Appendix C STANDARD ORTHOGONAL ARRAYS AND

LINEAR GRAPHS*

^{*} The orthogonal arrays and linear graphs are reproduced with permission from Dr. Genichi Taguchi and with help from Mr. John Kennedy of American Supplier Institute, Inc. For more details of the orthogonal arrays and linear graphs, see Taguchi [T1] and Taguchi and Konishi [T5].

$$L_4 (2^3)$$

L₄ (2³) Orthogonal Array

Expt.	1	Colun	ın
No.		2	3
1	1	1	1
2	1	2	2
3	2	1	2
4	2	2	1

Linear Graph for L



 $L_8 (2^7)$

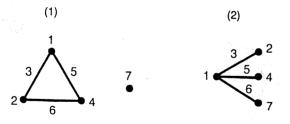
L₈ (2⁷) Orthogonal Array

Interaction Table for L_8

Expt.				olun	nn		
No.	1	2	3	4	5	6	7
1	1	1	1	1	1	1	1
2	1	i	1	2	2	2	2
3	1	2	2	i	ı	2	2
4	1	2	2	2	2	1	ī
5	2	ì	2	1	2	1	2
6	2	1	2	2	1	2	1
7	2	2	1	1	2	2	il
8	2	_2	1	2	1	Ī	2

					Colum	n		
	Column	1	2	. 3	4	5	6	7
,	1	(1)	3	2	5	4	7	6
1	2		(2)	1	6	7	4	5
1	3			(3)	7	6	5	. 4
1	4				(4)	1	2	3
1	5					(5)	3	2
	6						(6)	1
1	7						/	(7)

Linear Graphs for L_8



 $L_9 (3^4)$

L₉ (3⁴) Orthogonal Array

Expt.		Col	umn	
No.	1	2	3	4
1	1	1	1	1
3	1	2	2	2
3	1	3	3	3
4	2	1	2	3
5	2 2	2	3	ı
6	2	3	1	2
7	3	1	3	2
8	3	2	1	3
9	3	3	2	1

Linear Graphs for L₉

$$L_{12}(2^{11})$$

L₁₂ (2¹¹) Orthogonal Array

Expt.						Colu	mn				
No.	1	2	3	4	5	6	7	8	9	10	11
1	1	ı	1	ı	1	1	1	1	1	ı	1
2	1	1	1	i	i	2	2	2	2	2	2
3.	1	1	2	2	2	1	1	1	2	2	2
4	1	2	i	2	2	1	2	2	i	i	2
5	1	2	2	1	2	2	1	2	1	2	1
6	1	2	2	2	1	2	2	1	2	ī	1
7	2	1	2	2	1.	1	2	2	1	2	1
8	2	I	2	i	2	2	2	ı	1	1	2
9	2	1	1	2	2	2	1	2	2	<u> </u>	1
10	2 .	2	2	1	1	ī	i	2	2	i	2
11	2	2	1	2	1	2	i	ī	ī	2	2
12	2	2	1	1	2	1	2	ı	2	2	ī

Note: The interaction between any two columns is confounded partially with the remaining nine columns. Do not use this array if the interactions must be estimated.

 $L_{16} (2^{15})$

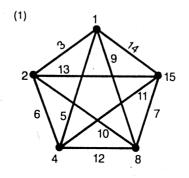
L₁₆ (2¹⁵) Orthogonal Array

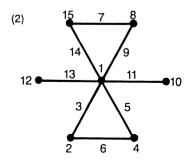
Expt.								(Colun	ın ·					
No.	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
1	i	i	1	1	1	1	i	ı	1	1	ı	1	1	1	1
2	1	1	1	1	ı	i	i	2	2	2	2	2	2	2	2
3	1	1	1	2	2	2	2	1	13	1	1	2	2	2	. 2
4	1	1	1	2	2	2	2	2	2	2	2	1	1	. 1	1
5	1	2	2	1	1	2	2	1	ı	2	2	1	1	2	2
6	1	2	2	1	1	2	2	2	2	.1	i	2	2	1	1
7	1	2	2	2	2	1	i	í	1	2	2	2	2	1	1
8	i	2	2	2	2	1 -	1	2	2	1	1	1	1	2	2
9	2	1	2	1	2	ı	. 2	1	2	1	2	1	2	1	2
10	2	1	2	1	2	1	2	2	ı	2	1	2	1	2	1
11	2	1	2	2	1	2	i	1	2	i	2	2	1	2	1
12	2	1	2	2	1	2	1	2	ı	2	1	i	2	1	2
13	2	2	1	1	2	2	1	1	2	2	1	1	2	2	1
14	2	2	. 1	1	2	2	1	2	1	ı	2	2	1	1	2
15	2	2	1	2	i	1	2	1	2	2	1	2	1	ı	2
16	2	2	1	2	1	1	2	2	i	1	2	1	2	2	1

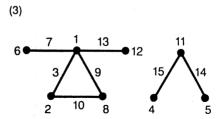
Interaction Table for L_{16} (2¹⁵)

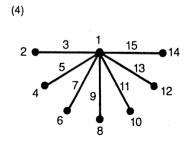
								٦C	olur	nn					
Column	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
1	(1)	3	2	5	4	7	6	9	8	11	10	13	12	15	14
2		(2)	1	6	7	4	5	10	11	8	9	14	15	12	13
3			(3)	7	6	5	4	11	10	9	8	15	14	13	12
4				(4)	i	2	3	12	13	14	15	8	9	10	11
5					(5)	3	2	13	12	15	14	9	8	11	10
6						(6)	1	14	15	12	13	10	11	8	9
7							(7)	15	14	13	12	11	10	9	8
8								(8)	ı	2	3	4	5	6	7
9							******		(9)	3	2	5	4	7	6
10										(10)	i	6	7	4	5
11											(11)	7	6	5	4
12												(12)	i	2	3
13													(13)	3	2
14												- '		(14)	1
15															(15)

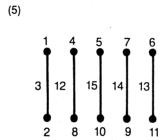
Linear Graphs for L₁₆

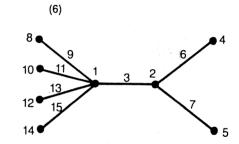












 L'_{16} (4⁵)

L'₁₆ (4⁵) Orthogonal Array

Expt.		C	olumn		
No.	1	2	3	4	5
1	1	1	1	i	1
	1	2	2	2	2 3 4
3	1	3	3		3
2 3 4	ı	4	4	4	4
5	2	1	2	3	4
6	2	2	1	4	3 2 1
1 . 7	1 2	. 3	4	1	2
8	2 2 2 2	4	3	2	1
9	3	1	3	4	2
10	3 3 3	2	4	3	2 1
11	3	3	1	2	4
12	3	4	2	1	3
13	4	1	4	2	3
14	4		3	1	4
15	4 4	2	3 2	4	3 4 1 2
16	4	4	1	3	2

Note: To estimate the interaction between columns 1 and 2, all other columns must be kept empty.

Linear Graph for L' 16

$$L_{18} (2^1 \times 3^7)$$

 L_{18} (2¹ × 3⁷) Orthogonal Array

Expt.					lumn			
No.	1	2	3	4	5	6	7	8
1	1	1	1	ı	1	1	1	ı
2	li	i	2	2	2	2	2	2
3	l i	i	3	3	3	3		
1	١.	•		3		3	3	3
4	1	2	1	ì	2	2	3	3
5	1	2	2	2	3	3	1	1
6	1	2	3	3	1	1	2	2
7	1	3	1	2	1	3	2	3
8	1	3	2	3	2	1	3	ı
9	1	3	3	1	3	2	ī	2
10	2	1	Ī	3	3	2	2	1
11	2	i	2	ì	1	3	3	2
12	2	i	3	2	2	1	í	3
12	_					'	'	3
13	2	2	1	2	3	1	3	2
14	2	2	2	3	1	2	1	3
15	2	2	3	1	2	3	2	1
16	2	3	Ī	3	2	3	ī	2
17	2	3	2	ī	3	1	2	3
18	2	3	3	2	1	2	3	1
	Ľ	,			1			1

Note: Interaction between columns 1 and 2 is orthogonal to all columns and hence can be estimated without sacrificing any column. The interaction can be estimated from the 2-way table of columns 1 and 2. Columns 1 and 2 can be combined to form a 6-level column. Interactions between any other pair of columns is confounded partially with the remaining columns.

Linear Graph for L₁₈

1 2 3 4 5 6 7

 L_{25} (5⁶)

L₂₅ (5⁶) Orthogonal Array

Expt.			Colu	ımn		
No.	1	2	3	4	5	6
1	ı	1	ı	1	1	ı
2	1	2	2	2	2	2
3	1	3	3	3	3	3 4
4	1	4	4	4	4	4
5	1	5	5	5	5	5
6	2	1	2	3	4	5
7	2 2	2	3	4	5	1 2 3
8	2 2	3	4	5	1	2
9	2	4	5	1	2	3
10	2	5	I	2	3	4
11	3	ı	3	5	2	4
12	3	2	4	1	3	5
13	3	3	5	2	4	1
14	3	4	1	3	5	2
15	3	5	2	4	1	1 2 3
16	4	1	4	2	5	3
17	4	2	5	3	1	3
18	4		1	4	2	5
19	4	3 4	2	5	3	1
20	4	5	3	1	4	5 1 2
21	5	1	5	4	3	2
22	5	2"	- 1	5	4	3
23	5	3	2	1	5	2 3 4 5
24	5	3 4	3		5 1 2	5
25	5	5	4	2	2	1

Note: To estimate the interaction between columns 1 and 2, all other columns must be kept empty.

