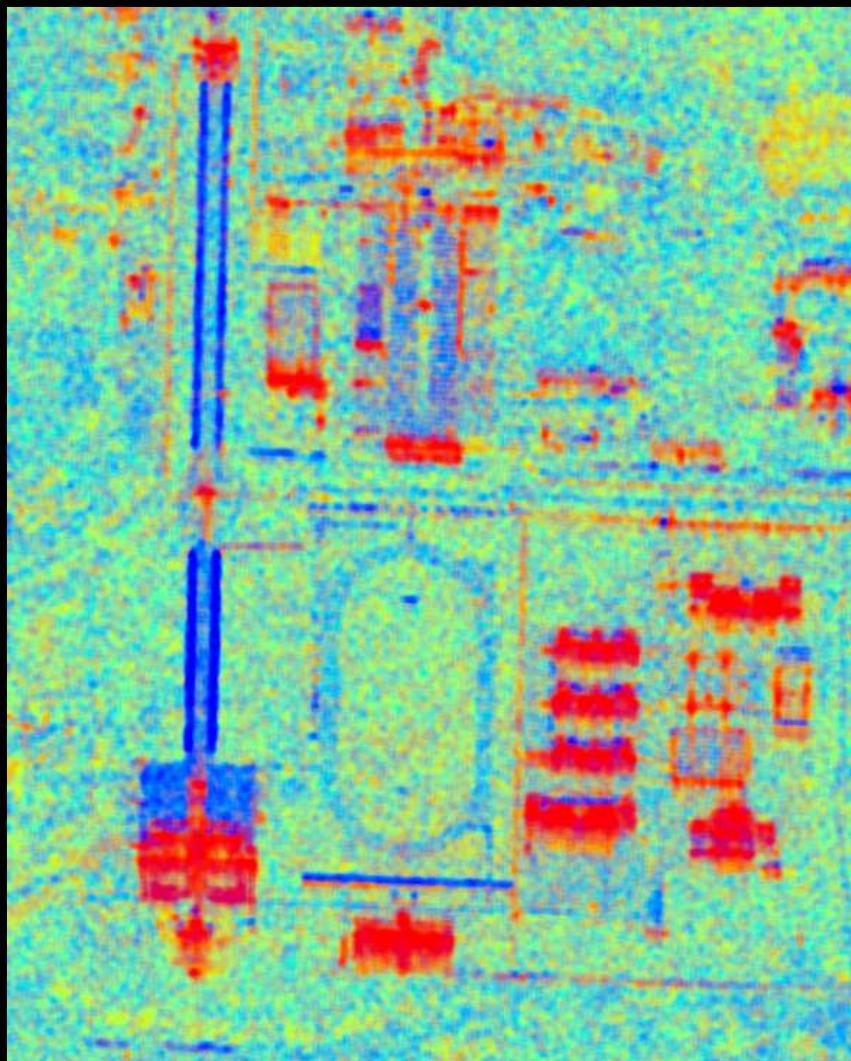


Results: CETC-38 X-PolSAR Data, Hainan Lingshui

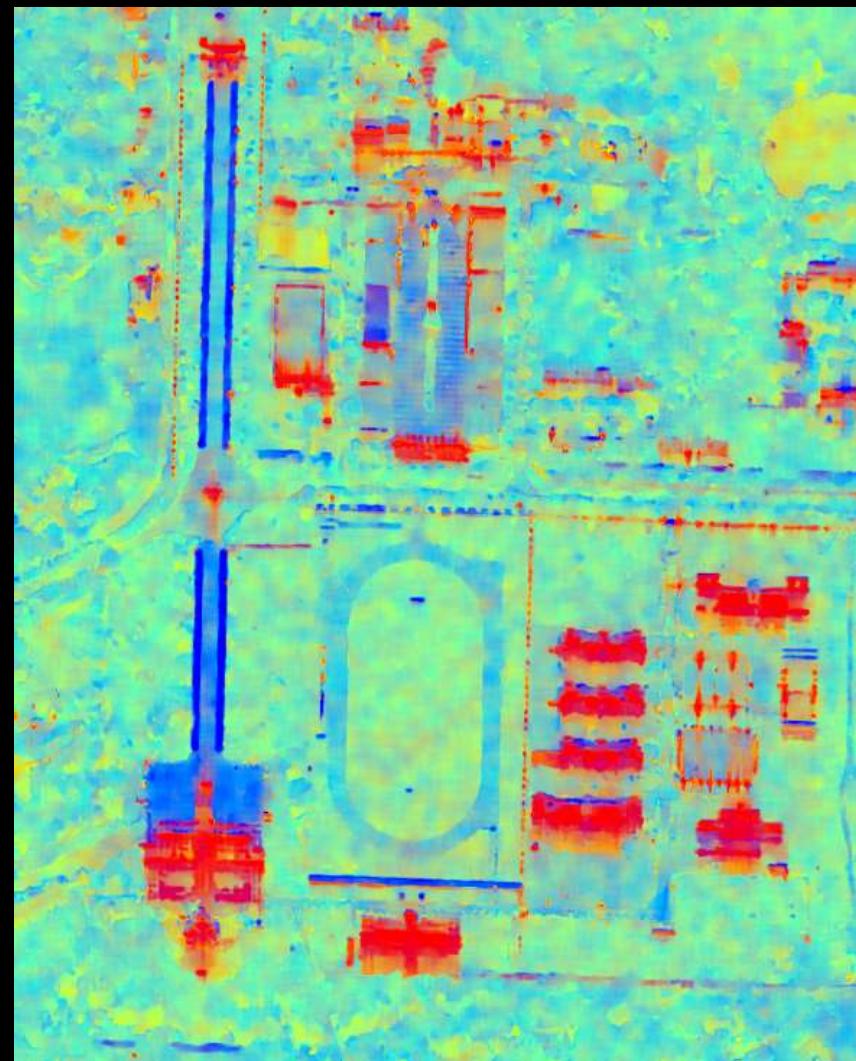




Results: Normalized Coherency Matrix



Original 7×7 SIRV estimator



Dual-domain filter result

Results: CETC-38 X-PolSAR Data, Hainan Lingshui



Before filtering



After filtering

Results: DLR FSAR S-PoISAR Data, Kaufbeuren

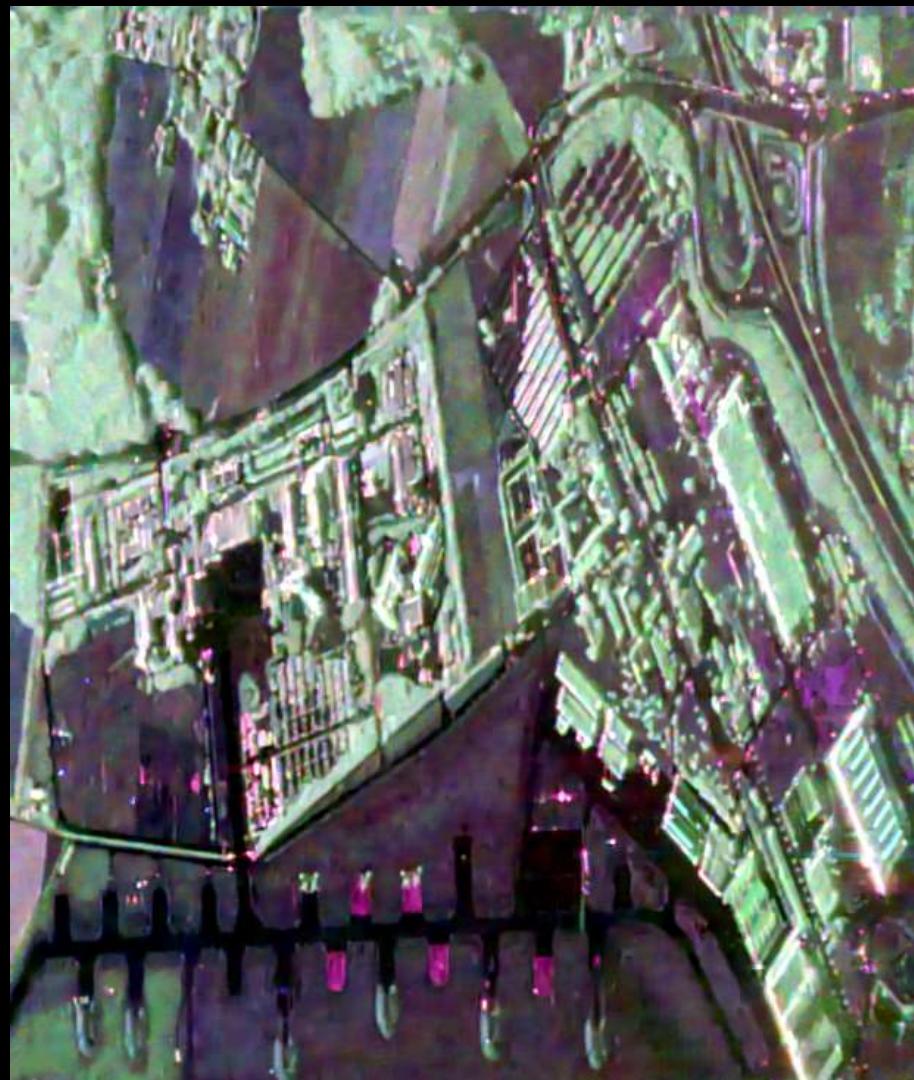
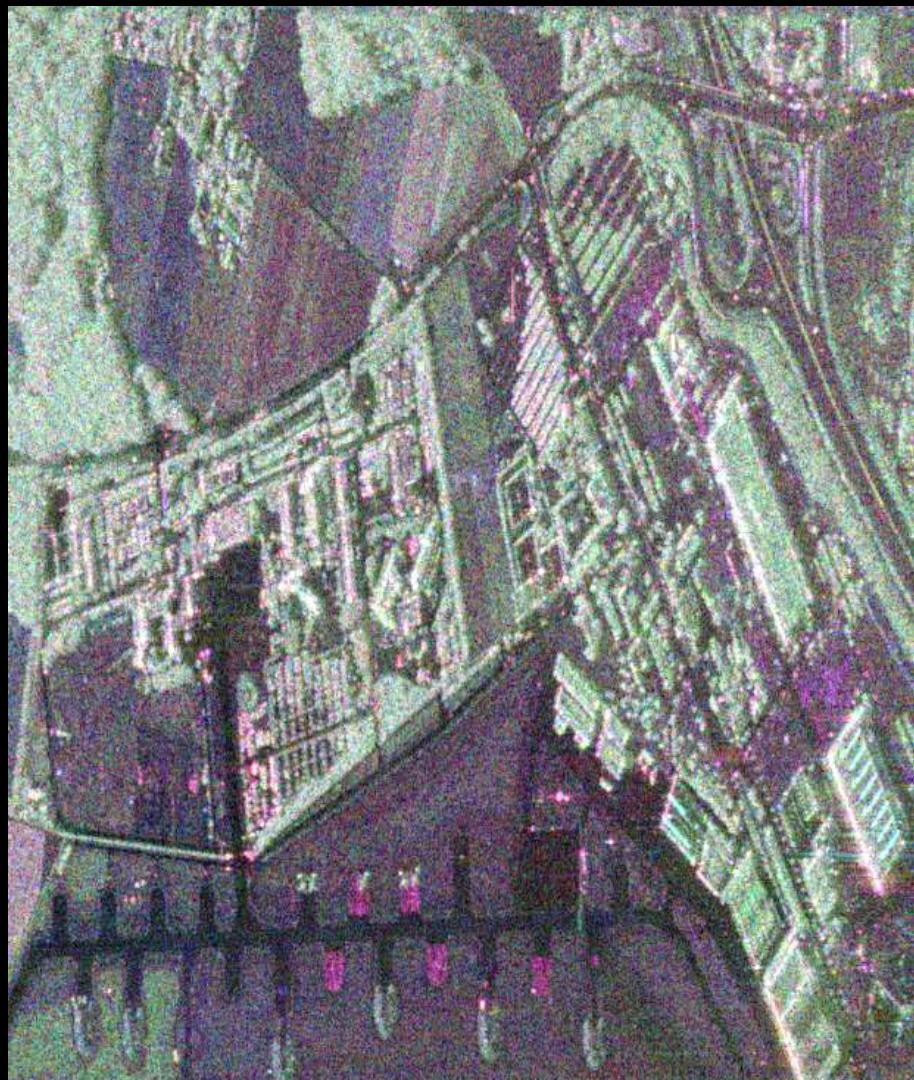




