
Assignment3

#Exercise1

1、

```
setwd("C:/Users/yidax/OneDrive/Desktop/613/HW3")
library(gmodels)
library(dplyr)
library(data.table)
library(ggplot2)
library(tidyverse)
library(lubridate)
library(tidyr)
library(magrittr)
library(xlsx)
library(plm)
library(data.table)
#Exercise 1
datstu <- fread("datstu_v2.csv")
#1
numbstudents<-nrow(datstu)
numbstudents
datsss <- fread("datsss.csv")
numbschools<-length(unique(datsss$schoolcode))
numbschools
program<-datstu[,11:16]
programvector<-unlist(program,use.names = FALSE)
numbprogram<-length(unique(programvector))
numbprogram

> numbstudents
[1] 340823
> datsss <- fread("datsss.csv")
> numbschools<-length(unique(datsss$schoolcode))
> numbschools
[1] 898
> program<-datstu[,11:16]
> programvector<-unlist(program,use.names = FALSE)
> numbprogram<-length(unique(programvector))
> numbprogram
[1] 33
```

2、

```

#2
sp1<-select(datstu,schoolcode1,choicepgm1)
sp2<-select(datstu,schoolcode2,choicepgm2)
sp3<-select(datstu,schoolcode3,choicepgm3)
sp4<-select(datstu,schoolcode4,choicepgm4)
sp5<-select(datstu,schoolcode5,choicepgm5)
sp6<-select(datstu,schoolcode6,choicepgm6)
append1<-rbind(sp1,sp2,sp3,sp4,sp5,sp6,use.names=FALSE)
numbchoice<-nrow(unique(append1))
numbchoice

> numbchoice
[1] 3086

```

3、

```

#3
Schooladdress<-select(datsss,schoolcode,sssdistrict)
Schooladdress<-unique(Schooladdress)
Studentadress<-select(datstu,1,5:10,17)
colnames(Schooladdress)[2]<-"Address"
colnames(Studentadress)[8]<-"Address"
colnames(Studentadress)[1]<-"Studentocde"
StuSchadress<-left_join(Studentadress,Schooladdress,by = "Address" )
StuSchadress<-na.omit(StuSchadress)
Adresssame<- filter(StuSchadress,schoolcode1==schoolcode|schoolcode2==schoolcode
|schoolcode3==schoolcode|schoolcode4==schoolcode
|schoolcode5==schoolcode|schoolcode6==schoolcode)

Adresssame<-unique(Adresssame)
length(unique(Adresssame$Studentocde))

> length(unique(Adresssame$Studentocde))
[1] 254096

```

4、

```

#4
datstu3<-na.omit(datstu)
datstu4<-select(datstu3,5:10,18)
rank1<-datstu4%>%filter(rankplace=="1")%>%select(,1)
rank2<-datstu4%>%filter(rankplace=="2")%>%select(,2)
rank3<-datstu4%>%filter(rankplace=="3")%>%select(,3)
rank4<-datstu4%>%filter(rankplace=="4")%>%select(,4)
rank5<-datstu4%>%filter(rankplace=="5")%>%select(,5)
rank6<-datstu4%>%filter(rankplace=="6")%>%select(,6)
Rank<-rbind(rank1,rank2,rank3,rank4,rank5,rank6,use.names=FALSE)
Ranksummary<-data.frame(table(Rank$schoolcode1))

```

	Var1	Freq
1	10101	374
2	10102	220
3	10103	389
4	10104	209
5	10105	324
6	10106	359
7	10107	288
8	10108	292
9	10109	283
10	10110	445
11	10111	520
12	10112	274
13	10114	318
14	10115	222
15	10116	416
16	10117	428
17	10118	469
18	10119	370
19	10120	248
20	10121	452




