# GRAVITATIONAL WAVES FROM SUPERMASSIVE BLACK HOLE COALESCENCE IN A HIERARCHICAL GALAXY FORMATION MODEL

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#### **ABSTRACT**

We investigate the expected gravitational wave emission from coalescing supermassive black hole (SMBH) binaries resulting from mergers of their host galaxies. When galaxies merge, the SMBHs in the host galaxies sink to the center of the new merged galaxy and form a binary system. We employ a semianalytic model of galaxy and quasar formation based on the hierarchical clustering scenario to estimate the amplitude of the expected stochastic gravitational wave background due to inspiraling SMBH binaries and bursts due to the SMBH binary coalescence events. We find that the characteristic strain amplitude of the background radiation is  $h_c(f) \sim 10^{-16} (f/1~\mu \text{Hz})^{-2/3}$  for  $f \leq 1~\mu \text{Hz}$  just below the detection limit from measurements of the pulsar timing provided that SMBHs coalesce simultaneously when host galaxies merge. The main contribution to the total strain amplitude of the background radiation comes from SMBH coalescence events at 0 < z < 1. We also find that a future space-based gravitational wave interferometer such as the planned *Laser Interferometer Space Antenna* might detect intense gravitational wave bursts associated with coalescence of SMBH binaries with total mass  $M_{\text{tot}} < 10^7~M_{\odot}$  at  $z \gtrsim 2$  at a rate  $\sim 1.0~\text{yr}^{-1}$ . Our model predicts that burst signals with a larger amplitude  $h_{\text{burst}} \sim 10^{-15}$  correspond to coalescence events of massive SMBH binary with total mass  $M_{\text{tot}} \sim 10^{8}~M_{\odot}$  at low redshift  $(z \lesssim 1)$  at a rate  $\sim 0.1~\text{yr}^{-1}$ , whereas those with a smaller amplitude  $(h_{\text{burst}} \sim 10^{-17})$  correspond to coalescence events of less massive SMBH binaries with total mass  $M_{\text{tot}} \sim 10^{6}~M_{\odot}$  at high redshift  $(z \gtrsim 3)$ .

Subject headings: black hole physics — galaxies: evolution — galaxies: formation — gravitational waves — quasars: general

#### 1. INTRODUCTION

In recent years there has been increasing observational evidence that many nearby galaxies have central supermassive black holes (SMBHs) in the mass range of  $10^6-10^9~M_{\odot}$  and that their physical properties correlate with those of spheroids of their host galaxies. First, the estimated mass of a SMBH in a galactic center,  $M_{\rm BH}$ , is roughly proportional to the mass of the spheroid,  $M_{\rm spher}$ . The ratio of  $M_{\rm BH}/M_{\rm spher}$  is 0.001-0.006 in each galaxy (e.g., Kormendy & Richstone 1995; Magorrian et al. 1998; Merritt & Ferrarese 2001b). Second, the mass of a SMBH correlates with the velocity dispersion of stars in the spheroid,  $\sigma_{\rm spher}$ , as  $M_{\rm BH} \propto \sigma_{\rm spher}^n$ , n=3.7-5.3 (e.g., Ferrarese & Merritt 2000; Gebhardt et al. 2000; Merritt & Ferrarese 2001a; Tremaine et al. 2002). These relations suggest that the formation of SMBHs physically links to the formation of spheroids that harbor the SMBHs.

In order to study the formation and evolution of SMBHs, it is necessary to construct a model that includes galaxy formation and merger processes. It has become widely accepted that quasars are fueled by accretion of gas onto SMBHs in the nuclei of host galaxies. Hydrodynamic simulations have shown that a merger of galaxies drives gas to fall rapidly onto the center of the merged system and fuels a nuclear starburst

leading to spheroid formation (e.g., Mihos & Hernquist 1994, 1996; Barnes & Hernquist 1996). Some observations of quasar hosts show that many quasars reside in spheroids of interacting systems or elliptical galaxies (e.g., Bahcall et al. 1997; McLure et al. 1999; Dunlop et al. 2003; Kauffmann et al. 2003). Thus the major merger of galaxies is a possible mechanism for quasar activity, SMBH evolution, and spheroid formation.

In the standard hierarchical structure formation scenario in a cold dark matter (CDM) universe, dark matter halos (dark halos) cluster gravitationally and merge. In each merged dark halo, a galaxy is formed as a result of radiative gas cooling, star formation, and supernova feedback. Several galaxies in a common dark halo sometimes merge and a more massive galaxy is assembled. When galaxies merge, SMBHs in the centers of the galaxies sink toward the center of the new merged galaxy and subsequently form a SMBH binary. If the binary loses enough energy and angular momentum, it will evolve to the gravitational wave—emitting regime and begin inspiraling, eventually coalescing with a gravitational wave burst.

An ensemble of gravitational waves from a number of inspiraling SMBH binaries at different redshifts can be observed as a stochastic background at frequencies  $\sim 1n-1~\mu Hz$ , which can be detected by pulsar timing measurements (Detweiler 1979). Gravitational wave bursts from coalescence events can be detected by a Doppler tracking test of interplanetary spacecraft (Thorne & Braginsky 1976). Future space interferometers such as the *Laser Interferometer Space Antenna* (*LISA*) might detect quasi-monochromatic wave sources associated with inspiraling SMBH binaries and gravitational wave bursts associated with SMBH binary coalescence.

In order to estimate the feasibility of detecting such gravitational waves, we need to know the SMBH coalescence rate, which depends on the complex physical processes before

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<sup>&</sup>lt;sup>5</sup> Throughout this paper, we refer to bulge or elliptical galaxies as "spheroid."

coalescence. A possible scenario of forming SMBHs consists of four stages: First, a seed massive black hole in the center of a galaxy grows to an intermediate-mass black hole (IMBH) via runaway collapse in a dense star cluster (Portegies Zwart et al. 2004). Second, a galaxy that contains an IMBH in its center merges with another galaxy with an IMBH. Third, the two IMBHs sink to the center of the gravitational potential well owing to dynamical friction until a "hardening" regime (Volonteri et al. 2003). Finally, physical processes such as three-body processes, gas dynamics, and the "Kozai" mechanism drive the binary to the gravitational wave emission regime (e.g., Begelman et al. 1980; Makino 1997; Gould & Rix 2000; Yu 2002; Armitage & Natarajan 2002; Blaes et al. 2002; Volonteri et al. 2003; Milosavljevic & Merritt 2003). However, the efficiency with which two SMBHs are brought together is still unknown.

