CSIE 5432/5433 HW3 PDF

YiWenLai

TOTAL POINTS

40 / 0

QUESTION 1

1P4 o/o

- + 20 pts Correct for 4 choices.
- + 10 pts Correct for 3 choices.
- \checkmark + 0 pts Correct for 2 choices / Choose "I have no idea" option.
 - 5 pts Correct for 1 choice.
 - 10 pts Correct for 0 choices.
- 1 correct: 3, 4

QUESTION 2

2 P11 20 / 0

- √ + 20 pts Correct
 - + 15 pts Almost correct
 - + 5 pts Get answers without mathematical

derivation.

- + O pts Without choices
- 10 pts Incorrect
- 10 pts Almost without any description.
- 10 pts Your explanation doesn't make sense to me
- 20 pts Violate the class policy

QUESTION 3

3 P13 20 / 0

- + 20 pts Correct answer
- √ + 20 pts Correct answer but without explaination

to **option (a)**.

- + **0 pts** Without choices. / Correct answer with few explaination
 - 10 pts Incorrect / No answer
 - 5 pts minor wrong
 - 5 pts Without **clearly** explaination to your

solution

+ 0 pts Click here to replace this description.

QUESTION 4

4 P19 Code check o / o

- √ + 0 pts Correct
 - 20 pts No code found.
 - 10 pts Not selected pages

1. b

$$(0.1)^{2} \left(1 - \frac{11+1}{N}\right) < 0.006$$

$$1 - \frac{12}{N} \leq 0.6$$

$$N \leq \frac{12}{0.4} = 30$$
**

2. a

Since if X^TX is invertible, whas an unique solution, and if X^TX is singular, then whas multiple solutions. Therefore, There is at least one solution for the normal equation.

3. c

4. e

For the first option, it is the definition of the slide. For the second option, since \theta_head is the likelihood of the result, and \v is the max observed value, thus \v maximizes the likelihood function.

For the other options, follow the below figure.

$$\frac{1}{N} \sum_{i=1}^{N} \sum_{j=1}^{N} \sum_{j=1}^{N} \sum_{j=1}^{N} \sum_{i=1}^{N} \sum_{j=1}^{N} \sum_{j=1}^{N} \sum_{i=1}^{N} \sum_{j=1}^{N} \sum_{i=1}^{N} \sum_{j=1}^{N} \sum_{j=1}^{N} \sum_{i=1}^{N} \sum_{j=1}^{N} \sum_{i=1}^{N} \sum_{j=1}^{N} \sum_{j=1}^$$

5. a

Given N values, calculate the possible \theta for generating this uniform distribution. Since it's uniform distribution, the probability of each value is 1 / \theta_head, then the likelihood of n points is 1\theta_head multiplied over n times.

6. b

If the term of $y_n \neq sign(x_t^T x_n)$ needed to be preserved, the term $-y_n w^T x$, which will be positive, can only be preserved by min max operation in option (b).

7. a

Just take the derivative of the exponential error function and multiplied by -1.

8. b

$$\begin{cases}
b_{E}(u)^{T}(w-u) + \frac{1}{2}(w-u)^{T} A_{E}(u)(w-u) \rightarrow min \\
\int \frac{d}{dw-u}
\end{cases}$$

$$b_{E}(u) + A_{E}(u)(w-u) = 0, \quad w-u \neq V = -A_{E}(u)^{T} b_{E}(u)$$

9. b

1P4 o / o

- + 20 pts Correct for 4 choices.
- + 10 pts Correct for 3 choices.
- \checkmark + 0 pts Correct for 2 choices / Choose "I have no idea" option.
 - **5 pts** Correct for 1 choice.
 - 10 pts Correct for 0 choices.
- 1 correct: 3, 4

10. b

$$\frac{\partial err(W,x,y)}{\partial W i k} = \frac{\partial}{\partial W i k} \left(-\frac{k}{k-1} \ln h_{k}(x) \right)$$

$$= \frac{\partial}{\partial W i k} \left(-\frac{k}{k-1} \ln h_{k}(x) \right)$$

$$= -\left(x i \left(y = k \right) - \frac{\partial}{\partial W i k} \ln \left(\sum e^{x} p(W x^{x}) \right)$$

