Carnegie Mellon University Trees Indexes (Part II)



_ecture #08



Database Systems 15-445/15-645 Fall 2018

Andy Pavlo Computer Science Carnegie Mellon Univ.

ADMINISTRIVIA

Project #1 is due Wednesday Sept 26th @ 11:59pm

Homework #2 is due Friday Sept 28th @ 11:59pm

Project #2 will be released on Wednesday Sept 26th. First checkpoint is due Monday Oct 8th.



TODAY'S AGENDA

Additional Index Usage

Skip Lists

Radix Trees

Inverted Indexes



Most DBMSs automatically create an index to enforce integrity constraints.

- → Primary Keys
- → Unique Constraints
- → Foreign Keys (?)

```
CREATE TABLE foo (
   id SERIAL PRIMARY KEY)
  val1 INT NOT NULL,
  val2 VARCHAR(32) UNIQUE
);
```

CREATE UNIQUE INDEX foo_pkey
ON foo (id);

CREATE UNIQUE INDEX foo_val2_key
ON foo (val2);



Postgre will not allow creating foreign key unless it guarantee this field has unique index on that Most DBMSs automatically create an index to enforce integrity constraints.

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CREATE TABLE bar (
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  val VARCHAR(32)
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PARTIAL INDEXES

Create an index on a subset of the entire table. This potentially reduces its size and the amount of overhead to maintain it.

One common use case is to partition indexes by date ranges.

→ Create a separate index per month, year.

```
CREATE INDEX idx_foo
ON foo (a, b)
WHERE c = 'WuTang';
```



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here in

→ Create a separate index per month, year.

A common way to manually partition the db in order to avoid overhead scan. Similarly we avoid use xxx * in Elasticsearch when querying.

```
CREATE INDEX idx_foo
ON foo (a, b)
WHERE c = 'WuTang';
```

```
SELECT b FROM foo
WHERE a = 123
AND c = 'WuTang';
here index works if given c = 'Wu Tang'
```



COVERING INDEXES

If all of the fields needed to process the query are available in an index, then the DBMS does not need to retrieve the tuple.

CREATE INDEX idx_foo
ON foo (a, b);

SELECT b FROM foo
WHERE a = 123;

This reduces contention on the DBMS's buffer pool resources.

does not need to move tuple from disk to buffer pool and return less use on buffer pool manager —> less latches used



INDEX INCLUDE COLUMNS

Embed additional columns in indexes to support index-only queries.

Not part of the search key.

```
CREATE INDEX idx_foo
ON foo (a, b)
INCLUDE (c)
```



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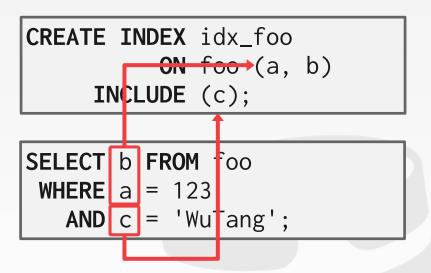


INDEX INCLUDE COLUMNS

Embed additional columns in indexes to support index-only queries.

Not part of the search key.

index only includes (a, b)





The index does not need to store keys in the same way that they appear in their base table.

```
SELECT * FROM users
WHERE EXTRACT(dow

⇒ FROM login) = 2;
```



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```
SELECT * FROM users
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```

```
CREATE INDEX idx_user_login
ON users (login);
```



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You can use expressions when declaring an index.

```
SELECT * FROM users
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```

```
CREATE INDEX __user_login
ON users __gin);
```



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You can use expressions when declaring an index.

CREATE INDEX __user_login
ON users __gin);

```
CREATE INDEX idx_user_login
ON users (EXTRACT(dow FROM login));
```



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You can use expressions when declaring an index.

```
SELECT * FROM users
 WHERE EXTRACT (dow
       ♥FROM login) = 2
CREATE INDEX
                _user_login
    ON users
```

```
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    ON users (EXTRACT(dow FROM login));
```



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CREATE INDEX Luser_login You can use expressions when ON users

declaring an index.

expression index

CREATE INDEX idx_user_login ON users (EXTRACT(dow FROM login));

SELECT * **FROM** users

WHERE EXTRACT (dow

♥ FROM login) = 2

partial index