Linear Graph for L₂₅

 $L_{27} (3^{13})$

L₂₇ (3¹³) Orthogonal Array

Expt.						(Colur	nn					
No.	1	2	3	. 4	5	6	7	8	9	10	11	12	13
1	1	ı	1	1	1	1	1	ı	1	1	1	1	1
2	1	1	1	1	2	2	2	2	2	2	2	2	2
3	1	I	1	-1	3	3	3	3	3	3	3	3	3
4	1	2	2	2	1	1	I	2	2	2	3	3	3
5	1	2	2	2	2	2	2	3	3	3	1	1	1
6	1	2	2	2	3	3	3	1	I	1	2	2	2
7 '	1	3	3	3	1	1	1	3	3	3	2	2	2
8	1	3	3	3	2	2	2	1	1	1	3	3	3
9	1	3	3	3	3	3	3	2	2	2	1	1	1
10	2	1	2	3	1	2	3	ı	2	3	1	2	3
11	2	1	2	3	2	3	1	2	3	1	2	3	1
12	2	l	2	3	3	i	2	3	1	2	3	1	2
13	2	2	3	1	1	2	3	2	3	ı	3	1	2
14	2	2	3	1	2	3	1	3	ı	2	1	2	3
15	2	2	3	1	3	i	2	1	2	3	2	3	1
16	2	3	1	2	i	2	3	3	1	2	2	3	1
17	2	3	1	2	2	3	1	1	2	3	3	1	2
18	2	3	i	2	3	1	2	2	3	I	. 1	2	3
19	3	1	3	2	1	3	2	1	3	2	1	3	2
20	3	1	3	2	2	1	3	2	1	3	2	1	3
21	3	1	3	2	3	2	1	3	2	1	3	2	1
22	3	2	1	3	1	3	2	2	1	3	3	2	ı
23	3	2	i	3	2	i	3	3	2	1	1	3	2
24	3	2	i	3	3	2	1	1	3	2	2	1	3
25	3	3	2	1	1	3	2	3	2	ı	2	1	3
26	3	3	2	1	2	1	3	1	3	2	3	2	1
27	3	3	2	1	3	2	1	2	1	3	1	3	2

Interaction Table for L_{27} (3¹³)

	· -												
Column	1	2	3	4	,		Colun 7						
Column	<u> </u>			4	5	6	. 7	8	9	10	11	12	13
1	(1)	3	2 4	2 3	6 7	5 7	5	9 10	8 10	8 9	12 13	11 13	11 12
2		(2)	1 4	1	8 11	9 12	10 13	5 11	6 12	7 13	5	6 9	7 10
3			(3)	! 2	9 13	10 11	8 12	7 12	5 13	6 11	6 10	7 8	5 9
4				(4)	10 12	8 13	9 11	6 13	7 11	5 12	7 9	5 10	6
5					(5)	1 7	1 6	2 11	3 13	4 12	2 8	4 10	3
6				•		(6)	1 5	4 13	2 12	3 11	3 10	2 9	4 8
7							(7)	3 12	4 11	2 13	4 9	3 8	2 10
8								(8)	1 10	1	2 5	3 7	4
9									(9)	1 8	4	2 6	3 5
10										(10)	3 6	4 5	2 7
11					1						(11)	1 13	1 12
12												(12)	1 11
13													(13)

Linear Graph for L₂₇



Appendix C

 L_{32} (2³¹)

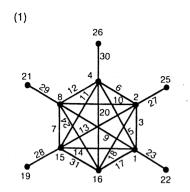
L₃₂ (2³¹) Orthogonal Array

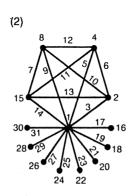
Expt.											-				Col	um	n														
No.	1	2	3	4	5	6	7	8	9	10	11	12	13					18	19	20	21	22	23	24	25	26	27	28	29	30	31
1	1	1	ı	1	1	l	1	1	1	1	1	1	ı	1	i	i	1	1	1	1	1	1	١	1	i	1	1	1	i	ı	1
2	ı	1	1	1	1	1	1	1	1	1	1	1	1	1	1	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2
3	1	1	1	l I	1	1	1	2	2	2	2	2	2	2	2	1	1	1	1	1 2	1	2	2	2	2	2	2	2	2	2	2 1
5	1	1	1	2	2	2	2	1	1	1	ı	2	2	2	2	1	1	1	١	2	2	2	2	1	1	. 1	1	2	2	2	2
6	1	1	1	2	2	2	2	2	1	1 2	1	2	2	2	2	2	2	2	2	1 2	1	1	1	2	2	2	2	. I	1	1	1
8	1	1	1	2	2	2	2	2	2	2	2	ı	1		1	2	2	2	2	1	1	1	1	1	1	1	1	2	2	2	2
	Ŀ.									_																					
9	1	2	2	ı	l	2	2	i.	1	2	2	I	1	2	2	1	1	2	2	ì	ì	2	2	ı	1	2	2	1	ì	2	2
10	1	2	2	1	1	2	2	1	1	2	2	1	1	2	2	2	2	1	1	2	2	1	1	2	2	1	1	2	2	1	1
11 12	1	2	2	i 1	1	2	2	2	2	1	I I	2	2	1	1	1	1 2	2	2	1 2	2	2	2	2	2	1	1	2	2	1 2	1
12																															
13	1	2	2	2	2	1	i	1	1	2	2	2	2	1	1	1	1	2	2	2	2	I	1	1	1	2	2	2	2	1	ì
14	1	2	2	2	2	1	1	1	1	2	2	2	2	1	1	2	2	1	١	1	1	2	2	2	2	1	1	1	1	2	2
15 16	1	2	2	2	2	1	1	2	2	1	1	1	1	2	2	1	1	2	2	2	2	1 2	1 2	2	2	1 2	1 2	1 2	1	2	2
19	Ľ.																		,	'					- 1					1	'
17	2	1	2	1	2	1	2	1	2		2	1	2	1	2	1	2	1	2	1	2	ì	2	1	2	1	2	i	2	ı	2
18	2	1	2	1	2	1	2	1	2	1	2	1	2	1	2	2	1	2	1	2	1	2	1	2	1	2	1	2	1	2	1
19 20	2 2	1	2	1	2	!	2	2	1	2	1	2	1	2	1	1	2	1	2	1 2	2	1	2	2	1	2	1	2	1	2	1
20		1				1			1		i		1		1	2	1	2	1	-2	1	2	1	1	2	1	2	1	2	1	2
21	2	1	2	2	ı	2	1	1	2		2	2		2	1	i	2	i	2	2	1	2	1	ŀ	2	l	2	2	1	2	ı
22	2	1	2	2	!	2	1	1	2	1	2	2	1	2	1	2	i	2	1	1	2	1	2	2	1	2	1	. 1	2	1	2
23 24	2 2	I	2	2	1	2	1	2	1	2	1	1	2	1	2	1	2	1 2	2	2	1 2	2	1 2	2	1 2	2	1 2	1 2	2	2	2
25	2	2	1	1	2	2	1	1	2		1	1	2	2	1	1	2	2	1	1	2		i	1	2	2	1	1	2	2	1
26	2	2	1	1	2	2	1	1	2	2	1	١	2	2	1	2	1	1	2	2	1	1	2			1	2	2		1	2
27 28	2 2	2	1	1	2	2	1	2	1	1	2	2	1 1	1	2	1 2	2	2	1 2	1	2 1	2 1	1 2	2	1 2	2	2	2		1 2	2 1
40	Ľ																														
29	2	2	1	2	1	1	2	1	2	2	1	2	ı	1	2	ì	2	2	1	2	١	1	2	1	2	2	1	2	1	1	2
30	2	2	1	2	1	1	2	ı	2	_	1	2	1	1	2	2	1	. 1	2		2		1	2		1	2			2	1
31	2	2	1	2	1	ı	2	2	1	-	2	- 1	2	2	1	1	2	2	1	2	1	1	2	2		1	2			2	1
32	2	2	1	2	1	1	2	2	1	1	2	i	2	2	1	2	ı	1	2	ı	2	2	1	1	2	2	ı	2	1	ì	2

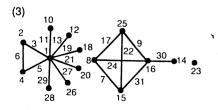
Interaction Table for L_{32} (2³¹)

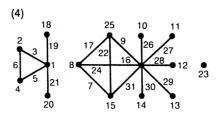
																	lumn														
Column	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	10	31
1	(1)	3	2	5	4	7	6	9	8	11	10	13	12		14	17		19			20	23	22	25	24	27	26				30 29
2		(2)	1	6	7	4	5		н	8	9	14	15	12	13	18	19	16	17	22	23	20	21	26	27	24 25	25 24	30 31		-	28
3			(3)		6	5	4	11		9	8	15	14	13	12	19	18	17	16	23	22 17	21 18	20 19	27 28	26 29	30	31	24			27
4				(4)	1	2	3	12	13	14	15	8	9	10	11	20	21	22	23	16											
5					(5)	3	2	13	12	15	14	9	8	п	10	21	20	2.3	22	17	16	19	18	29	28	31	30	25		27	26
6	1					(6)		14		12	13	10	н	8	9	22	23	20	21	18	19	16	17	30	31 30	28 29	29	26 27		24 25	25 24
7	1						(7)	1.15		13	12	11	10	9	8	23	22	21	20	19	18	17 30	16 31	31 16	17	18	19	20		22	23
8	-							(8)	1	2	3	4	5	6	7	24	25	26	27	28	29	. 30	31								
9	Π								(9)	3	2	5	4	7	6	25	24	27	26	29	28	31	30	17	16	19	18	21		23	22
10	1									(10)		6	7	4	5	26	27	24	25	30	31	28	29	18	19	16	17	22	23 22	20 21	21
11	1										(11)		6	5	4	27	26	25	24	31	30	29	28	19	18 21	17 22	16 23	16	17	18	19
12												(12)	1	2	3	28	29	.30	31	24	25	26	27	20							
13	T												(13)	3	2	29	28	31	30	25	24		26	21	20		22	17	16	19	11
14														(14)		30	31	28	29	26	27		25	22	23		21	18	19	16	17
15	1														(15)		30	29	28	27	26		24	23	22 9	10	20 11	19 12	18	17 14	10
16																(16)	1	2	3	4	5	6	7								
17	T																(17)		2	5	4	7	6	9	8	11		13	12	15	1
18	1																	(18) 1	6	7	4	5	10			9	14	15	12	1
19	-																		(19)		6	5	4	11	10			15 8	9	10	i
20	١					-														(20)) 1	2	3	12	13	, 14					
21	T																				(2)) 3							8	11	1
22																						(2:	2) 1	14						8	9
23	1																						(23) 15					10 5	9	
24	1																							(24) 1			_			
25	1									-															(2	5) 3			4	7	
26	- 1																									(2	5) 1		7	4	
27	- 1																										(2	1) 7	. 6	5	
28																												(28	1) 1	2	
29	7																												(29	3	
30	-																													(30	
31	- 1																														1

Linear Graphs for L₃₂

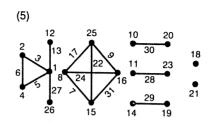


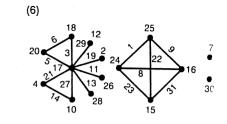


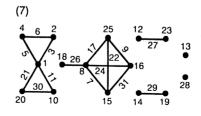


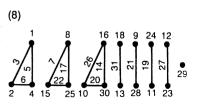


Linear Graphs for L_{32} (Continued)

