GC-3 Workshop: Measurement Invariance Testing in R

Yichi Zhang

11/03/2022

Outline

- Brief overview of measurement invariance (MI)
 - Definition of MI, measurement noninvariance, partial invariance
 - Importance of validating the MI assumption
 - Levels of MI
- Illustrative example
 - Investigate MI of the mini-IPIP (International Personality Item Pool) scale across gender.
 - Small Exercise

Motivating Example

 The Positive and Negative Affect Schedule (PANAS) scale has been found to function differently for participants from different cultural backgrounds.

Table 1. Positive and Negative Affect Schedule (PANAS) Scorecard [27].

1 Very Slightly or Not a	t All A Little	3 Moderately	4 Quite a Bit	5 Extremely
1. 1	Interested	11. Irritable		
2. 1	Distressed		12. Alert	
3. I	Excited		13. Ashamed	
4. 1	Upset	14. Inspired		
5. \$	Strong		15. Nervous	
6. ¢	6. Guilty		16. Determined	
7 . 9	7. Scared		17. Attentive	
8. 1	8. Hostile		——————————————————————————————————————	
9. I	Enthusiastic	19. Active		
10. Proud			20. Afraid	

 Are the observed differences in scale scores caused by real differences in negative affect or the different cultural meanings of scale items?

What Is Measurement Invariance (MI)?

Formal definition:

$$f(Y|\eta,g)=f(Y|\eta),$$

for all Y, η, g (Mellenbergh, 1989)

 Implied meaning: Using the same questionnaire in different groups (such as countries or at various points in time, or under different conditions) does measure the same construct in the same way.

What Is Measurement Noninvariance (MNI)?

- If there is a violation of MI => Measurement noninvariance/Item bias/Differential item functioning
 - The scale has different measurement properties across groups for individuals with the same latent construct level
 - E.g., Male consistently reported a higher score than female in mathmatics self-efficacy scale.
- If MI only holds for a subset of items => Partial invariance

How To Test For MI?

- Multi-Group Confirmatory Factor Analysis (MGCFA)
 - Likelihood ratio test to compare nested models, which means one model with equality constraints of a particular parameter and the other without such constraints.
 - E.g., the invariance of loadings can be tested by comparing the model with freely estimated loadings and the model with has equality constraints of loadings across groups
- Item Response Theory

Multi-Group Confirmatory Factor Analysis (MGCFA)

- CFA assumes the observed items load on a latent factor that represents the construct
- A single-factor MG-CFA

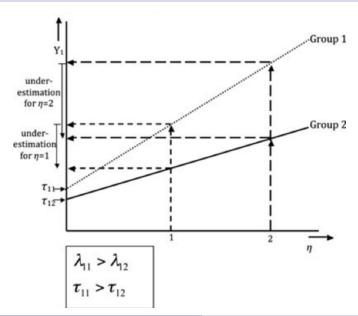
$$y_{ik} = \nu_k + \lambda_k \eta_{ik} + \epsilon_{ik}$$

- y_{ik} and η_{ik} are the observed continuous response and the latent construct score for the *i*th person in the *k*th group
- ν_k represents intercepts, λ_k represents factor loadings, and the unique factor variables represents ϵ_{ik} .

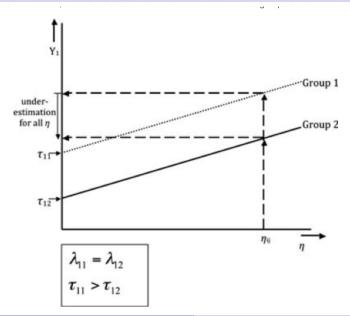
Levels Of MI Testing

- Configural Invariance: the same model holds for all the groups
- Metric/Weak Invariance: factor loadings (slopes) are the same across the groups
- Scalar/Strong Invariance: intercepts and loadings are the same across the groups
- Strict Invariance: unique factor invariance, intercepts and loadings are the same across the groups

