

CS323 Homework Assignment 1

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Collaboration Statement: This is my own work. I worked on it by myself without consulting anyone else.

1. Explanations for ComplexCode4:

First, let's note that this code has two nested for-loops. The first for loop goes from `int i = 1` to when `int i` is less than `N` and increases by a factor of 2.

The second for loop goes from `int j = 0` until when `j` is less than some number `N` and the overall loop increments by a factor of 2 which can be shown by the math equation 2^n . Therefore the overall asymptotic complexity of the code is $\log n$ times N .

2. Explanations for ComplexCode5:

The first for-loop decreases by 1 so it goes from some number `N` to 0. The second for-loop goes from 100 to some number `N`. The last for-loop goes 15 to some number `N*2` but increases by 5. The overall asymptotic complexity is therefore N^3 based on the three for loops.

Overall this code is because the two while loops cause the iterator to move in a second order growth instead of in a linear growth.

3. Explanations for ComplexCode17:

The solution is N^2 . Since there is a for-loop the first loop goes from `int i` when it is zero to when `i` is less than some number `N` so this means that asymptotic complexity is at least N . The next item to consider is that the if-clause which says `!x.contains` the array index. This clause is going to add an integer to the arraylist from integers 0 to `N` since the command checks if the `ArrayList x` contains the element in the arraylist. So the two factors to consider are the first for loop that goes from integers 0 to `N` and then the second if statement which adds the element in the arraylist.

4. Explanations for ComplexCode18:

This solution is $N \log n$. This is because the tree's fundamental coding structure looks like a branch going across and multiplying in an exponential way similar to 1 to 2 to 4 to 8 to 16 to etc. So the $\log n$ makes sense because the data structure that is used is a tree however the N in the solution of $N \log n$ is because of the for loop which goes from $\text{int } i = 0$ when i is less than N .

5. Explanations for ComplexCode20:

The reason that this code is $\log N$ is because the recursion allows the function to be repeated exponentially by so for example, it will be $N/2$ then $N/4$ then $N/8$ then $N/16$ so N is being divided by factors of 2. This means that two to some power x will be equal to N so the running time analysis is $\log N$.