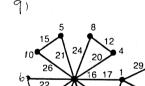


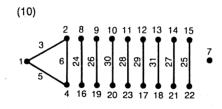


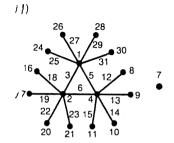


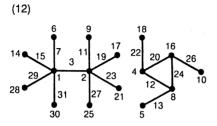


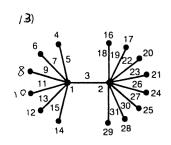
Appendix C











$$L'_{32} (2^1 \times 4^9)$$

 L'_{32} (2¹ × 4⁹) Orthogonal Array

Expt.					Co	olum	n			
No.	1	2	3	4	5	6	7	8	9	10
1	1	1	1	1	1	1	1	1	1	1
2	1	ı	. 2	2	2	2	2	2	2	2
3	1	1	3	3	3	3	3	3	3	3
4	1	1	4	4	4	4	4	4	4	4
5	1	2	1	1	2	2	3	3	4	4
6	1	2	2	2	1	1	4	4	3	3
7	1	2	3	3	4	4	- 1	1	2	2
8	1	2	4	4	3	3	2	2	. 1	1
9	1	3	ı	2	3	4	1	2	3	4
10	1	3	2	1	4	3	2	1	4	3
11	1	3	3	4	1	2	3	4	1	2
12	1	3	4	3	2	ì	4	3	2	ı
13	1	4	1	2	4	3	3	4	2	1
14	1	4	2	1	3	4	4	3	1	2
15	1	4	3	4	2	1	i	2	4	3
16	1	4	4	3	1	2	2	1	3	4
17	2	1	1	4	1	4	2	3	2	3
18	2	1	2	3	2	3	1	4	Ī	4
19	2	1	3	2	3	2	4	i	4	1
20	2	i	4	1	4	1	3	2	3	2
21	2	2	1	4	2	3	4	1	3	2
22	2	2	2	3	1	4	3	2	4	1
23	2	2	3	2	4	1	2	3	1	4
24	2	2	4	1	3	2	1	4	2	3
25	2	3	1	3	3	1	2	4	4	2
26	2	3	2	4	4	2	ī	3	3	1
27	2	3	3	i	1	3	4	2	2	4
28	2	3	4	2	2	4	3	ī	· i	3
29	2	4	1	3	4	2	4	2	1	3
30	2	4	2	4	3	ī	3	1	2	4
31	2	4	3	1	2	4	2	4	3	1
32	2	4	4	2	. 1	3	ĩ	3	4	2

Note: Interaction between columns 1 and 2 is orthogonal to all columns and hence can be estimated without sacrificing any column. It can be estimated from the 2-way table of these columns. Columns 1 and 2 can be combined to form an 8-level column. Interactions between any two 4-level columns is confounded partially with each of the remaining 4-level columns.

Linear Graph for L'32

 $L_{36} (2^{11} \times 3^{12})$

 L_{36} (2¹¹ × 3¹²) Orthogonal Array

-																								
	Expt. No.	1	2	3	4	5	6	7	8	9	10	11	Colum 12		14	15	16	17	18	19	20	21	22	23
	1 2 3	1	1 1	1 1 1	1 1 1	1 1 1	1 1	1 1 1	1 1 1	1 1	1 1 1	1 1	1 2 3	1 2 3	1 2 3	1 2 3	1 2 3	1 2 3	1 2 3	1 2 3	1 2 3	1 2 3	1 2 3	1 2 3
	4 5 6	1 1 1	1 1	1	1 1 1	1 1 1	2 2 2	2 2 2	2 2 2	2 2 2	2 2 2	2 2 2	1 2 3	1 2 3	1 2 3	1 2 3	2 3 1	2 3 1	2 3 1	2 3 1	3 1 2	3 1 2	3 1 2	3 1 2
	7 8 9 10	1 1 1 1	1 1 2 2	2 2 2 1	2 2 2 2 2	2 2 2 2 2	1 1 1 1 1	1 1 1 2 2	1 1 1 2 2	2 2 2 1	2 2 2 1	2 2 2 2 2	1 2 3 1 2	1 2 3 1 2	2 3 1 3	3 1 2 2 3	1 2 3 1 2	2 3 1 3	3 1 2 2 3	3 1 2 3 1	1 2 3 2 3	2 3 1 1 2	2 3 1 3	3 1 2 2 3
-	12	1	2	i 2	2	2	2	2	2 2	i -	1 2	2	3	3	3	1	3	2] 	3	3 1 3	3	2	1 2
	14 15 16	1 1	2 2 2	2 2 2	1 1 2	2 2	2 2 2	1 1 2	2 2	1 1 2	2 2	1 1	2 3 1	3 1 2	1 2 3	2 3 2	1 2	3 1	3	1 2 2	1 2 3	3 1 3	2 3 2	3 !
	17 18	1	2 2	2 2	2 2	1	2 2	2 2	1	2	1	1	2 3	3	1 2	3	3	3	1 2	3	1 2	1 2	3	3
	19 20 21 22 23 24	2 2 2 2 2 2 2	1 1 1 1 1	2 2 2 2 2 2	2 2 2 1 1	1 1 2 2 2	1 1 2 2 2	2 2 2 2 2 2	2 2 2 1 1	1 1 1 1	2 2 2 1 1	1 1 2 2 2	1 2 3 1 2 3	2 3 1 2 3 1	1 2 3 2 3 1	3 1 2 3 1 2	3 1 2 3 1 2	3 1 2 1 2 3	1 2 3 2 3 1	2 3 1 1 2 3	2 3 1 1 2 3	1 2 3 3 1 2	2 3 1 3 1 2	3 1 2 2 3 1
	25 26 27 28 29 30	2 2 2 2 2 2 2	! ! ! 2 2	1 1 2 2 2	2 2 2 1 1	2 2 2 1 1	2 2 2 1 1	1 1 1 1 1	2 2 2 2 2 2 2	2 2 2 2 2 2	1 1 1 1 1	1 1 1 2 2 2	1 2 3 1 2 3	3 1 2 3 1 2	2 3 1 2 3 1	1 2 3 2 3 1	2 3 1 2 3 1	3 1 2 1 2 3	3 1 2 1 2 3	1 2 3 3 1 2	3 1 2 2 3 1	1 2 3 3 1 2	2 3 1 1 2 3	2 3 1 3 1 2
	31 32 33 34 35 36	2 2 2 2 2 2 2	2 2 2 2 2 2	1 1 1 1 1	2 2 2 1 1	1 1 2 2 2	2 2 2 1 1	1 1 2 2 2	1 1 1 1	1 1 2 2 2	2 2 2 2 2 2	2 2 2 1 1	1 2 3 1 2 3	3 1 2 3 1 2	3 1 2 1 2 3	3 1 2 2 3 1	2 3 1 3 1 2	3 1 2 2 3 1	2 3 1 3 1 2	2 3 1 1 2 3	1 2 3 2 3 1	2 3 1 2 3 1	1 2 3 3 1 2	1 2 3 1 2 3

Note: Interaction between any two columns is partially confounded with the remaining columns.

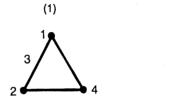
 $L'_{36} (2^3 \times 3^{13})$

 L'_{36} (2³ × 3¹³) Orthogonal Array

			_																٦
Expt. No.	1	2		3	4	5	6	7	olu 8			11	13	2]	13	14	15	1	6
1 2	1	l 1		 	1 1	1 2	1 2	1 2	1 2	1 2	1 2	1 2	1 2		1 2	1 2	1 2	1 2	- 1
3	i	i		1	i	3	3	3	3	3	3	3	3		3	3	3	3	- 1
4	1	2		2	1	1	1	1	1	2	2	2	2		3	3. 1	3	3	3
5 6	1	2		2 2	1	2 3	2 3	2	2	1	1	ı	1		2	2	2		2
7	2	1		2	1	1	1	2	3	1	2	3		3	1	2	2		3
8	2 2	1		2	1	2	2. 3	3	1	2	3	1 2		1 2	2	3	3		i 2
10	2	2		1	1	ı	i	3	2	ì	3	2		3	2	i	3		2
11 12	2 2	2		1	1	2	2	1 2	3	2	1 2	3		1 2	3	2	1 2		3 1
13	1			1	2	1	2	3		3				3	3	2	1		2
14	1	1		1	2	2	3	1	2	1	3	2	2	i	1	3	2		3
15	1	1		1	2	3	1	2	3	2	1			2	2	1	2		1
16 17	1 1	2		2	2	1 2	2	1	3	2				3	1	1	3		2
18	1	2	2	2	2	3	1	2	1	3	3	3	2	1	2	2	1		3
19	2 2		l	2	2	1 2	2	1 2	3	3			1 2	2	2	1 2			3
20 21	2		i	2	2	3	ı	3	2	2			3	1	1	3			2
22	2		2	1	2	1	2	2	3	3			2	1 2	1 2	3			2
23	2 2		2 2	1	2	2	1	1	2	:		3	1	3	3				1
25	1		1	1	3	1	3		1				3	1	3			2	2
26 27			1	1	3	2	1 2	3	2			l 2	1 2	2 3	1 2			3 1	3
28	1		2	2	3	1	3		2			i	i	3	2			1	3
29 30			2	2	3	2 3	1		3			2 3	2 3	1	3			2	1 2
31	- 1	2	1	2	3	1	3					3	2	2				1	1
32 33	- 1	2	1	2	3	2			1 2		3 1	1	3 1	3	3			2	2
34	-	2	2	1	3				2	2	3	2	3	1	- 2			2	3
35 36		2	2	1	3					3 I	1	3	1	2			3 1	1	2
30			_								-	·	-					_	

Notes: (i) The interactions 1×4 , 2×4 and 3×4 are orthogonal to all columns and hence can be obtained without sacrificing any column. (ii) The 3-factor interaction between columns 1, 2, and 4 can be obtained by keeping only column 3 empty. Thus, a 12-level factor can be formed by combining columns 1, 2, and 4 and by keeping column 3 empty. (iii) Columns 5 through 16 in the array $L_{36}(2^3 \times 3^{13})$ are the same as the columns 12 through 23 in the array $L_{36}(2^{11} \times 3^{12})$.