```
CREATE INDEX idx_user_login
    ON foo (login)
 WHERE EXTRACT(dow FROM login) = 2;
```



OBSERVATION

The easiest way to implement a **dynamic** orderpreserving index is to use a sorted linked list.

All operations have to linear search.

 \rightarrow Average Cost: O(N)

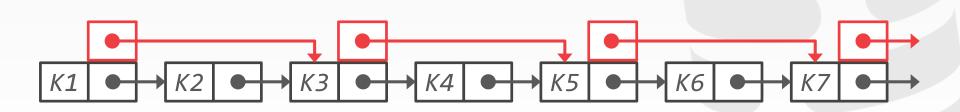


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SKIP LISTS

Multiple levels of linked lists with extra pointers that **skip** over intermediate nodes.

Maintains keys in sorted order without requiring global rebalancing.

Skip Lists: A Probabilistic Alternative to Balanced Trees

Skip lists are a data structure that can be used in place of balanced trees. Skip lists use probabilistic balancing rather than strictly enforced balancing and us a result the algorithms for insertion and deletion in skip lists are much simpler and significantly faster than equivalent algorithms for balanced trees.

William Pugh

Binary trees can be used for representing abstract data types used as declinearies an oldered lists. They work well when the elements are inserted in a random order. Some sequences of operations, such an investiga the elements in order, produce in a section of the elements in order, produce in a torse possible to randomly germate the list of firms to be inserted, free would own well with high probability for any size part sequence. In most cases operate must be answered on-line, so modernly permuting the inputs in superior. Bulletoned result algorithms to arrange the tree as operations are performed to make the contract of the con