To date, a number of attempts have been made to calculate the SMBH coalescence rate taking the physical processes in the "second" and "third" stages into account. Some authors use phenomenological models of galaxy mergers based on number counts of quasars and spheroids (e.g., Thorne & Braginsky 1976; Fukushige et al. 1992; Haehnelt 1994; Rajagopal & Romani 1995; Jaffe & Backer 2003). Others use merger rates of dark halos (not galaxies) based on the formalisms of Press & Schechter (1974) and Lacey & Cole (1993) (e.g., Haehnelt 1994; Menou et al. 2001). Volonteri et al. (2003) calculated the SMBH coalescence rate taking into account the conditions under which "subhalos" with SMBHs in a dark halo sink to the dark halo center (see also Wyithe & Loeb 2003; Sesana et al. 2004). However, none of these models include baryonic gas evolution and galaxy formation processes. Because the SMBH formation process is relevant to the spheroids of host galaxies rather than to dark halos, we need to evaluate how the baryonic gas processes such as star formation and radiative cooling affect the SMBH coalescence rate.

In this paper we estimate the SMBH coalescence rate using a new semianalytic (SA) model of Enoki et al. (2003; an extended model of Nagashima et al. 2001) in which the SMBH formation is incorporated into the galaxy formation. Then, we calculate the spectrum of gravitational wave background from inspiraling SMBH binaries, using the formulation given by Jaffe & Backer (2003), and compare our result with that from a pulsar timing measurement. We also estimate the event rate of gravitational wave bursts from SMBH coalescence events that might be detected by future planned space laser interferometers on the basis of an argument in Thorne & Braginsky (1976).

In SA models, the merging histories of dark halos are realized using a Monte Carlo algorithm, and evolution of baryonic components within the dark halos is calculated using simple analytic models for gas cooling, star formation, supernova feedback, galaxy merging, and other processes. SA models have successfully reproduced a variety of observed features of galaxies, such as their luminosity functions, color distributions, and so on (e.g., Kauffmann et al. 1993; Cole et al. 1994, 2000; Somerville & Primack 1999; Nagashima et al. 2001, 2002). Kauffmann & Haehnelt (2000) introduced a unified model that includes the formation of both galaxies and SMBHs within the framework of their SA model (see also Cattaneo 2001; Menci et al. 2003; Islam et al. 2003; Granato et al. 2004). Our SA model reproduces not only these observational features but also the observed present black hole mass function and the quasar luminosity functions at different redshifts (Enoki et al. 2003).

The paper is organized as follows: in  $\S$  2 we briefly review our SA model for galaxy formation and SMBH growth; in  $\S$  3 we calculate the spectrum of gravitational wave background and the event rate of gravitational wave bursts; and in  $\S$  4 we provide summary and conclusions.

# 2. GALAXY MERGER/BLACK HOLE COALESCENCE RATE

In this section we briefly describe our SA model of galaxy formation and SMBH growth. Details are given in Nagashima et al. (2001) and Enoki et al. (2003).

## 2.1. Model of Galaxy Formation

First, we construct Monte Carlo realizations of the merging histories of dark halos from the present to higher redshifts using the method of Somerville & Kolatt (1999), which is based on the extended Press-Schechter formalism (Press & Schechter 1974; Bond et al. 1991; Bower 1991; Lacey & Cole 1993). The merger histories of dark halos depend on the cosmological model. The adopted cosmological model is a low-density, spatially flat cold dark matter (ACDM) universe with the present density parameter  $\Omega_m = 0.3$ , the cosmological constant  $\Omega_{\Lambda} = 0.7$ , the Hubble constant h = 0.7 ( $h \equiv H_0/100$  km s<sup>-1</sup> Mpc<sup>-1</sup>), and the present rms density fluctuation in spheres of  $8 h^{-1}$  Mpc radius  $\sigma_8 = 0.9$ . Dark halos with circular velocity  $V_{\rm circ} < 40 \, {\rm km \ s^{-1}}$  are treated as diffuse accretion matter. This condition comes from an estimation of the Jeans mass in the ultraviolet background radiation field (e.g., Thoul & Weinberg 1996). The adopted time step of the merging histories of dark halos is a redshift interval of  $\Delta z = 0.06(1+z)$ , corresponding to dynamical timescale of dark halos that collapse at redshift z. The highest redshift in each merging path, which depends on the present dark halo mass, is about  $z \sim 20-30$ .

Next, for each merging path of dark halos, we calculate the evolution of the baryonic component from higher redshifts to the present. If a dark halo has no progenitor halos, the mass fraction of the gas in the halo is given by  $\Omega_b/\Omega_m$ , where  $\Omega_b$  is the baryonic density parameter. Here we use  $\Omega_b = 0.02 \ h^{-2}$ . When a dark halo collapses, the gas in the halo is shockheated to the virial temperature of the halo (the hot gas). At the same time, the gas in dense regions of the halo cools owing to efficient radiative cooling, sinks to the center of the halo, and settles into a rotationally supported disk until the subsequent collapse of the dark halo. We call this cooled gas the "cold gas." Stars are formed from the cold gas at a rate of  $\dot{M}_* = M_{\rm cold}/\tau_*$ , where  $M_{\rm cold}$  is the mass of the cold gas and  $\tau_*$  is the timescale of star formation. We assume  $\tau_* = \tau_*^0 (V_{\rm circ}/300~{\rm km~s^{-1}})^{\alpha_*}$ . The free parameters  $\tau_*^0$  and  $\alpha_*$  are chosen to match the observed mass fraction of cold gas in the disks of spiral galaxies. With star formation, supernovae occur and heat up the surrounding cold gas to the hot gas phase (supernova feedback). The reheating rate is given by  $\dot{M}_{\rm reheat} = \beta(V_{\rm circ})\dot{M}_{*}$ , where  $\beta(V_{\rm circ}) = (V_{\rm hot}/V_{\rm circ})^{\alpha_{\rm hot}}$ . The free parameters of  $V_{\mathrm{hot}}$  and  $\alpha_{\mathrm{hot}}$  are determined by matching the observed local luminosity function of the galaxies. Given the star formation rate as a function of time, we calculate the luminosity and color of each galaxy from the star formation history of the galaxy by using a stellar population synthesis model. We use the population synthesis code by Kodama & Arimoto (1997).

