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# SENSITIVITY ANALYSIS OF PARAMETER INFLUENCE ON THERMAL DESIGN IN UPMSAT 3

STUDY CASE 3  
MSC IN SPACE SYSTEMS

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MADRID, 9 DE MARZO DE 2024



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# Chapter 1

## Introduction

In the context of thermal testing, the effectiveness of sensor placement plays an important role in ensuring, not only the accuracy and reliability of test results but also the significance of them. The motivation to improve thermal testing is highlighted by the substantial costs—both in terms of finances and time—associated with thermal testing procedures, which makes even more necessary to get useful results.

Traditional approaches to sensor positioning often fall short in defining thermal experiments due to the complexity of representing the physical processes and properties in a thermal mathematical model. Thus, an adequate parameter selection is key when trying to reduce a thermal mathematical model. This might seem obvious at first sight, but complex thermal mathematical models can have up to thousands of parameters and surpass the million of nodes, so the job of selecting the parameters that capture the physics of the problem for every charge case must not be underestimated.

Throughout this study case we have developed an efficient tool to identify the input parameters that have a significant influence on any of the possible outcomes. This tool has been used on 3 different thermal models in order to get a proper validation:

- A 4 nodes model, which is a simple model where that allows to test the method in a controlled environment.
- A real FPGA model with 8 nodes that is used to test the method in a real, yet simple scenario.
- The UPMSat-3, a real satellite that is currently being developed by the Universidad Politécnica de Madrid. This model is used to test the method in a real scenario.

The results of this work can be applied, in general, to many fields, however the work has been focused on spacecraft and space instruments thermal modeling and testing, in the context of the Space sector. The examples used along the document are centered on space hardware and for that reason, in the next section, the spacecraft thermal control topic is introduced with a brief summary of the particularities of the space environment

## 1.1 Spacecraft Thermal Control

The thermal design of a spacecraft is primarily influenced by the conditions it encounters during its mission in space. From a thermal perspective, the space environment is characterized by a vacuum, Solar radiation (both direct and reflected by nearby planets, known as albedo), and the infrared emission of celestial bodies.

The main driver of a spacecraft thermal design is the in-flight environment where it needs to operate. From a thermal point of view, the space environment is characterized by the vacuum, the incoming Solar radiation, both direct and reflected by a nearby planet (albedo), and the infrared emission of the planet. Because a spacecraft operates in a vacuum, the only possible thermal interaction between the spacecraft and its environment is through radiation. On an Earth orbit, solar irradiance is the main heat load, with a mean value of 1366 W/m<sup>2</sup> and a seasonal variation of  $\pm 1.7\%$  due to the eccentricity of the orbit of the Earth around the Sun. The solar irradiance value scales with the square of the distance to the Sun, and its spectrum can be modeled, from a thermal point of view, as a black body at some 5762 K, where 99 % of the spectral emissive power of the Sun lies in the range 0.15 to 10  $\mu\text{m}$  wavelength.

### 1.1.1 Thermal mathematical modelling

When creating a thermal model for an analysis of something space-related, the most common method is the lumped parameters [INSERTAR REFERENCIA], which consist of discretizing the physical system to a finite set of nodes, each of those representing an isotherm tiny volume with some properties associated to itself (with the thermal capacity of the material being among them).

The nodes are interconnected between themselves by the lineal (conductive and convective -if possible-)  $G_{L_{ij}}$  and radiative  $G_{R_{ij}}$  thermal conductances. The thermal charges are summed up in  $Q_i$  (with  $i$  being the number of the node); within this term, the solar charge, the planetary albedo, the electrical dissipation of the payloads or the infrared earth emission are

represented among others. Now, using the equation of energy balance,

$$C_i \frac{dT_i}{dt} = Q_i + \sum_{j=1}^n G_{Lij} (T_j - T_i) + \sum_{j=1}^n G_{Rij} \sigma (T_j^4 - T_i^4) \quad (1.1)$$

we get a system of ordinary differential equations that can be solved through numerical methods.