Linear Graphs for L'36





 L_{50} (2¹ × 5¹¹) Orthogonal Array

Expt.						Col	umn					r
No.	1	2	3	4	5	6	7	8	9	10	11	12
1	ı	1	1	ı	1	1	1	1	1	1	1	1
2	1	1	2	2	2	2	2	2	2	2	2	2
3	1	1	3	3	3	3	3	3	3	3	3	3
4	1	1	4	4	4	4	4		4	4	4	4
5	1	1	5	5	5	5	5	5	5	5	5	5
6	1	2	ı	2	3	4	5	1	2	3	4	5
7 8	1	2	2	3	4	,5	1	2	3	4	5	1
9	1	2	3	4	5	1	2	3	4	5	1	2
10	l ;	2	4 5	5 · I	1 2	2	3 4	4	5	1	2	3
	<u> </u>							5	1	2	3	4
11 12	1	3	1 2	3 4	5	2	4	4	1	3	5	2
13	i ;	3	3	5	1 2	3 4	5 1	5 1	2	4	1	3
14	i	3	4	1	3	5	2	2	4	5 1	2	5
15	1	3	5	2	4	1	3	3	5	2	4	1
16	1	4	- i	4	2	5	3	5	3	1	4	2
17	1	4	2	5	3	1	4	1	4	2	5	3
18	1	4	3	ī	4	2	5	2	5	3	1	4
19	1	4	4	2	5	3	1	3	1	4	2	5
20	1	4	5	3	1	4	2	4	2	5	3	1
21	1	5	ı	5	4	3	2	4	3	2	1	5
22	1	5	2	1	5	4	3	5	4	3	2	1
23	1	5	3	2	i	5	4	i	5.	4	3	2
24	1	5	4	3	2	4	5	2	- 1	5	4	3
25	1	5	5	4	3	2	1	3	2	1	5	4
26	2	ı	i	i	4	5	4	3	2	5	2	3
27	2	1	2	2	5	1	5	4	3	1	3	4
28	2	1	3	3	1	2	1	5	4	2	4	5
29 30	2	l I	4 5	4 5	2	3 4	2	1 2	5 1	3 4	5 1	1
31 32	2	2	1	2	1	3	3	2	4	5	5	4
33	2	2	2	3	2	4	4	3	5	1	1	5
34	2	2	4	5	3 4	5 1	5 1	4 5	1 2	2	2	1
35	2	2	5	1	5	2	2	. 1	3	4	3 4	3
36	2	3	1	3	3	1	2	5	5	4	2	4
37	2	3	2	4	4	2	3	1	1	5	3	5
38	2	3	3	5	5	3	4	2	2	1	4	1
39	2	3	4	Ī	1	4	5	3	3	2	5	2
40	2	3	5	2	2	5	1	4	4	3	1	3

(Continued)

 L_{50} (2¹ × 5¹¹) (Continued)

Expt.						Co	lum	n				
No.	1	2	3	4	5	6	7	8	9	10	11	12
41	2	4	1	4	5	4	1	2	5	2	3	3
42	2	4	2	5	l	5	2	3	1	3	4	4
43	2	4	3	1	2	1	3	4	2	4	5	5
44	2	4	4	2	3	2	4	5	3	5	1	ì
45	2	4	5	3	4	3	5	1	4	1	2	2
46	2	5	1	5	2	2	5	3	4	4	3	1
47	2	5	2	1	3	3	1	4	5	5	4	2
48	2	5	3	2	4	4	2	5	1	i	5	3
49	2	5	4	3	5	5	3	1	2	2	1	4
50	2	5	5	4	1	ı	4	2	3	3	2	5

Note: Interaction between columns 1 and 2 is orthogonal to all columns and hence can be estimated without sacrificing any column. It can be estimated from the 2-way table of these two columns. Columns 1 and 2 can be combined to form a 10-level column.

Linear Graphs for L₅₀



Appendix C

 L_{54} (2¹ × 3²⁵) Orthogonal Array

F .																								<u> </u>		
Expt. No.	1	2	3	4	5	6	7	8	9	10	11		Col 13			16	17	18	19	20	21	22	23	24	25	26
1 2	l	1	1	1	1	1	1	1	1	1 2	1 2	1 2	1	1 2	1 2	1 2	1 2	1 2	1 2	1 2	1 2	1	1 2	1	1	i
3	i	1	i	1	1	1	i	1	3	3	3	3	3	3	3	3	3	3	3	3	3	2	3	2	2	2
4	i	1	2	2	2	2	2	2	ı	ı	i	i	1	1	2	3	2	3	2	3	2	3,	2	3	2	3
5	i	1	2	2	2	2	2	2	2	2	2	2	2	2	3	1	3	ı	3	l	3	1	3	1	3	1
6	1	1	2	2	2	2	2	2	3	3	3	3	3	3	1	2	1	2	1	2	1	2	1	?	1	2
8	1	1	3	3	3	3	3	3	1	1	1	1 2	1 2	1	3	2	3	2	3	2	3	2	3	3	3	2
9	i	i	3	3	3	3	3	3	3	3	3	3	3	3	2	1	2	1	2	1	2	ı	2	ı	2	1
10	1	2	1	1	2	2	3	3	1	i	2	2	3	3	1	1	ı	ı	2	3	2	3	3	2	3	2
11 12	1	2	1	1	2	2	3	3	2	2	3	3	1	1 2	2	2	2	2	3	1 2	3	1 2	1 2	3	1 2	3 1
 																										
13 14	1	2	2	2	3	3	I I	1	1	1	2	2	3	3	2	3	2	3	3	2	3	2	2	2	1 2	1 2
15	1	2	2	2	3	3	1	1	3	3	1	1	2	2	1	2	ı	2	2	ı	2	ı	3	3	3	3
16	1	2	3	3	ı	1	2	2	1	1	2	2	3	3	3	2	3	2	1	1	1	1	2	3	2	3
17 18	1	2	3	3	1	1	2	2	2	2	3	3	2	1	1 2	3	2	3	2	2	2	2	3	1 2	3	1 2
	1																									
19 20	1	3	1	2	1	3	2	3	1	2	2	3	2	3	2	1	2	3	2	1	3	2	2	3	3	2
21	1	3	I	2	ı	3	2	3	3	1	3	2	1	2	3	3	1	2	3	3	2	1	1	2	2	1
22	1	3	2	3	2	1	3	ı	1	2	1	3	2	3	2	3	3	2	2	3	1	1	3	2	1	1
23	1	3	2	3	2	1	3	1	2	3	2	1	3,	1	3	1	1 2	3	3	2	2	2	1	3	2	2
25	1	3	3	1	3	2	-1	2		2	1	3	2	3	3	2		1	3	2	2	3	1	1	2	3
26	i	3	3	i	3	2	i	2	2	3	2	1	3	1	1	3	2	2	1	3	3	1	2	2	3	1
27	1	3	3	1	3	2	1	2	3	1	3	2	ı	2	2	1	3	3	2	1	1	2	3	3	ı	2
28 29	2 2	1	1	3	3	2	2	l I	1 2	3 1	3	2	2	1 2	1 2	1 2	3 1	2	3	2	2	3	2	3	1	1
30	2	·	1	3	3	2	2	1	3	2	2	1	1	3	3	3	2	j	1 2	3	1	1 2	3	1 2	2	2
31	2	ı	2	1	1	3	3	2	1	3	3	2	2	1	2	3		1	1	1	3	2	3	2	2	3
32	2	1	2	1	1	3	3	2	2	ı	ı	3	3	2	3	1	2	2	2	2	i	3	1	3	3	1
33	2	1	2	1	1	3	3	2	3	2	2	1	1	3	ı	2	3	3	3	3	2	1	2	1	ı	2
34	2 2	1	3	2	2	1	i 1	3	1 2	3	3	2	2	1 2	3	2	2	3	2	3	1	1	1 2	1 2	3	2
36	2	i	3	2	2	ì	1	3	3	2	2	Ī	ī	3	2	1	1	2	ı	2	3	3	3	3	2	1
37	2	2	ı	2	3	1	3	2	1	2	3	ı	3	2	1	ı	2	3	3	2	ı	1	3	2	2	3
38 39	2 2	2	l ,	2	3	i	3	2	2	3	1	2	ı	3	2	2	3	1	1	3	2	2	١	3	3	1
39			1		3	1	3	2	3	1	2	3	2	1	3	3	1	2	2	1	3	3	2	1	1	2

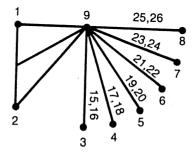
(Continued)

 L_{54} (2¹ × 3²⁵) (Continued)

Expt. No.	١.				_								Co	lum	n											
140.	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26
40	2	2	2	3	1	2	1	3	1	2	3	1	3	2	2	-	_									
41	2	2	2	3	1	2	1	3	2	3	1	2	,	_	_	3	3	2	I	1	2	3	1	ı	3	2
4,2	2	2	2	3	1	2	i	3	3	1	2	3	2	3	3	1	I	3	2	2	3	i	2	2	i	3
				_		_							2		ı	2	2	l	3	3	1	2	3	3	2	1
43	2	2	3	1	2	3	2	1	1	2	3	,	3	2	3	_			_							
44	2	2	3	1	2	3	2	i	,	3	1	2	,	_		2	1	1	2	3	3	2	2	3	1	ì
45	2	2	3	1	2	3	2	i	3	1	2	3	1	3	1	3	2	2	3	ı	1	3	3	ı	2	2
46	2	3	1	•	_	-		Ċ	,	•	2	3	2	i	2	ı	3	3	1	2	2	1	1	2	3	3
47	2	-	- :	3	2	3	I	2	1	3	2	3	I	2	1	1	3	2	2	3	3	2	1	1	2	3
48	2	3	1	3	2	3	ı	2	2	i	3	ı	2	3	2	2	1	3	3	1	1	3	2	2	3	
40		3	I	3	2	3	I	2	3	2	1	2	3	1	3	3	2	l	1	2	2	1	3	3) 	2
49	2	3	2	,	3	,			_																_	_
50	2	3	2	,	3	. !	2	2	1	3	2	3	1	2	2	3	ı	1	3	2	1	1	2	3	3	2
51	2	3	2	:	-		2	3	2	I	3	1	2	3	3	1	2	2	1	3	2	2	3	1	1	3
		-	_	•	3	ı	2	3	3	2	1	2	3	ı	I	2	3	3	2	1	3	3	1	,	2	1
52	2	3	3	2	1	2	3	1	ı	3	2	3	1	2	3	2	2	3			-	_		~	2	•
53	2	3	3	2	1	2	3	1	2	ı	3	ī	,	3	1	3	3	3	1	1	_	3	3	2	ı	1
54	2	3	3	2	1	2	3	1	3	2	1	2	3	1	2	1	,	1	2	2	3	i	ı	3	2	2
								-	_	-	•	۷	,	•	2	1	i	2	3	3	1	2	2	1	3	3

Notes: (i) Interaction between columns 1 and 2 is orthogonal to all columns and hence can be estimated without sacrificing any column. Also, these columns can be combined to form a 6-level column. (ii) The interactions 1×9 , 2×9 , and $1 \times 2 \times 9$ appear comprehensively in the columns 10, 11, 12, 13, and 14. Hence, the aforementioned interactions can be obtained by keeping columns 10 through 14 empty. Also, columns 1, 2, and 9 can be combined to form a 18-level column by keeping columns 10 through 14 empty.