When several progenitor halos merge, a newly formed larger dark halo contains at least two or more galaxies that originally resided in the individual progenitor halos. We identify the central galaxy in the new common halo with the central galaxy contained in the most massive progenitor halos. Note that cooled hot gas accretes only to central galaxies. Other galaxies are regarded as satellite galaxies. These galaxies merge by either dynamical friction or random collision. Satellite galaxies merge with the central galaxy owing to dynamical friction in the following timescale:

$$\tau_{\rm fric} = \frac{260}{\ln \Lambda_{\rm C}} \left(\frac{R_H}{\rm Mpc}\right)^2 \left(\frac{V_{\rm circ}}{10^3 \text{ km s}^{-1}}\right) \left(\frac{M_{\rm sat}}{10^{12} M_{\odot}}\right)^{-1} \text{Gyr}, \quad (1)$$

where  $R_H$  and  $V_{\rm circ}$  are the radius and the circular velocity of the new common halo, respectively,  $\ln \Lambda_{\rm C}$  is the Coulomb logarithm, and  $M_{\rm sat}$  is the mass of the satellite galaxy, including its dark halo (Binney & Tremaine 1987). When the time passing after a galaxy became a satellite exceeds  $\tau_{\rm fric}$ , the satellite galaxy infalls onto the central galaxy. On the other hand, satellite galaxies merge with each other in the timescale of random collision. Under the condition that the satellite galaxies become gravitationally bound and merge during encounters, the collision timescale is (Makino & Hut 1997)

$$\tau_{\text{coll}} = \frac{500}{N^2} \left(\frac{R_H}{\text{Mpc}}\right)^3 \left(\frac{r_{\text{gal}}}{0.12 \text{ Mpc}}\right)^{-2} \times \left(\frac{\sigma_{\text{gal}}}{100 \text{ km s}^{-1}}\right)^{-4} \left(\frac{\sigma_{\text{halo}}}{300 \text{ km s}^{-1}}\right)^3 \text{Gyr}, \quad (2)$$

where N is the number of satellite galaxies,  $r_{\rm gal}$  is a radius of a satellite, and  $\sigma_{halo}$  and  $\sigma_{gal}$  are the one-dimensional velocity dispersions of the common halo and the satellite galaxy, respectively. With a probability of  $\Delta t/\tau_{\rm coll}$ , where  $\Delta t$  is the time step corresponding to the redshift interval  $\Delta z$ , a satellite galaxy merges with another randomly picked satellite. Let us consider the case in which two galaxies of masses  $m_1$  and  $m_2(>m_1)$  merge. If the mass ratio,  $f=m_1/m_2$ , is larger than a certain critical value of  $f_{\text{bulge}}$  (major merger), we assume that a starburst occurs: all of the cold gas turns into stars and hot gas that fills the dark halo, and all of the stars populate the bulge of a new galaxy. On the other hand, if  $f < f_{\text{bulge}}$  (minor merger), no starburst occurs and a smaller galaxy is simply absorbed into the disk of a larger galaxy. These processes are repeated until the output redshift. We classify galaxies into different morphological types according to the B-band bulgeto-disk luminosity ratio, B/D. In this paper, galaxies with  $B/D > \frac{2}{3}$ , and  $B/D \le \frac{2}{3}$  are classified as elliptical/S0 and spiral galaxies, respectively. The parameter  $f_{\text{bulge}}$  is fixed by a comparison with the observed type mix.

Model parameters are determined by a comparison with observations of galaxies in the local universe, such as luminosity functions and the cold gas mass fraction in spiral galaxies. Our SA model can reproduce the galaxy number counts and photometric redshift distribution of galaxies in the Hubble Deep Field. The adopted parameters of this model are tabulated in Table 1. Some of the model parameters ( $\sigma_8$ ,  $\Omega_b$ , and fraction of invisible stellar mass  $\Upsilon$ ) are updated and slightly different from our previous paper (Nagashima et al. 2001; Enoki et al. 2003). The update of  $\sigma_8$  and  $\Omega_b$  causes only a slight change of  $\Upsilon$ , and we have confirmed that the modification hardly affects our results. Using this SA model, we can estimate the galaxy merger rate at each redshift.

TABLE 1
MODEL PARAMETERS

Parameter	Value
Cosmological	
$\Omega_m$	0.3
$\Omega_{\Lambda}$	0.7
h	0.7
$\sigma_8$	0.9
$\Omega_b (h^{-2})$	0.02
Astrophysical	
V <sub>hot</sub> (km s <sup>-1</sup> )	280
$\alpha_{ m hot}$	2.5
$\tau^0_*$ (Gyr)	1.5
$\alpha_*$	-2
$f_{\text{bulge}}$	0.5
Υ	1.7

## 2.2. The Growth of SMBH

Let us briefly summarize the growth model of SMBHs introduced by Enoki et al. (2003). In this model, it is assumed that SMBHs grow by coalescence when their host galaxies merge and are fueled by accreted cold gas during major mergers of galaxies. When the host galaxies merge, preexisting SMBHs sink to the center of the new merged galaxy as a result of dynamical friction (or other mechanisms such as gas dynamics), evolve to the gravitational wave emission regime, and eventually coalesce. Although the timescale for this process is unknown, for the sake of simplicity we assume that SMBHs instantaneously evolve to the gravitational wave emission regime and coalesce. Gasdynamical simulations have demonstrated that the major merger of galaxies can drive substantial gaseous inflows and trigger starburst activity (e.g., Mihos & Hernquist 1994, 1996; Barnes & Hernquist 1996). Thus, it is reasonable to assume that during a major merger of galaxies, a certain fraction of the cold gas that is proportional to the total mass of stars newly formed at starburst accretes onto the newly formed SMBH and this accretion process leads to a quasar activity. Under this assumption, the mass of cold gas accreted on a SMBH is given by

$$M_{\rm acc} = f_{\rm BH} \Delta M_{*, \rm burst},$$
 (3)

where  $f_{\rm BH}$  is a constant and  $\Delta M_{*,\,\rm burst}$  is the total mass of stars formed at starburst. The free parameter  $f_{\rm BH}$  is fixed by matching the observed relation between a spheroid mass and a black hole mass  $M_{\rm BH}/M_{\rm spher}=0.001-0.006$  (e.g., Magorrian et al. 1998); we find that the favorable value of  $f_{\rm BH}$  is nearly 0.03.