Results: AIRCAS C-PolSAR Data, Hebei Zunhua



Results: DLR ESAR L-SAR Oberpfaffenhofen



Results: GF-3 Sea Wave Recovery



Results: GF-3 City, Xi An



Single Look
Complex

Results: GF-3 City, Xi An



Filtering
Result

Comparisons

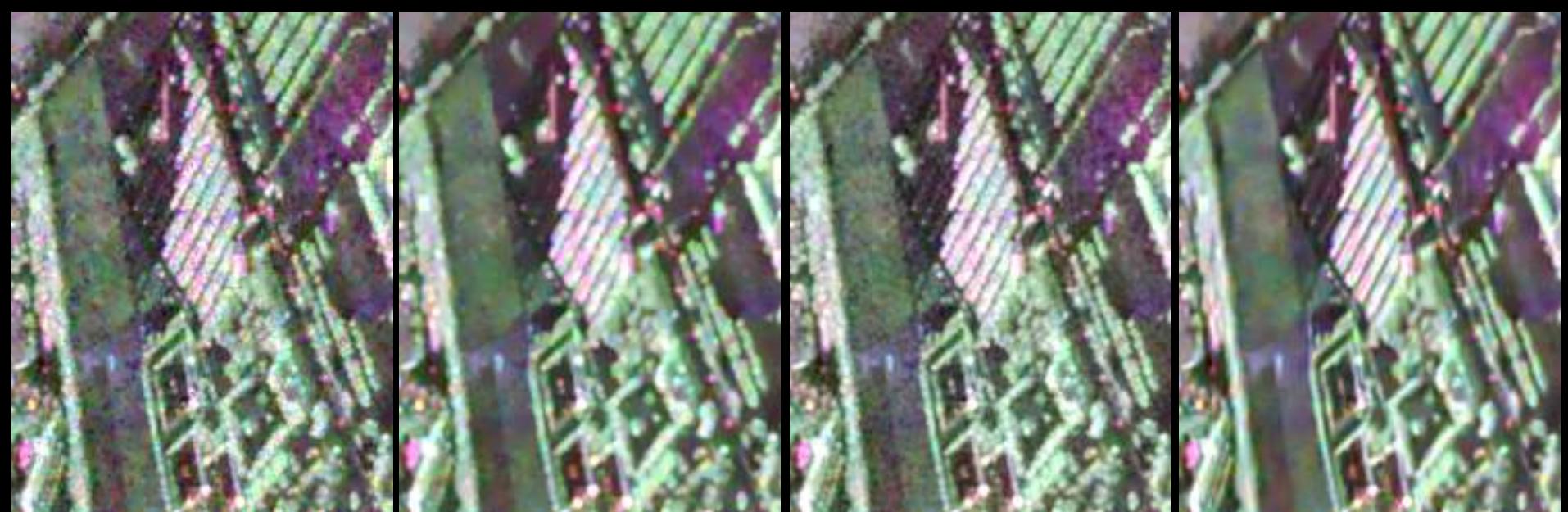


Improved Sigma

Nonlocal pretest

Mean shift

Dual-domain



Improved Sigma

Nonlocal pretest

Mean shift

Dual-domain
30

Separated Multiplicative Noise (Ratio Image)

CETC-38 X-band data	$E_r[T_{11}]$	$E_r[T_{22}]$	$E_r[T_{33}]$	$SD_r[T_{11}]$	$SD_r[T_{22}]$	$SD_r[T_{33}]$
Improved sigma	0.8702	0.8719	0.8802	0.5879	0.5967	0.5983
Nonlocal pretest	0.9006	0.8992	0.9197	0.9174	0.9183	0.9110
Mean shift	0.7846	0.7843	0.8058	0.9403	0.9824	0.9603
Dual-domain filter	0.9906	0.9913	0.9909	1.0020	1.0094	0.9997
F-SAR S-band data	$E_r[T_{11}]$	$E_r[T_{22}]$	$E_r[T_{33}]$	$SD_r[T_{11}]$	$SD_r[T_{22}]$	$SD_r[T_{33}]$
Improved sigma	0.8904	0.8928	0.8936	0.5555	0.5630	0.5603
Nonlocal pretest	0.9034	0.8961	0.9041	0.7755	0.7780	0.7731
Mean shift	0.8855	0.8807	0.8752	0.7817	0.7835	0.7327
Dual-domain filter	1.0031	1.0303	1.0403	0.9344	0.9654	0.9699

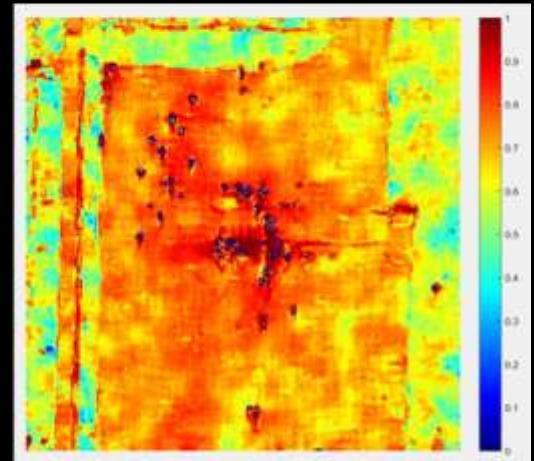
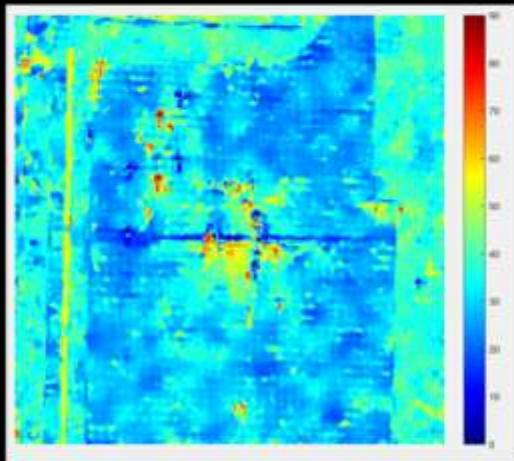
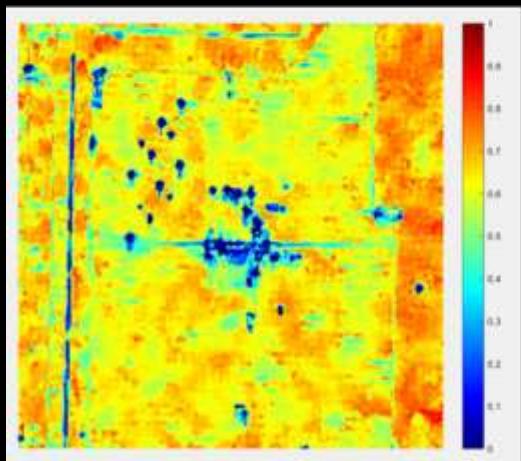
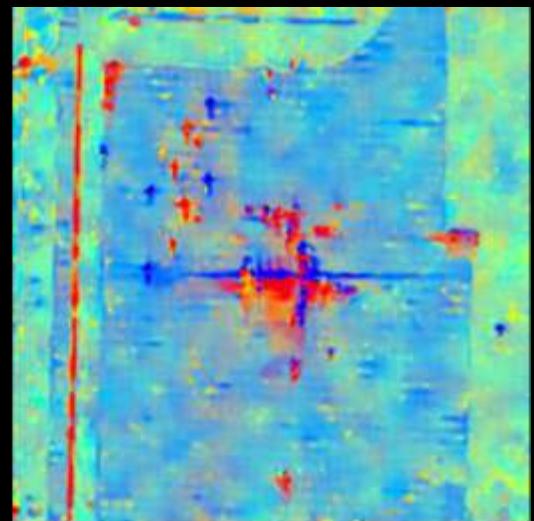
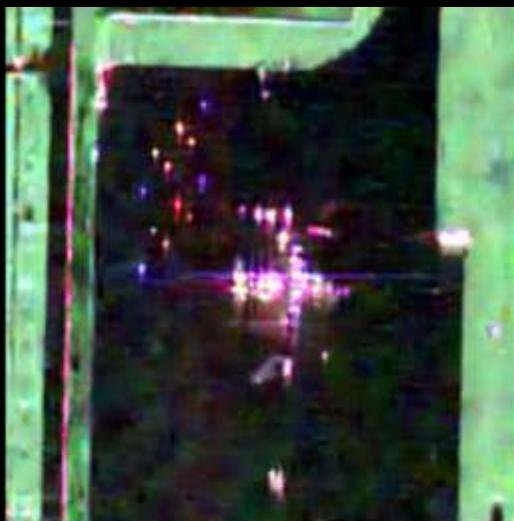
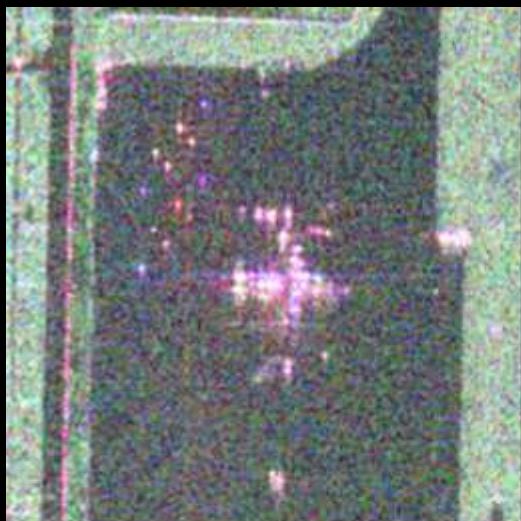
$$E_r = \frac{1}{N} \sum_{n=1}^N \left(\frac{I_0}{I_1} \right)_n, SD_r = \sqrt{\frac{1}{N} \sum_{n=1}^N (r_n - 1)^2}$$

- Calculate on 1000×800 single-look PolSAR image

Theoretical value: $E_r = 1; SD_r = \sqrt{1/look} = 1$.

If E_r deviates too much from 1, it shows radiation distortion.
If SD_r far less than 1 , the speckle suppression is not complete.
If SD_r is greater than the theoretical value, the results deviate from the true RCS.

Point Targets Preservation

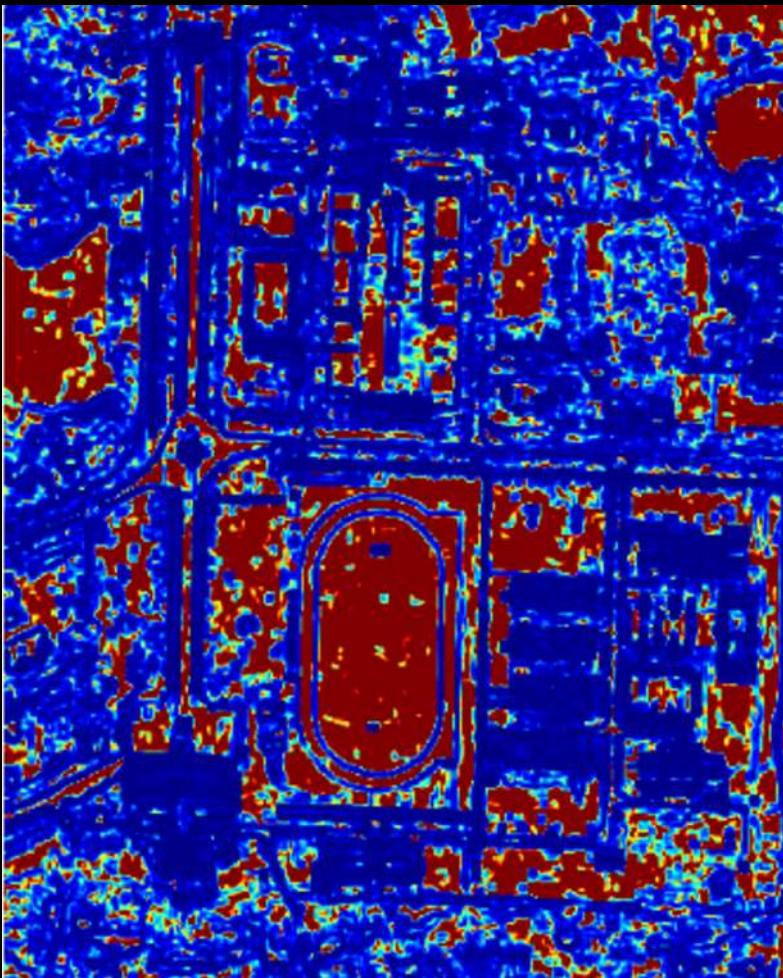
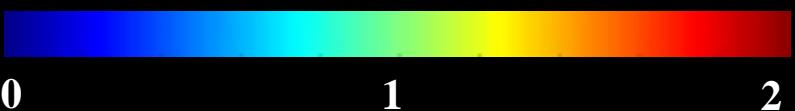
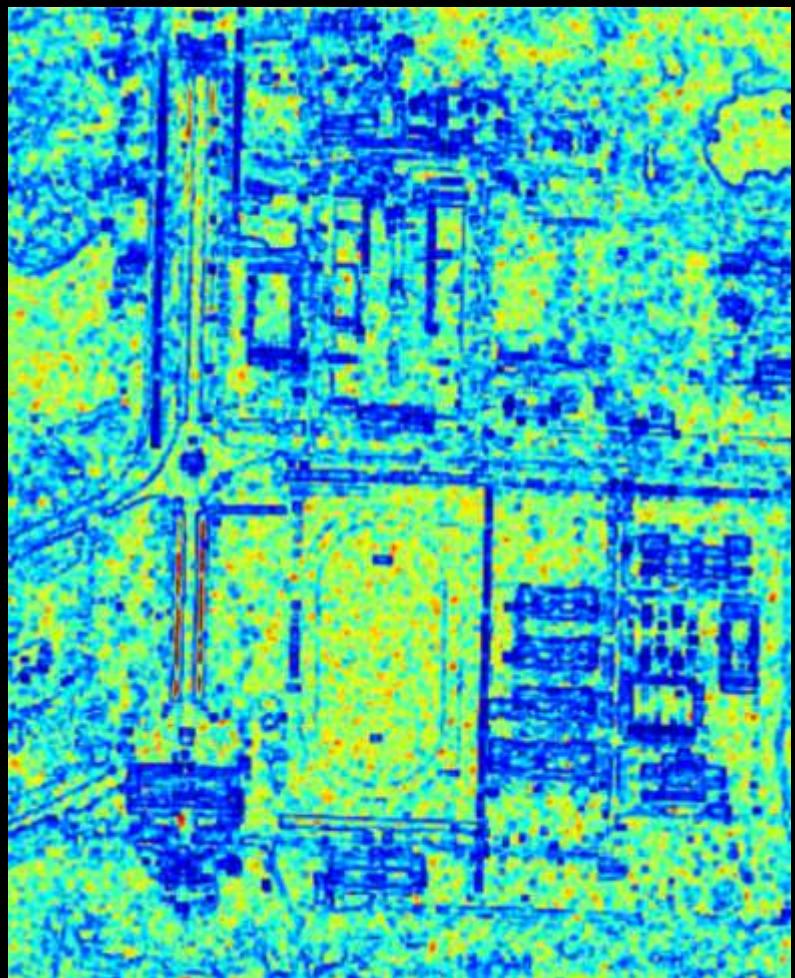