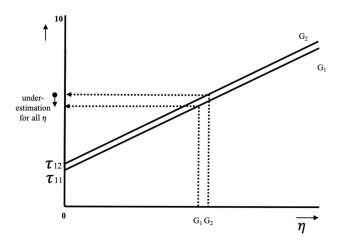
Configural Invariance



Metric Invariance



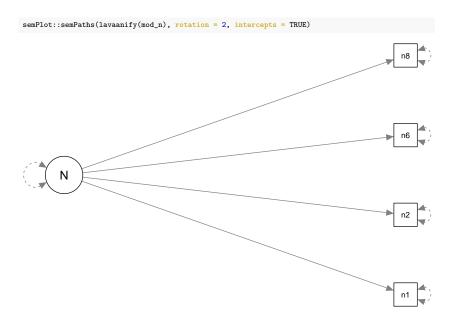
Scalar Invariance



Illustrative Example

- Goal: Examine measurement invariance of the mini-IPIP across gender.
- Data: Collected from 1994 Spring to 1996 Fall (Ock et al., 2020)
 - 564 participants (239 males, 325 females)
 - 20 items in total, four items per dimension (Agreeableness, Conscientiousness, Extraversion, Neuroticism, Openness to Experience)
 - 5-point Likert-type scale from 1 (*very inaccurate*) to 5 (*very accurate*).

Model Specification



Testing Metric Invariance

- Metric Invariance add equality constraints on factor loadings across gender
- The Likelihood Ratio Test (LRT) suggests the metric invariance model has similar fit as the configural invariance model

Testing Scalar Invariance

- Scalar Invariance add equality constraints on factor loadings and intercepts across groups
- The LRT suggests the scalar invariance model fit significantly worse than the metric invariance model

```
# fit scalar invariance model
fit_sca <- cfa(mod = mod_n, data = data, group = "sex",
              group.equal = c("loadings", "intercepts"),
              std.lv = TRUE)
# Likelihood Ratio test of scalar invairance model and metric invariance model
lavTestLRT(fit_met, fit_sca)
## Chi-Squared Difference Test
##
                AIC
                       BIC Chisq Chisq diff Df diff Pr(>Chisq)
## fit met 7 6542.5 6633.6 6.8001
## fit_sca 10 6553.1 6631.1 23.3668
                                    16.567
                                                    3 0.0008676 ***
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
```

Option 1: Sequential MI Testing By Scale Items

- Manually searching for noninvariant parameters (loadings, intercepts, residuals)
- Find the item associated with the largest change in $\chi^2 =>$ item n1

```
fit_sca2 <- cfa(mod_n, data = data, group = "sex",
               group.equal = c("loadings", "intercepts"),
               group.partial = "n2 ~1", std.lv = TRUE)
lavTestLRT(fit_sca2, fit_sca)
## Chi-Squared Difference Test
##
##
           Df AIC BIC Chisq Chisq diff Df diff Pr(>Chisq)
## fit_sca2 9 6552.5 6634.9 20.753
## fit sca 10 6553.1 6631.1 23.367
                                                          0.106
                                       2.6133
fit_sca6 <- cfa(mod_n, data = data, group = "sex",
               group.equal = c("loadings", "intercepts"),
               group.partial = "n6 ~1", std.lv = TRUE)
lavTestLRT(fit_sca6, fit_sca)
## Chi-Squared Difference Test
##
                        BIC Chisq Chisq diff Df diff Pr(>Chisq)
##
                 ATC
## fit sca6 9 6554.0 6636.4 22.308
```

0.3035

fit_sca 10 6553.1 6631.1 23.367 1.0589 1

Testing Strict Invariance

 The partial strict invariance model fit significantly worse than the partial scalar invariance model

Option 2: pinSearch Function From pinsearch Package

- This function automates the iterative search for noninvariant parameters (loadings, intercepts, residuals)
- Item n1 has noninvariant intercepts across groups

Testing Strict Invariance

- Items n1,n2 has noninvariant unique factor variances across gender
- Effect size (Standardized mean difference) is 0.239

Partial Strict Invariance Model

- Conclusion: items n6, n8 are strict invariant, item n2 is strong/scalar invariant, item n1 is weak/metric invariant
- Final model: partial strict invariance model with freely estimated intercept for item n1 and unique factor variances for items n1 and n2.

Exercise time

Please complete the file "exercise.RMD".

Additional Topic:

- MI testing for categorical data
- Approximate invariance for many groups
- Practical significance of MI