# Problem Chosen ABCDEF

## 2023 MCM/ICM Summary Sheet

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## 1 Problem Statement

In order to indicate the origin of the toll way problems, the following background is worth mentioning. The problem is stated here.

# 2 Assumptions and Justifications

#### 2.1 Assumptions

#### 2.2 Symbols and Definitions

Table 1: Symbols and Definitions.

| Notations | Description |
|-----------|-------------|
| η         | 1           |
| ξ         |             |
| P         |             |
| r         |             |
| x         |             |
| X         |             |
| N         |             |
| n         |             |

## 2.3 Symbols and Definitions

# 3 Mathematical Models

#### 3.1 Basic Model

$$\sum_{t} \tag{1}$$

According to Equation (1)

$$\begin{cases} \frac{dS_2}{dt} = -R_0 \cdot S_2(I_1 + I_2) \\ \frac{dI_2}{dt} = R_0 \cdot S_2(I_1 + I_2) - \frac{I_2}{r} \\ \frac{dS_1}{dt} = \rho \left[ 1 - \frac{S_1 + (1 + v/r)I_1}{K_1} \right] - R_0 \cdot S_1(I_1 + I_2) - v \cdot S_1 \\ \frac{dI_1}{dt} = R_0 \cdot S_1(I_1 + I_2) - \frac{I_1}{r + v} \end{cases}$$
(2)

| Notations          | Description   |  |
|--------------------|---|--|
| a                  | Persuasion of comments  |  |
| $s(X \to Y)$       | Degree of support between $X$ and $Y$ , indicating how often the rules can be used for analysis |  |
| $c(X \to Y)$       | Confidence between $X$ and $Y$ , indicating the frequency of transactions in $Y$ containing $X$ |  |
| X                  | Promotion/The 'verified purchase' is 'N'  |  |
| $\overline{X}$     | No promotion or The 'verified purchase' is 'Y'  |  |
| Y                  | Poor feedback   |  |
| $\overline{Y}$     | Favourable feedback   |  |
| Z                  | Poor evaluation support rate  |  |
| $\overline{Z}$     | Favourable support rate   |  |
| $f_{V}$            | Amount of platform commentators   |  |
| $f_{\overline{V}}$ | Amount of common customers  |  |
| $a_V$              | Support rate of comments written by writers   |  |
| $a_{\overline{V}}$ | Support rate of comments written by non writers   |  |
| $a_T$              | Overall weighted support rate   |  |
| $Q_{\mu}(v)$       | Amount of comments, dependent variable in multiple linear regression                            |  |
| $\mu_i$            | Regression coefficient of multiple linear regression, $\{i = 0, 1, 2, 3\}$                      |  |
| $v_i$              | Independent variable of multiple linear regression, $\{i = 0, 1, 2, 3\}$                        |  |
| $v_1$              | Amount of no promotions in monthly reviews  |  |
| $v_2$              | Number of disapproval of poor feedback and approval of favorable feedback in each month         |  |
| $v_3$              | Frequency of good keywords in each month  |  |
| ξ                  | Random error term of multiple linear regression   |  |
| $r^2$              | Sample determination coefficient discrimination coefficient                                     |  |
| SSR                | Regression sum of squares   |  |
| SST                | Sum of squares of total variation   |  |
| T                  | Weighted mean value of star rating in the train set   |  |
| $\widetilde{T}$    | Weighted mean value of star rating in the testing set   |  |
| std                | Standard deviation of the result in training set and testing set                                |  |
| D                  | Future value of products  |  |
| arphi              | Weighted star rating  |  |
| δ                  | The rate of positive keywords in reviews  |  |