H

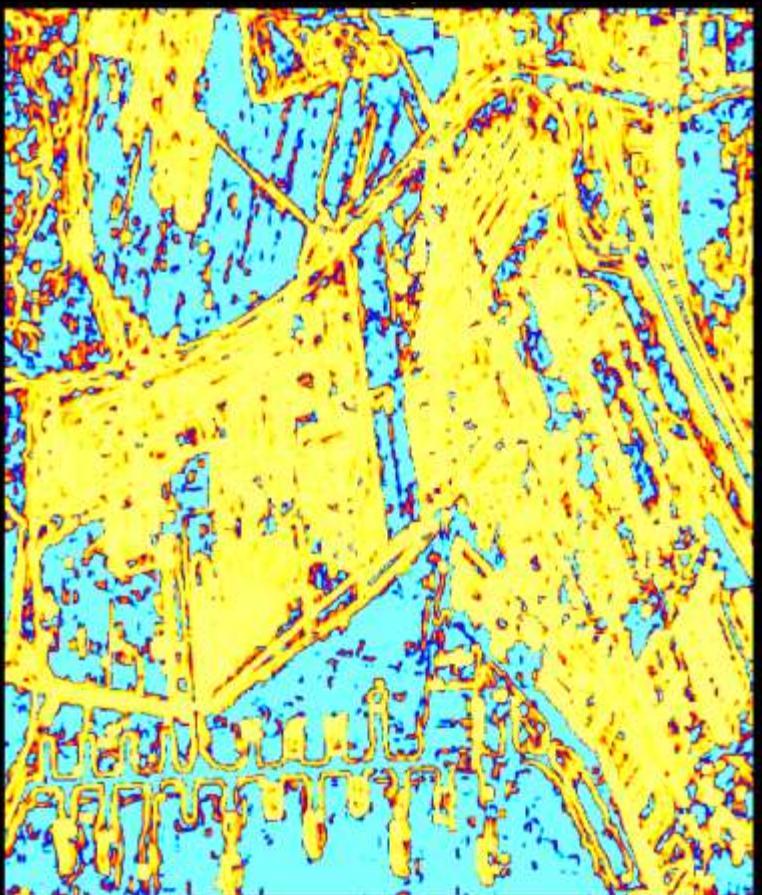
Alpha

A

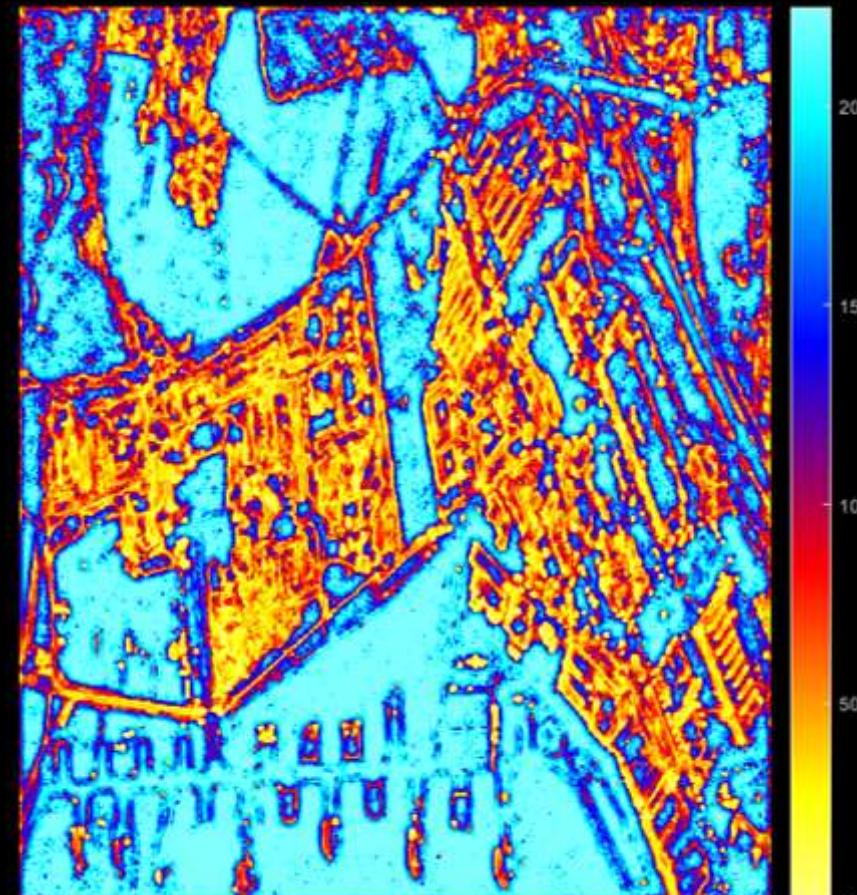
Tm-ENL: From 1 to 100



By-product: High-Resolution Heterogeneity

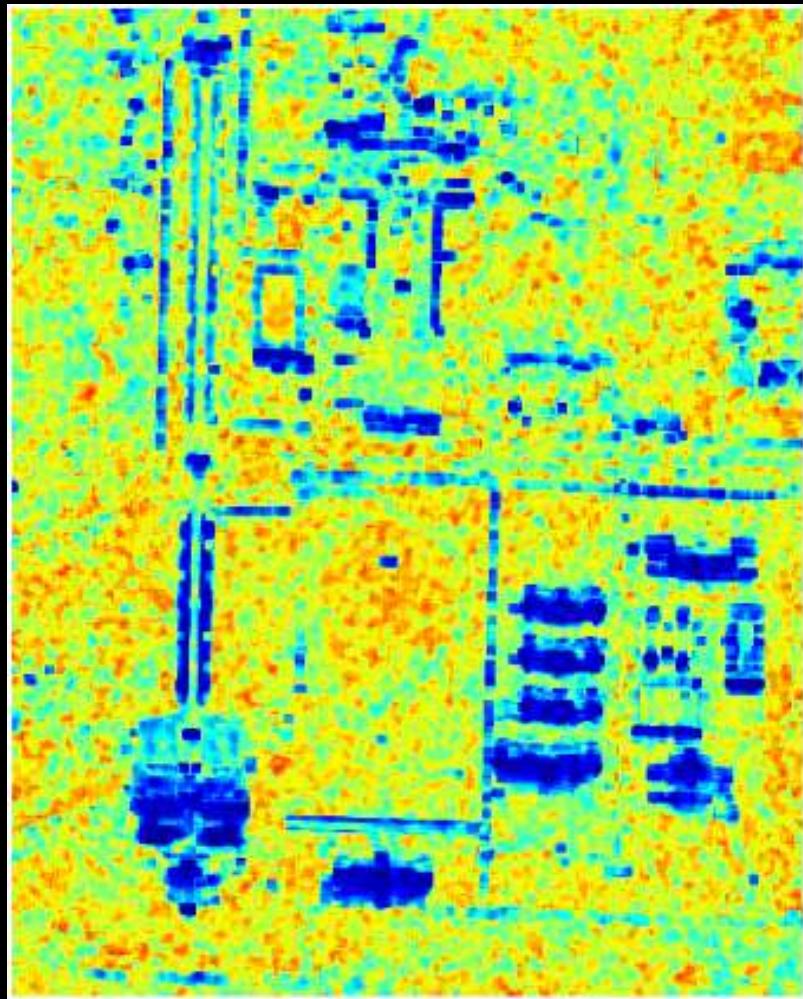


Trace-moment ENL
(Low-Resolution)

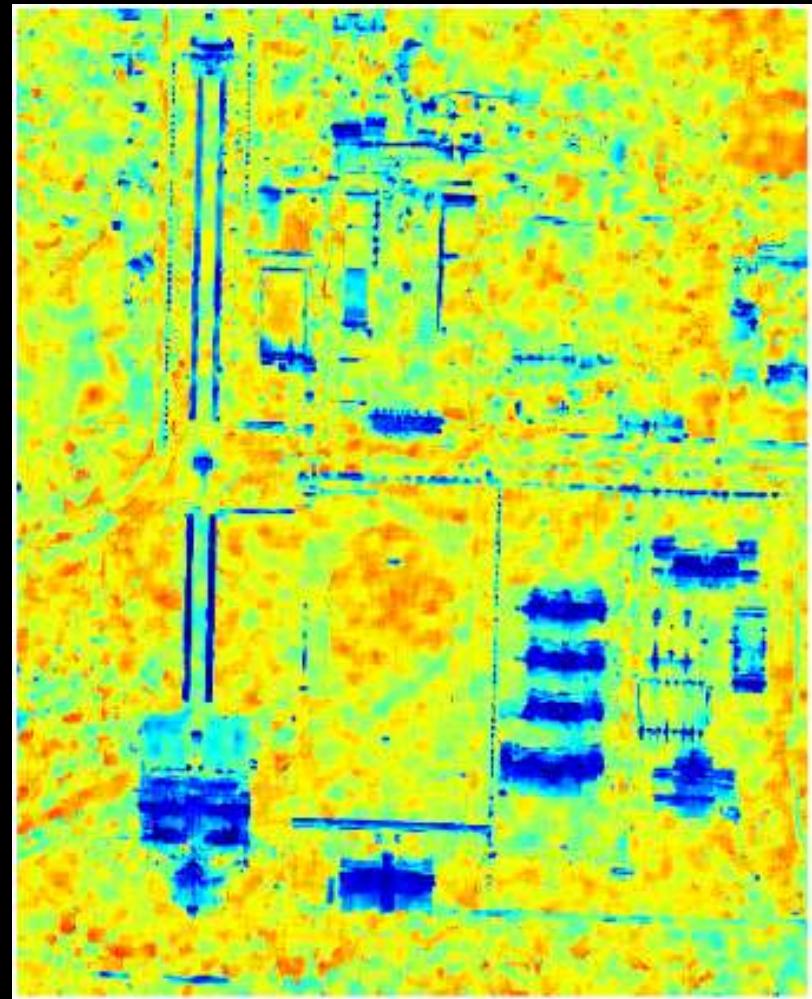


The number of similar samples
(polarimetric domain filtering)

By-product: High-Resolution H/alpha/A



81-look



SIRV based dual-domain filter

By-product: Texture Extraction

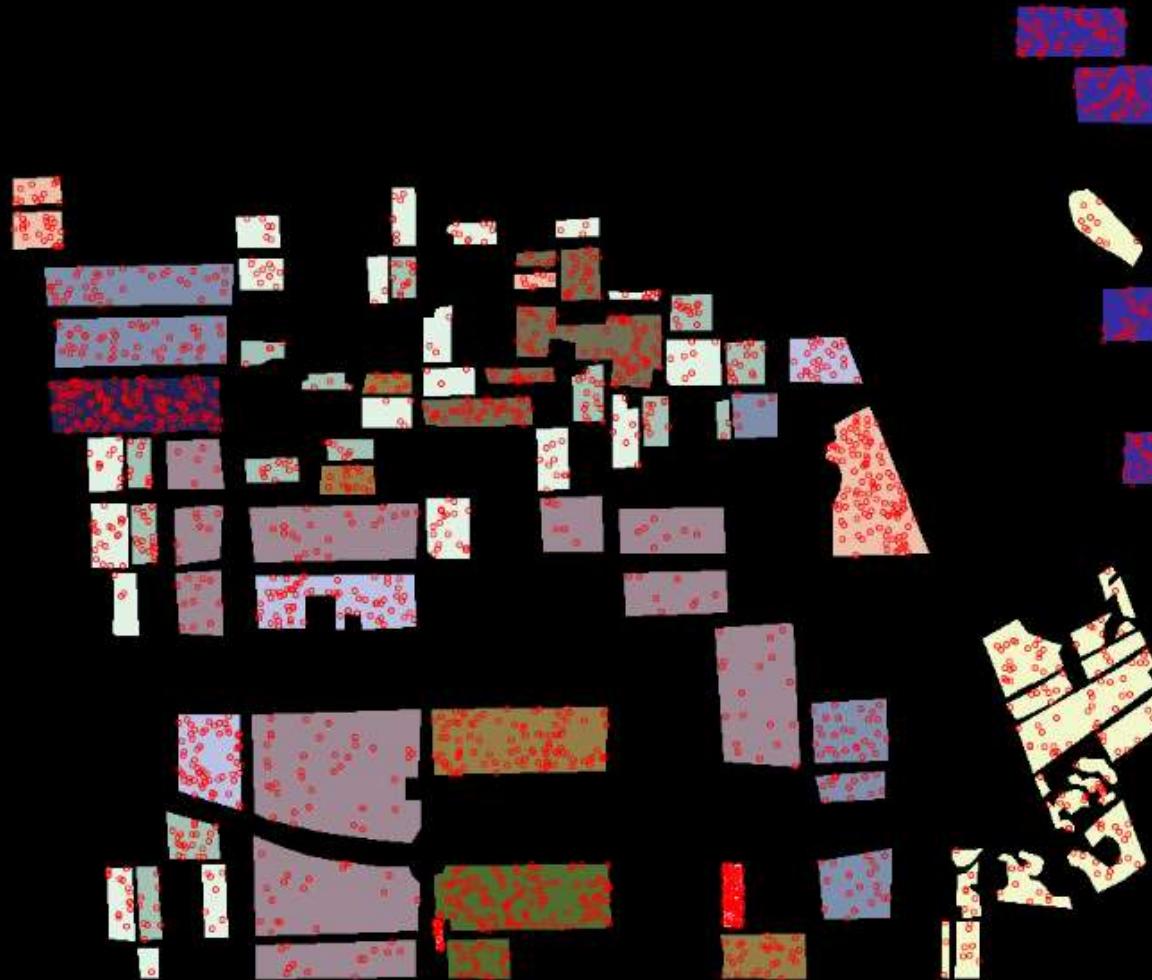


natural clutter
(before dual-domain filtering)