5、

```
#5|
admittedschool<- apply(datstu4, 1, function(x) return(x[x[7]]))
score<-datstu3$score
adscore<-data.frame(admittedschool,score)
adscore<-na.omit(adscore)
cutoff<-by(adscore$score,adscore$admittedschool,min)
cutoffschool<-data.frame(schoolcode = as.numeric(names(cutoff)), 'score' = matrix(cutoff))
```

	schoolcode	socre
1	10101	284
2	10102	343
3	10103	316
4	10104	245
5	10105	260
6	10106	293
7	10107	281
8	10108	248
9	10109	257
10	10110	343
11	10111	371
12	10112	316
13	10114	319
14	10115	274
15	10116	205
16	10117	330
17	10118	275
18	10119	235
19	10120	243
20	10121	335

6、

```
#6
quality<-by(adscore$score,adscore$admittedschool,mean)
qualityschool<-data.frame(schoolcode = as.numeric(names(quality)), 'socre' = matrix(quality))
```

	schoolcode 	socre 
1	10101	320.1898
2	10102	394.1273
3	10103	353.8226
4	10104	297.0096
5	10105	351.2778
6	10106	339.9081
7	10107	311.6597
8	10108	303.3459
9	10109	282.0353
10	10110	407.3124
11	10111	412.0635
12	10112	375.5620
13	10114	345.9937
14	10115	315.8333
15	10116	289.9736
16	10117	369.6238
17	10118	315.2111
18	10119	288.6459
19	10120	278.9919
20	10121	382.4071

#Exercise2

```

#Exercise2
Append2 = data.frame('choice1' = paste0(datstu$schoolcode1,datstu$choicepgm1),
                     'choice2' = paste0(datstu$schoolcode2,datstu$choicepgm2),
                     'choice3' = paste0(datstu$schoolcode3,datstu$choicepgm3),
                     'choice4' = paste0(datstu$schoolcode4,datstu$choicepgm4),
                     'choice5' = paste0(datstu$schoolcode5,datstu$choicepgm5),
                     'choice6' = paste0(datstu$schoolcode6,datstu$choicepgm6),
                     'rank' = datstu$rankplace,
                     'score' = datstu$score)

Append2<-na.omit(Append2)
#Size
Admittedschool2<-apply(Append2,1,function(x) return(x[as.numeric(x[7])]))
Freadmitted<-data.frame(table(Admittedschool2))
colnames(Freadmitted)[1]<-"choice"
#cutoff
score2<-Append2$score
adscore2<-data.frame(Admittedschool2,score2)
adscore2<-na.omit(adscore2)
cutoff2<-by(adscore2$score2,adscore2$Admittedschool2,min)
cutoffscore<-data.frame(choice = names(cutoff2), 'socre' = matrix(cutoff2))
colnames(cutoffscore)[2]<-"cut_score"
#quality
quality2<-by(adscore2$score2,adscore2$Admittedschool2,mean)
qualityscore<-data.frame(choice = names(quality2), 'socre' = matrix(quality2))
colnames(qualityscore)[2]<-"quality_score"
#Data
Append3 = data.frame('choice' = c(paste0(datstu$schoolcode1,datstu$choicepgm1),
                                paste0(datstu$schoolcode2,datstu$choicepgm2),
                                paste0(datstu$schoolcode3,datstu$choicepgm3),
                                paste0(datstu$schoolcode4,datstu$choicepgm4),
                                paste0(datstu$schoolcode5,datstu$choicepgm5),
                                paste0(datstu$schoolcode6,datstu$choicepgm6)),
                    'schoolcode'=c(datstu$schoolcode1,datstu$schoolcode2,datstu$schoolcode3,
                                datstu$schoolcode4,datstu$schoolcode5,datstu$schoolcode6))

#quality
quality2<-by(adscore2$score2,adscore2$Admittedschool2,mean)
qualityscore<-data.frame(choice = names(quality2), 'socre' = matrix(quality2))
colnames(qualityscore)[2]<-"quality_score"
#Data
Append3 = data.frame('choice' = c(paste0(datstu$schoolcode1,datstu$choicepgm1),
                                paste0(datstu$schoolcode2,datstu$choicepgm2),
                                paste0(datstu$schoolcode3,datstu$choicepgm3),
                                paste0(datstu$schoolcode4,datstu$choicepgm4),
                                paste0(datstu$schoolcode5,datstu$choicepgm5),
                                paste0(datstu$schoolcode6,datstu$choicepgm6)),
                    'schoolcode'=c(datstu$schoolcode1,datstu$schoolcode2,datstu$schoolcode3,
                                datstu$schoolcode4,datstu$schoolcode5,datstu$schoolcode6))

Append3<-na.omit(Append3)
Append3<-unique(Append3)
colnames(Append3)[2]<-'schoolcode'
Append4<-left_join(Append3,datsss,by = 'schoolcode')%>%
  left_join(Freadmitted, by='choice')%>%
  left_join(cutoffscore, by='choice')%>%
  left_join(qualityscore, by='choice')
Append4<-unique(Append4)
Append4<-na.omit(Append4)
#Append4 is the required school-program level dataset containing required variables.