Figure 1 shows the model prediction of the growth rate of the averaged SMBH mass,  $\langle \dot{M}_{\rm BH} \rangle$ . We define the averaged SMBH mass growth rate as

$$\langle \dot{M}_{\rm BH} \rangle = \frac{\int \dot{M}_{\rm BH} \phi_{\rm BH}(M_{\rm BH}, z) \, dM_{\rm BH}}{\int \phi_{\rm BH}(M_{\rm BH}, z) \, dM_{\rm BH}}, \tag{4}$$

where  $\dot{M}_{\rm BH}$  is the mass increase rate of SMBH with  $M_{\rm BH}$  at z and  $\phi_{\rm BH}(M_{\rm BH},z)$  is the black hole mass function.  $\dot{M}_{\rm BH}$  is given by  $\dot{M}_{\rm BH} = (M_{\rm acc} + M_{\rm coal})/\Delta t$ , where  $M_{\rm coal}$  is the mass increment due to the SMBH binaries' coalescence (the mass of the

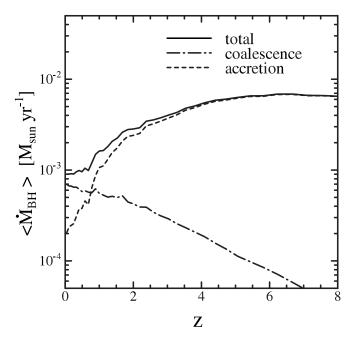


Fig. 1.—Averaged SMBH mass growth rate,  $\langle \dot{M}_{BH} \rangle$ , of the model. The solid, dot-dashed, and short dashed lines indicate the SMBH mass growth rate due to the total SMBH coalescence, and gas accretion, respectively.

smaller SMBH). This figure shows that the SMBH mass growth is mostly due to gas accretion and does not depend on the initial seed masses. At lower redshift ( $z \le 1$ ), since the cold gas is depleted by star formation, the SMBH coalescence becomes a dominant process of the SMBH mass growth.

Figure 2a shows the black hole mass functions in our model at a series of various redshifts. This indicates that the number density of the most massive black holes increases monotonically with time in our scenario in which SMBHs grow by an accretion of cold gas and by coalescence. In this figure, we superpose the black hole mass function at z=0 obtained by Salucci et al. (1999). The present mass function in our model is quite consistent with the observation. Our galaxy formation model includes dynamical friction and random collision as

galaxy merging mechanisms. For comparison, in Figure 2b we also plot the black hole mass functions at z = 0 of two other models: a no random collision model (no-rc model) and a no dynamical friction model (no-df model). In the no-rc and no-df models, mergers due to random collision and dynamical friction, respectively, are switched off. This figure shows that the mass functions for low-mass black holes are determined by random collisions between satellite galaxies and those for high-mass black holes are influenced by dynamical friction. The shape of the black hole mass function depends on detailed gas processes. The important contribution of mass increment of SMBHs in central galaxies is the cold gas, which is accreted only to central galaxies. Supernova feedback removes this cold gas more efficiently in smaller galaxies with  $V_{\rm circ} < V_{\rm hot} = 280~{\rm km~s^{-1}}~(M_{\rm gal} < 10^{12}~M_{\odot})$ . Thus, the growth of the SMBHs in small central galaxies suffers from supernova feedback. In the no-rc model, SMBHs mainly exist central galaxies. Therefore, the shape of the black hole mass function in the no-rc model has a bump at the high-mass end  $(M_{\rm BH} \sim 10^9~M_{\odot})$  that corresponds to SMBHs in the central galaxies  $(M_{\rm gal} \sim 10^{12}~M_{\odot})$ . On the other hand, in the no-df model, high-mass SMBHs cannot be produced since galaxies cannot merge with the massive central galaxy.

Enoki et al. (2003) investigated the environments and clustering properties of quasars using this SA model, which can also reproduce quasar luminosity functions at different redshifts. While our approach is similar to that of Kauffmann & Haehnelt (2000), their star formation and feedback models are different from ours, and their model does not include the random collision process. Therefore, their resultant model description differs from ours in equation (3). Using the SA model incorporated with this SMBH growth model, we estimate the comoving number density,  $n_c(M_1, M_2, z) dM_1 dM_2 dz$ , of the coalescing SMBH binaries with mass  $M_1 \sim M_1 + dM_1$  and  $M_2 \sim M_2 + dM_2$  at z in a given redshift interval dz.

It is difficult to know how SMBH binaries manage to shrink to a gravitational wave emission regime after their host galaxies merge, because not all physical processes and conditions related to this problem (dynamical friction, stellar distribution, triplet SMBH interaction, gas dynamical effects, and so on) are yet clear. Nevertheless, many authors have tackled this

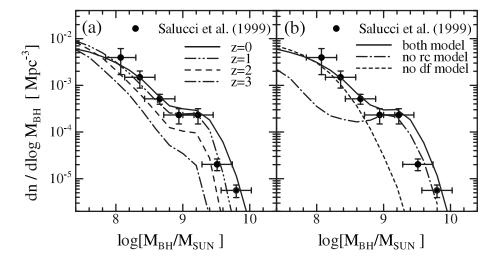


Fig. 2.—(a) Black hole mass function of the model at a series of redshifts. The solid, double-dot-dashed, and dot-dashed lines indicate the results at z = 0, 1, 2, and 3, respectively. The symbols with error bars are the present black hole mass function obtained by Salucci et al. (1999). (b) Black hole mass function of models for three models at z = 0. The solid, dot-dashed, and short-dashed lines indicate the "both," no-rc, and no-df models), respectively. The "both model" includes dynamical friction and random collision as the galaxy merging mechanisms.

problem (e.g., Begelman et al. 1980; Makino 1997; Gould & Rix 2000; Yu 2002; Armitage & Natarajan 2002; Blaes et al. 2002; Milosavljevic & Merritt 2003). In what follows, for simplicity we assume that SMBHs coalesce simultaneously when host galaxies merge. In other words, the efficiency of SMBH coalescence is assumed to be maximum. Note that Volonteri et al. (2003) constructed a SMBH growth model in which the merging history of dark halos with SMBHs in their center is derived from cosmological Monte Carlo simulations. Although they incorporated the dynamical evolution of SMBH binaries and triplet SMBH interactions into their model, no galaxy formation process is taken into account.

#### 3. GRAVITATIONAL RADIATION

# 3.1. Background Radiation from SMBH Binaries

In order to calculate the spectrum of gravitational wave background radiation from SMBH binaries, it is necessary to follow the orbit evolution of each binary. However, it is difficult to set initial conditions. To avoid this problem, we adopt a formulation by Jaffe & Backer (2003; see also Rajagopal & Romani 1995).