Skip lots are a probabilistic attenuitie to balanced trees. Skip lines are hanced by consulting a mandon number generator. Although skip lists have bed werel-sace performance, no input sequence consistently produces he werst-sace performance transh like quickover blens the give element in choless that the properties of the properties of the properties of the testing the properties of the properties of the properties of the that 20 clements, the chance that a search will take more than 3 times the expected time in less that one in a millioni. Skip line have balance properties similar to that of warch's tree built by another meetings, etc. of or require inserties.

to Bulleting of this structure probabilistically is easier than explicitly insufaining the balance, For many applications, skip hiss are a more natural representation than symptomic skip hiss are a more natural representation than rese, also leading to simple apportfism. The simple thinks the single city of key list algorithms makes them easier to implement and provides significant constant factors speed improvements over balanced tree and self-adjusting tree algorithms. Skip hists are also very an easier bis configured to require an approach of the control of the contr

SKIP LISTS

We might need to examine every node of the list when searching a linked list $(F(gure\ la))$. If the list is stored in sorted order and every other node of the list sides has a pointer to the node two ahead it in the list $(F(gure\ lb))$, we have to examine no more than $\lceil n/2 \rceil + 1$ nodes (where n is the length of the list).

Also giving every fourth node a pointer four ahead (Figure 1c) requires that no more than [n4] + 2 nodes be examined. If every (2²) nodes has a pointer 2 nodes shead (Figure 1a), the number of nodes that must be examined can be reduced to [log₂ n which envil could be impaction. This data structure could be used for fast searching, but insertion and deletion would be impraction.

A node that has a floward pointers to called a level a node it for the first point p and p

SKIP LIST ALGORITHMS This section gives algorithms to search for, insert and delete

elements in a dictionary or symbol table. The Search operation returns the contenent of the value associated with the desired key or failure if the key is not present. The Dieser operation associates a specified key with a new value (inserting the key if it had not already been present). The Delete operation deletes the specified key, It is easy to support additional operations such as "find the minimum key" or "find the next key"

Each element is represented by a node, the level of which is chosen randomly when the node is interest without regard for the number of elements in the data structure. A level i node has i floward pointers, inducted I though! A web not need to store the level of a node in the node. Level see excepted at some appropriate constant Mader-of!. The level of list is the maximum level currently in the list (or 1 if the list is empty). The hode of a list has forward pointers at levels one through Model-or!. The forward pointers of the hoader as I levels higher than the current maximum level of the list point.





