## 110550136

## Environment

- Windows
- g++
- Dev C++ 5.11
- How to run my program: (in CMD)

```
C:\Users\user\Desktop\NYCU\Algorithm\Exercise#3>g++ -o test 110550136.cpp

C:\Users\user\Desktop\NYCU\Algorithm\Exercise#3>test

4 6
0 4 6 7 7 7 7
0 2 4 6 8 9 10
0 6 8 8 8 8 8 8
0 2 3 4 4 4 4

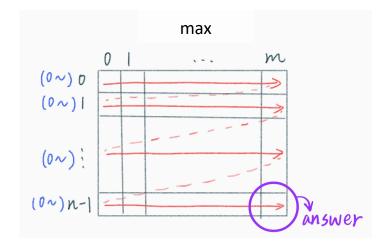
output 
18
```

## Solution

two tables:

Table	profit	max
Size	n*(m+1)	n*(m+1)
Meaning of (i,j)	profit of the i <sup>th</sup> project	maximal profit of 0th~ith
0 <= i < n , 0 <= j <= m	with j resources	projects with j resources

- Button-up method:
  - start from length=1, that is, the first project (0<sup>th</sup>) with resource= 0, 1, ..., m
- $\rightarrow$  continue with length=2, the <u>first two projects</u> ( $0^{th}\sim 1^{th}$ ) with resource= 0, 1, ..., m
- $\rightarrow$  length=3, the <u>first three projects (0<sup>th</sup>~2<sup>th</sup>)</u> with resource= 0, 1, ..., m
- **→** ...
- $\rightarrow$  length=n, all projects (0<sup>th~</sup>(n-1)<sup>th</sup>) with resource= 0, 1, ..., m
- → length=n and resource=m is the answer we look for



```
Algorithm
```

```
create table profit with size n*(m+1);
create table max with size n*(m+1);
fill in profit from the input data;
fill in the first row of max since max[0][j]=profit[0][j];
// fill in max row by row, and column by column
for (int i=1; i<n; i++)
                                 // the second row to the last row
  for (int j=0; j<=m; j++) // the first column to the last column
   int tmp=-1000;
                                 // initialize tmp as a very small number
   for (int k=0; k<=j; k++) // the new added project with 0~j resources
   {
      if (profit[i][k] + max[i-1][j-k] > tmp)
        tmp=profit[i][k] + max[i-1][j-k];
   }
   max[i][j]=tmp; // tmp is the maximal profit of 0<sup>th</sup>~i<sup>th</sup> projects with j resources
  }
print max[n-1][m];
→ have optimal structure:
     max[i][j] = \lceil profit[i][j]
                                                                  , if i = 0
                \max(profit[i][k] + max[i-1][j-k]), 0 <= k <= j , if i >= 1
```

- → have overlapping subproblems:
  - ex. max[2][2] and max[2][3] have to solve max[1][0], max[1][1], and max[1][2]
- dynamic programming

## **Time Complexity**

time complexity of a dynamic programming algorithm depends on the product of:

- number of subproblems overall  $\rightarrow \theta(n^*(m+1))$
- number of choices of each subproblem  $\rightarrow \theta(m+1)$
- time complexity =  $\theta(nm^2)$