almost no natural clutter
(after dual-domain filtering) 36

Application: Dual-domain filter + PolSAR Classification



Groundtruth + Randomly select 150 training pixels for each class

Application: Dual-domain filter + PolSAR Classification



Felevoland

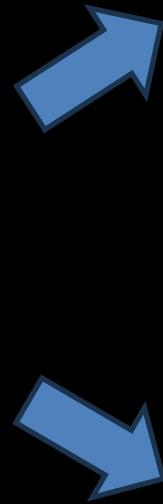
Accuracy: 0.9822
Kappa: 0.9795

Directly use RF without any feature extraction

Application: Dual-domain filter + PolSAR Classification



Pauli-RGB block of original PolSAR data



Dual-domain Filter+classifier



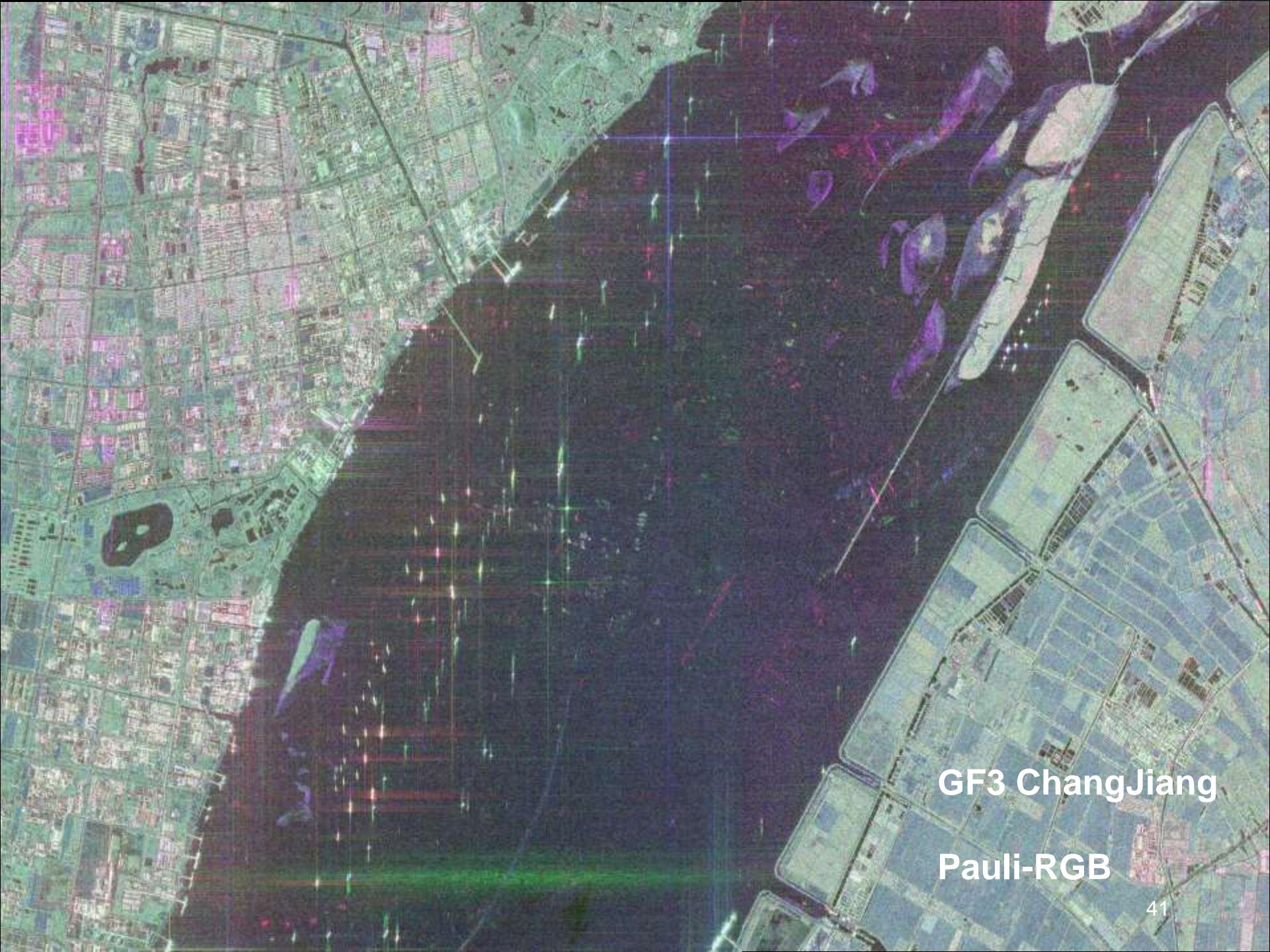
Boxcar 5*5+classifier

Application: Dual-domain filter + Improved FDD3



GF-3 Xi'An

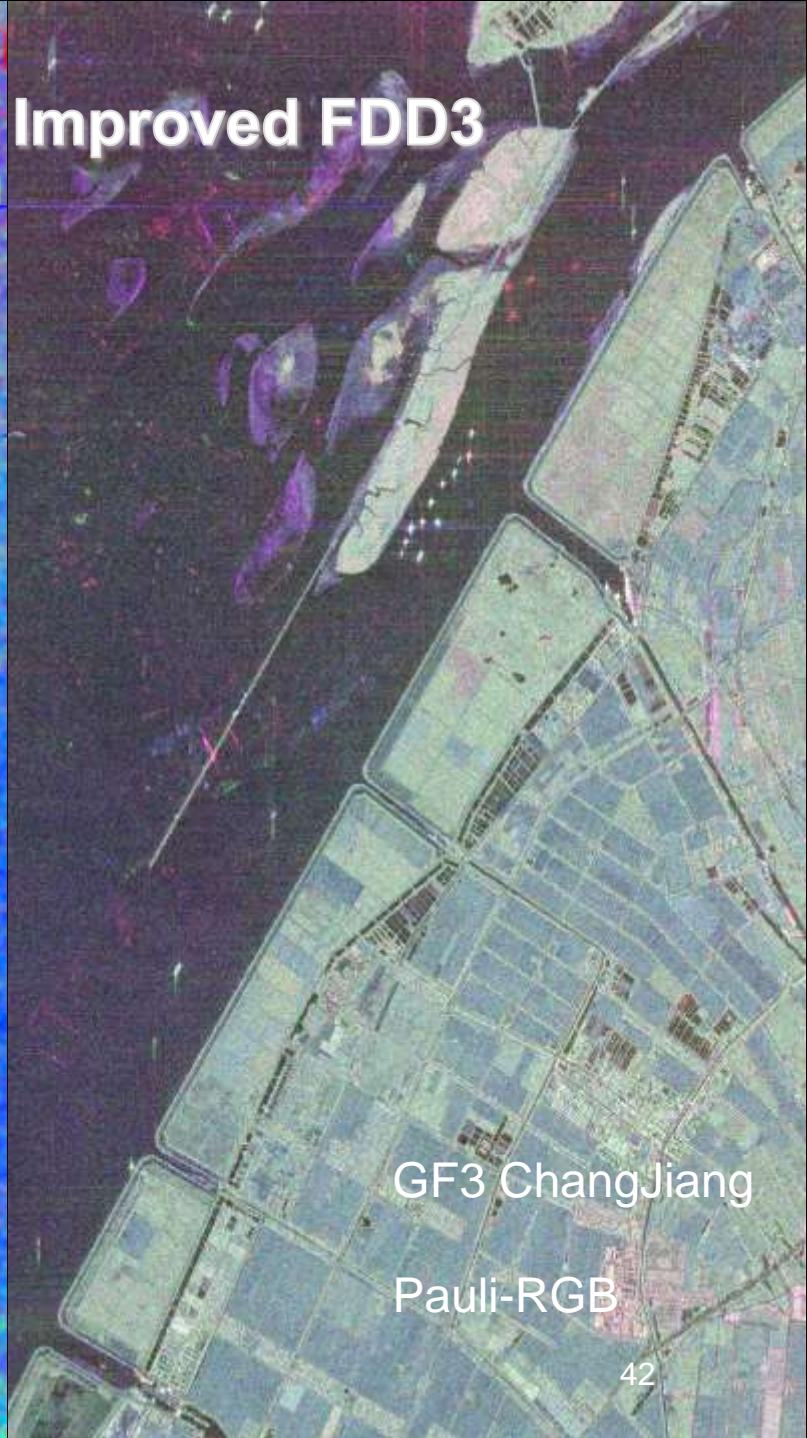
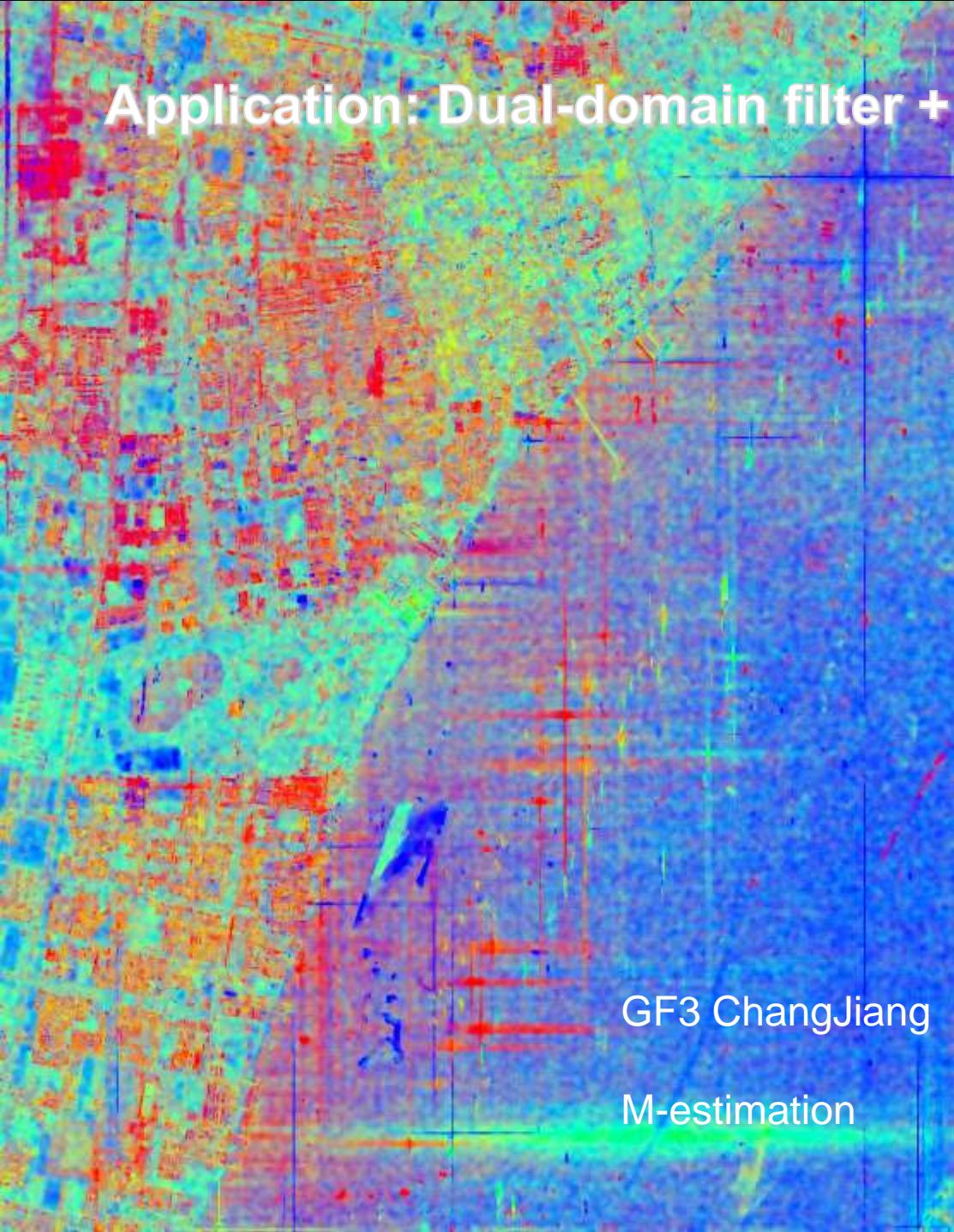