Linear Graph for L₅₄



 L_{64} (2⁶³)

L₆₄ (2⁶³) Orthogonal Array

Expt.															C	oluı	mn														
No.	1	2	3	4	5	6	7	8	9	10	11	12	13	14				18	19	20	21	22	23	24	25	26	27	28	29	30	31
1 2 3 4 5 6 7	1 1 1 1 1	1 1 1 1 1	1 1 1 1 1	1 1 1 1 1	1 1 1 1 1 1	1 1 1 1 1 1 1	1 1 1 1 1 1	1 1 1 2 2 2	1 1 1 2 2	1 1 1 2 2 2	1 1 1 2 2 2	1 1 1 2 2 2	I I I 2 2 2	1 1 1 2 2 2	1 1 1 2 2	1 1 2 2 1 1	1 1 2 2 1 1	1 1 2 2 1 1	1 1 2 2 1 1	1 1 2 2 1 1	1 1 2 2 1 1	1 1 2 2 1 1	1 1 2 2 1 1	1 1 2 2 2 2 2	1 1 2 2 2 2 2	1 1 2 2 2 2 2	1 1 2 2 2 2 2	1 1 2 2 2 2 2	1 1 2 2 2 2 2	1 1 2 2 2 2	1 1 2 2 2 2 2
8	1	1	1	1	1	1	1	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	1	1	1	1	1	ı	1	1
9 10 11 12 13 14 15	1 1 1 1 1	1 1 1 1 1 1 1	1 1 1 1 1 1	2 2 2 2 2 2 2 2 2	2 2 2 2 2 2 2 2 2	2 2 2 2 2 2 2 2 2	2 2 2 2 2 2 2 2 2	1 1 1 2 2 2 2	1 1 1 2 2 2 2	1 1 1 2 2 2 2	1 1 1 2 2 2 2	2 2 2 1 1 1	2 2 2 1 1 1	2 2 2 1 1 1	2 2 2 1 1 1	1 2 2 1 1 2 2	1 2 2 1 1 2 2	1 2 2 1 1 2 2	1 2 2 1 1 2 2	2 1 1 2 2 1	2 1 1 2 2 1 1	2 1 1 2 2 1	2 1 1 2 2 1	1 2 2 2 2 1 1	1 2 2 2 2 1 1	1 1 2 2 2 2 1 1	1 1 2 2 2 2 2 1 1	2 1 1 1 2 2	2 2 1 1 1 2 2	2 1 1 1 2 2	2 1 1 1 2 2
17 18 19 20 21 22 23 24	1 1 1 1 1 1	2 2 2 2 2 2 2 2 2	2 2 2 2 2 2 2 2 2	1. 1. 1. 1. 1. 1.	1 1 1 1 1 1	2 2 2 2 2 2 2 2	2 2 2 2 2 2 2 2	1 1 1 2 2 2 2	1 1 1 2 2 2 2 2	1	2 2 2 1 1	1 1 1 2 2 2 2	1 1 1 2 2 2 2	2 2 2 1 1 1	2 2 2 1 1 1	1 1 2 2 1 1 2 2	1 2 2 1 1 2 2	2 1 1 2 2 1	2 1 1 2 2 1	1 2 2 1 1 2 2	1 2 2 1 1 2 2	2 1 1 2 2 1	2 1 1 2 2 1	1 2 2 2 2 1	1 1 2 2 2 2 1 1	2 1 1 1 2 2	2 1 1 1 2 2	1 2 2 2 2 1	1 1 2 2 2 2 2 1	2 1 1 1 2 2	2 2 1 1 1 2 2
25 26 27 28 29 30 31 32	1 1 1 1 1 1	2 2 2 2 2 2 2 2 2	2 2 2 2 2 2 2 2 2 2	2 2 2 2 2 2 2 2 2	2 2 2 2 2 2 2 2 2	1 1 1 1 1	1 1 1 1 1 1	1 1 1 2 2 2 2	1 1 1 2 2 2 2	1	2 2 2 2 1 1 1	2 2 2 2 1 1 1	2 2 2 1 1 1	1 1 1 2 2 2 2	1 1 1 2 2 2 2	1 1 2 2 1 1 2 2	1 1 2 2 1 1 2 2	2 2 1 1 2 2 1	2 1 1 2 2 1	2 1 1 2 2 1	2 2 1 1 2 2 1	1 2 2 1 1 2 2	1 1 2 2 1 1 2 2	1 1 2 2 2 2 1 1	1 2 2 2 2 1	2 2 1 1 1 2 2	2 1 1 1 1 2 2	2 1 1 1 1 1 2	2 2 1 1 1 1 2	1 1 2 2 2 2 2 1	1 1 2 2 2 2 2 1
33 34 35 36 37 38 39 40	2 2 2 2 2 2 2 2 2 2 2	1 1 1 1 1	2 2 2 2 2 2 2 2 2	1 1 1 1 1	2 2 2 2 2 2 2 2	1 1 1 1 1	2 2 2 2 2 2 2 2 2	1 1 1 2 2 2 2	2 2 2 2 1 1 1	2 1 2 2 2 2	2 2 2 1 1	1 1 1 2 2 2 2	1	1 1 1 2 2 2 2	2 2 2 1 1 1	1 2 2 1 1 2 2	1 2 2 1	1 2 2 1 1 2 2	1 2 2 1	1 2 2 1 1 2 2	2 1 1 2 2 1	1 2 2 1 1 2	1 2 2 1		1 1 1 2	1 2 2 2 2 2	1 1	1 2 2 2 2	1	1 1 2 2 2 2 1 1	2 2 1 1 1 2 2

(Continued)

L₆₄ (2⁶³) (Continued)

Expt.															C	olur	nn														
No.	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	31
41	2	1	2	2	1	2	1	1	2	1	2	2	ı	2	1	1	2	1	2	2	1	2	1	ı	2	1	2	2	1	2	ı
42	2	1	2	2	1	2	1	i	2	1	2	2	1	2	1	1	2	1	2	2	1	2	1	1	2	1	2	2	1	2	1
43	2	1	2	2	1	2	i	1	2	1	2	2	1	2	1	2	1	2	1	1	2	1	2	2	ì	2	ì	1	2	1	2
44	2	1	2	2	1	2	1	1	2	1	2	2	1	2	1	2	1	2	ı	1	2	1	2	2	1	2	1	1	2	1	2
45	2	1	2	2	1	2	1	2	1	2	ł	1	2	1	2	1	2	1	2	2	1	2	1	2	1	2	1	1	2	ı	2
46	2	1	2	2	1	2	1	2	1	2	1	i	2	i	2	ì	2	i	2	2	ı	2	1	2	1	2	1	ł	2	1	2
47	2	1	2	2	1	2	1	2	ı	2	1	ì	2	1	2	2	l	2	1	1	2	1	2	ı	2	l	2	2	1	2	l
48	2	ì	2	2	1	2	1	2	1	2	1	1	2	ı	2	2	ı	2	1	1	2	1	2	ı	2	1	2	2	ı	2	1
49	2	2	1	ı	2	2	1	1	2	2	1	1	2	2	1	1	2	2	ı	1	2	2	1	1	2	2	1	1	2	2	l
50	2	2	1	1	2	2	i	i	2	2	1	1	2	2	1	1	2	2	1	1	2	2	1	1	2	2	1	1	2	2	1
51	2	2	1	1	2	2	1	1	2	2	1	1	2	2	1	2	1	1	2	2	i	1	2	2	- 1	1	2	2	1	1	2
52	2	2	1	1	2	2	1	١	2	2	1	i	2	2	1	2	1	- 1	2	2	1	1	2	2	1	1	2	2	1	١	2
53	2	2	1	1	2	2	1	2	1	1	2	2	1	ì	2	1	2	2	1	1	2	2	1	2	1	1	2	2	1	1	2
54	2	2	1	1	2	2	1	2	1	1	2	2	1	1	2	ı	2	2	1	1	2	2	1	2	1	1	2	2	1	I	2
55	2	2	ı	1	2	2	1	2	1	1	2	2	_1	1	2	2	1	I	2	2	1	1	2	1	2	2	1	1	2	_	
56	2	2	1	1	2	2	ı	2	1	ı	2	2	1	1	2	2	1	1	2	2	1	1	2	1	2	2	1	ı	2	2	I
57	2	2	1	2	1	1		1	2	2	1	2	1	1	2	1	2	2	1	2	1	1	2	1	2	2	1	2	ı	1	2
58	2	2	1	2	1	1	2	1	2	2	1	2	1	1	2	1	2	2	1	2	1	1	2	1	2	2	1	2	1	1	2
59	2	2	i	2	1	1	2	1	2	2	1	2	1	1	2	2	1	١	2	1	2	2	- 1	2	1	1	2	: 1	2	2	. 1
60	2	2		2	i	1	2	1	2	2	i	2	1	1	2	2	1	1	2	1	2	2	. 1	2	: 1	1	2	: 1	2	2	1
61	2	2		2	. 1	i	2	2	1	1	2	. 1	2	2	1	1	2	2	- 1	2	1	1	2	2	. 1	. 1	2	: 1	2	. 2	. 1
62	2			2	. 1	i	2	2	1	1	2	1	2	2	1	1	2	2	. 1	2	ı	1	2	2	: 1	. 1	2	! 1	2	2	. 1
63	2			2	. 1	1	2	2	1	1	2	. 1	2	2	1	2	1	1	2	. 1	2	2	! 1	1	2	2 2	: 1	2	! !	. 1	2
64	2			_		1	2		1	ı	2		2	2	1	2	ì	1	2	i	2	2	: 1	1	2	2 2	! !	2	2 1	. 1	2

L₆₄ (2⁶³) (Continued)

