# Package 'cdcatR'

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|--|
| Title Cognitive Diagnostic Computerized Adaptive Testing   |
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| <b>Description</b> Provides a set of functions for conducting cognitive diagnostic computerized adaptive testing applications (Chen (2009) <doi:10.1007 s11336-009-9123-2="">). It includes different item selection rules such us the global discrimination index (Kaplan, de la Torre, and Barrada (2015) <doi:10.1177 0146621614554650="">) and the nonparametric selection method (Chang, Chiu, and Tsai (2019) <doi:10.1177 0146621618813113="">), as well as several stopping rules. Functions for generating item banks and responses are also provided. To guide item bank calibration, model comparison at the item level can be conducted using the two-step likelihood ratio test statistic by Sorrel, de la Torre, Abad and Olea (2017) <doi:10.1027 1614-2241="" a000131="">.</doi:10.1027></doi:10.1177></doi:10.1177></doi:10.1007> |
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| R topics documented:   |
| att.plot   |

| att   | nlot                        | Plot | s fo | r a | ttri | ihu | ite i | ma | ist | or | v e | cti | im | ate | o ç |   |  |   |  |  |  |  |   |  |    |
|-------|-----------------------------|------|------|-----|------|-----|-------|----|-----|----|-----|-----|----|-----|-----|---|--|---|--|--|--|--|---|--|----|
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# **Description**

This function generates a plot monitoring the attribute mastery estimates (*x-axis*: Item position, *y-axis*: Mastery posterior probability estimate). If a parametric CD-CAT has been conducted, posterior probabilites (with confident intervals) of mastering each attribute are plotted. If a nonparametric CD-CAT has been conducted (and pseudo-probabilites have been computed), both nonparametric classification and pseudo-posterior probabilities (with confident intervals) of mastering each attribute are plotted. Pseudo-posterior probabilities is a method in progress. Caution in the interpretation is advised. Colors are used in the plots to indicate mastery (green), non-mastery (red), or uncertainty (blue).

#### Usage

```
att.plot(cdcat.obj, i, k = NULL)
```

## **Arguments**

| cdcat.obj | An object of class cdcat  |
|-----------|---|
| i         | Scalar numeric. It specifies the examinee to be plotted   |
| k         | Numeric vector. It specifies the attribute/s to be plotted. Default is NULL, which plots all attributes |

## Value

att.plot returns a plot of class ggplot.

| C | dcat | Cognitively based computerized adaptive test application |
|---|------|--|
|   |      |  |

## **Description**

cdcat conducts a CD-CAT application for a given dataset. Different item selection rules can be used: the general discrimination index (GDI; de la Torre & Chiu, 2016; Kaplan et al., 2015), the Jensen-Shannon divergence index (JSD; Kang et al., 2017; Minchen & de la Torre, 2016; Yigit et al., 2018), the posterior-weighted Kullback-Leibler index (PWKL; Cheng, 2009), the modified PWKL index (MPWKL; Kaplan et al., 2015), the nonparametric item selection method (NPS; Chang et al., 2019), or random selection. Fixed length or fixed precision CD-CAT can be applied. Fixed precision CD-CAT with NPS is available, by using the pseudo-posterior probability of each student mastering each attribute (experimental).

#### **Usage**

```
cdcat(
   fit = NULL,
   dat = NULL,
   itemSelect = "GDI",
   MAXJ = 20,
   FIXED.LENGTH = TRUE,
   att.prior = NULL,
   initial.distr = NULL,
   precision.cut = 0.8,
   NPS.args = list(Q = NULL, gate = NULL, pseudo.prob = TRUE, w.type = 1, seed = NULL),
   n.cores = 2,
   print.progress = TRUE
)
```

#### **Arguments**

| fit An object of class GDINA or gdina | . Calibrated item bank with the GDINA::GDINA |
|---------------------------------------|--|
|---------------------------------------|--|

(Ma & de la Torre, 2020) or CDM::gdina (Robitzsch et al., 2020) R packages

functions

dat Numeric matrix of dimensions N number of examinees x J number of items.

Dataset to be analyzed. If is.null(dat) the data is taken data from the fit

object (i.e., the calibration sample is used)

itemSelect Scalar character. Item selection rule: GDI, JSD, MPWKL, PWKL, NPS, or random

MAXJ Scalar numeric. Maximum number of items to be applied regardless of the

FIXED. LENGTH argument. Default is 20

FIXED.LENGTH Scalar logical. Fixed CAT-length (TRUE) or fixed-precision (FALSE) application.