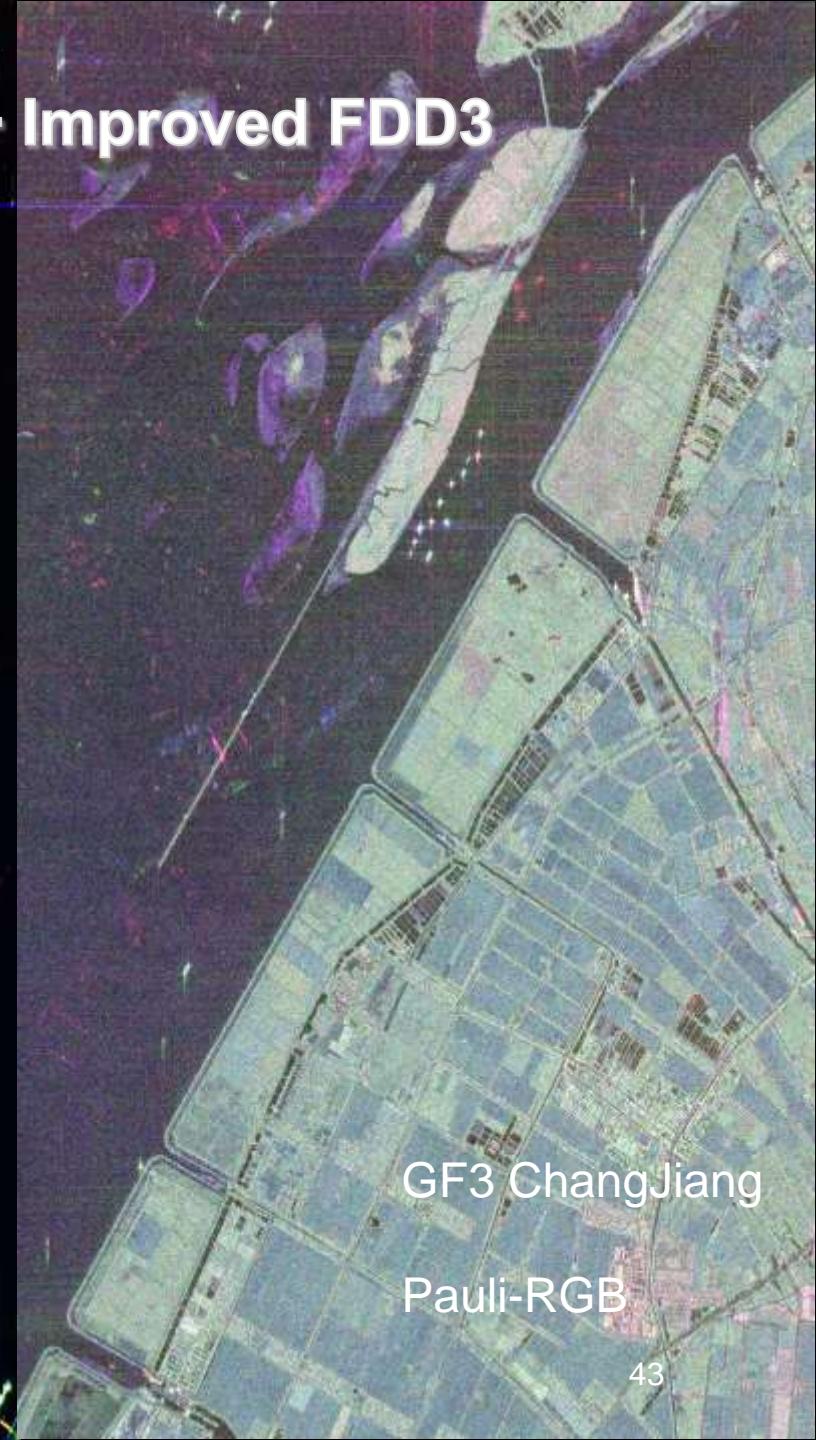
GF3 ChangJiang

Pauli-RGB

Application: Dual-domain filter + Improved FDD3



Application: Dual-domain filter + Improved FDD3



GF3 ChangJiang

Pauli-RGB



GF3 ChangJiang

Whole scene PolSAR image
No loss of resolution

SIRV-based dual-domain filter +
Improved FDD3





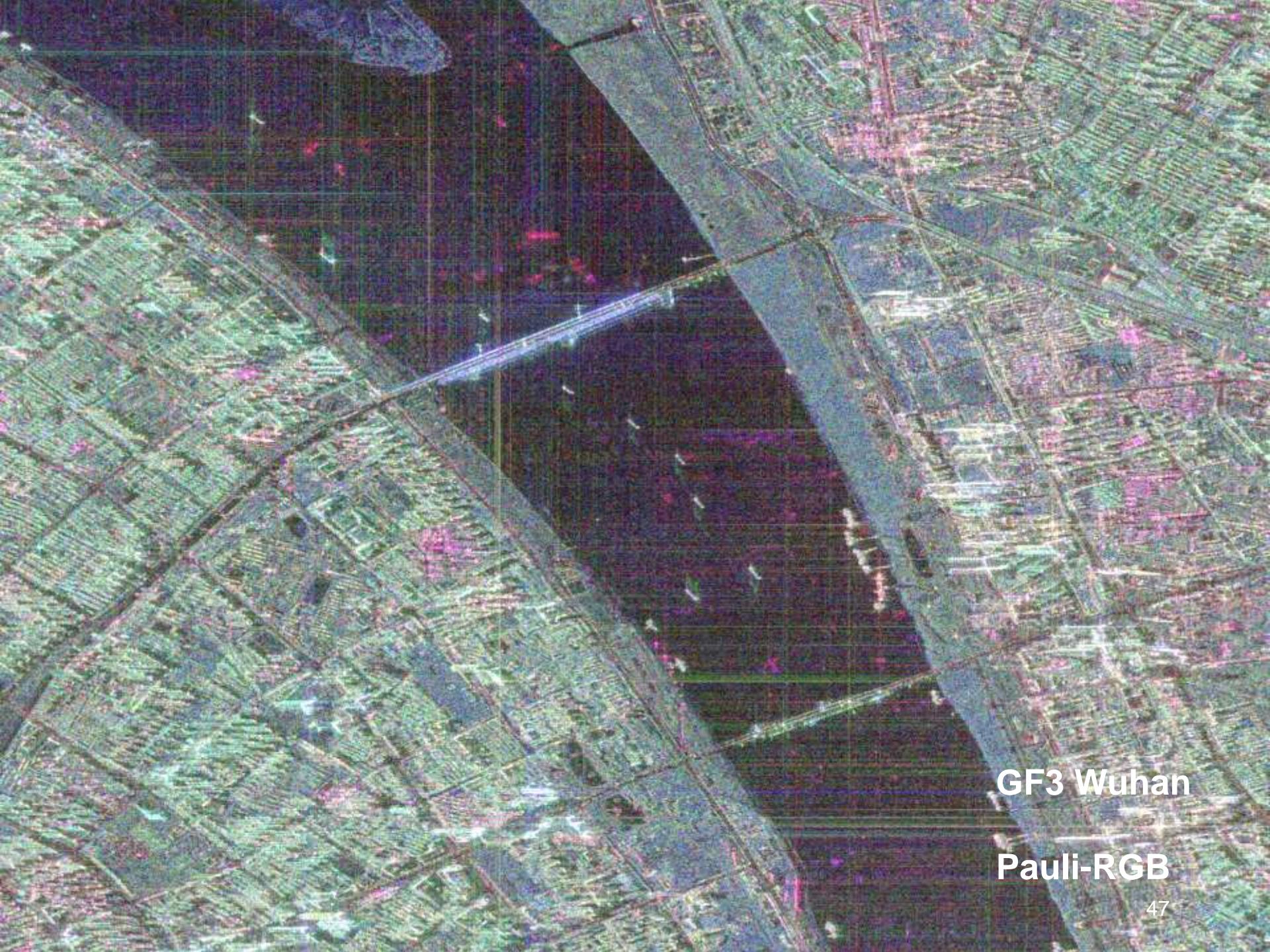
GF3 Shanghai

Pauli-RGB

Application: Dual-domain filter + Improved FDD3

GF3 Shanghai



A GF3 Wuhan Pauli-RGB satellite image showing a dense urban area with a grid-like street pattern. The image is color-coded using the Pauli-RGB transform, where roads appear in shades of red and orange, buildings in green and yellow, and water bodies in blue. A large, dark triangular shadow from a satellite or aircraft is cast across the center-left portion of the image, obscuring some of the urban details.

GF3 Wuhan

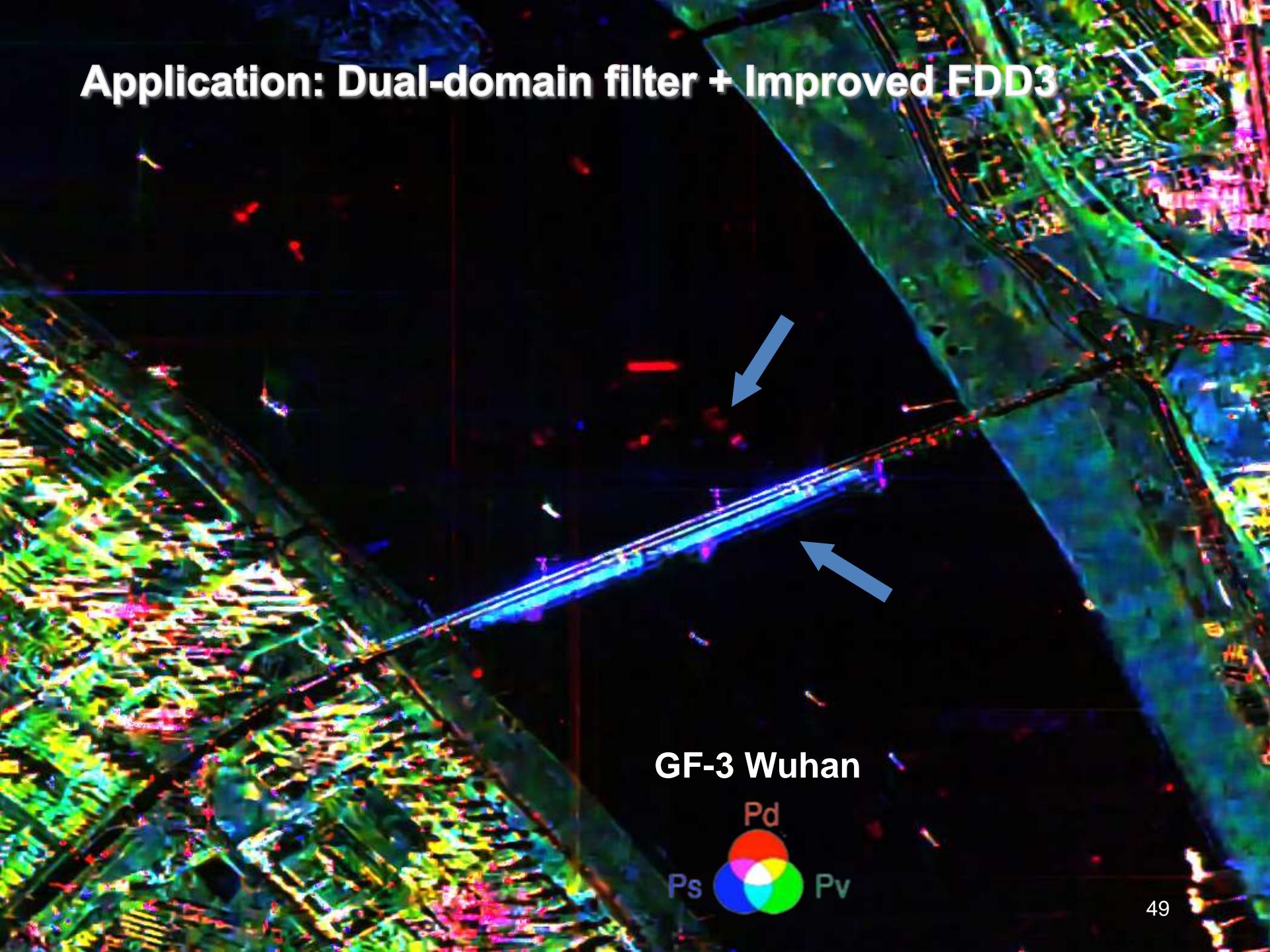
Pauli-RGB

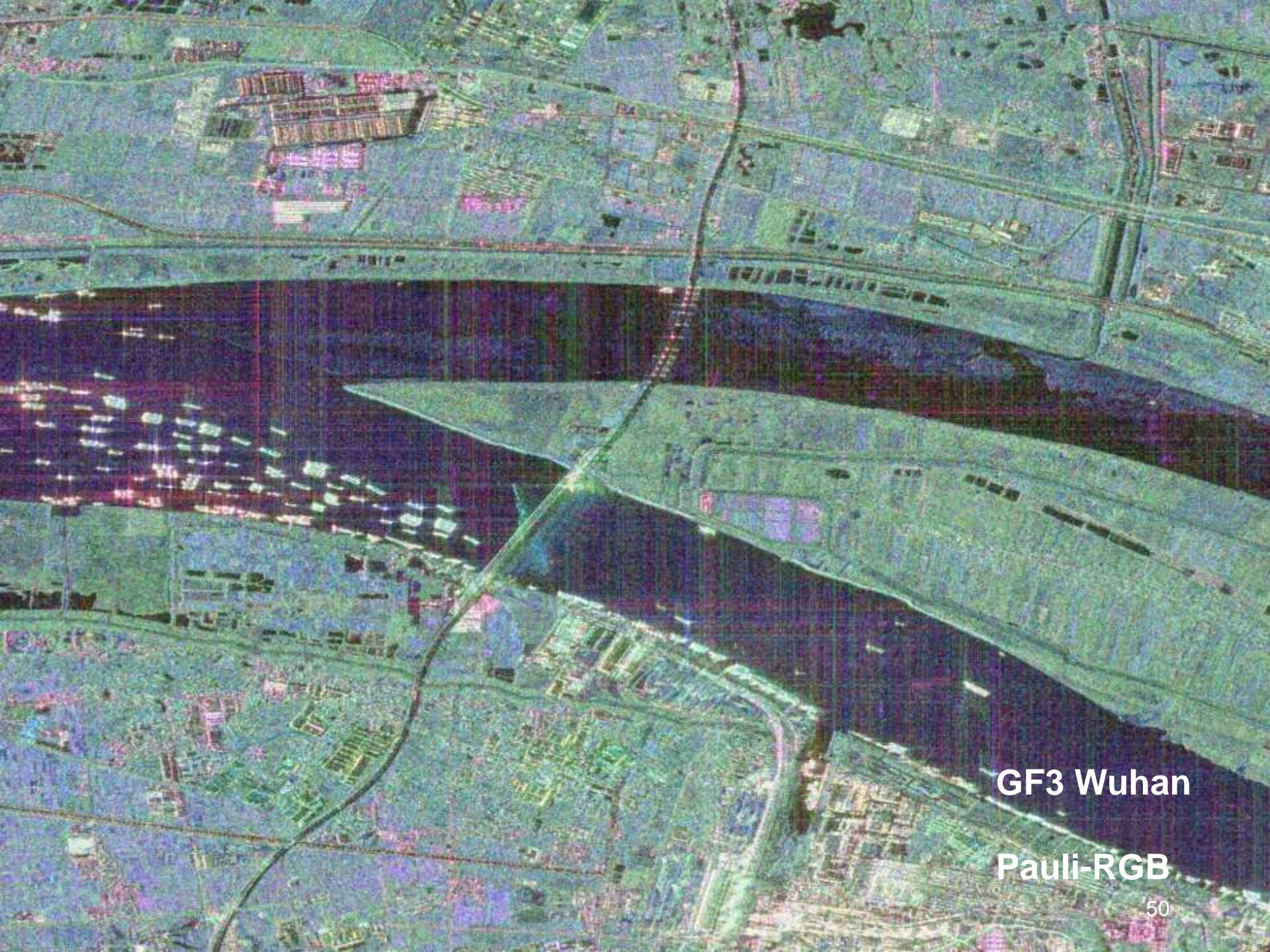
Application: Dual-domain filter + Improved FDD3