```

	choice	schoolcode	V1	schoolname	sssdistrict	ssslong	ssslat	Freq	cut_score
1	50112Home Economics	50112	330	KUMASI SENIOR HIGH/TECH. SCHOOL KUMASI	Kumasi Metro	-1.5971872	6.682060	50	293
2	50112Home Economics	50112	380	KUMASI SENIOR HIGH/TECH. SCHOOL KUMASI	Kumasi Metro	-1.5971872	6.682060	50	293
3	50112Home Economics	50112	413	KUMASI SENIOR HIGH/TECH. SCHOOL KUMASI	Kumasi Metro	-1.5971872	6.682060	50	293
4	50112Home Economics	50112	424	KUMASI SENIOR HIGH/TECH. SCHOOL KUMASI	Kumasi Metro	-1.5971872	6.682060	50	293
5	50112Home Economics	50112	493	KUMASI SENIOR HIGH/TECH. SCHOOL KUMASI	Kumasi Metro	-1.5971872	6.682060	50	293
7	70102General Arts	70102	110	MAWULI SENIOR HIGH. SCHOOL HO	Ho Municipal	0.5261422	6.717607	120	345
8	70102General Arts	70102	128	MAWULI SENIOR HIGH. SCHOOL HO	Ho Municipal	0.5261422	6.717607	120	345
9	70102General Arts	70102	166	MAWULI SENIOR HIGH. SCHOOL HO	Ho Municipal	0.5261422	6.717607	120	345
10	70102General Arts	70102	390	MAWULI SENIOR HIGH. SCHOOL HO	Ho Municipal	0.5261422	6.717607	120	345

	schoolcode	V1	schoolname	sssdistrict	ssslong	ssslat	Freq	cut_score	quality_score
nomics	50112	330	KUMASI SENIOR HIGH/TECH. SCHOOL, KUMASI	Kumasi Metro	-1.5971872	6.682060	50	293	312.3200
nomics	50112	380	KUMASI SENIOR HIGH/TECH. SCHOOL, KUMASI	Kumasi Metro	-1.5971872	6.682060	50	293	312.3200
nomics	50112	413	KUMASI SENIOR HIGH/TECH. SCHOOL, KUMASI	Kumasi Metro	-1.5971872	6.682060	50	293	312.3200
nomics	50112	424	KUMASI SENIOR HIGH/TECH. SCHOOL, KUMASI	Kumasi Metro	-1.5971872	6.682060	50	293	312.3200
nomics	50112	493	KUMASI SENIOR HIGH/TECH. SCHOOL, KUMASI	Kumasi Metro	-1.5971872	6.682060	50	293	312.3200
ts	70102	110	MAWULI SENIOR HIGH. SCHOOL, HO	Ho Municipal	0.5261422	6.717607	120	345	366.1250
ts	70102	128	MAWULI SENIOR HIGH. SCHOOL, HO	Ho Municipal	0.5261422	6.717607	120	345	366.1250
ts	70102	166	MAWULI SENIOR HIGH. SCHOOL, HO	Ho Municipal	0.5261422	6.717607	120	345	366.1250
ts	70102	390	MAWULI SENIOR HIGH. SCHOOL, HO	Ho Municipal	0.5261422	6.717607	120	345	366.1250
ts	70102	429	MAWULI SENIOR HIGH. SCHOOL, HO	Ho Municipal	0.5261422	6.717607	120	345	366.1250
ts	70102	433	MAWULI SENIOR HIGH. SCHOOL, HO	Ho Municipal	0.5261422	6.717607	120	345	366.1250