We start by calculating the expected amplitude of gravitational radiation emitted by a binary. We assume that a binary orbit is circular for simplicity.<sup>6</sup> The amplitude is given by (Thorne 1987)

$$h_{s}(z, f, M_{1}, M_{2}) = 4\sqrt{\frac{2}{5}} \frac{\left(GM_{\text{chirp}}\right)^{5/3}}{c^{4}D(z)} \left(2\pi f_{p}\right)^{2/3}$$

$$= 3.5 \times 10^{-17} \left(\frac{M_{\text{chirp}}}{10^{8} M_{\odot}}\right)^{5/3}$$

$$\times \left[\frac{D(z)}{1 \text{ Gpc}}\right]^{-1} \left[\frac{f(1+z)}{10^{-7} \text{ Hz}}\right]^{2/3}, \quad (5)$$

where  $M_{\rm chirp} = [M_1 M_2 (M_1 + M_2)^{-1/3}]^{3/5}$  is the chirp mass of the system and c is the speed of light;  $f_p$  is the reciprocal of the proper rest-frame period of the binary, which is related to the observed frequency, f, of the gravitational wave from the binary in a circular orbit as  $f = 2f_p/(1+z)$ . D(z) is the comoving distance to the binary

$$D(z) = \frac{c}{H_0} \int_0^z \frac{dz'}{\sqrt{\Omega_{\rm m}(1+z')^3 + \Omega_{\Lambda}}}.$$
 (6)

Next we calculate  $\nu(M_1, M_2, z) dM_1 dM_2 dz$ , the number of coalescing SMBH binaries with mass  $M_1$  and  $M_2$  in mass intervals  $dM_1$  and  $dM_2$  per observers' time occurring at z in a given redshift interval dz,

$$\nu(M_1, M_2, z) = \frac{dV}{dt_0} n_c(M_1, M_2, z)$$

$$= \frac{1}{(1+z)} \frac{dV}{dt_p} n_c(M_1, M_2, z), \tag{7}$$

<sup>6</sup> Note that the initial orbit of a binary is not necessarily circular. Since the amplitude and timescale of gravitational wave emissions are sensitive to eccentricity of a binary orbit (Peters & Matthews 1963), the initial distribution of eccentricity affects the final expected amplitudes. However, we assume that the orbit becomes circular immediately.

where  $t_0$  is the observers' time,  $t_p$  is the proper rest-frame time at z, and dV is the comoving volume element at  $z \sim z + dz$  given by

$$\frac{dV}{dt_p} = 4\pi (1+z)cD(z)^2. \tag{8}$$

The timescale of the emitting gravitational waves of a binary measured in the rest-frame is

$$\tau_{\rm GW} \equiv f_p \frac{dt_p}{df_p}.$$
 (9)

Since the timescale in the observer frame is  $\tau_{\rm GW,obs} = \tau_{\rm GW}(1+z)$ , for a binary in a circular orbit at redshift z, it is expressed as (Peters & Matthews 1963)

$$\tau_{\text{GW, obs}}(M_1, M_2, z, f) = \frac{5}{96} \left(\frac{c^3}{GM_{\text{chirp}}}\right)^{5/3} (2\pi f_p)^{-8/3} (1+z)$$

$$= 1.2 \times 10^4 \left(\frac{M_{\text{chirp}}}{10^8 M_{\odot}}\right)^{-5/3}$$

$$\times \left(\frac{f}{10^{-7} \text{ Hz}}\right)^{-8/3} (1+z)^{-5/3} \text{ yr.} \quad (10)$$

As a SMBH binary evolves with time, the frequency becomes higher. We assume that the binary orbit is quasi-stationary (i.e., the phase-evolution timescale is less than  $\tau_{\rm GW}$ ) until the radius equals  $3R_{\rm S}$ , where  $R_{\rm S}$  is the Schwarzschild radius: the radius of the innermost stable circular orbit (ISCO) for a particle and a nonrotating black hole. Then the maximum frequency  $f_{\rm max}$  is

$$f_{\text{max}}(M_1, M_2, z) = \frac{c^3}{6^{3/2} \pi G M_1 (1+z)} \left(1 + \frac{M_2}{M_1}\right)^{1/2}$$
$$= 4.4 \times 10^{-5} (1+z)^{-1}$$
$$\times \left(\frac{M_1}{10^8 M_{\odot}}\right)^{-1} \left(1 + \frac{M_2}{M_1}\right)^{1/2} \text{ Hz}, \quad (11)$$

where  $M_1$  and  $M_2$  are SMBH masses ( $M_1 > M_2$ ). The number of coalescencing SMBH binaries as a source of gravitational wave source with observed frequency f at redshift z is estimated as

$$\nu(M_1, M_2, z) dz dM_1 dM_2 \tau_{\text{GW, obs}} \theta(f_{\text{max}} - f),$$
 (12)

where  $\theta(x)$  is the step function. Therefore, from equations (5), (7), (10), and (13), we finally obtain the spectrum of the gravitational wave background radiation,

$$h_c^2(f) = \int dz \, dM_1 \, dM_2 \, h_s^2 \nu$$

$$\times (M_1, M_2, z) \tau_{\text{GW, obs}} \theta(f_{\text{max}} - f)$$

$$= \int dz \, dM_1 \, dM_2 \, \frac{4\pi c^3}{3} \left(\frac{GM_{\text{chirp}}}{c^3}\right)^{5/3}$$

$$\times (\pi f)^{-4/3} (1 + z)^{-1/3} n_c(M_1, M_2, z) \theta(f_{\text{max}} - f). \quad (13)$$

We note that equation (13) agrees with the result of Phinney (2001) except for the step function,  $\theta(f_{\text{max}} - f)$ . The original

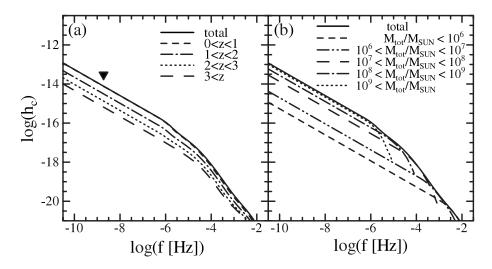


Fig. 3.—Spectrum of gravitational wave background radiation,  $h_c(f)$ , from SMBH binaries in (a) different redshift intervals and (b) in different total mass ranges. (a) The total spectrum (solid line) and the other lines show those in different redshift intervals  $0 \le z < 1$  (dashed line),  $1 \le z < 2$  (dot-dashed line),  $2 \le z < 3$  (short-dashed line), and  $3 \le z$  (long-dashed line). The filled triangle shows the current limit from pulsar timing measurements Lommen (2002). (b) The total spectrum (solid line) and the other lines show those in different total mass intervals  $M_{\text{tot}} \le 10^6 \ M_{\odot}$  (dashed line),  $10^6 M_{\odot} < M_{\text{tot}} \le 10^7 \ M_{\odot}$  (dot-dot-dashed line),  $10^7 \ M_{\odot} < M_{\text{tot}} \le 10^8 \ M_{\odot}$  (long-dashed line),  $10^8 \ M_{\odot} < M_{\text{tot}} \le 10^9 \ M_{\odot}$  (dot-dashed line), and  $10^9 \ M_{\odot} < M_{\text{tot}}$  (short-dashed line).

formulation of Jaffe & Backer (2003) does not include this effect either.