Default is TRUE

att.prior Numeric vector of length  $2^K$ , where K is the number of attributes. Prior distri-

bution for MAP/EAP estimates. Default is uniform

initial.distr Numeric vector of length  $2^{k}$ , where K is the number of attributes. Weighting

distribution to initialize itemSelect at item position 1. Default is uniform

precision.cut Scalar numeric. Cutoff for fixed-precision (assigned pattern posterior probabil-

ity > precision.cut; Hsu, Wang, & Chen, 2013). When itemSelect = "NPS" this is evaluated at the attribute level using the pseudo-posterior probabilities for each attribute (K assigned attribute pseudo-posterior probability > precision.cut). Default is .80. A higher cutoff is recommended when itemSelect

= "NPS"

NPS.args A list of options when itemSelect = "NPS". Q = Q-matrix to be used in the anal-

ysis. gate = "AND" or "OR", depending on whether a conjunctive o disjunctive nonparametric CDM is used. pseudo.prob = pseudo-posterior probability of each examinee mastering each attribute (experimental). w.type = weight type used for computing the pseudo-posterior probability (experimental): 1 = Power-of-2 weight; 2 = Exponential weight. seed = Numeric vector of length 1. NPS

has a random component, so a seed is required for consistent results.

n. cores Scalar numeric. Number of cores to be used during parallelization. Default is 2

print.progress Scalar logical. Prints a progress bar to the console. Default is TRUE

#### Value

cdcat returns an object of class cdcat.

**est** A list that contains for each examinee the mastery posterior probability estimates at each step of the CAT (est.cat) and the items applied (item.usage)

**specifications** A list that contains all the specifications

#### References

Chang, Y.-P., Chiu, C.-Y., & Tsai, R.-C. (2019). Nonparametric CAT for CD in educational settings with small samples. *Applied Psychological Measurement*, *43*, 543-561.

Cheng, Y. (2009). When cognitive diagnosis meets computerized adaptive testing: CD-CAT. *Psychometrika*, 74, 619-632.

de la Torre, J., & Chiu, C. Y. (2016). General method of empirical Q-matrix validation. *Psychometrika*, 81, 253-273.

George, A. C., Robitzsch, A., Kiefer, T., Gross, J., & Uenlue, A. (2016). The R Package CDM for cognitive diagnosis models. *Journal of Statistical Software*, 74, 1-24. doi:10.18637/jss.v074.i02

Hsu, C. L., Wang, W. C., & Chen, S. Y. (2013). Variable-length computerized adaptive testing based on cognitive diagnosis models. *Applied Psychological Measurement*, *37*, 563-582.

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Robitzsch, A., Kiefer, T., George, A. C., & Uenlue, A. (2020). CDM: Cognitive Diagnosis Modeling. R package version 7.5-15. https://CRAN.R-project.org/package=CDM

Yigit, H. D., Sorrel, M. A., de la Torre, J. (2018). Computerized adaptive testing for cognitively based multiple-choice data. *Applied Psychological Measurement*, 43, 388-401.