GF-3 Wuhan



Application: Dual-domain filter + Improved FDD3





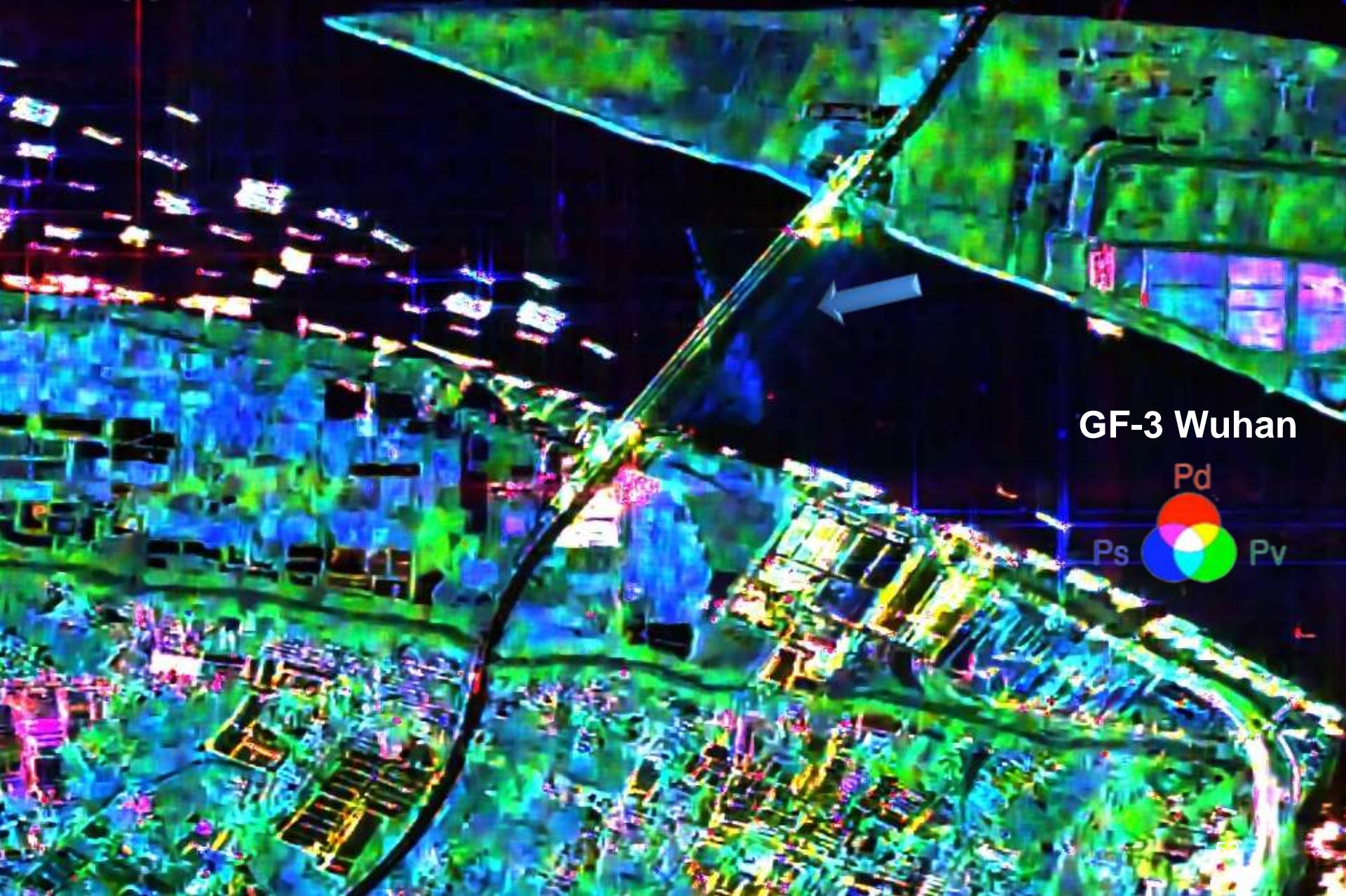
GF3 Wuhan

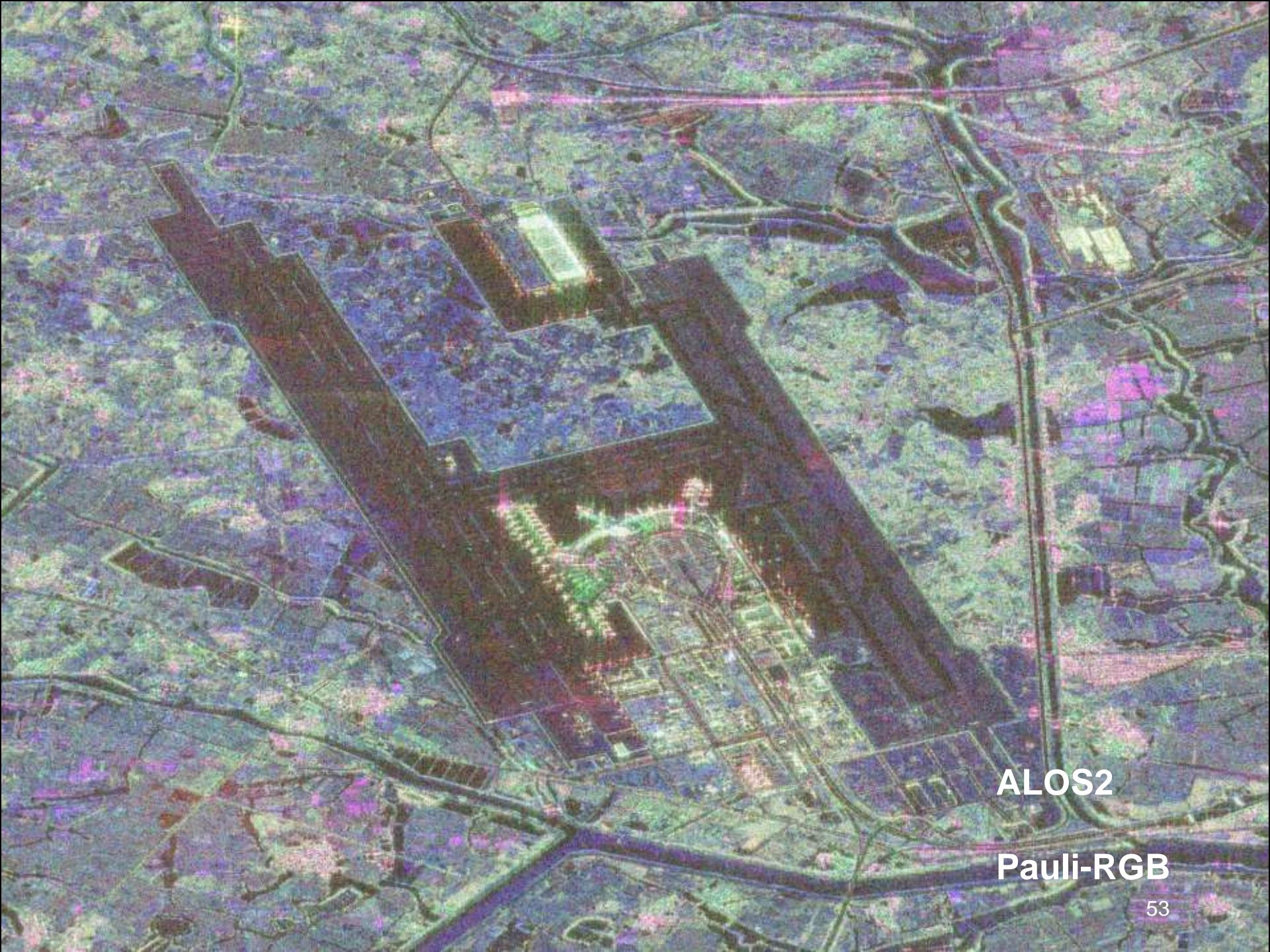
Pauli-RGB

Application: Dual-domain filter + Improved FDD3



Application: Dual-domain filter + Improved FDD3

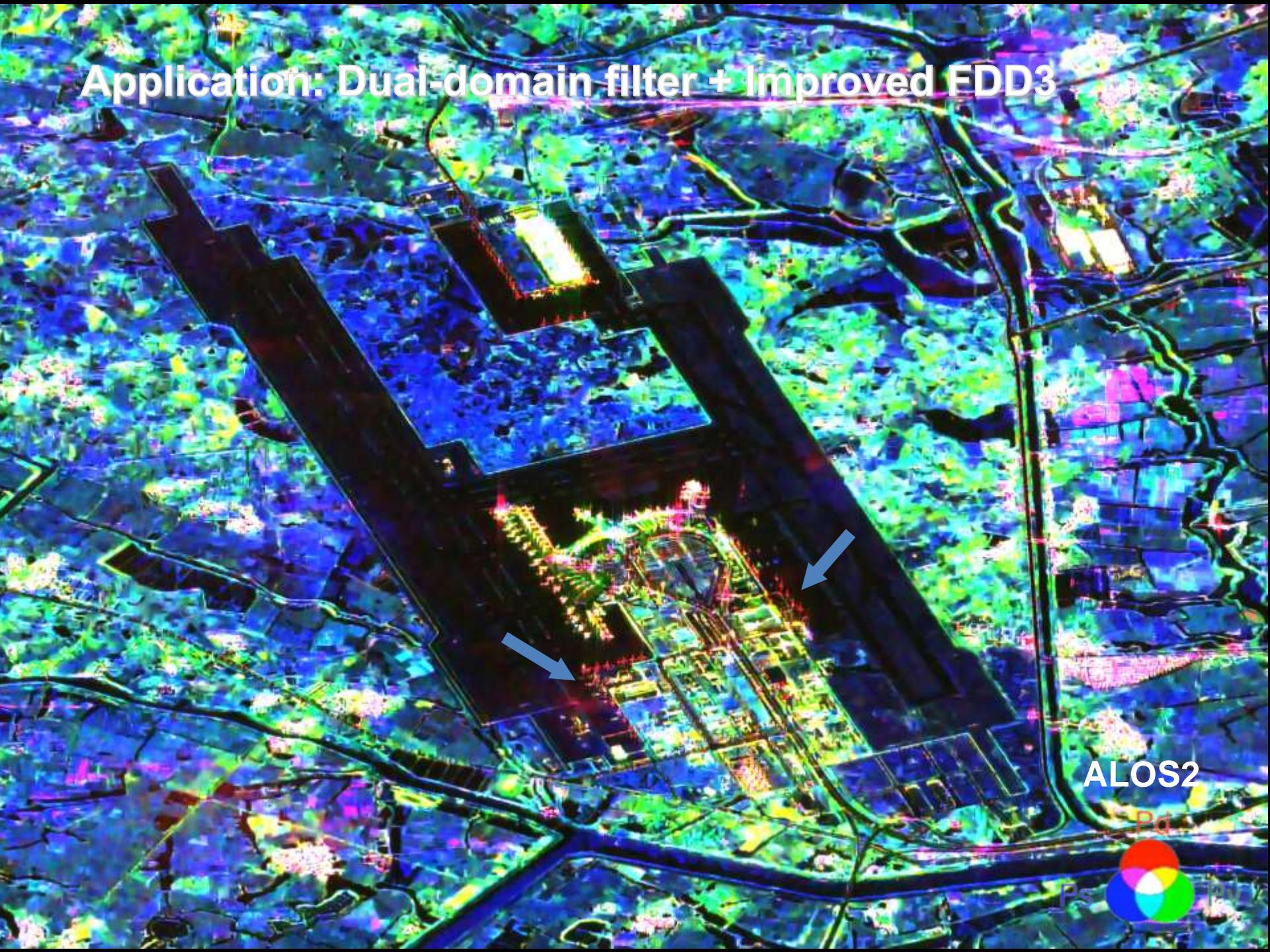




ALOS2

Pauli-RGB

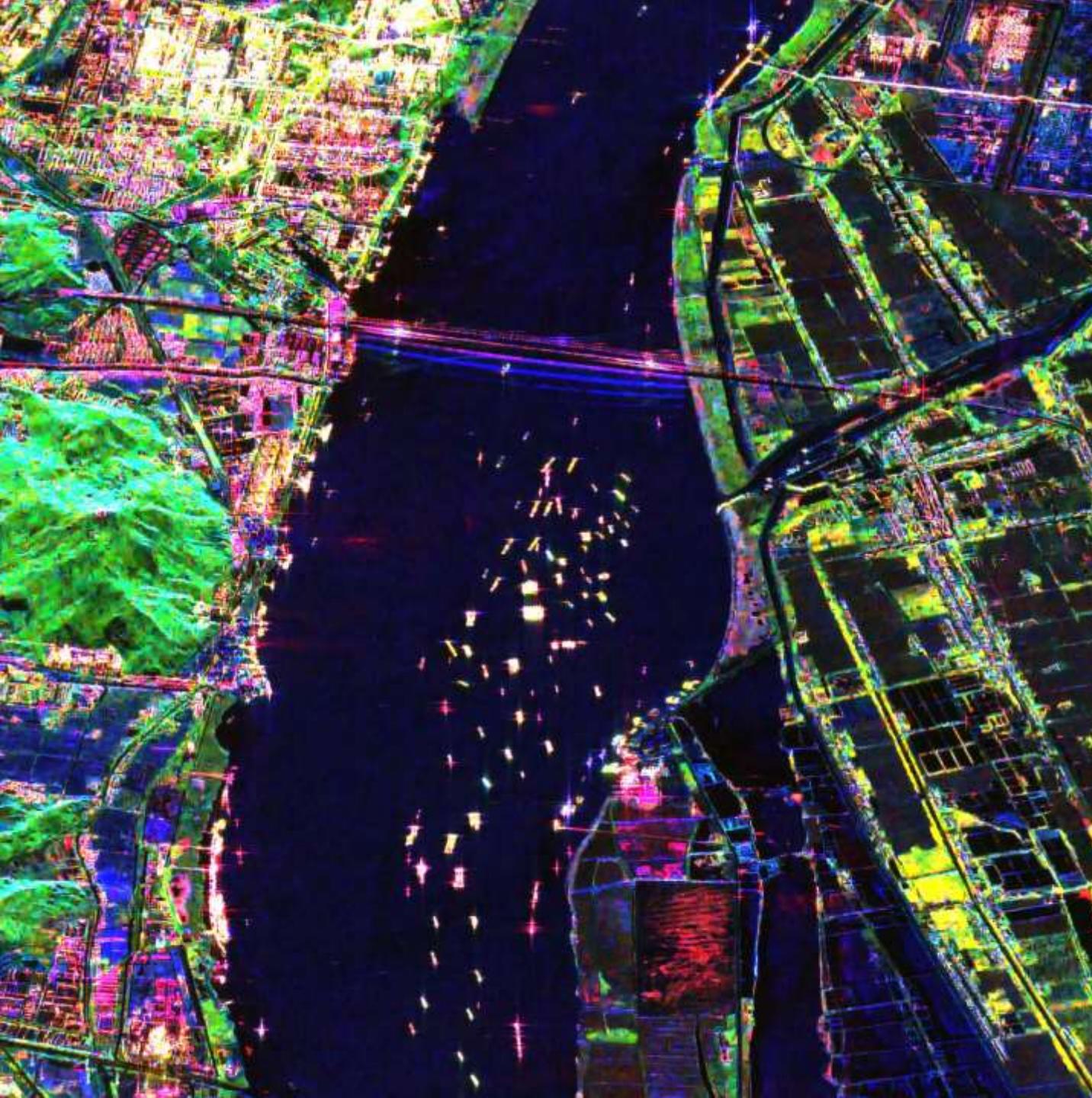
Application: Dual-domain filter + Improved FDD3





ALOS2

Pauli-RGB



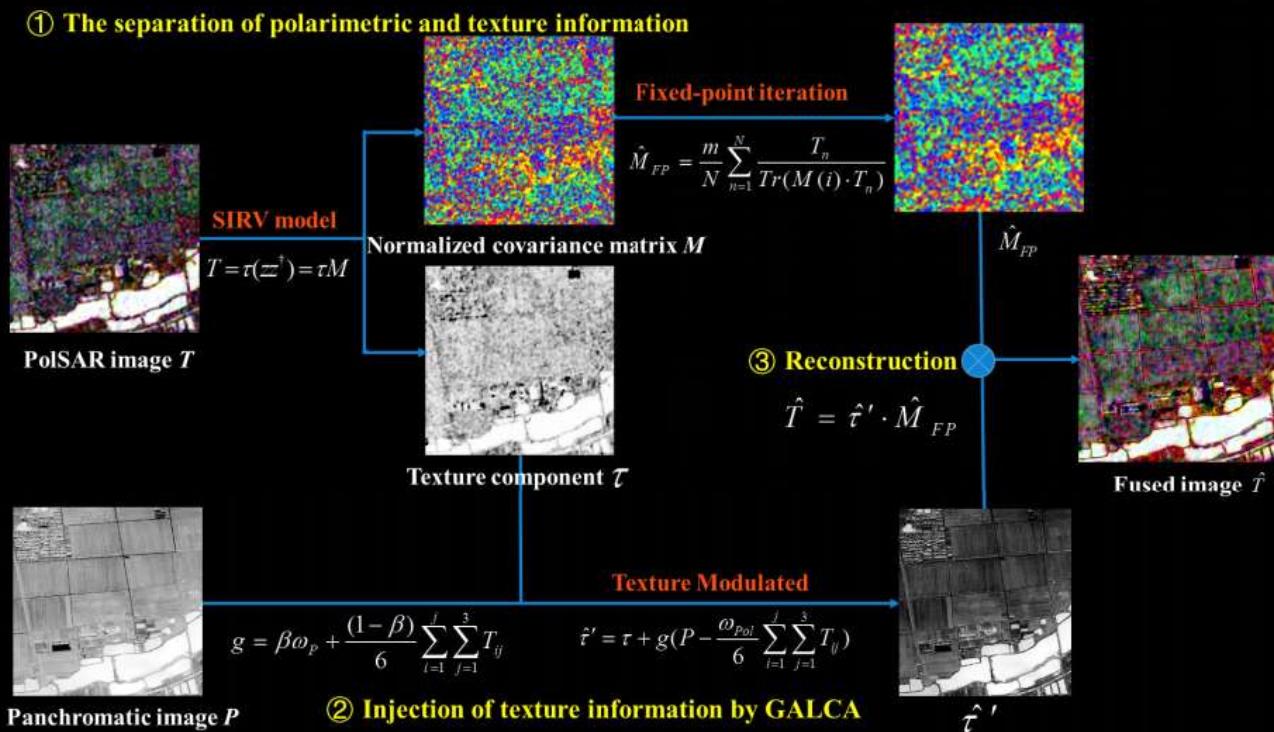
SIRV-based dual-domain filter +
Improved FDD3

ALOS2



Application: Beyond PolSAR

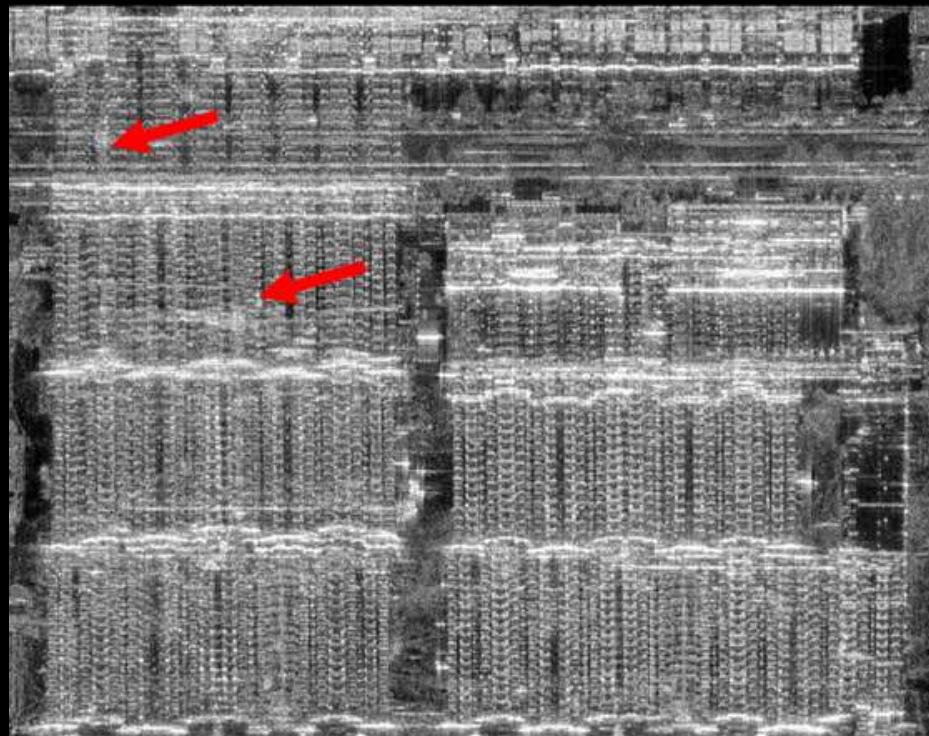
- SIRV-based dual-domain filter for panchromatic and PolSAR image fusion



Dual-Domain Super-Resolution Image Fusion Method [Liu. W. et al., 2022]

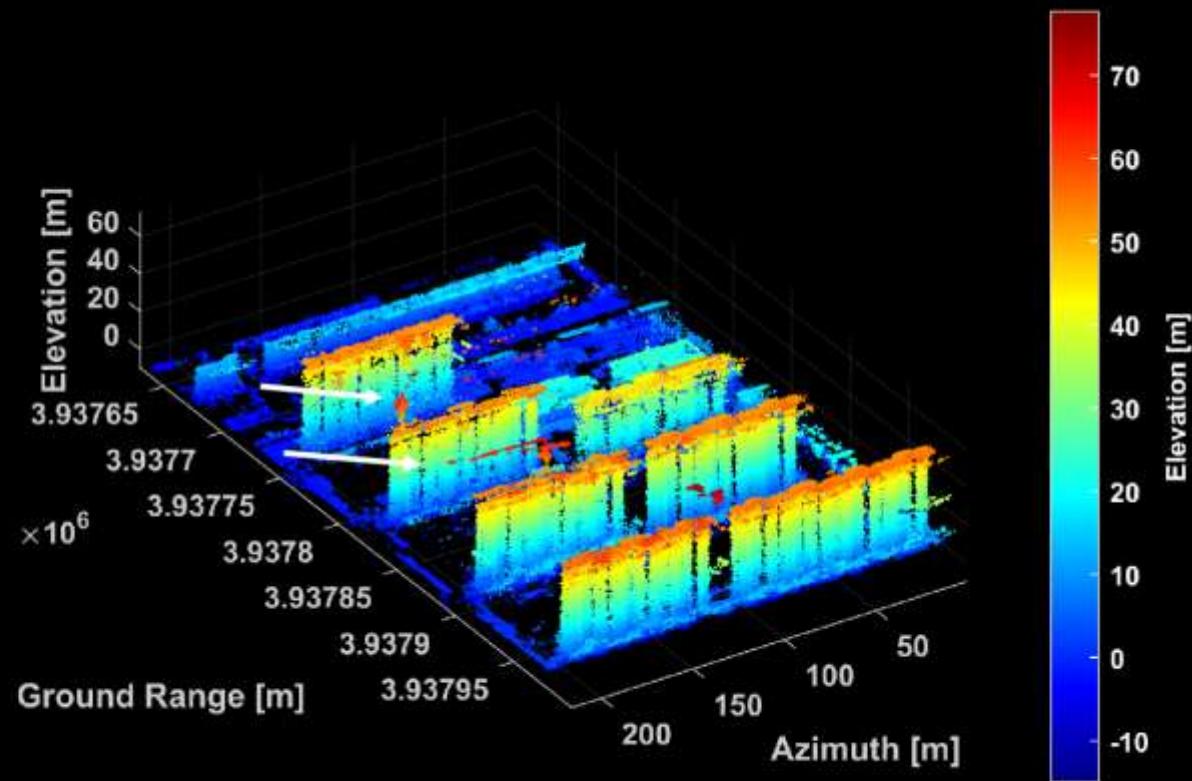
Application: Beyond PolSAR

- Clutter decomposition for the improvement of TomoSAR data quality.
 - AIRCAS Yuncheng Array-InSAR data



Application: Beyond PolSAR

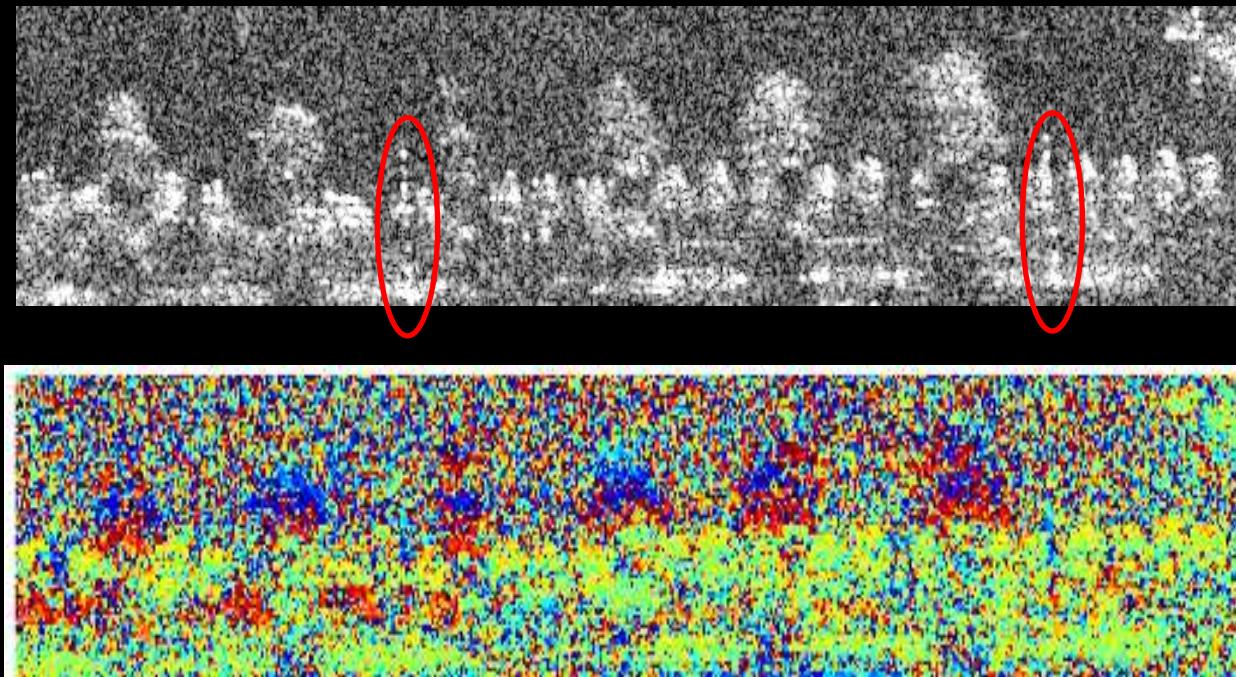
- Clutter decomposition for the improvement of TomoSAR data quality.
 - AIRCAS Ku Yuncheng Array-InSAR data



Ref: 任烨仙.稀疏阵列层析SAR相位定标与三维成像[D].复旦大学,2023.