#Exercise3

```
#Exercise3
Dat<-na.omit(datstu)
Dat<-select(Dat,5:18)
Dat$schoolcode<-apply(Dat,1,function(x) return(x[as.numeric(x[14])]))
Dat$schoolcode<-as.numeric(Dat$schoolcode)
schdis<-na.omit(datsss)
datjsss<- fread("datjsss.csv")
datjsss<-rename(datjsss,jsslong = point_x, jsslats = point_y)
Bigdata<-left_join(Dat,schdis,by="schoolcode")
Bigdata<-left_join(Bigdata,datjsss,by="jssdistrict")
Bigdataedited<-select(Bigdata,ssslong, jsslong, jsslats, ssslats)
Bigdataedited<-unique(Bigdataedited)
Bigdataedited<-na.omit(Bigdataedited)
Bigdataedited <- mutate(Bigdataedited,dist = sqrt( (69.172*(ssslong - jsslong) * cos(jsslats/57.3)) ^2 + (69.172 * (ssslats - jsslats) * sin(jsslats/57.3)) ^2 ))
```

	ssslong	jsslong	jsslat	ssslat	dist
1	-1.1970884	-0.75524253	5.617353	5.130001	45.404991
2	-1.1970884	-1.19708836	5.130001	5.130001	0.000000
3	-1.1970884	-1.00538456	5.401725	5.130001	22.968725
4	-1.1970884	-1.55970335	5.572999	5.130001	39.524867
5	-1.1970884	-0.50863892	5.544896	5.130001	55.410029
6	-1.1970884	-1.00645339	5.201528	5.130001	14.033432
7	-1.1970884	-2.63174391	7.503565	5.130001	191.407178
8	-1.1970884	-1.26436615	5.495795	5.130001	25.723259
9	-1.1970884	-0.39751053	5.664688	5.130001	66.310912
10	-1.1970884	-1.30659389	5.153656	5.130001	7.719514
11	-1.1970884	-1.01707423	5.638250	5.130001	37.276595
12	-1.1970884	-0.19711526	5.607396	5.130001	76.349930
13	-1.1970884	-1.37461698	5.777995	5.130001	46.458354
14	-1.1970884	0.10686218	5.914734	5.130001	104.859841
15	-1.1970884	-1.56275165	6.559323	5.130001	102.012337
16	-1.1970884	-0.72363549	5.404561	5.130001	37.732218
17	-0.6355287	-0.63552868	6.619226	6.619226	0.000000
18	-0.6355287	-0.19711526	5.607396	6.619226	76.220297
19	-0.6355287	-0.47498974	5.944515	6.619226	47.960275
20	-0.6355287	-0.24114588	5.721143	6.619226	67.793736