# 3.2 Improved Model

Additional assumptions for the model improvement

# 4 Results and Solutions

Result analysis

Discussions

#### **Algorithm 1:** Competitive selection

```
Input: the set of data patterns X
     Output: the set of prototype seeds \mathbb{S}^*
 1 Compute the Euclidean distance dist(\mathbf{x}_m, \mathbf{x}_n)
 2 Compute the density D(\mathbf{x}_m) \geq \gamma
 3 Select eligible \mathbf{x}_m for the candidate seed set \mathbb{C}^0 \leftarrow \{\mathbf{x}_m \mid C(\mathbf{x}_m, \gamma) = 1\}
 4 Initialize \mathbb{C}^* \leftarrow \mathbb{C}^0
 5 while \mathbb{C}^* \neq \phi do
           Initialize \mathbb{S}^j \leftarrow \mathbb{S}^*
 6
           Select the winning seed from the candidate set \mathbf{x}_s^j \leftarrow \arg \max D(\mathbf{x}_m), \mathbf{x}_m \in \mathbb{C}^j
 7
           Update \mathbb{S}^* \leftarrow \mathbb{S}^j \cup \{\mathbf{x}_s^j\}
 8
           Update j \leftarrow j + 1
10 end
11 return S*
```

# 5 Model Evaluation and Sensitivity Analysis

#### **5.1** Model Evaluation

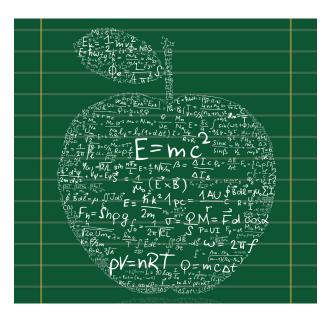


Figure 1: Figure illustration.

#### **5.2** Sensitivity Analysis

Matrix with column and row labels:

$$\begin{array}{ccc}
1 & 2 \\
1 & (x1 & x2) \\
2 & (x3 & x4) \\
3 & (x5 & x6)
\end{array}$$

 $V_{12}$  $\infty$  $V_2$ 0 5  $V_3$ 5 0 3  $\infty$ 5  $\infty$  $\infty$  $V_4$ 3 0 3  $\infty$  $V_5$  $\infty$  $\infty$ 0 2  $\infty$  $V_6$  $\infty$ 3  $\infty$  $V_7$ 6  $\infty$  $\infty$ 5  $\infty$  $V_9$ 3 0 5 4  $V_{10}$ 0 5  $\infty$  $\infty$  $\infty$  $\infty$ 4  $\infty$  $\infty$  $\infty$  $\infty$  $\infty$  $\infty$  $\infty$ 5 0  $V_{11}$ 2  $\infty$  $V_{12}$ 0 6  $\infty$ 6  $\infty$  $V_{13}$ 6 2  $\infty$  $\infty$  $\infty$ 6  $\infty$  $V_{14}$  $\infty$  $V_{15}$ 0  $V_{16}$ 2. 7 3 8 4 0  $V_{17}$ 3 5 6  $\infty$  $\infty$  $\infty$  $\infty$  $\infty$  $\infty$ 5 0 3  $\infty$ 1  $\infty$  $V_{19}$ 5  $\infty$  $\infty$  $\infty$ 3 0  $\infty$  $V_{20}$ 3 8 0 2  $\infty$  $V_{21}$  $\infty$  $V_{22}$  $\infty$  $\infty$  $\infty$ 4 5 3  $\infty$  $V_{23}$  $\infty$  $\infty$  $\infty$ 1 3 0 4 0  $\infty$ 

# 6 Strengths and Weaknesses

# 6.1 Strengths

The models have the following strengths:

- Advantage 1
- Advantage 2

#### 6.2 Weaknesses

The models have the following weaknesses:

- · Weakness 1
- Weakness 2

#### 7 Conclusions

#### References

[1] P. Y. Pawar and S. H. Gawande, "A Comparative Study on Different Types of Approaches to Text Categorization," *International Journal of Machine Learning and Computing*, vol. 2, no. 4, pp. 423-426, 2012.

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# Report

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