## **Examples**

```
#----#
res.FIXJ <- cdcat(fit = fit, dat = dat, FIXED.LENGTH = TRUE,
                MAXJ = 20, n.cores = 2)
res.VARJ <- cdcat(fit = fit, dat = dat, FIXED.LENGTH = FALSE,
                MAXJ = 20, precision.cut = .80, n.cores = 2)
#-----#
res.FIXJ$est[[1]] # estimates for the first examinee (fixed-length)
res.VARJ$est[[1]] # estimates for the first examinee (fixed-precision)
att.plot(cdcat.obj = res.FIXJ, i = 1) # plot for the first examinee (fixed-length)
att.plot(cdcat.obj = res.VARJ, i = 1) # plot for the first examinee (fixed-precision)
# FIXJ summary
res.FIXJ.sum.real <- cdcat.summary(cdcat.obj = res.FIXJ, alpha = att) # vs. real accuracy
res.FIXJ.sum.real$recovery$plotPCV
res.FIXJ.sum.real$recovery$plotPCA
res.FIXJ.sum.real$item.exposure$plot
# VARJ summary
res.VARJ.sum.real <- cdcat.summary(cdcat.obj = res.VARJ, alpha = att)</pre>
res.VARJ.sum.real$recovery
res.VARJ.sum.real$CATlength$stats
res.VARJ.sum.real$CATlength$plot
res.VARJ.sum.real$item.exposure$plot
# vs. maximum observable accuracy
att.J <- GDINA::personparm(fit, "MAP")[, -(K+1)] # GDINA package
\# att.J <- t(sapply(strsplit(as.character(fitpattern\map.est), ""), as.numeric)) \# CDM package
class.J <- GDINA::ClassRate(att, att.J) # upper-limit for accuracy</pre>
res.FIXJ.sum.obse <- cdcat.summary(cdcat.obj = res.FIXJ, alpha = att.J)</pre>
res.FIXJ.sum.obse$recovery$plotPCV + ggplot2::geom_hline(yintercept = class.J$PCV[K],
                                                      color = "firebrick3")
res.FIXJ.sum.obse$recovery$plotPCA + ggplot2::geom_hline(yintercept = class.J$PCA,
                                                      color = "firebrick3")
# Example 2.
# CD-CAT simulation for multiple
# GDINA objs and comparison of
# performance on a validation sample #
#----#
Q <- sim180combination$simQ
K \leftarrow ncol(Q)
parm <- sim180combination$specifications$item.bank$simcatprob.parm</pre>
dat.c <- sim180combination$simdat[,,1]</pre>
att.c <- sim180combination$simalpha[,,1]</pre>
dat.v <- sim180combination$simdat[,,2]</pre>
att.v <- sim180combination$simalpha[,,2]</pre>
#----(multiple) Model estimation----#
fitTRUE <- GDINA::GDINA(dat = dat.c, Q = Q, catprob.parm = parm,</pre>
          control = list(maxitr = 0), verbose = 0)
fitGDINA <- GDINA::GDINA(dat = dat.c, Q = Q, verbose = 0)</pre>
fitDINA <- GDINA::GDINA(dat = dat.c, Q = Q, model = "DINA", verbose = 0)
LR2step <- LR.2step(fitGDINA)</pre>
models <- LR2step$models.adj.pvalues</pre>
fitLR2 <- GDINA::GDINA(dat = dat.c, Q = Q, model = models, verbose = 0)</pre>
```

```
#----#
fit.l <- list(fitTRUE, fitLR2, fitGDINA, fitDINA)</pre>
res.FIXJ.l <- lapply(fit.l, function(x) cdcat(dat = dat.v,fit = x,</pre>
                                          FIXED.LENGTH = TRUE, n.cores = 2))
res.VARJ.1 <- lapply(fit.1, function(x) cdcat(dat = dat.v, fit = x,
                                          FIXED.LENGTH = FALSE, n.cores = 2))
#-----#
fitbest <- GDINA::GDINA(dat = dat.v, Q = Q, catprob.parm = parm,
         control = list(maxitr = 1), verbose = 0)
fitbest.acc <- GDINA::personparm(fitbest, "MAP")[, -(K+1)]</pre>
class.J <- GDINA::ClassRate(att.v, fitbest.acc) # upper-limit for accuracy</pre>
# FIXJ comparison
res.FIXJ.sum <- cdcat.summary(cdcat.obj = res.FIXJ.1, alpha = att.v)</pre>
res.FIXJ.sum$recovery$PCVcomp + ggplot2::geom_hline(yintercept = class.J$PCV[K],
                                               color = "firebrick3")
res.FIXJ.sum$recovery$PCAmcomp + ggplot2::geom_hline(yintercept = class.J$PCA,
                                               color = "firebrick3")
res.FIXJ.sum$item.exposure$stats
res.FIXJ.sum$item.exposure$plot
# VARJ comparison
res.VARJ.sum <- cdcat.summary(cdcat.obj = res.VARJ.l, alpha = att.v)</pre>
res.VARJ.sum$recovery
res.VARJ.sum$item.exposure$stats
res.VARJ.sum$item.exposure$plot
res.VARJ.sum$CATlength$stats
res.VARJ.sum$CATlength$plot
# Example 3.
# Nonparametric CD-CAT for
# small-scale assessment
#----#
Q <- sim180DINA$simQ
K \leftarrow ncol(Q)
N <- 50
dat <- sim180DINA$simdat[1:N.]</pre>
att <- sim180DINA$simalpha[1:N,]
#-----#
res.NPS.FIXJ <- cdcat(dat = dat, itemSelect = "NPS", FIXED.LENGTH = TRUE,
                   MAXJ = 25, n.cores = 2,
                   NPS.args = list(Q = Q, gate = "AND", pseudo.prob = TRUE, w.type = 1,
                   seed = 12345))
res.NPS.VARJ <- cdcat(dat = dat, itemSelect = "NPS", FIXED.LENGTH = FALSE,
                   MAXJ = 25, precision.cut = 0.90, n.cores = 2,
                   NPS.args = list(Q = Q, gate = "AND", pseudo.prob = TRUE, w.type = 1,
                   seed = 12345))
#----#
res.NPS.FIXJ$est[[1]] # estimates for the first examinee (fixed-length)
res.NPS.VARJ$est[[1]] # estimates for the first examinee (fixed-precision)
att.plot(res.NPS.FIXJ, i = 1) # plot for estimates for the first examinee (fixed-length)
att.plot(res.NPS.VARJ, i = 1) # plot for estimates for the first examinee (fixed-precision)
```

