

```
In [7]: ➤ from sympy import *  
from sympy.plotting import (plot, plot_parametric)
```

#1a Derivative and Critical Values

```
In [14]: ➤ x=symbols('x', real=True)  
f=x**nsimplify(4/5)*(x-4)**2  
df=diff(f,x)  
print("f'",df.simplify())  
cVals=solve(df,x)  
cVals.append(0)  
print("The critical values of f are:",cVals)
```

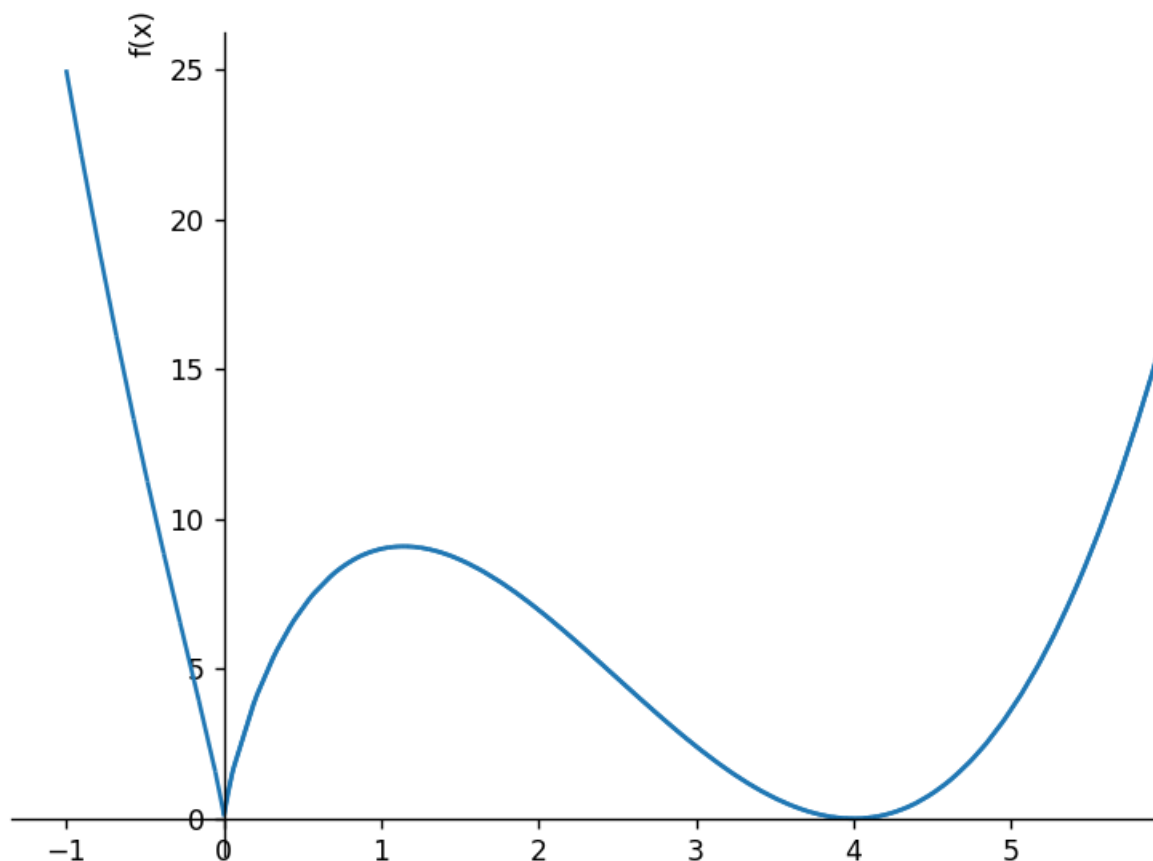
```
f' = 2*(x - 4)*(7*x - 8)/(5*x**(1/5))  
The critical values of f are: [8/7, 4, 0]
```

#1bc Graph of f and conclusion based on the graph

```
In [9]: ➤ matplotlib notebook
```

```
In [12]: g=abs(x)**(4/5)*(x-4)**2
plot((f,(x,-1,6,)),(g,(x,-1,6)))
print("The critical value of 8/7 is a local maximum.")
print("The critical value of 4 is a local minimum.")
print("The critical value of 0 is a local minimum.")
```

Figure 1



The critical value of 8/7 is a local maximum.
The critical value of 4 is a local minimum.
The critical value of 0 is a local minimum.

#2 Critical values of f

In [46]:



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#2b absolute extrema on [0,1]

In []:



In []:



In []:



#3a Mean Value Theorem: find c

In []:



#3b Illustration of MVT

In []:



#4a Simplify $f' - g'$

In []:



#4bc Conclusion based on answer to a

In []:



