

ECE 637 Digital Image Processing Laboratory: Image Restoration

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March 27, 2016

1 Minimum Mean Square Error (MMSE) Linear Filters

1.1 Plot Original Four Images

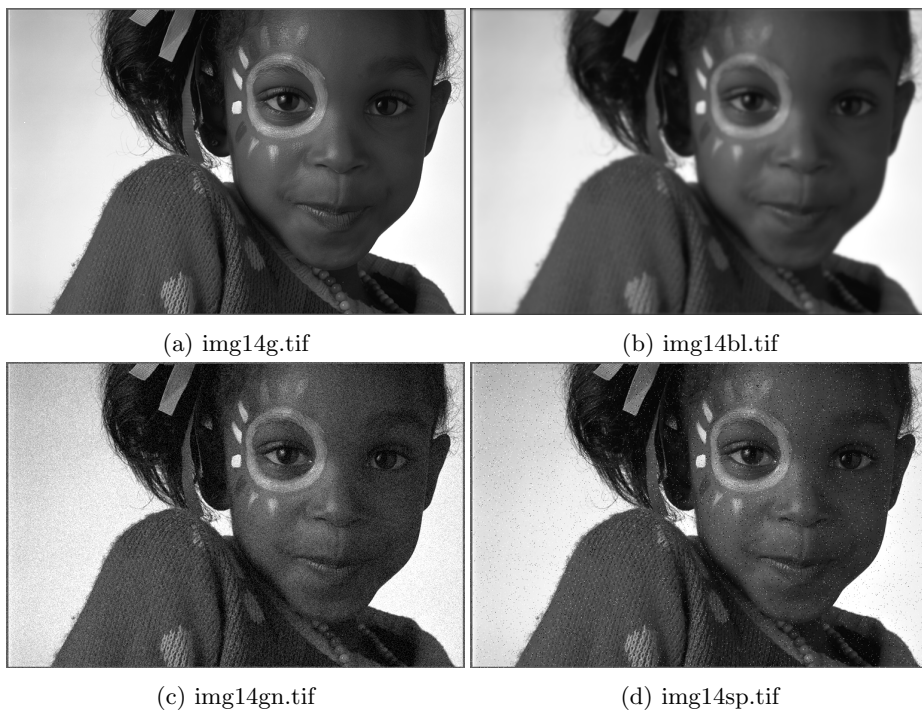
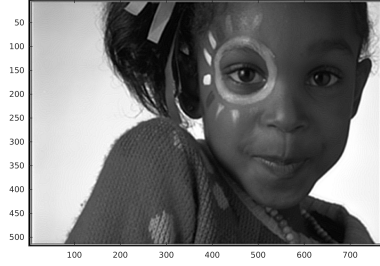
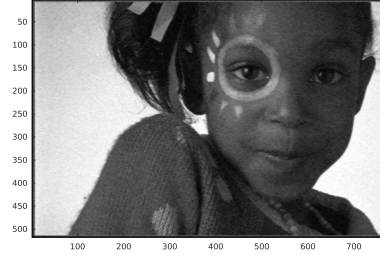


Figure 1: Original Fabulous Four Images

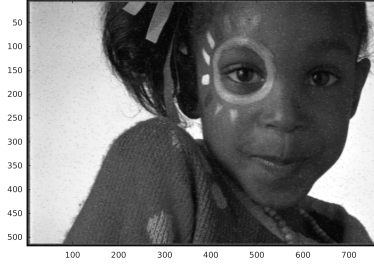
1.2 Plot the Blurred Image, and Two Noisy After Optimal Filtering