The values of the thermal conductances and capacitances are not always known, as they are usually a function of physical parameters such as geometry, pressure, torque, or surface finishing. There are several ways of calculating the lineal conductances [REFERENCIA], but when using reduced thermal models (where the geometry has been really simplified) it is usually better to take these  $G_L$  as parameters. As for the radiative conductances,  $G_R$ , they come from the Geometrical Mathematical Model, the GMM, that is, when defining the geometry of the thermal model, the geometry is also detailed in order to get the external thermal charges and the view factors, which, with the different surface coatings give the corresponding  $G_R$ . While the calculation -or at least the estimation- of the  $G_L$  can be done analytically and/or experimentally, the  $G_R$  are usually obtained numerically through a MonteCarlo analysis [REFERENCIA]

### 1.1.2 Analaysis cases

### 1.1.3 Reduced thermal mathematical models

## Chapter 2

# Mathematical formulation

### 2.1 Problem definition

### 2.2 Error definition

### 2.3 Model requirements

### 2.4 Data acquisition

### 2.5 Observability

### 2.6 Parameters and nodes reduction

In order to choose the most adequate parameters to determine the reduced model, the matrix of influence  $\mathbf{I}_\mathbf{X}$  is defined below:

$$\mathbf{I}_\mathbf{X} = \begin{bmatrix} \frac{\partial T_1}{\partial X_1} \delta X_1 & \frac{\partial T_1}{\partial X_2} \delta X_2 & \dots & \frac{\partial T_1}{\partial X_{N_P}} \delta X_{N_P} \\ \dots & \dots & \dots & \dots \\ \frac{\partial T_{N_N}}{\partial X_1} \delta X_1 & \frac{\partial T_{N_N}}{\partial X_2} \delta X_2 & \dots & \frac{\partial T_{N_N}}{\partial X_{N_P}} \delta X_{N_P} \end{bmatrix} = \mathbf{M} \delta \mathbf{X} \quad (2.1)$$

where  $\mathbf{M}$  is the jacobian or sensibility matrix and  $\delta \mathbf{X}$  is a vector containing the allowable variation of each parameter within the design. In the influence matrix  $\mathbf{I}_\mathbf{X}$  each column represents the temperature variation of the nodes that would be generated by a deviation on

the parameter  $\delta X_i$ . Therefore, the elements of this matrix have dimensions of temperature, showing the effect of every parameter in the model, which would not be possible using the jacobian matrix directly