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```
# FIXJ summary
res.NPS.FIXJ.sum.real <- cdcat.summary(cdcat.obj = res.NPS.FIXJ, alpha = att) # vs. real accuracy
res.NPS.FIXJ.sum.real$recovery$plotPCV
res.NPS.FIXJ.sum.real$recovery$plotPCA
res.NPS.FIXJ.sum.real$item.exposure$plot
# VARJ summarv
res.NPS.VARJ.sum.real <- cdcat.summary(cdcat.obj = res.NPS.VARJ, alpha = att)</pre>
res.NPS.VARJ.sum.real$recovery
res.NPS.VARJ.sum.real$CATlength$stats
res.NPS.VARJ.sum.real$CATlength$plot
res.NPS.VARJ.sum.real$item.exposure$plot
# vs. maximum observable accuracy
fit <- NPCD::AlphaNP(Y = dat, Q = Q, gate = "AND")
att.J <- fit$alpha.est
class.J <- GDINA::ClassRate(att, att.J) # upper-limit for accuracy</pre>
res.NPS.FIXJ.sum.obse <- cdcat.summary(cdcat.obj = res.NPS.FIXJ, alpha = att.J)</pre>
res. NPS. FIXJ. sum. obse\$recovery\$plotPCV + ggplot2::geom\_hline(yintercept = class.J\$PCV[K], the context of 
                                                                                                                                                                                          color = "firebrick3")
res.NPS.FIXJ.sum.obse%recovery%plotPCA + ggplot2::geom_hline(yintercept = class.J%PCA,
                                                                                                                                                                                          color = "firebrick3")
## End(Not run)
```

cdcat.summary

Summary information for a cdcat object

#### **Description**

This function provides classification accuracy, item exposure, and CAT length results for cdcat object. If a list of cdcat objects is included, these objects are compared through different tables and plots.

#### **Usage**

```
cdcat.summary(cdcat.obj, alpha, label = NULL)
```

## **Arguments**

cdcat.obj An object or list of objects of class cdcat

alpha Numeric matrix of dimensions N x K with the reference attribute patterns used

to compute attribute classification accuracy. It is expected that it will contain the true, generating alpha pattern or those estimated with the entire item bank. It is

a guideline to evaluate the cdcat results

label Character vector that contains the labels for the cdcat object(s). If NULL (by

default), the models are used as labels

## Value

cdcat.summary returns an object of class cdcat.summary.

**recovery** A list that contains the attribute classification accuracy results calculated at the pattern-(PCV) and attribute-levels (PCA). Two plots monitoring these variables are provided when FIXED.LENGTH = TRUE

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**item.exposure** A list that contains the item exposure rates results: descriptive statistics (stats) and a plot representing the item exposure rates (plot). Note that when FIXED.LENGTH = FALSE the overlap rate is calculated based on the average CAT length

**CATlength** If the object or list of objects of class cdcat are fixed-precision applications (i.e., FIXED.LENGTH = FALSE), this additional list is included. It contains descriptive statistics (stats) and a plot (plot) describing the CAT length

gen.data

Data generation

#### **Description**

This function can be used to generate datasets based on an object of class gen.itembank. The user can manipulate the examinees' attribute distribution or provide a matrix of attribute profiles. Data are simulated using the GDINA::simGDINA function (Ma & de la Torre, 2020).

# Usage