#Exercise4

#Exercise4

Append5<-datstu

#Recode the schoolcode into its first three digits

```
Append5$score_rev1 <- substr(Append5$schoolcode1, 1, 3) |
Append5$score_rev2 <- substr(Append5$schoolcode2, 1, 3)
Append5$score_rev3 <- substr(Append5$schoolcode3, 1, 3)
Append5$score_rev4 <- substr(Append5$schoolcode3, 1, 3)
Append5$score_rev5 <- substr(Append5$schoolcode5, 1, 3)
Append5$score_rev6 <- substr(Append5$schoolcode6, 1, 3)
```



```
#Recode the program variable into 4 categories
category = function(program){
  programed = 'others'
  if(program == 'General Arts' | program == 'Visual Arts'){programed = 'arts'}
  else if(program == 'Business' | program == 'Home Economics'){programed = 'economics'}
  else if(program == 'General Arts' | program == 'General Science'){programed = 'science'}
  else{
    return(programed)}
}

#Before running the function, we need to eliminate the N.A. Since N.A comes out 'others'
Append5<-na.omit(Append5)
Append5$pgm_rev1 = sapply(Append5$choicepgm1,category)
Append5$pgm_rev2 = sapply(Append5$choicepgm2,category)
Append5$pgm_rev3 = sapply(Append5$choicepgm3,category)
Append5$pgm_rev4 = sapply(Append5$choicepgm4,category)
Append5$pgm_rev5 = sapply(Append5$choicepgm5,category)
Append5$pgm_rev6 = sapply(Append5$choicepgm6,category)
#Create a new choice variable choice_rev
Append5$choice_rev1 = paste0(Append5$score_rev1,Append5$pgm_rev1)
Append5$choice_rev2 = paste0(Append5$score_rev2,Append5$pgm_rev1)
Append5$choice_rev3 = paste0(Append5$score_rev3,Append5$pgm_rev1)
Append5$choice_rev4 = paste0(Append5$score_rev4,Append5$pgm_rev1)
Append5$choice_rev5 = paste0(Append5$score_rev5,Append5$pgm_rev1)
Append5$choice_rev6 = paste0(Append5$score_rev6,Append5$pgm_rev1)

#cutoff for recoded choice
newcut<-select(Append5,31:36,18)
Admittedschool3<-apply(newcut, 1, function(x) return(x[as.numeric(x[7])]))
Score3<-Append5$score
Adscore3<-data.frame(Admittedschool3,Score3)
Adscore3<-na.omit(Adscore3)
cutoff3<-by(Adscore3$score3,Adscore3$Admittedschool3,min)
cutoffscore3<-data.frame(choice =names(cutoff3), 'socre' = matrix(cutoff3))
colnames(cutoffscore3)[2]<-"cut_score"
#quality for recoded choice
quality3<-by(Adscore3$score3,Adscore3$Admittedschool3,mean)
qualityscore3<-data.frame(choice = names(quality3), 'socre' = matrix(quality3))
colnames(qualityscore3)[2]<-"quality_score"
#Consider the 20,000 highest score students.
Order<-Append5[order(-score),]
order<-Order[1:20000,]
```

	rankplace	score_rev1	score_rev2	score_rev3	score_rev4	score_rev5	score_rev6	pgm_rev1	pgm_rev2	pgm_rev3	pgm_rev4
politian	1	301	301	501	501	104	101	science	economics	arts	economics
nasaman)	1	210	201	213	213	105	215	science	science	science	science
okobi)	1	210	201	101	101	206	210	science	science	science	science
nasaman)	1	301	203	303	303	210	206	science	science	science	science
	1	301	301	203	203	102	102	science	economics	science	economics
	1	301	101	102	102	102	101	science	science	science	science
	1	301	301	309	309	102	102	science	science	science	science
politian	1	501	201	401	401	201	210	science	science	science	science
ro	1	301	301	301	301	516	512	science	science	arts	science
politian	1	301	201	306	306	201	206	science	science	science	arts
nasaman)	1	101	301	201	201	101	101	science	science	science	others
	1	301	211	101	101	706	701	science	science	science	science
	1	101	301	101	101	101	102	science	science	science	science
	1	210	501	301	301	102	102	science	science	science	science
Municipal	1	101	402	301	301	312	309	science	science	science	science
	1	210	201	213	213	102	102	science	science	science	science
ro	1	301	501	203	203	516	512	science	science	science	economics
	1	301	401	303	303	102	102	economics	economics	economics	economics
(Nkawkaw)	1	301	501	505	505	210	210	science	science	science	science

