

6 (1) 是, 離散的

$$(2) X \sim B(10, 0.5), P(X \geq 6) \\ = 1 - P(X \leq 5) = 1 - 0.623 = 0.377$$

$$(3) P(X \leq 4) = 0.377$$

$$34. P(X=x) = \frac{e^{-\lambda} \cdot \lambda^x}{x!}$$

$$P(X=k) = \sum_{x=0}^k \frac{\lambda^x}{x!} e^{-\lambda}$$

令一個月內發生無預警停駛為 X

$$(1) P(X=0) = \frac{e^{-0.5} \cdot 0.5^0}{0!} = e^{-0.5} = 0.6065$$

$$(2) P(X \geq 1) = 1 - P(X=0) = 1 - e^{-0.5} = 0.3935$$

35. 令 X 為 10 呎寬、30 呎長的玻璃氣泡環的個數

$$X \sim P_0(3):$$

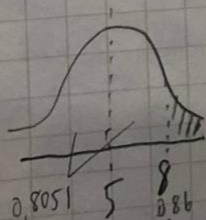
$$(1) P(X=0) = \frac{e^{-3} \cdot 3^0}{0!} = 0.0498$$

$$(2) P(X=2) = \frac{e^{-3} \cdot 3^2}{2!} = 0.224$$

$$\hookrightarrow P(X=2) = P(X \leq 2) - P(X \leq 1)$$

39. 令 X 為上網時間長度, 則 $X \sim N(5, 3.5^2)$

$$P(X > 8) = P\left(Z > \frac{8-5}{3.5}\right) = P(Z > 0.86) \\ = 1 - 0.8051 = 0.1949$$



8. 設 X 表示杯賽在 2012~2013 年

球季每場球的得分

$$X \sim N(13.2, 5.3^2)$$

$$(1) P(X > 15) = P\left(\frac{X-13.2}{5.3} > \frac{15-13.2}{5.3}\right)$$

$$= P(Z > 0.34)$$

$$= 1 - P(Z \leq 0.34)$$

$$= 1 - 0.6331 = 0.3669$$

$$(2) \bar{X} \sim N\left(13.2, \frac{5.3^2}{16}\right)$$

$$\frac{\bar{X}-13.2}{\frac{5.3}{\sqrt{16}}} \sim N(0, 1)$$

$$P(\bar{X} > 15) = P\left(\frac{\bar{X}-13.2}{\frac{5.3}{\sqrt{16}}} > \frac{15-13.2}{\frac{5.3}{\sqrt{16}}}\right)$$

$$= P(Z > 1.36) = 1 - P(Z \leq 1.36)$$

$$= 1 - 0.9131$$

$$= 0.0869$$