As shown in Figure 3, the spectrum changes its slope at  $f \sim 1~\mu \rm Hz$  owing to lack of power associated with the upper limit frequency,  $f_{\rm max}$ . This feature is consistent with the results of Wyithe & Loeb (2003) and Sesana et al. (2004). The predicted strain spectrum is  $h_c(f) \sim 10^{-16} (f/1~\mu \rm Hz)^{-2/3}$  for  $f \lesssim 1~\mu \rm Hz$ , just below the current limit from the pulsar timing measurements by Lommen (2002). In our model, we assume that SMBHs coalesce simultaneously when their host galaxies merge. Therefore, the efficiency of SMBH coalescence is maximum and the predicted amplitude of gravitational wave spectrum should be interpreted as the upper limit.

In Figure 3a we plot the spectra from binaries in different redshift intervals. This figure shows that the total spectrum of background radiation comes from coalescing SMBH binaries at low redshift,  $0 \le z < 1$ . In Figure 4 we plot the SMBH coalescence rate in observers' time unit a year,  $\nu(z) =$  $\int \nu(M_1, M_2, z) dM_1 dM_2$ . This figure indicates that the coalescence rate at low redshift is lower than the coalescence rate at high redshift. However, the main contribution to the background radiation is gravitational wave from the coalescing SMBH binaries at low redshift,  $0 \le z \le 1$ , because the distance from an observer to the SMBH binaries at low redshift is shorter and the mass of SMBHs at low redshift is higher. In Figure 3b we also plot the spectra from binaries in different total mass intervals ( $M_{\text{tot}} = M_1 + M_2$ ). This figure shows that for  $f \gtrsim 10^{-4}$  Hz the total spectrum of background radiation comes from coalescing SMBH binaries with total mass  $M_{\rm tot} \lesssim 10^8 \ M_{\odot}$ .

When SMBHs are spinning and/or when their masses are comparable, the definition of ISCO becomes vague and our assumption that the cutoff frequency  $f_{\rm max}$  corresponds to  $3R_{\rm S}$  may not be correct. To see the effects of the cutoff frequency, we plot the spectra for different values of  $f_{\rm max}$ , corresponding to  $3R_{\rm S}$ ,  $30R_{\rm S}$ , and no frequency cutoff, respectively (Fig. 5a). Lowering  $f_{\rm max}$  causes a suppression in the stochastic background at high frequencies ( $f \lesssim 10^{-7}$  Hz) since a large portion of high-frequency modes are cut off. As shown in this figure,

the cutoff radius does not affect the amplitude at the frequency of the pulsar timing measurement  $f \simeq 10^{-9}$  Hz.

Our galaxy formation model incorporates dynamical friction and random collision as galaxy merging mechanisms. In order to examine the effect of these two galaxy merger mechanisms on the spectrum of gravitational wave background radiation, in Figure 5b we also plot the spectrum of background radiation of the no-rc and no-df models. The no-df model cannot produce higher mass SMBH (see Fig. 2b). Consequently, the spectrum in the no-df model bends at larger frequency since the number of SMBHs with smaller  $f_{\rm max}$  decreases. Furthermore, in the no-df model, the amplitude of gravitational waves from each binary becomes smaller.

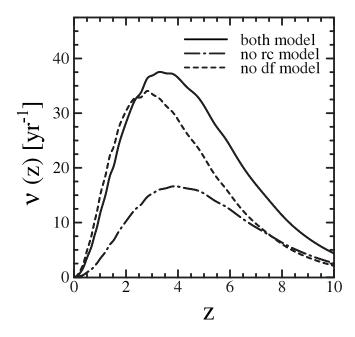


Fig. 4.—SMBH coalescence rate in observers' time unit 1 yr,  $\nu(z)$ . The solid, dot-dashed, and short-dashed lines indicate the "both," no-rc, and no-df model, respectively. The "both" model includes dynamical friction and random collision as the galaxy merging mechanisms.

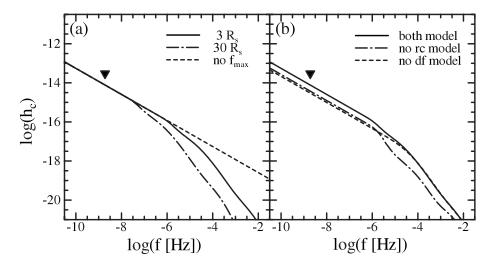


Fig. 5.—Spectrum of gravitational wave background radiation,  $h_c(f)$ , in (a) different  $f_{\text{max}}$  and (b) different galaxy merger models. The filled triangles show the current limit from pulsar timing measurements (Lommen 2002). (a) The solid, dot-dashed, and short-dashed lines indicate the results with  $f_{\text{max}}$  corresponding to  $3R_{\text{S}}$ ,  $30R_{\text{S}}$ , and no frequency cutoff, respectively. (b) The solid, dot-dashed, and short-dashed lines indicate the "both," no-rc, and the no-df models, respectively. The "both" model includes dynamical friction and random collision as the galaxy merging mechanisms.

However, the coalescence rate in the no-df model is higher than the rate in the no-rc model as shown in Figure 4. As a result, the amplitude of the spectrum in the no-df model is roughly equal to the amplitude in the no-rc model.

# 3.2. Gravitational Wave Burst from SMBH Coalescence

After an inspiraling phase, SMBHs plunge into a final death inspiral and merge to form a single black hole. We call a set of a plunge and a subsequent early nonlinear ring-down phase a "burst." In this subsection, we estimate the expected burst event rate per observers' time using the amplitude of burst gravitational waves given by Thorne & Braginsky (1976) and the SMBH coalescence rate calculated by our SA model,  $n_c(M_1, M_2, z)$ .

The gravitational wave amplitude is given by

$$h^2 = \frac{2GF_{\rm GW}}{\pi c^3 f_{\rm c}^2},\tag{14}$$

where  $F_{\rm GW}$  is the energy flux of the gravitational wave at the observer and  $f_c$  is the observed characteristic frequency;  $f_c$  from the gravitational wave burst occurring at z is

$$f_{\rm c} = \frac{c^3}{3^{3/2} G M_{\rm tot} (1+z)}$$
$$= 3.9 \times 10^{-4} \left(\frac{M_{\rm tot}}{10^8 M_{\odot}}\right)^{-1} (1+z)^{-1} \text{ Hz}, \qquad (15)$$

where  $M_{\text{tot}}$  is total mass of the black holes. The energy flux from the burst gravitational wave occurring at z is given by

$$F_{\rm GW} = \frac{\epsilon M_{\rm tot} c^2 f_{\rm c}}{4\pi D(z)^2 (1+z)},\tag{16}$$

where  $\epsilon$  is the efficiency of the energy release and D(z) is the distance to the source from the observer given by equation (6).