(a) Filtered Blurred Image



(b) Filtered Noisy Image



(c) Filtered Noisy Image with Spots

Figure 2: Distorted Images After Optimal Filtering

1.3 Results of MMSE Filters, θ^*

For the blurred image,

$$\theta^* = \begin{bmatrix} 1.7122 & 0.7401 & 0.9280 & 0.8153 & -0.9378 & -1.8137 & 1.8075 \\ -1.4864 & -1.8092 & -0.9006 & -0.5821 & -2.9833 & 0.5828 & 1.3537 \\ -0.9434 & -2.7623 & 0.3063 & 2.9781 & 0.7147 & -2.7348 & -0.8187 \\ 2.0282 & -0.5532 & 3.6350 & 3.4485 & 3.2368 & -3.1583 & 0.6775 \\ 1.6263 & -3.0881 & -0.4136 & 5.0773 & -0.1598 & -1.4265 & 0.7996 \\ -0.3035 & 0.3035 & 0.3035 & 0.3035 & 0.3035 & 1.5040 & 0.9250 \\ 1.2638 & 1.2638 & 1.2382 & 1.8732 & 1.1491 & 1.2882 & 1.0076 \end{bmatrix}$$

For the noisy image,

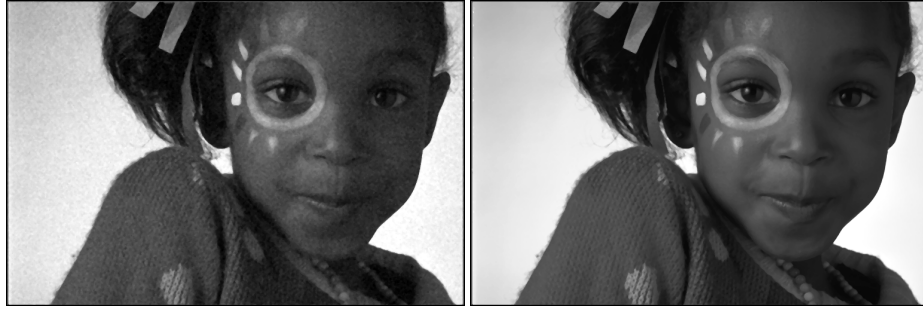
$$\theta^* = \begin{bmatrix} 0.0165 & -0.0055 & -0.0105 & -0.0091 & -0.0050 & -0.0044 & -0.0053 \\ 0.0259 & 0.0053 & -0.0125 & -0.0153 & -0.0222 & 0.0079 & -0.0043 \\ 0.0044 & 0.0355 & 0.0674 & 0.0476 & 0.0423 & 0.0307 & 0.0154 \\ 0.0050 & 0.0205 & 0.0731 & 0.2306 & 0.1117 & 0.0268 & 0.0127 \\ -0.0080 & 0.0464 & 0.0470 & 0.0891 & 0.0650 & 0.0088 & 0.0140 \\ 0.0302 & 0.0091 & 0.0290 & -0.0175 & -0.0118 & -0.0063 & 0.0183 \\ -0.0259 & 0.0066 & -0.0030 & 0.0011 & 0.0069 & 0.0192 & 0.0054 \end{bmatrix}$$

For the noisy image with spots,

$$\theta^* = \begin{bmatrix} 0.0080 & 0.0017 & -0.0010 & -0.0014 & 0.0252 & -0.0099 & -0.0407 \\ 0.0048 & -0.0016 & 0.0042 & -0.0203 & 0.0023 & -0.0006 & 0.0162 \\ -0.0016 & 0.0558 & 0.0413 & 0.0350 & 0.0612 & 0.0313 & -0.0068 \\ -0.0050 & 0.0267 & 0.0968 & 0.2652 & 0.0965 & 0.0497 & 0.0100 \\ 0.0257 & 0.0435 & 0.0212 & 0.1492 & 0.0154 & 0.0143 & 0.0079 \\ -0.0209 & 0.0214 & -0.0196 & -0.0287 & -0.0412 & 0.0038 & 0.0129 \\ -0.0185 & 0.0196 & 0.0199 & 0.0083 & 0.0233 & 0.0131 & -0.0110 \end{bmatrix}$$