## 2.7 Sensor positioning

## Chapter 3

### Application to a 4 nodes models



# Chapter 4

## Application to the UPMSat-3

### 4.1 Context

### 4.2 Thermal mathematical model

### 4.3 Model reduction

#### 4.3.1 Parameter identification

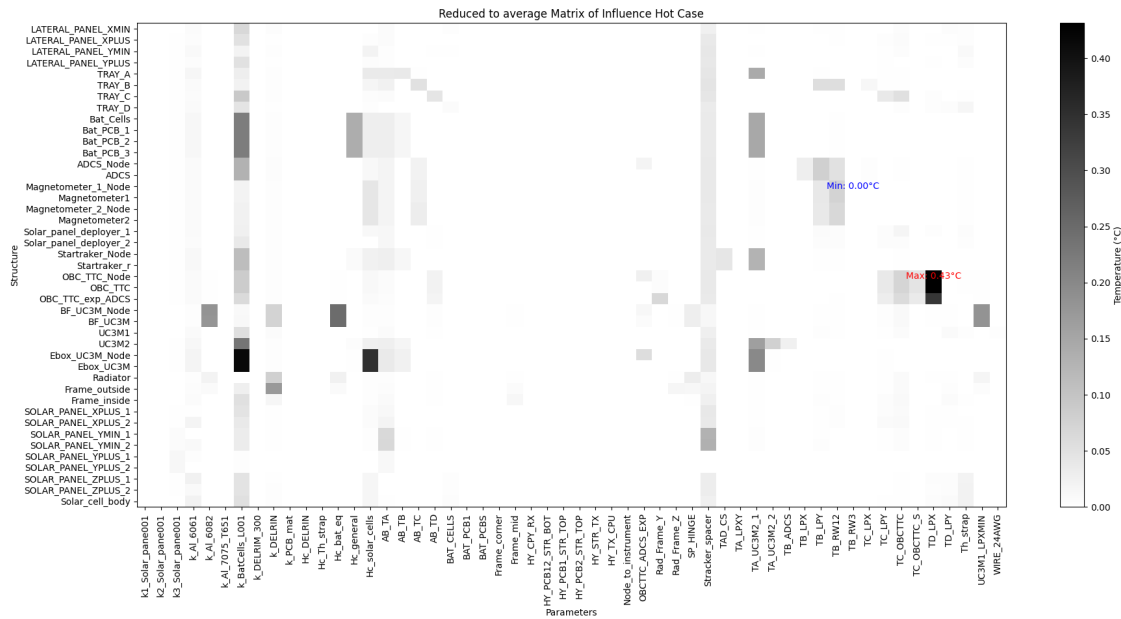


Figure 4.1: NO SIRVE, ES V0.