```
gen.data(
  N = NULL,
  R = 1,
  item.bank = NULL,
  att.profiles = NULL,
  att.dist = "uniform",
  mvnorm.parm = list(mean = NULL, sigma = NULL, cutoffs = NULL),
  higher.order.parm = list(theta = NULL, lambda = NULL),
  categorical.parm = list(att.prior = NULL),
  seed = NULL
)
```

## Arguments

seed

| N                | Scalar numeric. Sample size for the datasets   |  |  |  |  |  |
|------------------|--|--|--|--|--|--|
| R                | Scalar numeric. Number of datasets replications. Default is 1  |  |  |  |  |  |
| item.bank        | An object of class gen.itembank  |  |  |  |  |  |
| att.profiles     | Numeric matrix indicating the true attribute profile for each examinee ( $N$ examinees x $K$ attributes). If NULL (by default), att.dist must be specified   |  |  |  |  |  |
| att.dist         | Numeric vector of length $2^K$ , where $K$ is the number of attributes. Distribution for attribute simulation. It can be "uniform" (by default), "higher.order", "mvnorm", or "categorical". See simGDINA function of package GDINA for more information. Only used when att.profiles = NULL |  |  |  |  |  |
| mvnorm.parm      | A list of arguments for multivariate normal attribute distribution (att.dist = "mvnorm"). See simGDINA function of package GDINA for more information  |  |  |  |  |  |
| higher.order.pa  | ırm  |  |  |  |  |  |
|                  | A list of arguments for higher-order attribute distribution (att.dist = "higher.order"). See simGDINA function of package GDINA for more information   |  |  |  |  |  |
| categorical.parm |  |  |  |  |  |  |
|                  | A list of arguments for categorical attribute distribution (att.dist = "categorical").<br>See simGDINA function of package GDINA for more information  |  |  |  |  |  |

Scalar numeric. A scalar to use with set.seed

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#### Value

gen. data returns an object of class gen. data.

**simdat** An array containing the simulated responses (dimensions N examinees x J items x R replicates). If R = 1, a matrix is provided

**simalpha** An array containing the simulated attribute profiles (dimensions N examinees x K attributes x R replicates). If R = 1, a matrix is provided

specifications A list that contains all the specifications

#### References

Ma, W. & de la Torre, J. (2020). GDINA: The generalized DINA model framework. R package version 2.7.9. Retrived from https://CRAN.R-project.org/package=GDINA

## **Examples**

```
# Example 1.
# Generate dataset (GDINA item
# parameters and uniform attribute #
# distribution)
Q <- sim180GDINA$simQ
bank <- gen.itembank(Q = Q, mean.IQ = .70, range.IQ = .20, model = "GDINA")</pre>
simdata <- gen.data(N = 1000, item.bank = bank)</pre>
# Example 2.
# Generate multiple datasets (DINA #
# model and multivariate normal
# attribute distribution)
Q <- sim180GDINA$simQ
K \leftarrow ncol(Q)
bank <- gen.itembank(Q = Q, mean.IQ = .70, range.IQ = .20, model = "DINA")</pre>
cutoffs <- qnorm(c(1:K)/(K+1))
m <- rep(0,K)</pre>
vcov <- matrix(0.5,K,K)</pre>
diag(vcov) <- 1
simdata <- gen.data(N = 1000, R = 20, item.bank = bank, att.dist = "mvnorm",</pre>
               mvnorm.parm = list(mean = m, sigma = vcov, cutoffs = cutoffs))
# Example 3.
# Generate dataset (multiple
# models and higher-order
# attribute distribution)
Q <- sim180GDINA$simQ
```

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```
K <- ncol(Q)
model <- sample(c("DINA", "DINO", "ACDM"), size = nrow(Q), replace = TRUE)</pre>
bank <- gen.itembank(Q = Q, mean.IQ = .70, range.IQ = .20, model = model)</pre>
N <- 1000
theta <- rnorm(N)
lambda <- data.frame(a = runif(K, 0.7, 1.3), b = seq( -2, 2, length.out = K))
simdata <- gen.data(N = N, item.bank = bank, att.dist = "higher.order",</pre>
                  higher.order.parm = list(theta = theta,lambda = lambda))
# Example 4.
# Generate dataset (GDINA model
                                  #
# and given attribute profiles)
Q <- sim180GDINA$simQ
K \leftarrow ncol(Q)
bank <- gen.itembank(Q = Q, mean.IQ = .70, range.IQ = .20, model = "GDINA")</pre>
att.profiles <- matrix(data = c(1,0,0,0,0,0,0)
                              1,1,0,0,0,
                              1,1,1,0,0,
                              1,1,1,1,1), ncol = K, byrow = TRUE)
simdata <- gen.data(item.bank = bank, att.profiles = att.profiles)</pre>
```