SKIP LISTS

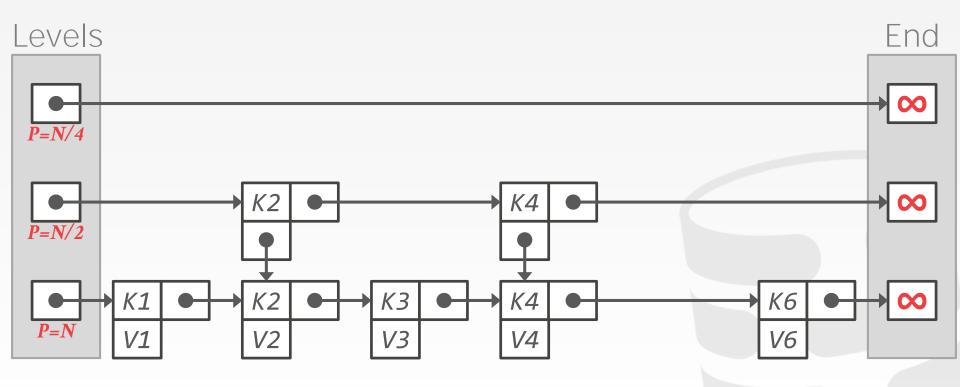
A collection of lists at different levels

- → Lowest level is a sorted, singly linked list of all keys
- \rightarrow 2nd level links every other key
- → 3rd level links every fourth key
- → In general, a level has half the keys of one below it

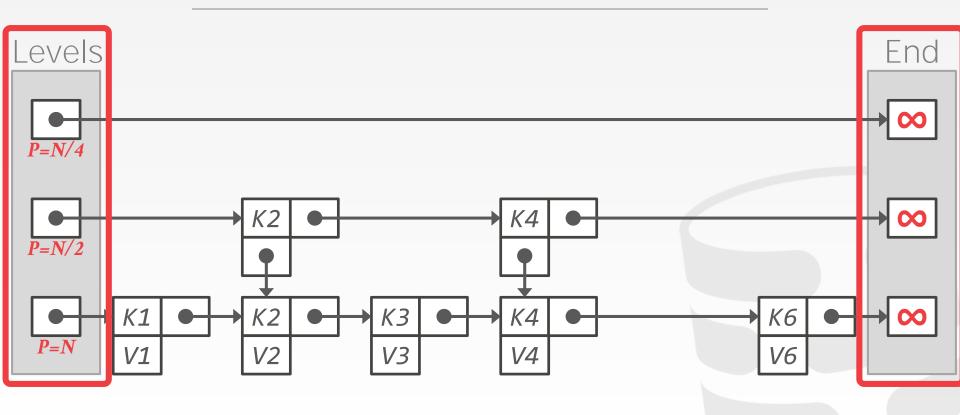
To insert a new key, flip a coin to decide how many levels to add the new key into.

Provides approximate O(log n) search times.

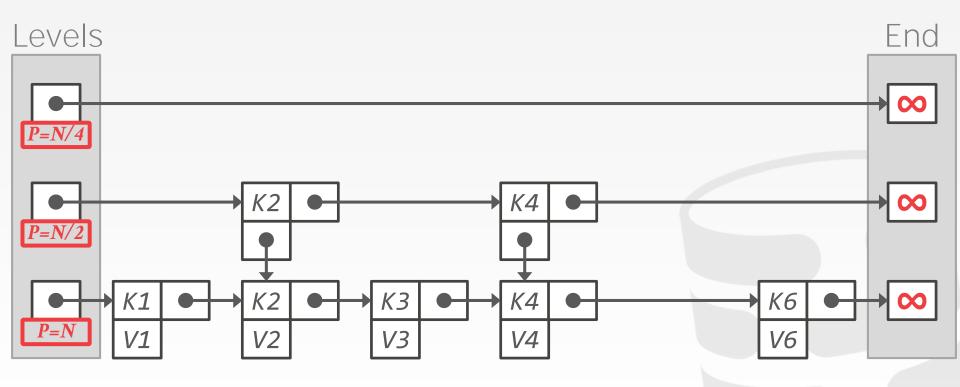




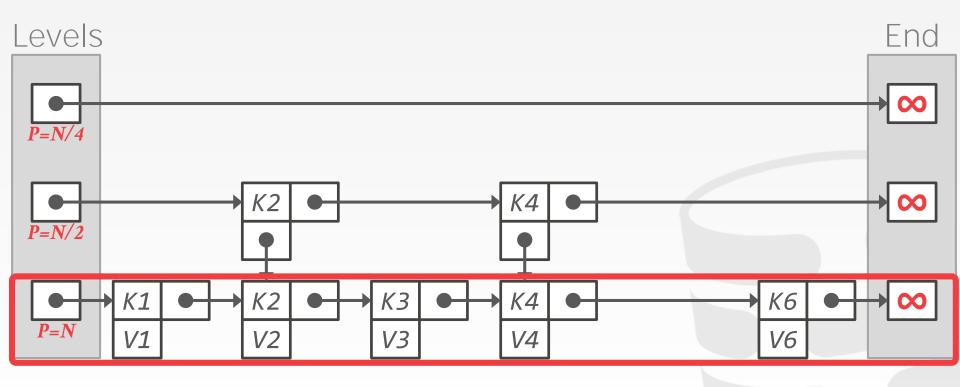




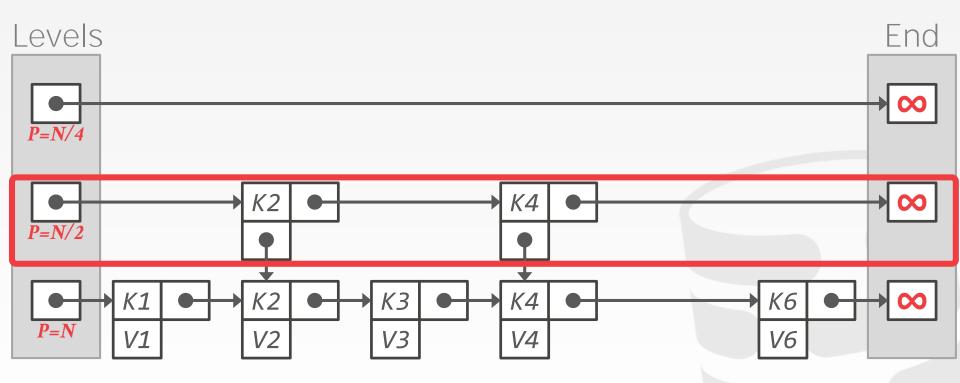




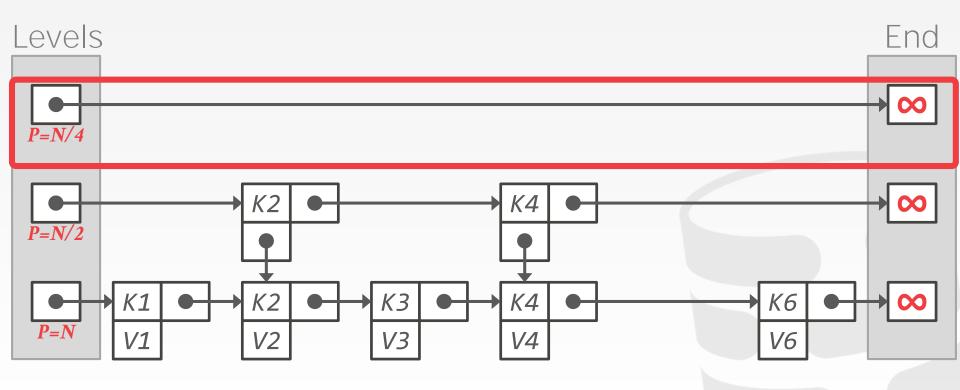




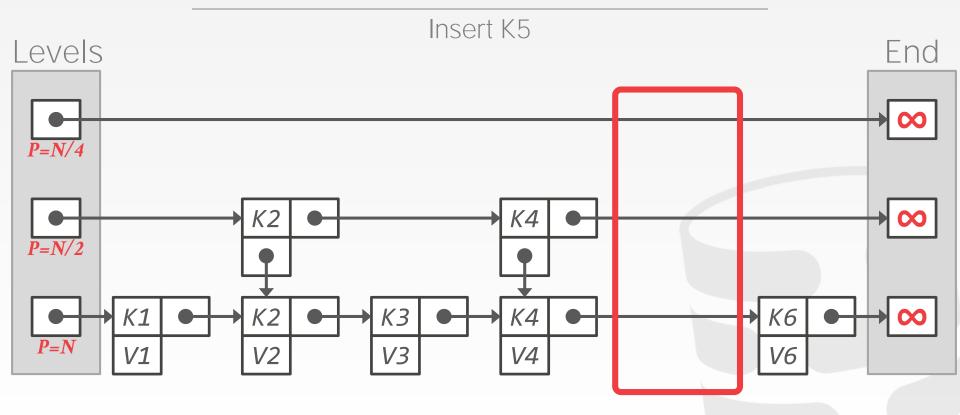




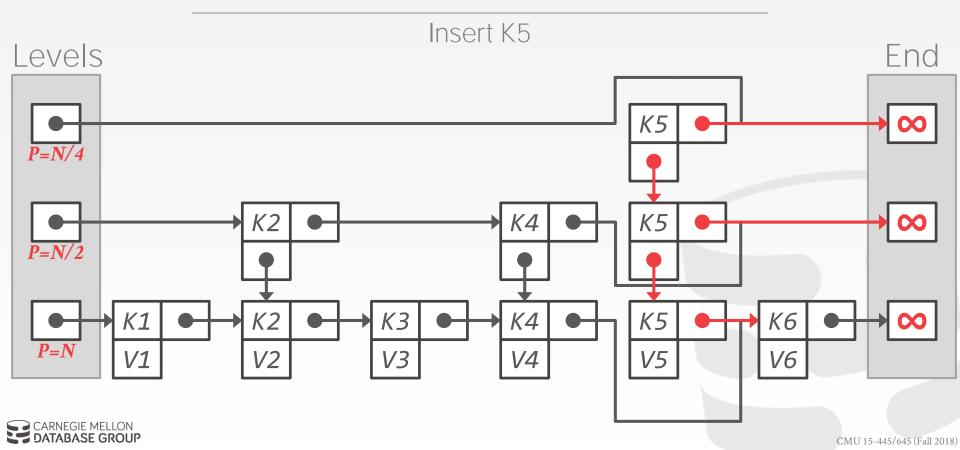


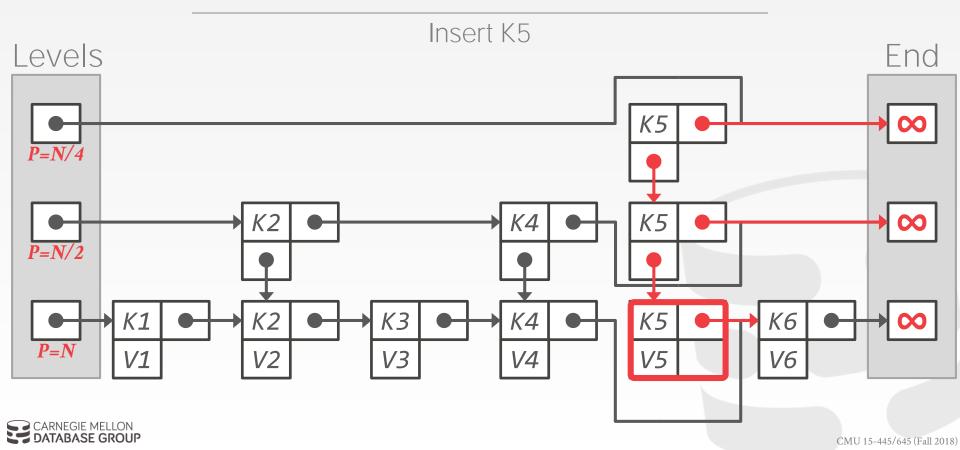


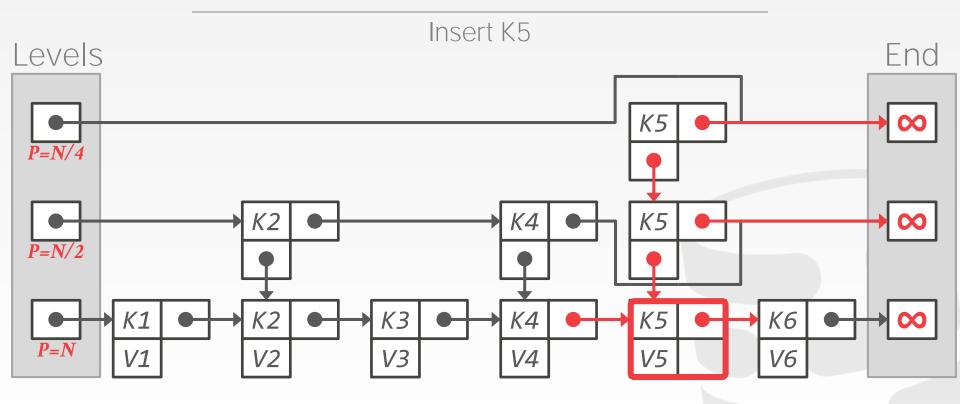




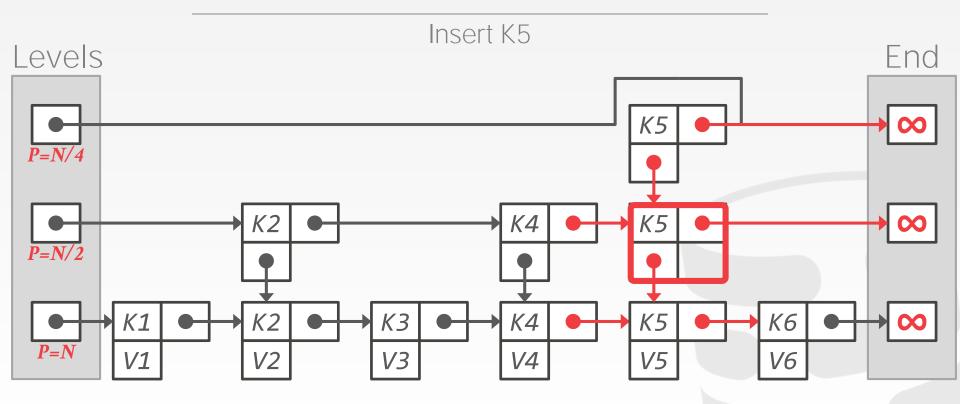




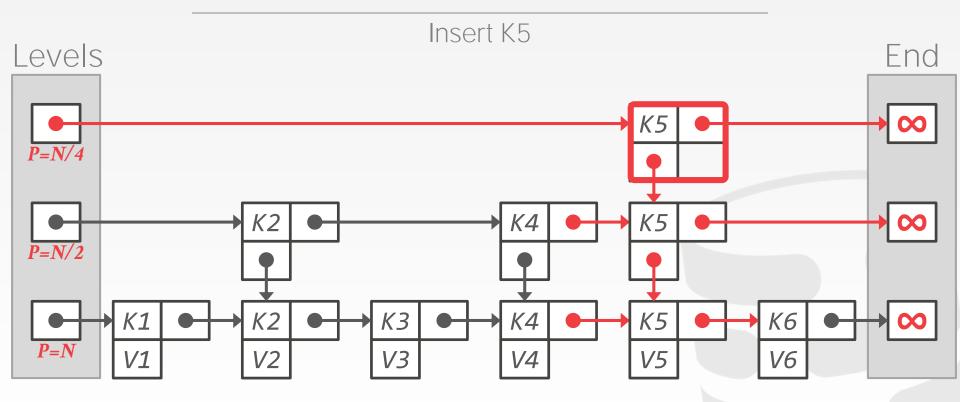




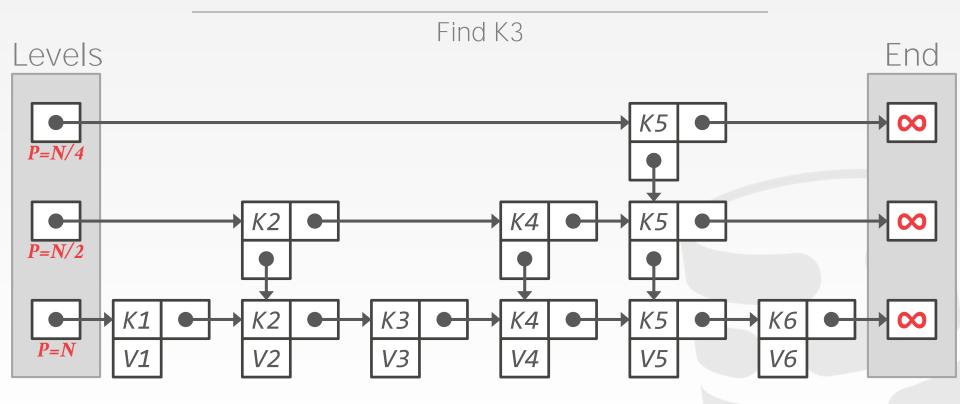




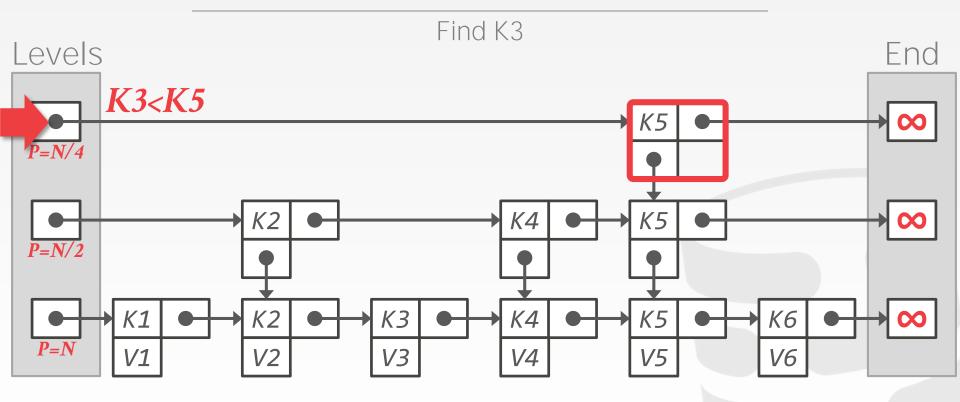




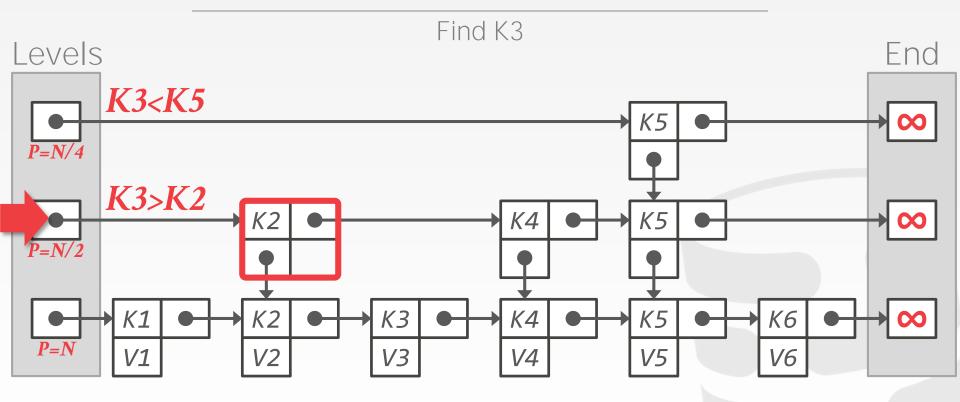




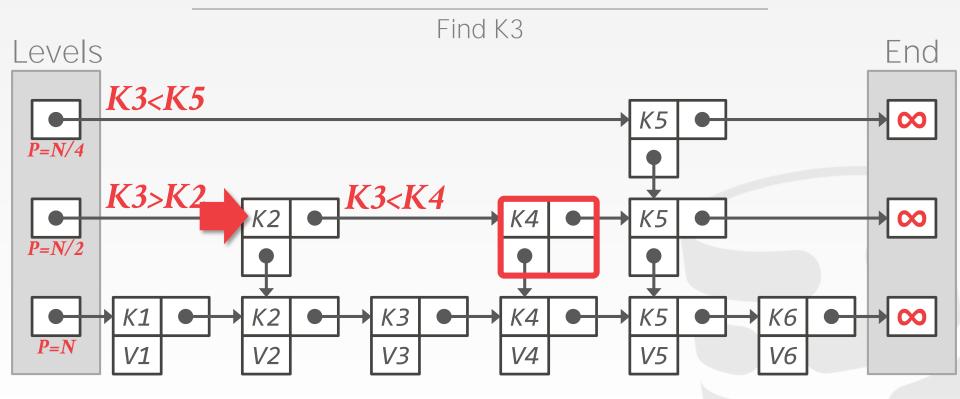




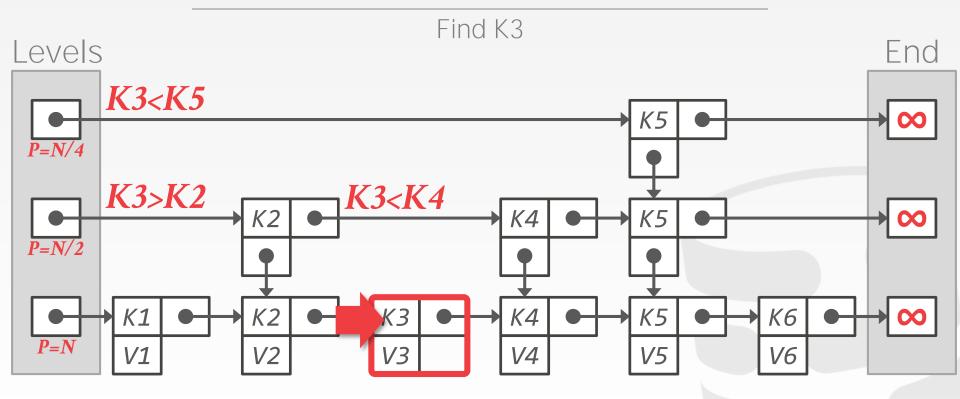










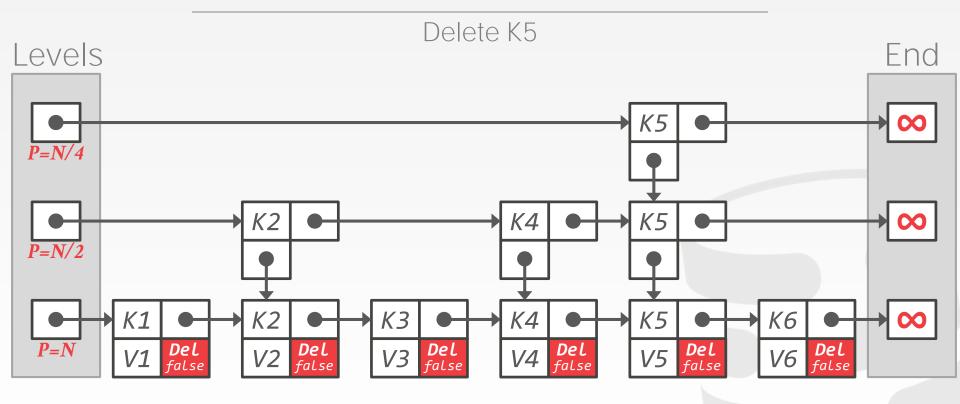




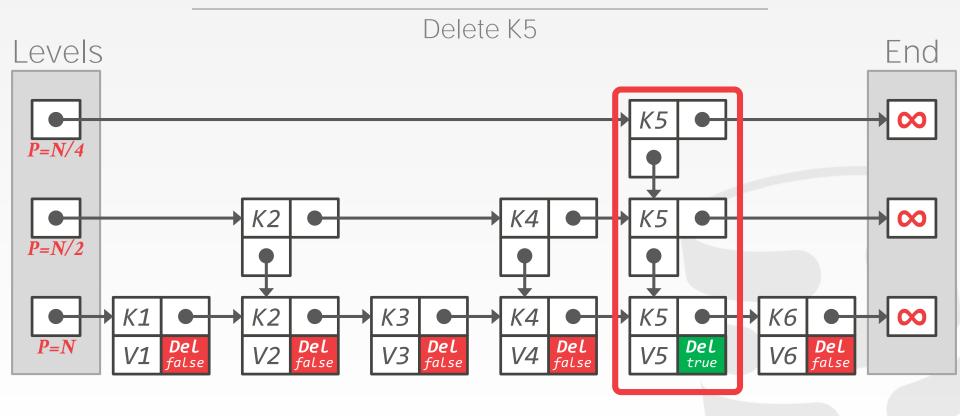
First **logically** remove a key from the index by setting a flag to tell threads to ignore.

Then **physically** remove the key once we know that no other thread is holding the reference.

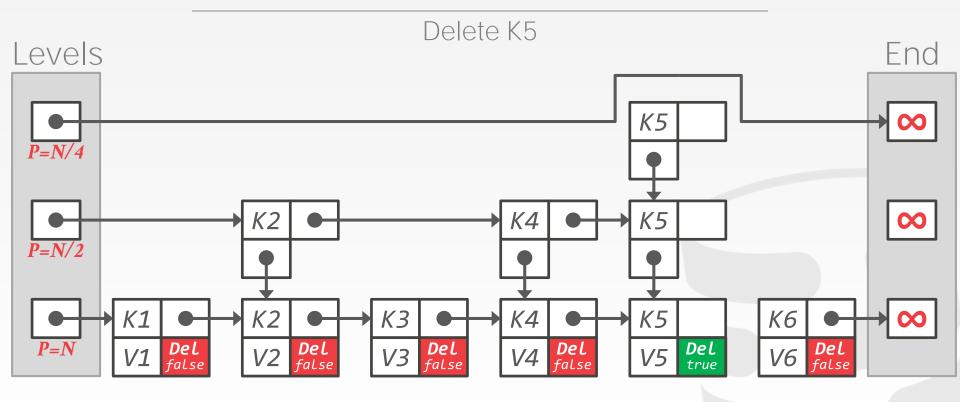




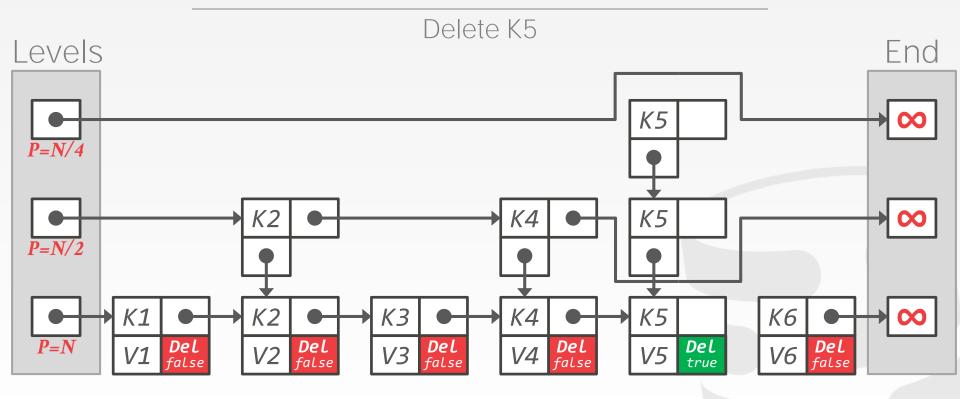




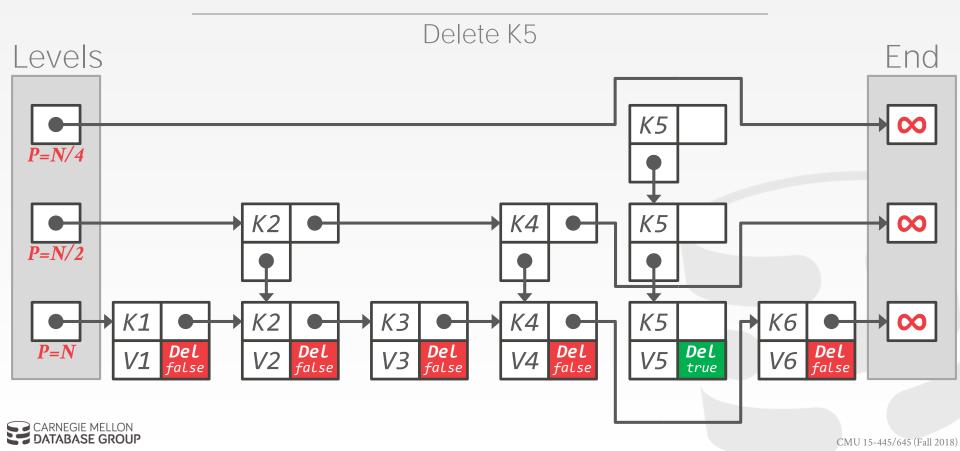


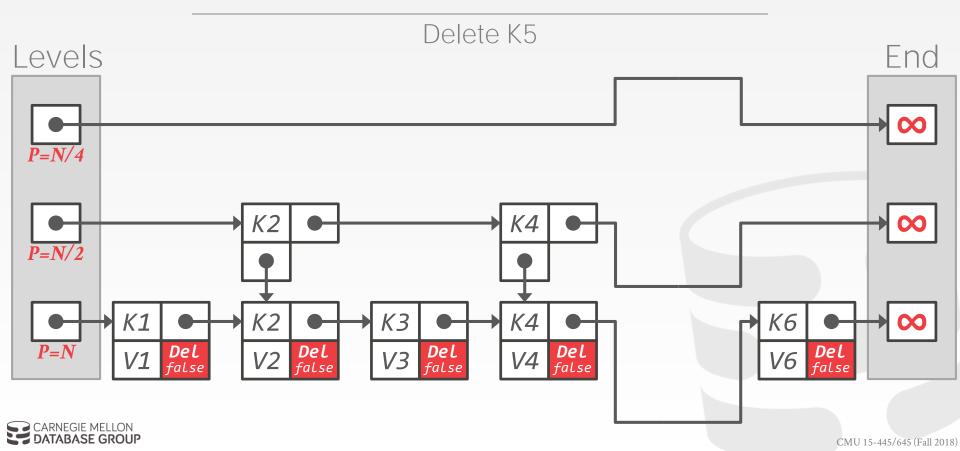