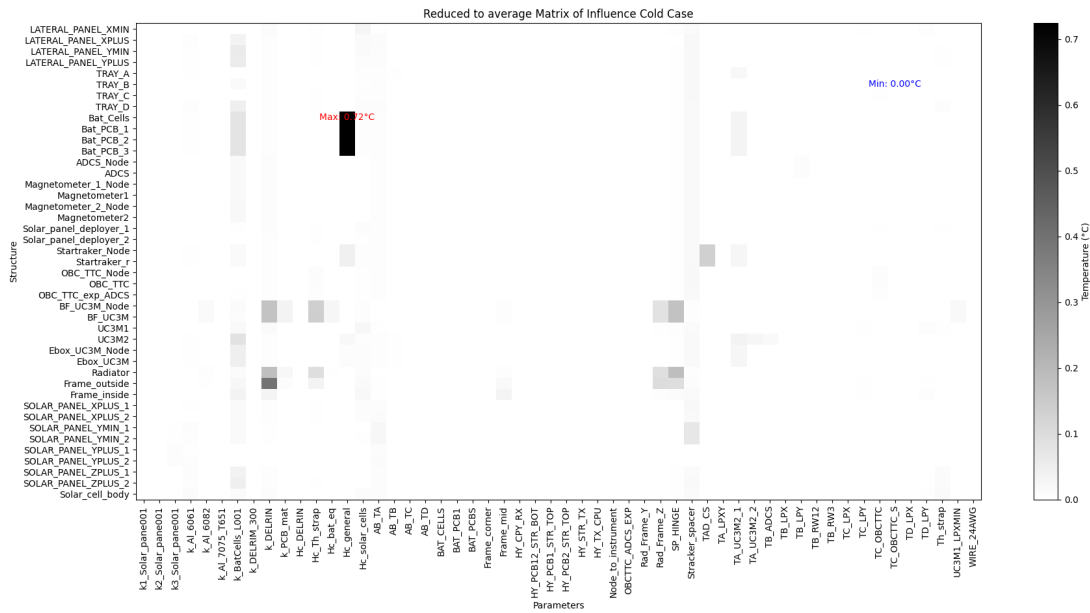


Figure 4.2: NO SIRVE, ES V0

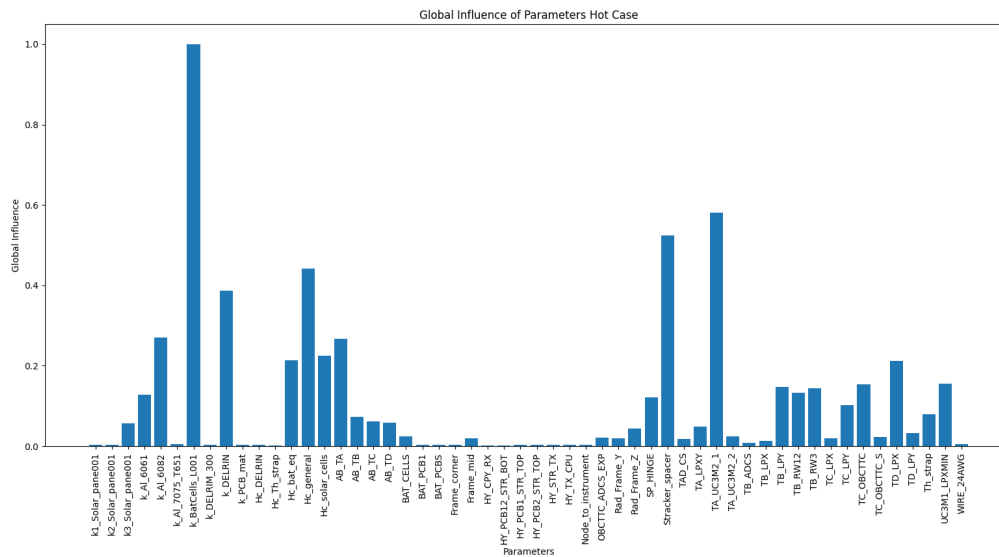


Figure 4.3: NO SIRVE, ES V0

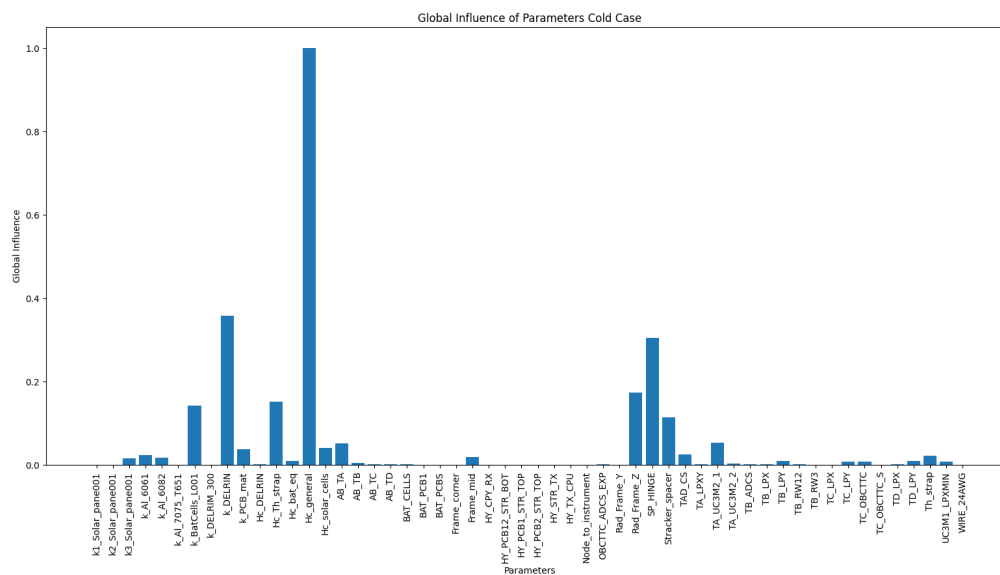


Figure 4.4: NO SIRVE, ES V0

### 4.3.2 Nodal reduction

### 4.3.3 Results



## Chapter 5

### Application to UPMSat 3

Table 5.1: Parameter List

number	param
1	AB_TA
2	AB_TB
3	AB_TC
4	AB_TD
5	Frame_corner
6	Frame_mid
7	GL_BF
8	GL_THB
9	HY_CPY_RX
10	HY_PCB12_STR_BOT
11	HY_PCB1_STR_TOP
12	HY_PCB2_STR_TOP
13	HY_STR_TX
14	HY_TX_CPU
15	Hc_bat_eq
16	Hc_general
17	Hc_solar_cells
18	OBCTTC_ADCS_EXP
19	Rad_Frame_Y
20	Rad_Frame_Z
21	SP_HINGE
22	Stracker_spacer
23	TAD_CS
24	TA_LPXY
25	TA_UC3M2_1
26	TA_UC3M2_2



# Appendices

# Anexo A

## Título del anexo

Aquí puedes meter la información que no sea imprescindible en el cuerpo del trabajo pero si que interese que esté en el documento.