gen.itembank

Item bank generation

# Description

This function can be used to generate an item bank. The user can provide a Q-matrix or create one defining a set of arguments. Item quality is sampled from a uniform distribution with mean = mean.IQ and range = range.IQ. Item parameters are generated so that the monotonicity constraint is satisfied.

# Usage

```
gen.itembank(
  Q = NULL,
  gen.Q = list(J = NULL, K = NULL, propK.J = NULL, nI = 1, minJ.K = NULL, max.Kcor = 1),
  mean.IQ,
  range.IQ,
  model = "GDINA",
  min.param = 0,
  seed = NULL
)
```

## Arguments

Numeric matrix of length J number of items x K number of atributes. Q-matrix

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| gen.Q     | A list of arguments to generate a Q-matrix if Q is not provided. $J = \text{number of items}$ (scalar numeric). $K = \text{number of attributes}$ (scalar numeric). $\text{propK.J} = \text{numeric vector summing up to 1}$ that determines the proportion of 1-attribute, 2-attribute,, items. The length of propK. J determines the maximum number of attributes considered for an item (see Examples below). $\text{nI} = \text{Scalar numeric that}$ sets the minimum number of identity matrices to be included in the Q-matrix. $\text{minJ.K} = \text{numeric vector of length } K$ that sets the minimum number of items measuring each attribute. $\text{max.Kcor} = \text{scalar numeric that sets}$ the maximum positive correlation allowed between two attributes |
|-----------|---|
| mean.IQ   | Item discrimination (mean for the uniform distribution). $mean.IQ = P(1) - P(0)$ (Sorrel et al., 2017; Najera et al., in press). Must be a scalar numeric between 0 and 1   |
| range.IQ  | Item discrimination (range for the uniform distribution). Must be a scalar numeric between $0\ \mathrm{and}\ 1$   |
| model     | A character vector of length $J$ with one model for each item, or a single value to be used for all items. The possible options include "DINA", "DINO", "ACDM", and "GDINA". One-attribute items will be coded in the output as "GDINA"   |
| min.param | Scalar numeric. Minimum value for the delta parameter of the principal effects of each attribute. Only usable if model = "ACDM" or model = "GDINA"  |
| seed      | Scalar numeric. A scalar to use with set. seed  |

#### Value

gen.itembank returns an object of class gen.itembank.

simQ Generated Q-matrix (only if gen.Q arguments have been used)

simcatprob.parm A list of success probabilities for each latent group in each item

simdelta.parm A list of delta parameters for each item

**check** A list that contains the mean.IQ and range.IQ for the item bank so that users can check whether these values match the expected results

specifications A list that contains all the specifications

## References

Najera, P., Sorrel, M. A., de la Torre, J., & Abad, F. J. (in press). Improving robustness in Q-matrix validation using an iterative and dynamic procedure. *Applied Psychological Measurement*.

Sorrel, M. A., Abad, F. J., Olea, J., de la Torre, J., & Barrada, J. R. (2017). Inferential item-fit evaluation in cognitive diagnosis modeling. *Applied Psychological Measurement*, *41*, 614-631.