SKIP LISTS

insert: flip coin to determine if insert on current level. Bottom level probability is 1 query: top down. Pointer to prune

delete: first set flag on pointers. When no more references, physically remove it **Advantages:**

- → Uses less memory than a typical B+Tree if you don't include reverse pointers.
- \rightarrow Insertions and deletions do not require rebalancing.

count of levels of skip lists may grow gradually

Disadvantages:

- → Not disk/cache friendly because they do not optimize locality of references.
- \rightarrow Reverse search is non-trivial.



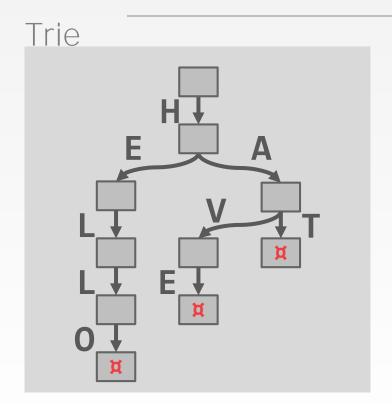
基数树

RADIX TREE

Represent keys as individual digits. This allows threads to examine prefixes one-by-one instead of comparing entire key.

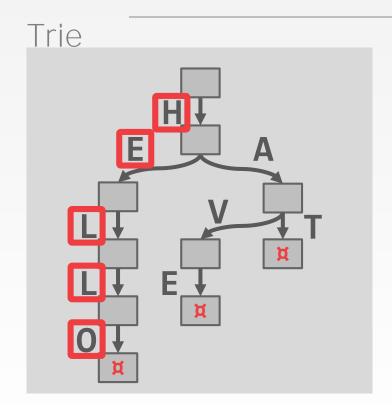
- \rightarrow The height of the tree depends on the length of keys.
- → Does not require rebalancing
- → The path to a leaf node represents the key of the leaf
- → Keys are stored implicitly and can be reconstructed from paths.





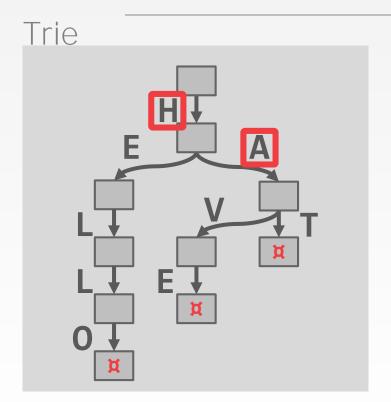
Keys: HELLO, HAT, HAVE





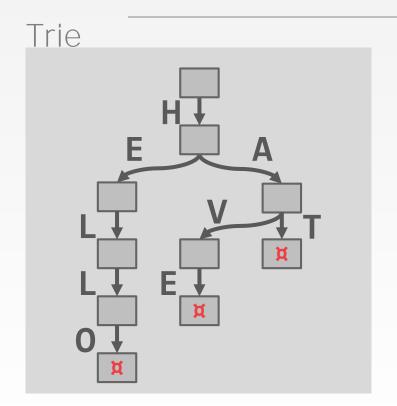
Keys: **HELLO HAT, HAVE**

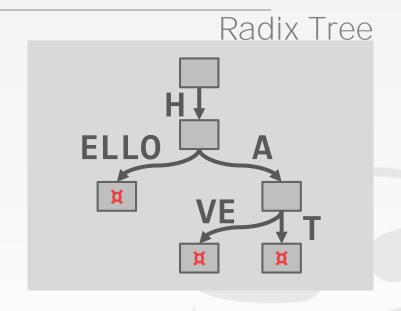




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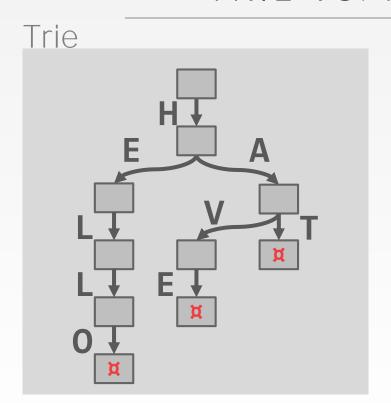


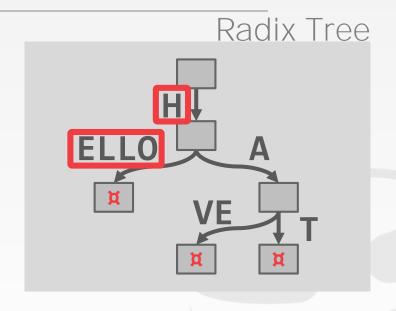




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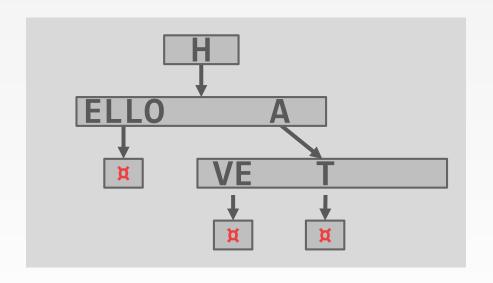




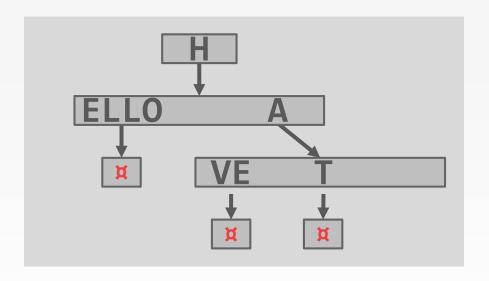


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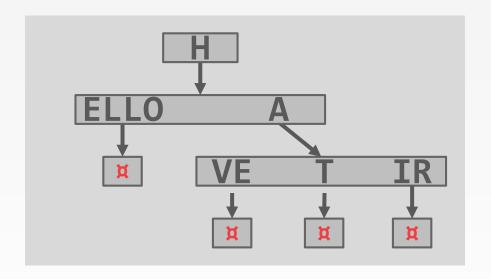