Expt.					-										(Colu	umn	1														
No.	32	33	34	35	36	37	38	39	40	41	42	43	44	45	46	47	48	49	50	51	52	53	54	55	56	57	58	59	60	61	62	63
1 2	1 2	1 2 1	2	1 2	1 2 1	1 2 1	1 2 1	1 2 1	1 2 1	1 2 1	1 2 1	1 2 1	1 2	1 2 1	1 2 1	1 2 1	1 2 2	1 2 2	1 2 2	1 2 2	1 2 2	1 2 2	1 2 2	1 2 2	1 2 2	1 2 2	1 2 2	1 2 2	1 2 2	1 2 2	1 2 2	1 2 2
3 4 5 6	1 2 1 2	1 1 2	2 1 2	1 1 2	1 1 2	1 1 2	1 1 2	1 1 2	2 2	2 2	2 2	2 2	2 2	2 2	2 2	2 2	1 1 2	1 1 2	1 1 2	1 1 2	1 1 2	1 1 2	1 1 2	1 1 2	1 2 1	1 2	1 2	1 2	1 2 1	1 2	1 2	1 2
7 8	1 2	1 2	1 2	1 2	1 2	1 2	1 2	1 2	2	2	2	2	2	2 1	2	2	2 1	2	2	2	2	2	2	2	' 1 2	1 2	1 2	1 2	1 2	1 2	1 2	1 2
9 10 11 12 13 14 15	1 2 1 2 1 2 1 2	1 2 1 2 1 2 1 2	1 2 1 2 1 2 1 2	1 2 1 2 1 2 1 2	2 1 2 1 2 1 2	2 1 2 1 2 1 2	2 1 2 1 2 1 2	2 1 2 1 2 1 2	1 2 1 2 2 1 2	1 2 1 2 2 1 2	1 2 1 2 2 1 2	1 2 1 2 2 1 2	2 1 2 1 1 2 1 2	2 1 2 1 1 2 1 2	2 1 2 1 1 2 1 2	2 1 2 1 1 2 1 2	1 2 2 1 1 2 2	1 2 2 1 1 2 2	1 2 2 1 1 2 2	1 2 1 1 2 2 1	2 1 2 2 1 1 2	2 1 2 2 1 1 2	2 1 2 2 1 1 2	2 1 2 2 1 1 2	1 2 2 1 2 1 1 2	1 2 2 1 2 1 1 2	1 2 2 1 2 1 1 2	1 2 2 1 2 1 1 2	2 1 2 1 2 2 2	2 1 2 1 2 2 1	2 1 2 1 2 2 1	2 1 1 2 1 2 2 1
17 18 19 20 21 22 23 24	1 2 1 2 1 2 1 2	1 2 1 2 1 2 1 2	2 1 2 1 2 1 2	2 1 2 1 2 1 2	1 2 1 2 1 2 1 2	1 2 1 2 1 2 1 2	2 1 2 1 2 1 2	2 1 2 1 2 1 2	1 2 1 2 2 1 2	1 2 1 2 2 1 2	2 1 2 1 1 2 1 2	2 1 2 1 1 2 1 2	1 2 1 2 2 1 2	1 2 1 2 2 1 2	2 1 2 1 1 2 1 2	2 1 2 1 1 2 1 2	1 2 2 1 1 2 2	1 2 2 1 1 2 2	2 1 2 2 1 1 2	2 1 2 2 1 1 2	1 2 2 1 1 2 2	1 2 2 1 1 2 2	2 1 1 2 2 1 1 2	2 1 2 2 1 1 2	1 2 2 1 2 1 1	1 2 2 1 2 1 1	2 1 2 1 2 2 1	2 1 2 1 2 2 1	1 2 2 1 2 1 1 2	1 2 2 1 2 1 1	2 1 1 2 1 2 2 1	2 1 2 1 2 2 1
25 26 27 28 29 30 31 32	1 2 1 2 1 2	1 2 1 2 1	2 1 2 1 2 1 2	2 1 2 1 2 1 2	2 1 2 1 2 1 2	2 1 2 1 2 1 2	1 2 1 2 1 2 1 2	1 2 1 2 1 2 1 2	1 2 1 2 2 1 2	1 2 1 2 1 2 1	2 1 2 1 1 2 1 2	2 1 2 1 1 2 1 2	2 1 2 1 2 1 2	1 2 1 1 2	1 2 1 2 2 1 2	1 2 2 1 2 1	1 2 2 1 1 2 2	1 2 1 1 2 2	2 1 2 2 1 1 2	2 1 1	2 1 1 2 2 1 1 2	2 1 2 2 1 1 2	1 2 2 1 1 2 2	1 2 2 1 1 2 2	1 2 2 1 2 1 1	1 2 2 1 2 1 1	2 1 2 1 2 2 1	2 1 2 1 2 2 1	2 1 2 1 2 2	2 1 2 1 2 2 1	1 2 2 1 2 1 1 2	1 2 2 1 2 1 1 2
33 34 35 36 37 38 39 40	1 2 1 2 1 2 1 2	1 2 1 2 1 2	2	2	2	2 1 2 1 2	2 1 2 1 2	2 1 2 1 2	1 2 1 2 2 1 2	2 1 1 1 2 1 2	2 1 2 2 1 2	2 1 2 1 2 1 2	1 2 1 2 2 1 2	2 1 2 2	2	2 1 1 2	2 1 1 2 2	2 1 2 2 1 1 2	1 2 2	2 2 1	2 2 1 1 2 2	2 1 2 2 1 1 2	2 1 1 2 2	2 1 2 2 1 1 2	2 2 1 2 1	1 2 1 2 2	2 2 1 2	1 2 1 2 2		2 1 2 2		2 1 2 1 2 2 1 2

L₆₄ (2⁶³) (Continued)

Expt.																	umr															
No.	32	33	34	35	36	37	38	39	40	41	42	43	44	45	46	47	48	49	50	51	52	53	54	55	56	57	58	59	60	61	62	63
41	1	2	1	2	2	1	2	1	ı	2	i	2	2	1	2	1	1	2	1	2	2	1	2	1	1	2	1	2	2	1	2	1
42	2	1	2	1	1	2	1	2	2	1	2	-1	1	2	1	2	2	1	2	1	i	2	1	2	2	1	2	1	1	2	1	2
43	1	2	١	2	2	ı	2	1	1	2	ı	2	2	1	2	1	2	1	2	1	1	2	1	2	2	1	2	1	1	2	1	2
44	2	1	2	1	1	2	1	2	2	1	2	1	1	2	1	2	i	2	1	2	2	1	2	1	1	2	1	2	2	i	2	1
45	1	2	1	2	2	1	2	1	2	1	2	ı	1	2	1	2	1	2	1	2	2	1	2	-1	2	ì	2	1	1	2	1	2
46	2	1	2	ı	1	2	1	2	1	2	1	2	2	1	2	1	2	ì	2	1	ı	2	1	2	1	2	ı	2	2	i	2	1
47	1	2	ì	2	2	i	2	1	2	i	2	1	1	2	1	2	2	1	2	1	1	2	ì	2	i	2	1	2	2	i	2	ì
48	2	1	2	1	1	2	1	2	1	2	1	2	2	ı	2	1	1	2	i	2	2	ı	2	1	2	1	2	1	1	2	1	2
49	\ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \	2	2	1	1	2	2	1	1	2	2	1	1	2	2	1	1	2	2	1	1	2	2	1	1	2	2	ı	1	2	2	1
50	2	1	1	2	2	ī	1	2	2	1	1	2	2	1	1	2	2	i	1	2	2	i	i	2	2	1	1	2	2	1	1	2
51	1	2	2	1	1	2	2	1	1	2	2	1	1	2	2	1	2	1	1	2	2	ì	1	2	2	1	1	2	2	j	1	2
52	2	1	1	2	2	1	- 1	2	2	1	1	2	2	1	- 1	2	1	2	2	- 1	1	2	2	1	1	2	2	1	ì	2	2	1
53	1	2	2	1	ı	2	2	1	2	1	i	2	2	- 1	1	2	1	2	2	1	ì	2	2	1	2	1	1	2	2	. 1	1	2
54	2	1	1	2	2	1	1	2	1	2	2	1	1	2	2	1	2	1	1	2	2	1	1	2	1	2	2	1	1	2	2	
55	1	2	2	1	1	2	. 2	1	2	1	1	2	2	1	1	2	2	1	1	2	2	1	1	2	1	2	2	1	1	2	_	-
56	2	. 1	1	2	2	1	ì	2	1	2	2	1	1	2	2	1	1	2	2	1	1	2	2	1	2	1	1	2	2	. 1	1	2
57	١,	2	2	1	2	1	1		1	2	2	1		! 1	1	2	1	2	2	: 1	2	1	1	2	. 1	2	2	1	2	! 1	1	2
58	2	_	1	2	1	2	. 2	. 1	2	1	1	2	. 1	2	2		2	1	1	2	. 1	2	2	. 1	2	. 1	1	2	. 1	2	2 2	1
59	li		. 2	1	2	. 1	1	2	1	2	. 2	1	2	1	1	2	. 2	1	1	2	. 1	2	2	. 1	2	1	1	2	: 1	2	2 2	! 1
60	12	_	1	2	. 1	2	2 2	1	2	i	1	2	! 1	2	2	1	1	2	2	! 1	2	. 1	ı	2	: 1	2	2	. 1	- 2	2 1	1	2
61	1		. 2	: 1	2	: 1	1	2	2	. 1	1	2	: 1	2	2	. 1	1	2	. 2	! 1	2	1	1	2	2	! 1	1	2	2 1	1 2	2 2	2 1
62	1 2	2 1	1	- 2	! 1	2	2 2	. 1	- 1	2	2	. 1	2	2 1	1	2	2	. 1	1	2	2 1	2	2	! 1	1	2	2 2	: 1	1 2	2 1	1 1	1 2
63	1	1 2	2 2	! 1	2	2 1	1	2	2	. 1	1	2	! !	1 2	2	: 1	2	. 1	1	2	2 1	2	2	! 1	. 1	2	2 2	! 1	1 2	2 1	i i	1 2
64	12	2 1	1	2	2 1	1 2	2 2	. 1	1	2	2 2	: 1	1	2 1	1	- 2	! 1	2	: 2	2 1	2	i	1	2	2 2	2 1	1	2	2	1 2	2 :	2 1

 L'_{64} (4²¹)