#### **Examples**

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```
# Example 2.
# Generate item bank providing a
# Q-matrix using multiple models
Q <- sim180GDINA$simQ
K <- ncol(Q)
model <- sample(c("DINA", "DINO", "ACDM"), size = nrow(0), replace = TRUE)</pre>
bank <- gen.itembank(Q = Q, mean.IQ = .70, range.IQ = .20, model = model)</pre>
# Example 3.
# Generate item bank without
                              #
# providing a Q-matrix (using
# gen.Q arguments)
bank <- gen.itembank(gen.Q = list(J = 150, K = 5, propK.J = c(0.4, 0.3, 0.2, 0.1),
                  nI = 3, minJ.K = 30, max.Kcor = 1),
                  mean.IQ = .80, range.IQ = .10, min.param = 0.1)
```

LR.2step

Item-level model comparison using 2LR test

#### **Description**

This function evaluates whether the saturated G-DINA model can be replaced by reduced CDMs without significant loss in model data fit for each item using two-step likelihood ratio test (2LR). Sorrel, de la Torre, Abad, and Olea (2017) and Ma & de la Torre (2018) can be consulted for details.

#### Usage

```
LR.2step(fit, p.adjust.method = "holm", alpha.level = 0.05)
```

#### **Arguments**

fit

Calibrated item bank with the GDINA::GDINA (Ma & de la Torre, 2020) or CDM::gdina (Robitzsch et al., 2020) R packages functions

p.adjust.method

Scalar character. Correction method for *p*-values. Possible values include "holm", "hochberg", "hommel", "bonferroni", "BH", "BY", "fdr", and "none". See p.adjust function from the stats R package for additional details. Default is holm

alpha.level

Scalar numeric. Alpha level for decision. Default is 0.05

# Value

LR2. step returns an object of class LR2. step

LR2 Numeric matrix. LR2 statistics

**pvalues** Numeric matrix. p-values associated with the 2LR statistics

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adj.pvalues Numeric matrix. Adjusted p-values associated with the 2LR statistics

df Numeric matrix. Degrees of freedom

models.adj.pvalues Character vector denoting the model selected for each item using the *largestp* rule (Ma et al., 2016). All statistics whose *p*-values are less than alpha.level are rejected. All statistics with *p*-value larger than alpha.level define the set of candidate reduced models. The G-DINA model is retained if all statistics are rejected. Whenever the set includes more than one model, the model with the largest *p*-value is selected as the best model for that item

#### References

Ma, W. & de la Torre, J. (2018). Category-level model selection for the sequential G-DINA model. *Journal of Educational and Behavorial Statistic*, 44, 45-77.

Ma, W. & de la Torre, J. (2020). GDINA: The generalized DINA model framework. R package version 2.7.9. Retrived from https://CRAN.R-project.org/package=GDINA

Ma, W., Iaconangelo, C., & de la Torre, J. (2016). Model similarity, model selection and attribute classification. *Applied Psychological Measurement*, 40, 200-217.

Robitzsch, A., Kiefer, T., George, A. C., & Uenlue, A. (2020). CDM: Cognitive Diagnosis Modeling. R package version 7.5-15. https://CRAN.R-project.org/package=CDM

Sorrel, M. A., de la Torre, J., Abad, F. J., & Olea, J. (2017). Two-step likelihood ratio test for item-level model comparison in cognitive diagnosis models. *Methodology*, 13, 39-47.

# **Examples**

sim180combination

Simulated data (180 items, a combination of DINA, DINO, and A-CDM items)

# **Description**

Simulated data, Q-matrix and item parameters for a 180-item bank with 5 attributes. Data generated using the gen. data function.

## Usage

sim180combination

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#### **Format**

A list with components:

simdat Numeric array. Simulated responses of 250 examinees for two replicates simQ Numeric matrix. Simulated Q-matrix simalpha Numeric array. Simulated attribute patterns of 250 examinees for two replicates specifications A list that contains all the specifications that were used in the gen.itembank function

sim180DINA

Simulated data (180 items, DINA model)

# **Description**

Simulated data, Q-matrix and item parameters for a 180-item bank with 5 attributes. Data generated using the gen.data function.

# Usage

sim180DINA

#### **Format**

A list with components:

simdat Numeric matrix. Simulated responses of 500 examinees simQ Simulated Q-matrix

simalpha Numeric matrix. Simulated attribute patterns of 500 examinees

specifications A list that contains all the specifications that were used in the gen.itembank function

sim180GDINA

Simulated data (180 items, G-DINA model)

# **Description**

Simulated data, Q-matrix and item parameters for a 180-item bank with 5 attributes. Data generated using the gen.data function.

#### Usage

sim180GDINA

## Format

A list with components:

simdat Numeric matrix. Simulated responses of 500 examinees

simQ Simulated Q-matrix

simalpha Numeric matrix. Simulated attribute patterns of 500 examinees

specifications A list that contains all the specifications that were used in the gen.itembank function

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