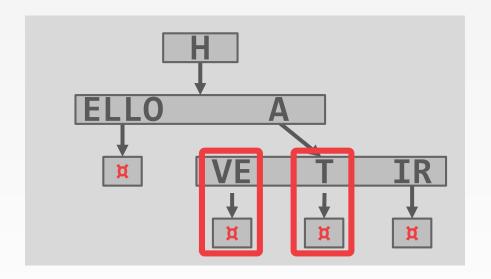
Insert HAIR



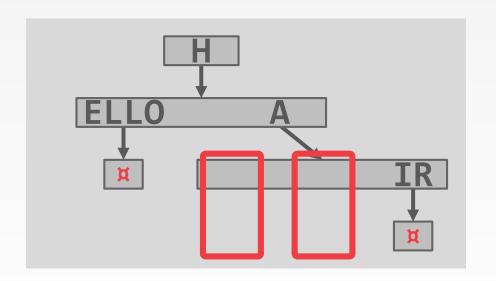


Insert HAIR

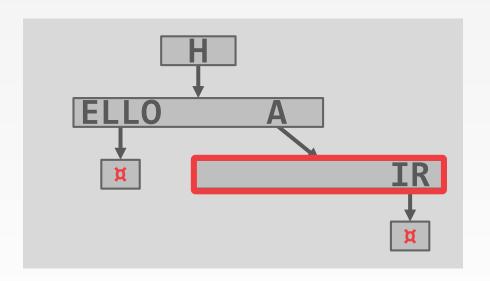




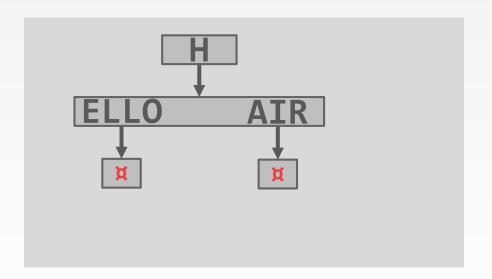














Not all attribute types can be decomposed into binary comparable digits for a radix tree.

- → **Unsigned Integers:** Byte order must be flipped for little endian machines.
- → **Signed Integers:** Flip two's-complement so that negative numbers are smaller than positive.
- → **Floats:** Classify into group (neg vs. pos, normalized vs. denormalized), then store as unsigned integer.
- → **Compound:** Transform each attribute separately.

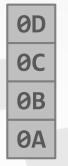


Int Key: 168496141



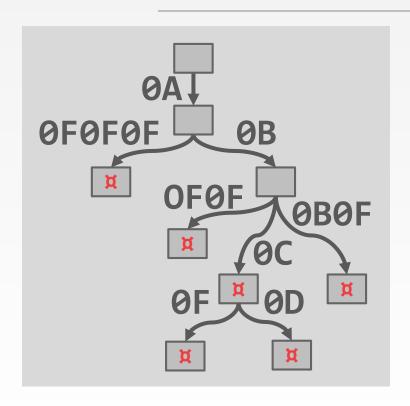
Hex Key: OA OB OC OD

OA OB OC OD Big Endian



Little Endian

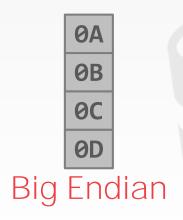




Int Key: **168496141**

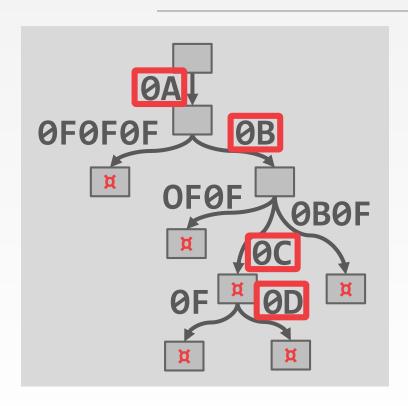


Hex Key: **0A 0B 0C 0D**





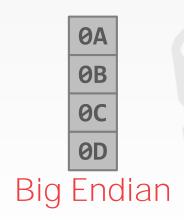




Int Key: **168496141**



Hex Key: **0A 0B 0C 0D**







IN-MEMORY TABLE INDEXES

Processor: 1 socket, 10 cores w/ 2×HT Workload: 50m Random Integer Keys (64-bit)





Source: Ziqi Wang
CMU 15-445/645 (Fall 2018)

OBSERVATION

The tree indexes that we've discussed so far are useful for "point" and "range" queries:

- \rightarrow Find all customers in the 15217 zip code.
- \rightarrow Find all orders between June 2018 and September 2018.

They are **not** good at keyword searches:

 \rightarrow Find all Wikipedia articles that contain the word "Pavlo"



WIKIPEDIA EXAMPLE