2 Weighted Median Filtering

2.1 Results of Median Filtering



(a) Median Filtered Blurred Image

(b) Median Filtered Noisy Image

Figure 3: Weighted Median Filtered Image

2.2 Code Listing

2.2.1 medfilter.h

```
#ifndef __MEDFILT_H_
#define __MEDFILT_H_
```

```

void error(char *name);
unsigned int filterp(struct TIFF_img in, int i, int j);
unsigned int** filter(struct TIFF_img in);

#endif

```

2.2.2 medfilter.c

```

#include <math.h>
#include <string.h>

#include "tiff.h"
#include "allocate.h"
#include "medfilter.h"

int main (int argc, char **argv) {
    FILE *fp;
    struct TIFF_img tiff;
    unsigned int** filtered;
    int i, j;

    if (argc != 3) {
        error(argv[0]);
    }

    /* open image file */
    if ((fp = fopen(argv[1], "rb")) == NULL) {
        fprintf(stderr, "cannot open file %s\n", argv[1]);
        exit(1);
    }

    /* read image */
    if (read_TIFF(fp, &tiff)) {
        fprintf(stderr, "error reading file %s\n", argv[1]);
        exit(1);
    }

    /* close image file */
    fclose(fp);

    /* check the type of image data */
    if (tiff.TIFF_type != 'g') {
        fprintf(stderr, "error: image must be grayscale\n");
        exit(1);
    }
}

```

```

        filtered = filter(tiff);
        for (i = 0; i < tiff.height; i++) {
            for (j = 0; j < tiff.width; j++) {
                tiff.mono[i][j] = filtered[i][j];
            }
        }

        /* Free segment map */
        free_img((void *)filtered);

        /* open image file */
        if ((fp = fopen(argv[2], "wb")) == NULL) {
            fprintf(stderr, "cannot open file %s\n", argv[3]);
            exit(1);
        }

        /* write image */
        if (write TIFF(fp, &tiff)) {
            fprintf(stderr, "error writing TIFF file %s\n", argv[3] );
            exit(1);
        }

        /* close image file */
        fclose(fp);

        /* de-allocate space which was used for the tiff */
        free_TIFF(&tiff);

        return(0);
    }

    void error(char *name) {
        printf("usage:  %s image.tiff output.tiff\n\n", name);
        printf("Filter an image with a weighted median filter\n");
        exit(1);
    }

    unsigned int filterp(struct TIFF_img in, int i, int j) {
        int m, n, k;
        unsigned int sum1, sum2;
        unsigned int tmp;
        unsigned int data[25];
        unsigned int weights[25] = {1, 1, 1, 1, 1,
                                     1, 2, 2, 2, 1,
                                     1, 2, 2, 2, 1,
                                     1, 2, 2, 2, 1,
                                     1, 2, 2, 2, 1,
    }

```

```

1, 1, 1, 1, 1};

k = 0;
for (m = i - 2; m < i + 3; m++) {
    for (n = j - 2; n < j + 3; n++) {
        data[k] = in.mono[m][n];
        k++;
    }
}

for (m = 0; m < 25; m++) {
    for (n = m + 1; n < 25; n++) {
        if (data[m] < data[n]) {
            tmp = data[m];
            data[m] = data[n];
            data[n] = tmp;

            tmp = weights[m];
            weights[m] = weights[n];
            weights[n] = tmp;
        }
    }
}

sum1 = weights[0];
sum2 = 34 - sum1;
for (m = 0; m < 25; m++) {
    if (sum1 > sum2) {
        return data[m];
    }

    sum1 += weights[m+1];
    sum2 -= weights[m+1];
}

return data[m];
}

unsigned int** filter(struct TIFF_img in) {
    int i, j;

    unsigned int** filtered = (unsigned int**) get_img(in.width,
                                                         in.height,
                                                         sizeof(unsigned int));

    for (i = 2; i < in.height - 2; i++) {
        for (j = 2; j < in.width - 2; j++) {

```

```
        filtered[i][j] = filterp(in, i, j);
    }
}

return filtered;
}
```