#Exercise5

```

#Propose a model specification.
#We use the recoded choices and the 20,000 highest score students.
Append6<-Order
#write the likelihood function
Append6$choice_rev1 <- as.numeric( as.factor(Append6$choice_rev1) )

like_function1<-function(param, Append6){
  choice_rev1 = Append6$choice_rev1
  score = Append6$score
  n_i<-nrow(Append6)
  n_j<-length(unique(Append6$choice_rev1))
  N_j<-n_j-1
  return1<-mat.or.vec(n_i,n_j)
  pn1<-param[1: N_j]
  pn2<-param[( N_j+1):(2* N_j)]
  for(j in 2:n_j){
    return1[,j]= pn1[j-1]+pn2[j-1]*score
  }
  prob = exp(return1)
  prob = sweep(prob, MARGIN=1, FUN="/", STATS=rowSums(prob))

  probc = NULL
  for (i in 1:n_i){
    probc[i] = prob[i, choice_rev1[i] ]
  }
  probc[probc >0.999999] = 0.999999
  probc[probc <0.000001] = 0.000001
  like = sum( log(probc) )
  return(- like)
}

lengthchoice<-length(unique(Append6$choice_rev1))
lengthchoice
#We have 249 choices, and we have 249*-1=497 estimates.
start1<- runif(497, -1, 1)
result<- optim(start1, fn = like_function1, method = "BFGS", control = list(trace = 6, maxit = 100), Append6= Append6)
estimate<-result$param
like<- result$value
like
#initial value 274348.340269

```

```

#probability
Prob<-function(param, Append6){
  choice_rev1 = Append6$choice_rev1
  score = Append6$score
  n_i<-nrow(Append6)
  n_j<-length(unique(Append6$choice_rev1))
  N_j<-n_j-1
  return1<-mat.or.vec(n_i,n_j)
  pn1<-param[1: N_j]
  pn2<-param[( N_j+1):(2* N_j)]
  for(j in 2:n_j){
    output1[,j]= pn1[j-1]+pn2[j-1]*score#this is because if starting with 1,
  }
  prob = exp(return1)
  prob = sweep(prob, MARGIN=1, FUN="/", STATS=rowSums(prob))
  probc = NULL
  for (i in 1:n_i){
    probc[i] = prob[i, choice_rev1[i] ]
  }
  probc[probc >0.999999] = 0.999999
  probc[probc <0.000001] = 0.000001
  like = sum( log(probc) )
  return(prob)
}

```

#Exercise6

```

Conditionallike<- function(param, choice_rev1, quality) {
  choice_rev1 = Append7$choice_rev1
  quality <- Append7$quality
  n_i <-nrow(data)
  n_j <-length(unique( choice_rev1 ))
  return2 <-mat.or.vec( n_i,n_j )
  N_j <-n_j - 1
  pn1<-param[1: N_j]
  pn2<-param[( N_j+1):(2* N_j)]
  for (i in 1:n_i) {
    return2[i,]<- pn1 * quality[i]
  }
  for (j in 2:n_j) {
    return2[,j]<- return2[,j] + pn1[ (j-1) ]
  }
  prob <-exp(return2)
  prob <-sweep(prob, MARGIN=1, FUN="/", STATS=rowSums(prob))

  probc <-NULL
  for (i in 1:n_i){
    probc[i] = prob[i, probc[i] ]
  }
  probc[probc >0.999999] = 0.999999
  probc[probc <0.000001] = 0.000001

  like <-sum( log(probc) )
  return(- like)
}

```

#Exercise7

```

#7
#I think the second model is better because the quality variable won't change easily while the effect
#of choice variable in the second model could be changed by omitting the "other

```