From equations (14), (15), and (16), the characteristic amplitude of the burst gravitational wave is

$$h_{\text{burst}} = \frac{3^{3/4} \epsilon^{1/2} G M_{\text{tot}}}{2^{1/2} \pi c^2 D(z)}$$
$$= 7.8 \times 10^{-16} \left(\frac{\epsilon}{0.1}\right)^{1/2} \left(\frac{M_{\text{tot}}}{10^8 M_{\odot}}\right) \left[\frac{D(z)}{1 \text{ Gpc}}\right]^{-1}. \tag{17}$$

Equations (15) and (17) show that we can estimate the amplitude and the characteristic frequency of the burst gravitational wave once we know the total mass and redshift of coalescing SMBHs. From equations (15) and (17) and  $n_c(M_1, M_2, z)$ , we obtain  $n_{\text{burst}}(h_{\text{burst}}, f_c, z) dh_{\text{burst}} df_c dz$ , which is the comoving number density of gravitational wave burst events occurring at z in a given redshift interval dz with amplitude  $h_{\text{burst}} \sim h_{\text{burst}} + dh_{\text{burst}}$  and with characteristic frequency  $f_c \sim f_c + df_c$ . Then the expected event rates of gravitational wave bursts per observers' time with amplitude  $h_{\text{burst}} \sim h_{\text{burst}} + dh_{\text{burst}}$  and characteristic frequency  $f_c \sim f_c + df_c$ ,  $\nu_{\text{burst}}(h_{\text{burst}}, f_c) dh_{\text{burst}} df_c$  is given by

$$\nu_{\text{burst}}(h_{\text{burst}}, f_c) = \int n_{\text{burst}}(h_{\text{burst}}, f_c, z) \frac{dV}{dt_0} dz.$$
 (18)

The integrated event rates of gravitational wave bursts per observers' time with amplitude  $h_{\rm burst} \sim h_{\rm burst} + dh_{\rm burst}$ ,  $\nu_{\rm burst}$  ( $h_{\rm burst}$ )  $dh_{\rm burst}$ , are given, respectively, as follows:

$$\nu_{\text{burst}}(h_{\text{burst}}) = \int \nu_{\text{burst}}(h_{\text{burst}}, f_c) df_c.$$
 (19)

In Figure 6 we plot the total integrated event rates of gravitational wave bursts and integrated event rates in different redshift intervals (Fig. 6a) and in different total mass intervals in (Fig. 6b). Here we set the efficiency of the energy release  $\epsilon = 0.1$ , while the precise value of this parameter is unknown. Flanagan & Hughes (1998) argued that the efficiency could reach 10%, which depends on alignments of spin and parameter choices. In most typical events, a conversion efficiency will probably be a few percent (Baker et al. 2001). From equation (17) one can see that the change of efficiency

<sup>&</sup>lt;sup>7</sup> The later ring-down phase at the linear perturbation regime is not included.

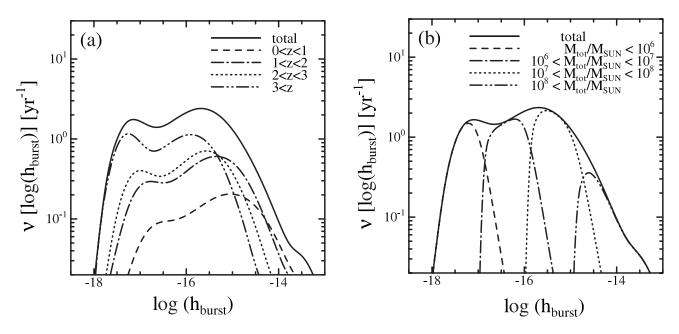


Fig. 6.—Integrated event rate of gravitational wave burst per observers' time unit 1 yr  $\nu_{\rm burst}[\log{(h_{\rm burst})}]$ . (a) The solid line shows the total integrated event rate, and the other lines show those in redshift of intervals  $0 \le z < 1$  (dotted line),  $1 \le z < 2$  (dot-dashed line),  $2 \le z < 3$  (short-dashed line), and  $3 \le z$  (double-dot-dashed line). (b) The solid line shows the total integrated event rate, and the other lines show those in different black hole mass intervals of  $M_{\rm tot} \le 10^6 \ M_{\odot}$  (dashed line),  $10^6 \ M_{\odot} < M_{\rm tot} \le 10^7 \ M_{\odot}$  (dot-dashed line),  $10^7 \ M_{\odot} < M_{\rm tot} \le 10^8 \ M_{\odot}$  (dotted line), and  $10^8 \ M_{\odot} < M_{\rm tot}$  (dot-dashed line).

results in the parallel displacement in the horizontal direction in Figure 6. The shape of  $\nu_{\rm burst}(h_{\rm burst})$  reflects the black hole mass functions and the SMBH coalescence rates, which depend on the complex galaxy formation processes. In Figure 6a one can notice that there are two peaks in the event rate in terms of  $h_{\rm burst}$ . A peak at  $h_{\rm burst}\sim 10^{-17}$  corresponds to bursts from SMBH binaries with  $M_{\rm tot}<10^6~M_{\odot}$  whose total number is the largest at high redshift (z>3). Another peak at  $h_{\rm burst}\sim 10^{-15}$  corresponds to bursts from SMBH binaries with  $10^7~M_{\odot} < M_{\rm tot} < 10^8~M_{\odot}$  whose coalescence probability is the largest at high redshift (z>3). Figure 6b indicates that burst signals with large amplitude ( $h_{\rm burst}\gtrsim 10^{-15}$ ) correspond to coalescence of "massive" SMBH binaries with  $M_{\rm tot}\gtrsim 10^8~M_{\odot}$  occurring at  $z\lesssim 1$ . This is because the distance from the earth

to SMBHs at low redshift is shorter and the mass of SMBHs at low redshift is larger. On the other hand, burst signals with amplitude ( $h_{\rm burst} \gtrsim 10^{-15}$ ) correspond to coalescence events of "less massive" SMBH binaries with  $M_{\rm tot} \lesssim 10^7~M_{\odot}$  occurring at  $z \gtrsim 2$ . These events dominate the expected burst event rate provided that the sensitivity of the detector is sufficiently good. This feature is quite important because it breaks the degeneracy between mass and distance. Our model predicts that the expected rates of the coalescence events due to SMBH binaries with small mass  $M_{\rm tot} < 10^6~M_{\odot}$  at low redshift and those with large mass  $M_{\rm tot} > 10^8~M_{\odot}$  at high redshift (z > 3) are small