L'₆₄ (4²¹) Orthogonal Array

		-																			
Expt. No.	1	2	3	4	5	6	7	8	0		olu 11		12	1.1	15	1.	17	10	10	20	
				_					_			12		14	15	10	1/	10	19	20	21
1	1	1	1	ı	1	ı	ı	1	i	1	ı	1	1	1	ı	ı	1	1	1	ı	.1
2	1	1	l	ì	1	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2
3	1	1	1	1	1	3	3	3	3	3	3	3	3	3	3	3	3	3	3	3	3
	1	1	1	1	i	4	4	4	4	4	4	4	4	4	4	4	4	4	4	4	4
6	1	2	2	2	2	1 2	1	1	1	2	2	2	2	3	3	3	3	4	4	4	4
7	1	2	2	2	2	3	2	2	2	1	1	1	1	4	4	4	4	3 2	2	2	3
8	i	2	2	2	2	4	4	4	4	3	3	3	3	2	2	2	2	1	1	1	1
														_			_			•	
9	1	3	3	3	3	1	1	i.	l	3	3	3	3	4	4	4	4	2	2	2	2
10	1	3	3	3	3	2	2	2	2	4	4	4	4	3	3	3	3	1	1	1	1
11 12	1	3	3	3	3	3 4	3	3	3	1	1	1	1	2	2	2	2	4	4	4	4
							. 4	4	4	2	2	2	2	1	1	1	1	3	3	3	3
13 14	1	4	4	4	4	2	1 2	1	1	4	4	4	4	2	2	2	2	3	3	3	3
15	li	4	4	4	4	3	3	3	3	2	2	2	2	4	1 4	1	1	4	4	4	4
16	i	4	4	4	4	4	4	4	4	ī	ī	1	1	3	3	3	3	2	2	2	2
	ļ																				
17	2	1	2	3	4	i	2	3	4	1	2	3	4	ı	2	3	4	ı	2	3	4
18	2	1	2	3	4	2	ı	4	3	2	1	4	3	2	1	4	3	2	1	4	3
19 20	2 2	1	2	3	4	3 4	4	2	2	3	3	2	2	3	4	1 2	2	3 4	4	1 2	2
21	2	2	1	4			2	3											3		1
22	2	2	1	4	3	1	1	4	4	2	1 2	4	3	3 4	4	1	2	3	3	2	1 2
23	2	2	i	4	3	3	4	ī	2	4		2	ī	1	2	3	4	2	1	4	3
24	2	2	i	4	3	4	3	2	1	3	4	1	2	2	ī	4	3	1	2	3	4
	_	_																			
25 26	2 2	3	4	l I	2	1 2	2	3	4	3	4	1	2	4	3	2	1	2	1	4	3
27	2	3	4	1	2	3	4	4	3	4	2	2	1	3	4	1	2	1	2	2	4 1
28	2	3	4	i	2	4	3	2	1	2	1	4	3	1	2	3	4	3	4	1	2
29	2	4	3	2	1	ı	2	3	4	4	3	2	1	2	1	4	3	3	4	1	2
30	2	4	3	2	i	2	1	4	3	3	4	ī	2	1	2	3	4	4	3	2	1
31	2	4	3	2	1	3	4	1	2	2	1	4	3	4	3	2	1	1	2	3	4
32	2	4	3	2	- 1	4	3	2	i	1	2	3	4	3	4	1	2	2	1	4	3
33	3	1	3	4	2	1	3	4	2	1	3	4	2	1	3	4	2	1	3	4	2
34	3	i	3	4	2	2	4	3	1	2	4	3	1	2	4	3	1	2	4	3	1
35	3	i	3	4	2	3	i	2	4	3	1	2	4	3	i	2	4	3	1	2	4
36	3	1	3	4	2	4	2	ı	3	4	2	l	3	4	2	1	3	4	2	1	3
37	3	2	4	3	1	i	3	4	2	2	4	3	1	3	1	2	4	4	2	1	3
38	3	2	4	3	i	2	4	3	1	1	3	4	2	4	2	ì	3	3	1	2	4
39	3	2	4	3	i	3	1	2	4	4	ı	1	3	ı	3	4	2	2	4	3	1
40	3	2	4	3	i	4	2	ı	3	3	2	2	4	2	4	3	i	1	3	4	2
·																					

 L'_{64} (4²¹) (Continued)

Expt.										С	olu	mn									
No.	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21
41	3	3	1	2	4	1	3	4	2	3	1	2	4	4	2	1	3	2	4	3	1
42	3	3	ı	2	4	2	4	3	1	4	2	i	3	3	1	2	4	1	3	4	2
43	3	3	ì	2	4	3	1	2	4	1	3	4	2	2	4	3	1	4	2	1	3
44	3	3	1	2	4	4	2	1	3	2	4	3	1	1	3	4	2	3	1	2	4
45	3	4	2	ı	3	1	3	4	2	4	2	1	3	2	4	3	1	3	1	2	4
46	3	4	2	1	3	2	4	3	1	3	1	2	4	1	3	4	2	4	2	1	3
47	3	4	2	1	3	3	1	2	4	2	4	3	ì	4	2	1	3	1	3	4	2
48	3	4	2	1	3	4	2	1	3	i	3	4	2	3	ì	2	4	2	4	3	1
49	4	1	4	2	3	1	4	2	3	1	4	2	3	ı	4	2	3	1	4	2	3
50	4	1	4	2	3	2	3	1	4	2	3	1	4	2	3	1	4	2	3	1	4
51	4	ì	4	2	3	3	2	4	1	3	2	4	1	3	2	4	1	3	2	4	1
52	4	ı	4	2	3	4	l	3	2	4	1	3	2	4	1	3	2	4	1	3	2
53	4	2	3	1	4	1	4	2	3	2	3	1	4	3	2	4	1	4	1	3	2
54	4	2	3	1	4	2	3	1	4	1	4	2	3	4	1	3	2	3	2	4	1
55	4	2	3	1	4	3	2	4	1	4	1	3	2	i	4	2	3	2	3	1	4
56	4	2	3	1	4	4	1	3	2	3	2	4	1	2	3	1	4	ı	4	2	3
57	4	3	2	4	1	ı	4	2	3	3	2	4	1	4	1	3	2	2	3	ı	4
58	4	3	2	4	1	2	3	1	4	4	t	3	2	3	2	4	1	1	4	2	3
59	4	3	2	4	1	3	2	4	i	1	4	2	3	2	3	1	4	4	. 1	3	2
60	4	3	2	4	1	4	ı	3	2	2	3	1	4	1	4	2	3	3	2	4	1
61	4	4	1	3	2	ì	4	2	3	4	1	3	2	2	3	1	4	3	2	4	1
62	4	4	1	3	2	2	3	1	4	. 3	2	4	1	1	4	2	3	4	1	3	2
63	4	4	1	3	2	3	2	4	1	2	3	i	4	4	i	3	2	1	4	2	3
64	4	4	1	3	2	4	1	3	2	1	4	2	3	3	2	4	1	2	3	1	4

 L_{81} (3⁴⁰)

L₈₁ (3⁴⁰) Orthogonal Array

Expt.										Co	lumn									
No.	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
1	1	1	1	1	1	1	- 1	1	1	1	1	1	ı	1	1	1	- 1	1	ı	1
2	1	1	1	1	1	1	1	1	1	1	1	1	I I	2	2	2	2	2	2	2
4	1	1	1	1	2	2	2	2	2	2	2	2	2	3 1	3 1	3	3	3 ·1	3	3
5	ì	1	1	i	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2
6	1	1	1	1	2	2	2	2	2	2	2	2	2	3	3	3	3	3	3	3
7 8	1	1	1	l i	3	3	3	3	3	3	/3 3	3	3	2	1 2	1 2	1 2	1 2	1 2	1
9	1	1	1	ì	3	3	3	3	3	3	3	3	3	3	3	3	3	3	3	2
10	1	2	2	2	1	1	1	2	2	2	3	3	3	1	1	1	2	2	2	3
11 12	1	2	2	2	1	1	1	2	2	2	3	3	3	2	2	2	3	3	3	i
13	1	2	2	2	1	1	1	2	2	2	3	3	3	3	3	3	1	1	1	2
14	i	2	2	2	2	2	2 2	3	3	3	1	1	l I	1 2	1 2	2	2	2	2	3
15	1	2	2	2	2	2	2	3	3	3	ı	1	ı	3	3	3	1	ı	1	2
16	1	2	2	2	3	3	3	1	1	ı	2	2	2	ı	1	1	2	2	2	3
17 18	1	2	2	2	3	3	3	1	1	1	2	2	2	2	2	2	3	3	3 1	1 2
19	1	3	3	3	1	1		3	3	3	2	2	2							
20	1	3	3	3	i	i	i.	3	3	3	2	2	2	1 2	1 2	1 2	3 1	3	3	2
21	1	3	3	3	i	I.	1	3	3	3	2	2	2	3	3	3	2	2	2	1,
22	1	3	3	3	2	2	2	1	1	i I	3	3	3	1 2	1 -	1	3	3	3	2
24	i	3	3	3	2	2	2	i	i	1	3	3	3	3	2	2	1 2	1	1	3
25	ı	3	3	3	3	3	3	2	2	2	1	i	i	ı	1	1	3	3	3	2
26 27	i i	3	3	3	3	3	3	2	2	2	1	- i - 1	1	2	2	2	1	1	l	3
														3		3	2	2	2	1
28 29	2	1	2	3	1	2 2	3	i	2	3	1	2	3	1	2	3	ı	2	3	1
30	2	i	2	3	i	2	3	1	2	3	1	2 2	3	2	3	1 2	2	3	2	2 3
31	2	1	2	3	2	3	1	2	3	ı	2	3	1	ı	2	3	1	2	3	1
32 33	2	1	2 2	3	2	3	1.	2	3	1	2	3	1	2	3	1	2	3	ı	2
34	2	1	2	3	3	3	1	2	3	1	2	3	1	3	1	2	3	1	2	3
35	2	ì	2	3	3	1	2	3	1	2 2	3	1	2	1	2	3	1 2	2	3 1	1 2
36	2	1	2	3	3	l	2	3	Ī	2	3	i	2	3	1	2	3	1	2	3
37	2	2	3	1	1	2	3	2	3	1	3	1	2	1	2	3	2	3	1	3
38 39	2	2	3	1	1	2	3	2	3	1	3	1	2	2	3	I	3	1	2	1
39			3	1	ı	2	3	2	3	ı	3	1	2	3	1.	2	1	2	3	2

(Continued)

 L_{81} (3⁴⁰) (Continued)