```
CREATE TABLE pages (
CREATE TABLE useracct (
  userID INT PRIMARY KEY,
                                    pageID INT PRIMARY KEY,
                                    title VARCHAR UNIQUE,
  userName VARCHAR UNIQUE,
                                    latest INT
                                   ♥ REFERENCES revisions (revID),
         CREATE TABLE revisions (
            revID INT PRIMARY KEY,
           userID INT REFERENCES useracct (userID),
           pageID INT REFERENCES pages (pageID),
           content TEXT,
           updated DATETIME
```

WIKIPEDIA EXAMPLE

If we create an index on the content attribute, what does that actually do?

CREATE INDEX idx_rev_cntnt
 ON revisions (content);

This doesn't help our query.
Our SQL is also not correct...

SELECT pageID FROM revisions
WHERE content LIKE '%Pavlo%';



INVERTED INDEX

An *inverted index* stores a mapping of words to records that contain those words in the target attribute.

- → Sometimes called a *full-text search index*.
- \rightarrow Also called a *concordance* in old (like really old) times.

The major DBMSs support these natively. There are also specialized DBMSs.





elasticsearch

QUERY TYPES

Phrase Searches

→ Find records that contain a list of words in the given order.

Proximity Searches

 \rightarrow Find records where two words occur within n words of each other.

Wildcard Searches

→ Find records that contain words that match some pattern (e.g., regular expression).



DESIGN DECISIONS

Decision #1: What To Store

- → The index needs to store at least the words contained in each record (separated by punctuation characters).
- \rightarrow Can also store frequency, position, and other meta-data.

Decision #2: When To Update

→ Maintain auxiliary data structures to "stage" updates and then update the index in batches.



CONCLUSION

B+Trees are still the way to go for tree indexes.

Inverted indexes are covered in <a>CMU 11-442.

We did not discuss geo-spatial tree indexes:

- → Examples: R-Tree, Quad-Tree, KD-Tree
- \rightarrow This is covered in CMU 15-826.



NEXT CLASS

How to make indexes thread-safe!