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11. e

$$min - \sum Su \left(\frac{\exp(w_{1}^{T} x_{n})}{\exp(w_{1}^{T} x_{n}) + \exp(w_{2}^{T} x_{n})} \right)$$

$$y_{n} = -1, \quad -2n \left(\frac{\exp(w_{1}^{T} x_{n})}{\exp(w_{1}^{T} x_{n}) + \exp(w_{2}^{T} x_{n})} \right) = 2n \left(1 + \exp(-(w_{2} - w_{1})^{T} x_{n}) \right)$$

$$= 2n \left(1 + \exp(-(w_{1} - w_{1})^{T} x_{n}) \right)$$

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12. e

		12.0														
В	С	D	E	F	G	Н	I	J	K	L	M	N	0	P	Q	R
0	1		1	0	1	0	0	1		-6	-2.5	16	-6	-4		-1
1	-0.5		1	1	-0.5	1	-0.5	0.25		-6.25	-0.5	9.75	-1.5	-3.25		-1
-1	0		1	-1	0	1	0	0		-6	7	12	-1	-5		-1
-1	2		1	-1	2	1	-2	4		10	17	36	-39	11		1
2	0		1	2	0	4	0	0		-3	9.5	15	-4	1		1
1	-1.5		1	1	-1.5	1	-1.5	2.25		1.75	12.5	13.75	-12.5	4.75		1
0	-2		1	0	-2	0	0	4		3	-9	13	-6	5		1

13. b

2 P11 20 / 0

√ + 20 pts Correct

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- + **5 pts** Get answers without mathematical derivation.
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$$min - \sum Su \left(\frac{\exp(w_{1}^{T} x_{n})}{\exp(w_{1}^{T} x_{n}) + \exp(w_{2}^{T} x_{n})} \right)$$

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0	1		1	0	1	0	0	1		-6	-2.5	16	-6	-4		-1
1	-0.5		1	1	-0.5	1	-0.5	0.25		-6.25	-0.5	9.75	-1.5	-3.25		-1
-1	0		1	-1	0	1	0	0		-6	7	12	-1	-5		-1
-1	2		1	-1	2	1	-2	4		10	17	36	-39	11		1
2	0		1	2	0	4	0	0		-3	9.5	15	-4	1		1
1	-1.5		1	1	-1.5	1	-1.5	2.25		1.75	12.5	13.75	-12.5	4.75		1
0	-2		1	0	-2	0	0	4		3	-9	13	-6	5		1

13. b

```
To get relationship between vc bound and input-size, we should suppose there are N datas.

Consider +- sign, there are 2dN hypothesis sets.

2^{N} \leq 2dN
N \leq \log_{2}d + \log_{2}N + 1
N \leq \log_{2}d + \frac{N}{2} + 1
```

```
14. d
15. c
```

```
import numpy as np
from numpy.linalg import inv
from numpy import linalg as LA
import math
```