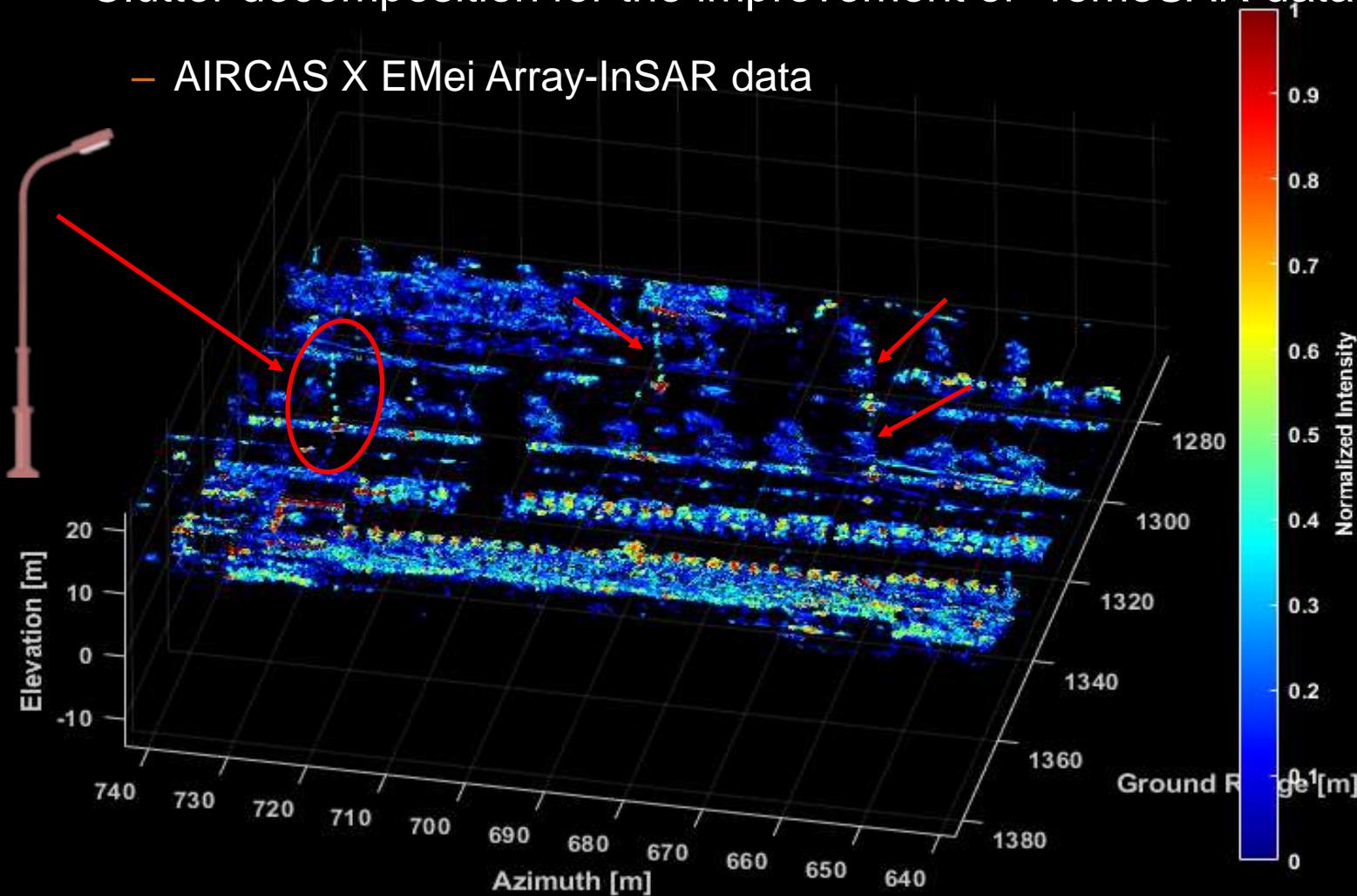
Application: Beyond PolSAR

- Clutter decomposition for the improvement of TomoSAR data quality.
 - AIRCAS X EMei Array-InSAR data

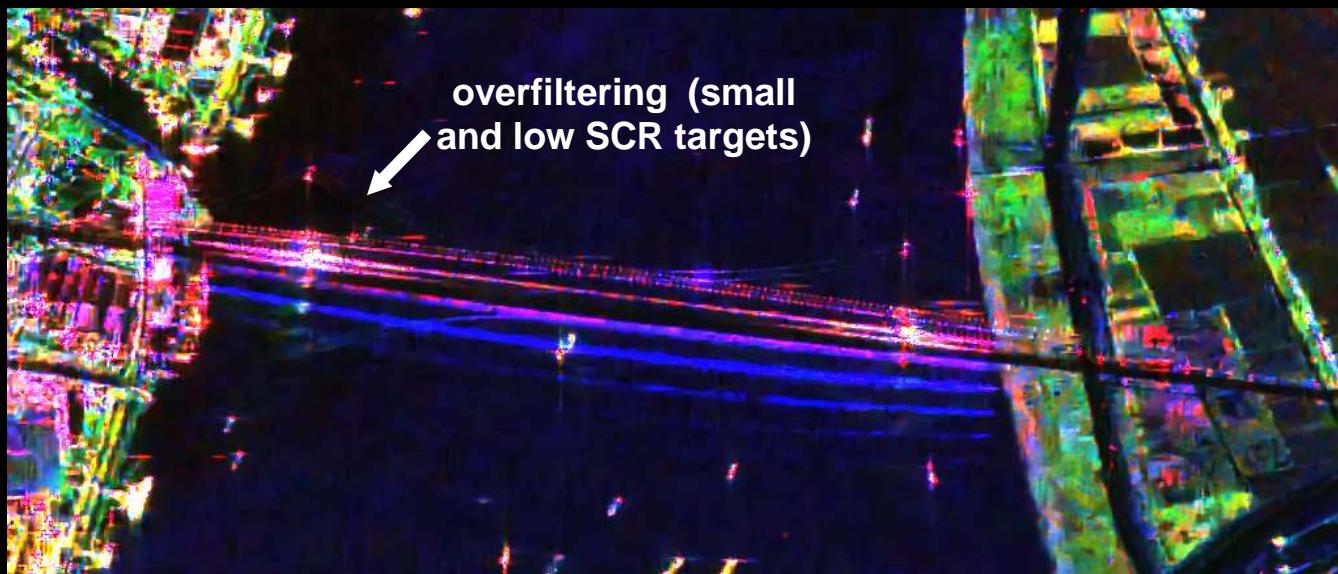
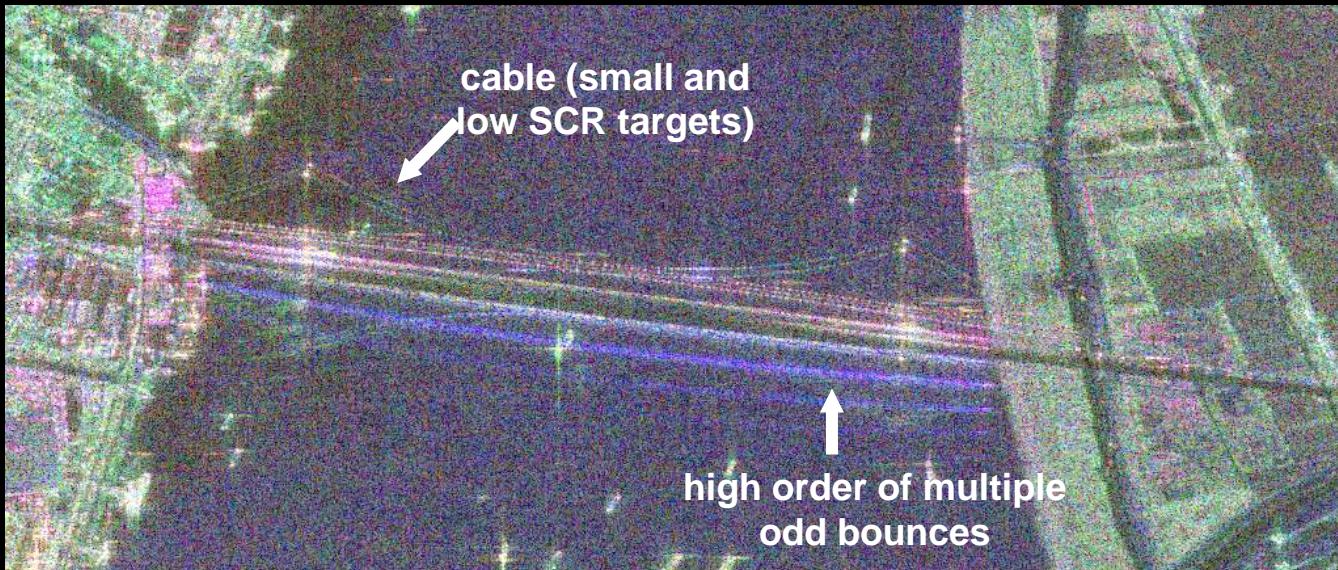


Application: Beyond PolSAR

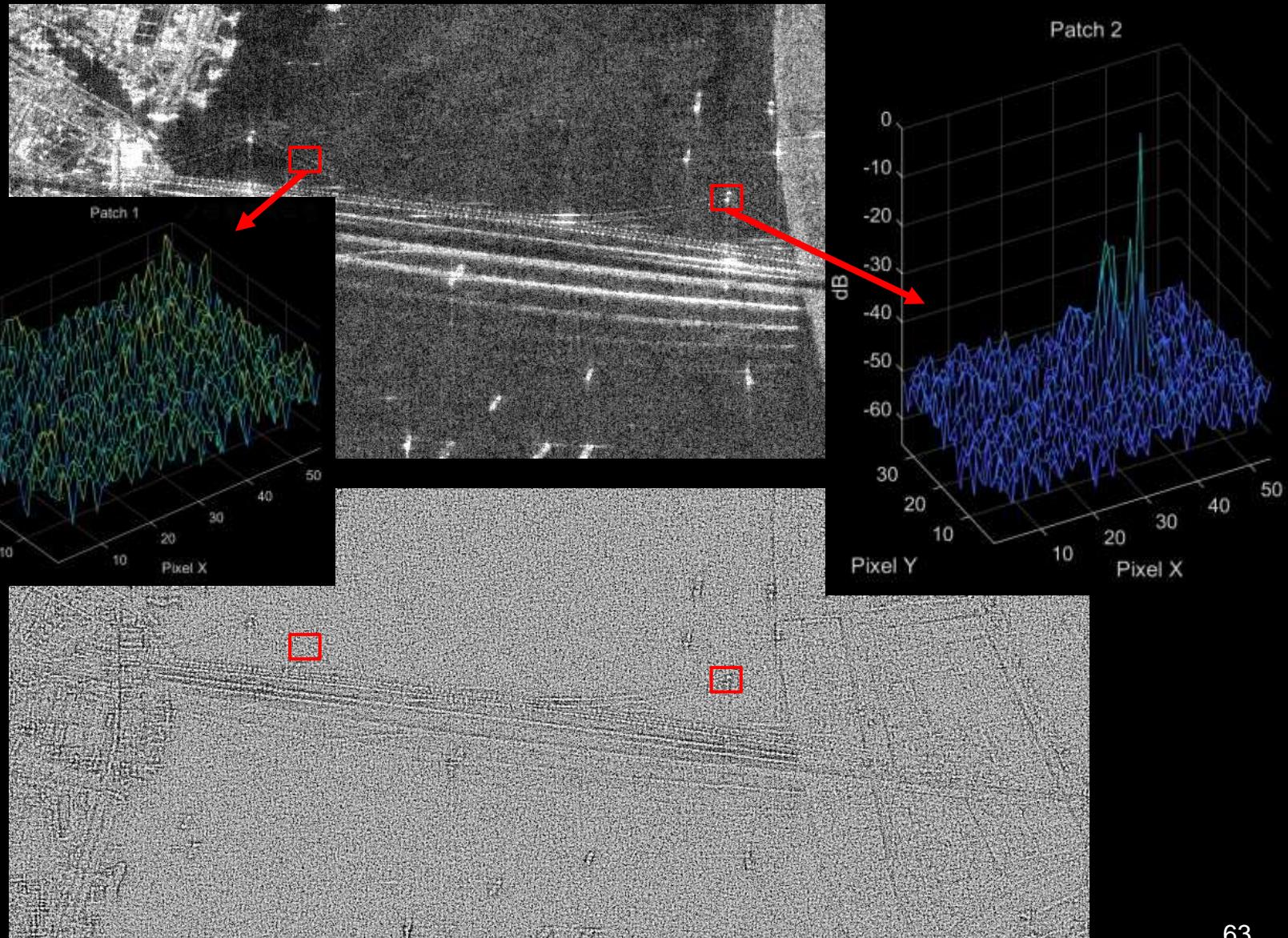
- Clutter decomposition for the improvement of TomoSAR data quality.
 - AIRCAS X EMei Array-InSAR data



Failure of SIRV-based dual-domain filter



Failure of SIRV-based dual-domain filter



Summary

- Divide *an unsolved difficult problem into two solved sub-problems*
- SIRV-based dual-domain filter
 - Decompose heterogeneous clutter
 - Enhance signal-to-clutter ratio
 - Favour three component decomposition

Thank you!