Figure 7 shows that the expected region for signal of gravitational wave bursts and the instrumental noise threshold

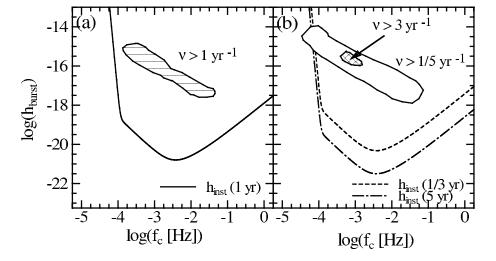


Fig. 7.—Expected signals of gravitational burst from SMBH. (a) The horizontally hatched area shows the region,  $\nu_{\text{burst}}[\log{(h_{\text{burst}})}, \log{(f_c)}] > 1\text{yr}^{-1}$ . The solid curve indicates the instrumental noise threshold for 1 yr of *LISA* observations. (b) The vertically hatched area shows the region,  $\nu_{\text{burst}}[\log{(h_{\text{burst}})}, \log{(f_c)}] > 1/5 \text{ yr}^{-1}$  and the diagonal cross-hatched area show the region,  $\nu_{\text{burst}}[\log{(h_{\text{burst}})}, \log{(f_c)}] > 3 \text{ yr}^{-1}$ . The dot-dashed and the short-dashed lines indicates the instrumental noise threshold for 5 yr and  $\frac{1}{3}$  yr of *LISA* observations, respectively.

for LISA,  $h_{\rm inst}$ . For randomly oriented sources, a sensitivity for a search of gravitational wave bursts in an observation time  $T_{\rm obs}$  is given by (Thorne 1987; Haehnelt 1994)

$$h_{\rm inst}^2 \sim \left(\frac{T_{\rm obs}}{1 \text{ yr}}\right)^{-1} 10 S_h f_c,$$
 (20)

where  $S_h$  is the spectral instrumental noise density. We compute  $h_{\rm inst}$  from the fitting formula for  $S_h$  of LISA (Hughes 2002). The expected region for  $\nu_{\rm burst}[\log{(h_{\rm burst})}, \log{(f_c)}] > 1$  yr<sup>-1</sup> is above this instrumental noise threshold. For comparison, we show the region for  $\nu_{\rm burst}[\log{(h_{\rm burst})}, \log{(f_c)}] > 1/5$  yr<sup>-1</sup> and  $\nu_{\rm burst}[\log{(h_{\rm burst})}, \log{(f_c)}] > 3$  yr<sup>-1</sup> in Figure 7b.

From Figures 6 and 7, we conclude that *LISA* can detect intense bursts of gravitational waves at a rate of  $\sim 1.0 \text{ yr}^{-1}$  assuming that the dominant part of these burst events occur at  $z \gtrsim 2$ . Even in the case of  $\epsilon = 0.001$ , *LISA* can detect intense bursts of gravitational waves in 1 yr of observation, since  $h_{\text{burst}} \propto \epsilon^{1/2}$ . In addition, we find that large-amplitude  $(h_{\text{burst}} \sim 10^{-15})$  signals correspond to coalescence events of massive SMBH binaries  $M_{\text{tot}} \sim 10^8 M_{\odot}$  at low redshift  $(z \lesssim 1)$  and small-amplitude  $(h_{\text{burst}} \sim 10^{-17})$  signals correspond to less massive SMBH binaries  $(M_{\text{tot}} \sim 10^6 M_{\odot})$  at high redshift  $(z \gtrsim 3)$ .

On the basis of an SA model (Kauffmann & Haehnelt 2000), Haehnelt (2003) concluded that *LISA* might detect SMBH coalescence events at a rate  $0.1-1.0~\rm yr^{-1}$  over the redshift range of  $0 \le z \le 5$ , although no explicit calculation on gravitational wave emission is done. Our result is consistent with his result.

## 4. SUMMARY AND CONCLUSIONS

In this paper we have estimated the coalescence rate of SMBH binaries in the centers of galaxies using a new semi-analytic model of galaxy and quasar formation (SA model) given by Enoki et al. (2003) on the basis of the hierarchical structure formation scenario. Then we calculated the spectrum of the gravitational wave background from inspiraling SMBH binaries on the basis of the formulation given by Jaffe & Backer (2003) and estimated the expected amplitudes and event rates of intense bursts of gravitational waves from coalescing SMBH binaries.

Our SA model includes dynamical friction and random collision as galaxy merging mechanisms and assumes that a SMBH is fueled by accretion of cold gas during a major merger of galaxies leading to a spheroid formation, and that SMBHs coalesce simultaneously when host galaxies merge. Many previous other studies have paid attention only to

SMBH growth and did not take galaxy formation processes into account. For investigating the relations between SMBH growth and galaxy formation processes, SA methods of galaxy and SMBH formation are suitable tools (Kauffmann & Haehnelt 2000; Cattaneo 2001; Enoki et al. 2003; Menci et al. 2003; Granato et al. 2004). Our SA model can reproduce not only observational properties of galaxies, but also the present SMBH mass function and the quasar luminosity functions at different redshifts (Nagashima et al. 2001; Enoki et al. 2003).

We have found that the gravitational wave background radiation spectrum for  $f \lesssim 1~\mu \text{Hz}$  has a characteristic strain  $h_c(f) \sim 10^{-16} (f/1~\mu \text{Hz})^{-2/3}$  just below the detection limit from the current measurements of the pulsar timing. The slope of the spectrum for  $f \gtrsim 1~\mu \text{Hz}$  gets steep owing to the upper limit in frequency set by the radius of the innermost stable circular orbit. The stochastic background radiation mainly comes from inspiraling SMBH binaries at 0 < z < 1. Therefore, the background radiation can probe inspiraling SMBH binaries at low redshift.

We have also found that *LISA* might detect intense bursts of gravitational waves due to the SMBH coalescence events at a rate  $0.1-1.0~\rm yr^{-1}$  and that the main contribution to the event rate comes from SMBH binary coalescence at high redshift ( $z \gtrsim 2$ ). Our model predicts that burst signals with a large amplitude correspond to coalescence of large-mass SMBH binaries at low redshift, while those with a small amplitude correspond to coalescence of small-mass SMBH binaries at high redshift. This prediction can be tested by future measurements of the amplitude and the phase evolution in gravitational waves from inspiraling SMBH binaries (Hughes 2002). Comparing these predictions with observations in future, we can put a stringent constraint on SMBH formation and evolution models.

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