	Expt.	1	2	3	4	5	6	7	8	9	Col	umn 11	12	13	14	15	16	17	18	19	20
+								<u>.</u>													
1	40	2	2	3	1	2	3	1	3	1	2	. 1	2	3	1	2	3	2	3	1	3
	41 42	2 2	2	3	1 1	2	3	1 1	3	1	2	1	2	3	2	3	1 2	3	1	2	2
	43	2	2	3	i	3	1	2	1	2	3	2	3	1	1	2	3	2	3	1	3
	44	2	2	3	i	3	i	2	i	2	3	2	3	1	2	3	1	3	1	2	1
	45	2	2	3	1	3	1	2	I	2	3	2	3	ı	3	1	2	1	2	3	2
	46 47	2	3	ı	2	.1	2	3	3	1	2	2	3	1	1	2	3	3	1	2	2
1	48	2 2	3	1	2	1	2	3	3	1	2	2	3	1	2	3	1	1 2	2	3	3 1
	49	2	3	ı	2	2	3	1	1	2	3	3	1	2	1	2	3	3	1	2	2
	50	2	3	1	2	2	3	i	i	2	3	3	1	2	2	3	1	ı	2	3	3
	51	2	3	I	2	2	3	1	1	2	3	3	i	2	3	1	2	2	3	1	1
-	52	2	3	1	2	3	1	2	2	3	1	1	2	3	-1	2	3	3	1	2	2
	53 54	2 2	3	1	2	3	1	2	2	3	1	1	2	3	3	3	1	1 2	2 3	3	3 1
I	55	3	1	3	2	1	3	2	1	3	2	1	3	2	ı	3	2	ı	3	2	1
	56	3	1	3	2	1	3	2	1	3 .	2	1	3	2	2	1	3	2	1	3	2
	57	3	1	3	2	1	3	2	1	3	2	1	3	2	3	2	1	3	2	1	3
	58 59	3	1	3	2	2	l I	3	2	1	3	2	1	3	1 2	3	2	1	3	. 2	1
	60	3	1	3	2	2	1	3	2	i	3	2	1	3	3	2	3	2	1 2	3	2
	61	3	1	3	2	3	2	1	3	2	1	3	2	1	ı	3	2	1	3	2	1
	62	3	1	3	2	3	2	i	3	2	. 1	3	2	1	2	1	3	2	1	3	2
	63	3	1	3	2	3	2	1	3	2	1	3	2	1	3	2	i	3	2	i	3
	64 65	3	2	1	3	1	3	2 2	2	1	3	3	2	1	1 2	3	2	2	1 2	3	3
	66	3	2	1	3	i	3	2	2	i	3	3	2	i	3	2	1	1	3	1	1 2
	67	3	2	1	3	2	i	. 3	3	2	i	1	3	2	1	3	2	2	1	3	3
	68	3	2	1.	3	2	1	3	3	2	1	1	3	2	2	1	3	3	2	1	i
	69	3	2	1	3	2	1	3	3	2	1	1	3	2	3	2	1	1	3	2	2
-	70 71	3	2	1	3	3	2	1	1	3	2	2	1	3	1 2	3	2	2	1	3	3
	72	3	2	1	3	3	2	1	1	3	2	2	1	3	3	2	1	1	3	2	2
	73	3	3	2	1	1	3	2	3	2	1	2	1	3	1	3	2	3	2	1	2
	74	3	3	2	1	1	3	2	3	2	ı	2	1	3	2	1	3	1	3	2	3
	75	3	3	2	. 1	1	3	2	3	2	1	2	1	3	3	2	1	2	1	3	1
	76 77	3	3	2	1	2	1	3	1	3	2	3	2	1	1	3	2	3	2	1	2
	78	3	3	2	1	2	1	3	. 1	3	2	3	2	1	3	2	1	2	1	3	1
	79	3	3	2	ı	3	2	1	2	1	3	1	3	2	1	3	2	3	2	1	2
	80	3	3	2	1	3	2	1	2	i	3	1	-3	2	2	1	3	1	3	2	3
	81	3	3	2	1	3	2	ı	2	. 1	3	1	3	2	3	2	ı	2	1	3	1

 L_{81} (3⁴⁰) (Continued)

Expt. No. 21 22 23 24 25 26 27 28 29 30 31 32 33 34 35 36 37 38	39 40
1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	
2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2	1 1 2 2
	3 3
4 1 1 2 2 2 2 2 2 2 3 <th>3 3</th>	3 3
$ \begin{bmatrix} 5 & 2 & 2 & 3 & 3 & 3 & 3 & 3 & 3 & 3 & 3$	1 1 2 2
7 1 1 3 3 3 3 3 3 3 3 3 2 2 2 2 2 2 2	
8 2 2 1 1 1 1 1 1 1 3 3 3 3 3 3 3 3	2 2 3
9 3 3 2 2 2 2 2 2 2 2 1 1 1 1 1 1	1 1
10 3 3 1 1 1 2 2 2 3 3 3 1 1 1 2 2 2 3	3 3
11 1 1 2 2 2 3 3 1 1 1 2 2 2 3 3 1 12 2 2 3 3 3 1 1 1 2 2 2 3 3 3 1 1 2	1 1
13 3 2 2 2 2 2 2 3 3	2 2
14 1 1 2 2 3 1 1 2	2 2
15 2 2 1 1 1 2 2 2 3 3 3 2 2 2 3 3 3 1	3 3
16 3 3 3 3 3 1 1 1 2 2 2 2 2 2 3 3 3 1	1 1
17 1 1 1 2 2 2 3 3 3 3 3 3 1 1 2	2 2
18 2 2 2 2 2 3 3 3 1 1 1 1 1 1 2 2 2 3	3 3
19 2 2 1 1 1 3 3 3 2 2 2 1 1 1 3 3 3 2	2 2
20	3 3
	1 1
22 2 2 2 2 1 1 1 3 3 3 3 3 3 2 2 2 1 23 3 3 3 3 3 2 2 2 1 1 1 1 1 3 3 3 2	1 1 2 2
24 1 1 1 3 3 3 2 2 2 2 2 1 1 3 3 3 2	2 2 3
25 2 2 3 3 3 2 2 2 1 1 1 2 2 2 1 1 1 3	3 3
26 3 3 1 1 1 3 3 3 2 2 2 3 3 3 2 2 2 1	1 1
27 1.	2 2
28 2 3 1 2 3 1 2 3 1 2 3 1 2 3 1 2 3 1	2 3
29 3 1 2 3 1 2 3 1 2 3 1 2 3 1 2 3 1 2 3 1 2 3 1 2	3 1
30 1 2 3 1 2 3 1 2 3 1 2 3 1 2 3 1 2 3	1 2
31 2 3 2 3 1 2 3 1 2 3 1 3 1 2 3 1 2 3 3 3 3	1 2
32 3 1 3 1 2 3 </th <th>2 3 1</th>	2 3 1
34 2 3 2 2 2 2 2 3 2 3 1 2	
35 3 1 1 2 3 1 2 3 1 2 3 3 1 2 3 1 2 3	3 l 1 2
36 1 2 2 3 1 2 3 1 2 3 1 1 2 3 1 2 3 1	2 3
37 1 2 1 2 3 2 3 1 3 1 2 1 2 3 2 3 1 3	1 2
38 2 3 2 3 1 3 1 2 1 2 3 2 3 1 3 1 2 1	2 3
39 3 1 3 1 2 1 2 3 2 3 1 3 1 2 1 2 3 2	3 1

 L_{81} (3⁴⁰) (Continued)

Expt.	21	22	23	24	25	26	27	28	29	Colu	ımn 31	32	33	34	35	36	37	38	39	40
40		2	2	3	1	3	1	2	1	2	3	3	1	2	1	2	3	2	3	1
41	1 2	3	3	1	2	1	2	3	2	3	1	1	2	3	2	3	1	3	1	2
42	3	ı	. 1	2	3	2	3	ı	3	ľ	2	2	3	1	3	1	2	1	2	3
43	1	2	3	1	2	1	2	3	2	3	1	2	3	1	3	1	.2	1	2	3
44	3	3	1 2	2	3 1	2	3.	2	3 1	1 2	2	3 1	1	2	1 2	2	3	2 3	3 1	2
46	3	1	1	2	3	3	1	2	2	3	1	1	2	3	3	1	2	2	3	1
47	1	2	2	. 3	ı	1	2	3	3	ł	2	2	3	l	1	2	3	3	1	2
48	2	3	3	1	2	2	3	I	1	2	3	3	ı	2	2	3	1	1	2	3
49 50	3	1	2	3	2	1	2	3	3	1 2	2	3	1	3	2	3	2	2	2	3
51	2	3	1	2	3	3	1	2	2	3	1	2	3	1	1	2	3	3	1	2
52	3	1	3	i	2	2	3	1	1	2	3	2	3	1	1	2	3	3	ı	2
53	1	2	1	2	3	3	1	2	2	3	ı	3	1	2	2	3	1	1	2	3
54	2	3	2	3	1	1	2	3	3	1	2	1	2	3	3	1	2	2	3	i
55 56	3	2	1 2	3	2	1 2	3	2	1 2	3	2	1	3	2	1 2	3 1	2	- 1	3 !	2
57	2	1	3	2	1	3	2	1	3	2	1	3	2	1	3	2	1	3	2	1
58	3	2	2	1	3	2	ı	3	2	1	3	3	2	1	3	2	- 1	3	2	١
59	1	3	3	2	1	3	2	1	3	2	1	1	3	2	1	3	2	- 1	3	2
60	2	ı	1	3	2	1	3	2	1	3	2	2	1	3	2	1	3	2	1	3
61	3	2	3	2	1 2	3	2	1	3	2	1 2	2	1 2	3	2	1 2	3	3	1	3
63	2	1	2	1	3	2	1	3	2	1	3	1	3	2	1	3	2	1	3	2
64	2	1	1	3	2	2	1	3	3	2	1	1	3	2	2	1	3	3	2	1
65	3	2	2	1	3	3	2	1	1 2	3	2	3	1	3	3	2	2	1	3	2
67	2	1	2	1	3	3	2	1	1	3	2	3	2	1	1	3	2	2	1	3
68	3	2	3	2	1	i	3	2	2	ì	3	ì	3	2	2	1	3	3	2	1
69	1	3	1	3	2	2	1	3	3	2	1	2	1	3	3	2	1	1	3	2
70 71	3	1 2	3	2	1	1	~3 1	2	2	1 2	3	2	1 2	3	3	2	1 2	1	3	3
72	i	3	2	1	3	3	2	1	1	3	2	ì	3	2	2	1	3	3	2	ł
73	1	3	1	3	2	3	2	- 1	2	1	3	1	3	2	3	2	. 1	2	1	3
74	3	1 2	2	1 2	3	1 2	3	2	3	2	1 2	2	1 2	3 1	. 1	3	2	3	2	. 1
75	1	3	2	1	3	1	1	2	3	2	1	3	2	1	2	1	3	. 1	3	2
77	2	1	3	- 2	1	2	1	3	1	3	2	1	3	2	3	2	1	2	1	3
78	3	2	1	3	2	3	2	1	2	1	3	. 2	1	3	1	3	2	3	2	1
79	1	3	3	2	1	2	1	3	ı	3	2	2	1	3	- 1	3	2	3	2	1
80 81	3	1 2	1 2	3 1	2	3 1	2	1 2	2	1 2	3	3	2	1 2	2	1	3 1	1 2	3	2
61	13				.,							- 1	.,							