3 P13 20 / 0

- + 20 pts Correct answer
- √ + 20 pts Correct answer but without explaination to **option (a)**.
 - + **O pts** Without choices. / Correct answer with few explaination
 - 10 pts Incorrect / No answer
 - **5 pts** minor wrong
 - **5 pts** Without **clearly** explaination to your solution
 - + **0 pts** Click here to replace this description.

```
To get relationship between vc bound and input-size, we should suppose there are N datas.

Consider +- sign, there are 2dN hypothesis sets.

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N \leq \log_{2}d + \log_{2}N + 1
N \leq \log_{2}d + \frac{N}{2} + 1
```

```
14. d
15. c
```

```
import numpy as np
from numpy.linalg import inv
from numpy import linalg as LA
import math
```

```
def theta func(s):
   return 1/(math.exp(-s)+1)
def square err(w):
   E in = LA.norm(X.dot(w)-y)
  return pow(E in,2) / X.shape[0]
def cross entropy err(w):
   en = []
   for i in range (1000):
       en.append(-1 * np.log(theta func(y[i] *
np.dot(w,X[i]))))
   return sum(en)/len(en)
def sign(s):
  if s > 0:
      return 1
  elif s < 0:
      return -1
train = []
with open('hw3 train.txt') as f:
  lines = f.readlines()
  for line in lines:
      nums = line.strip().split()
      data = [float(num) for num in nums]
      data.insert(0,1)
      train.append(data)
train = np.array(train)
X = train[:,:11]
y = train[:,-1]
test = []
with open('hw3 test.txt') as f1:
  lines = f1.readlines()
   for line in lines:
```

```
nums = line.strip().split()
       data = [float(num) for num in nums]
       data.insert(0,1)
       test.append(data)
test = np.array(test)
X test = test[:,:11]
y test = test[:,-1]
# print(X)
# Q14
X T = np.transpose(X)
tmp = X T.dot(X)
tmp = inv(tmp)
tmp = tmp.dot(X T)
w lin = tmp.dot(y)
E_lin = square_err(w_lin)
print("Q14 ",E lin)
#015
iterations = []
for i in range(1000):
  steps = 0
  w = np.zeros(11)
  learning rate = 0.001
  err = square err(w)
  while(True):
       if err <= 1.01*E lin:
           break
       else:
           steps += 1
           indexs = np.random.randint(0,1000,1)
           index = indexs[0]
```

```
w += 2 * learning rate
(y[index]-np.dot(w,X[index])) * X[index]
           err = square err(w)
   iterations.append(steps)
print("Q15 ",sum(iterations)/len(iterations))
# 016
ERR list = []
for i in range(1000):
  w = np.zeros(11)
   learning rate = 0.001
   for j in range (500):
       index = np.random.randint(0,1000,1)[0]
       w += learning rate * theta func(-1 * y[index] *
np.dot(w,X[index]) ) * y[index] * X[index]
   ERR list.append(cross entropy err(w))
print("Q16 ",sum(ERR list)/len(ERR list))
# 017
ERR list = []
for i in range(1000):
  w = w lin.copy() # Q17
  learning rate = 0.001
   for j in range (500):
       index = np.random.randint(0, 1000, 1)[0]
       w += learning rate * theta func(-1 * y[index] *
np.dot(w,X[index]) ) * y[index] * X[index]
   ERR list.append(cross entropy err(w))
print("Q17 ",sum(ERR list)/len(ERR list))
```

```
#Q 18
E in = 0.0
E \text{ out } = 0.0
for i in range(len(y)):
   if sign( np.dot(w lin.copy(), X[i]) ) != y[i] :
for j in range(len(y test)):
   if sign( np.dot(w_lin.copy(), X_test[j]) ) != y_test[j] :
       E out += 1
# print(E in,E out)
print("Q18 ", abs( (E in/len(y)) - (E out/len(y test)) ) )
#19 20
for Q in [3,10]:
  X train = []
  y train = []
  X \text{ test} = []
  y_test = []
   with open('hw3 train.txt') as f:
       lines = f.readlines()
       for line in lines:
           nums = line.strip().split()
           data = []
           for i in range(len(nums)-1):
               for p in range(Q):
                    data.append(pow(float(nums[i]),p+1))
           data.insert(0,1)
           label = float(nums[len(nums)-1])
           X train.append(data)
           y train.append(label)
```

```
X = np.array(X train)
y = np.array(y train)
with open('hw3 test.txt') as f:
    lines = f.readlines()
    for line in lines:
        nums = line.strip().split()
        data = []
        for i in range(len(nums)-1):
            for p in range(Q):
                data.append(pow(float(nums[i]),p+1))
        data.insert(0,1)
        label = float(nums[len(nums)-1])
        X test.append(data)
        y test.append(label)
X_test = np.array(X_test)
y_test = np.array(y_test)
X T = np.transpose(X)
tmp = X T.dot(X)
tmp = inv(tmp)
tmp = tmp.dot(X T)
w lin = tmp.dot(y)
E lin = square err(w lin)
E \text{ out} = 0.0
for i in range(len(y)):
    if sign( np.dot(w_lin.copy(), X[i]) ) != y[i] :
        E in += 1
for j in range(len(y test)):
    if sign( np.dot(w lin.copy(), X test[j]) ) != y test[j]
        E out += 1
```

```
# print(E_in,E_out)
if Q == 3:
    print("Q19 ", abs( (E_in/len(y)) - (E_out/len(y_test))

) )
else:
    print("Q20 ", abs( (E_in/len(y)) - (E_out/len(y_test)))
) )
```

4 P19 Code check o/o

- √ + 0 pts Correct
 - 20 pts No code found.
 - 10 pts Not selected pages