Remember from the tutorial:

- 1. No for loops! Use matrix multiplication and broadcasting whenever possible.
- 2. Think about numerical stability

```
In [4]: import nn_utils # module containing helper functions for checking the correctness
```

Task 1: Affine layer

Implement forward and backward functions for Affine layer

```
In [5]: class Affine:
         def forward(self, inputs, weight, bias):
             """Forward pass of an affine (fully connected) layer.
             Args:
                inputs: input matrix, shape (N, D)
                weight: weight matrix, shape (D, H)
                bias: bias vector, shape (H)
             Returns
                out: output matrix, shape (N, H)
             self.cache = (inputs, weight, bias)
             # TODO
             # Your code here
             out = np.dot(inputs, weight) + bias
             assert out.shape[0] == inputs.shape[0]
             assert out.shape[1] == weight.shape[1] == bias.shape[0]
```

```
return out
def backward(self, d out):
   """Backward pass of an affine (fully connected) layer.
   Args:
      d_out: incoming derivaties, shape (N, H)
   Returns:
      d_inputs: gradient w.r.t. the inputs, shape (N, D)
      d_weight: gradient w.r.t. the weight, shape (D, H)
      d_bias: gradient w.r.t. the bias, shape (H)
   inputs, weight, bias = self.cache
   # TODO
   # Your code here
   d_inputs = np.dot(d_out, weight.T)
   d_weight = np.dot(inputs.T, d_out)
   d_bias = np.sum(d_out, axis=0)
   assert np.all(d_inputs.shape == inputs.shape)
   assert np.all(d_weight.shape == weight.shape)
   assert np.all(d_bias.shape == bias.shape)
   return d_inputs, d_weight, d_bias
```

```
In [6]: affine = Affine()
    nn_utils.check_affine(affine)
```

All checks passed succesfully!

Task 2: ReLU layer

Implement forward and backward functions for ReLU layer

```
In [8]: relu = ReLU()
    nn_utils.check_relu(relu)
```

All checks passed succesfully!

Task 3: CategoricalCrossEntropy layer

Implement forward and backward for CategoricalCrossEntropy layer

```
In [9]: class CategoricalCrossEntropy:
          def forward(self, logits, labels):
              """Compute categorical cross-entropy loss.
              Args:
                 logits: class logits, shape (N, K)
                 labels: target labels in one-hot format, shape (N, K)
              Returns:
                 loss: loss value, float (a single number)
              # TODO
              # Your code here
              logits_shifted = logits - logits.max(axis=1, keepdims=True)
              log1= np.log(np.sum(np.exp(logits_shifted), axis=1, keepdims=True)) #to avo
              log_prob = logits_shifted - log1
              N = labels.shape[0]
              loss = -np.sum(labels * log_prob) / N
              probs = np.exp(log prob)
              # probs is the (N, K) matrix of class probabilities
              self.cache = (probs, labels)
              assert isinstance(loss, float)
              return loss
```

```
def backward(self, d_out=1.0):
               """Backward pass of the Cross Entropy loss.
                  d_out: Incoming derivatives. We set this value to 1.0 by default,
                      since this is the terminal node of our computational graph
                      (i.e. we usually want to compute gradients of loss w.r.t.
                      other model parameters).
               Returns:
                  d_logits: gradient w.r.t. the logits, shape (N, K)
                  d_labels: gradient w.r.t. the labels
                      we don't need d_labels for our models, so we don't
                      compute it and set it to None. It's only included in the
                      function definition for consistency with other layers.
               probs, labels = self.cache
               # Your code here
               N = labels.shape[0]
               d logits = d_out * (probs - labels) / N
               d_labels = None
               assert np.all(d_logits.shape == probs.shape == labels.shape)
               return d logits, d labels
In [10]: cross_entropy = CategoricalCrossEntropy()
```

All checks passed succesfully!

nn utils.check_cross_entropy(cross_entropy)

Logistic regression (with backpropagation) --- nothing to do in this section

```
# Define Layers
                 self.affine = Affine()
                 self.cross_entropy = CategoricalCrossEntropy()
             def predict(self, X):
                 """Generate predictions for one minibatch.
                 Args:
                     X: data matrix, shape (N, D)
                 Returns:
                     Y_pred: predicted class probabilities, shape (N, D)
                     Y_pred[n, k] = probability that sample n belongs to class k
                 logits = self.affine.forward(X, self.params["W"], self.params["b"])
                 Y_pred = softmax(logits, axis=1)
                 return Y_pred
             def step(self, X, Y):
                 """Perform one step of gradient descent on the minibatch of data.
                 1. Compute the cross-entropy loss for given (X, Y).
                 2. Compute the gradients of the loss w.r.t. model parameters.
                 3. Update the model parameters using the gradients.
                 Args:
                     X: data matrix, shape (N, D)
                     Y: target labels in one-hot format, shape (N, K)
                 Returns:
                     loss: loss for (X, Y), float, (a single number)
                 # Forward pass - compute the loss on training data
                 logits = self.affine.forward(X, self.params["W"], self.params["b"])
                 loss = self.cross_entropy.forward(logits, Y)
                 # Backward pass - compute the gradients of loss w.r.t. all the model parame
                 grads = \{\}
                 d_logits, _ = self.cross_entropy.backward()
                 _, grads["W"], grads["b"] = self.affine.backward(d_logits)
                 # Apply the gradients
                 for p in self.params:
                     self.params[p] = self.params[p] - self.learning_rate * grads[p]
                 return loss
In [12]: # Specify optimization parameters
         learning_rate = 1e-2
         max_epochs = 501
         report_frequency = 50
In [13]: log_reg = LogisticRegression(num_features=D, num_classes=K)
In [14]: | for epoch in range(max_epochs):
             loss = log_reg.step(X_train, Y_train)
```

```
if epoch % report_frequency == 0:
                 print(f"Epoch {epoch:4d}, loss = {loss:.4f}")
        Epoch
               0, loss = 2.3026
        Epoch 50, loss = 0.2275
        Epoch 100, loss = 0.1599
        Epoch 150, loss = 0.1306
        Epoch 200, loss = 0.1130
        Epoch 250, loss = 0.1009
        Epoch 300, loss = 0.0918
        Epoch 350, loss = 0.0846
        Epoch 400, loss = 0.0788
        Epoch 450, loss = 0.0738
        Epoch 500, loss = 0.0696
In [15]: y_test_pred = log_reg.predict(X_test).argmax(1)
         y_test_true = Y_test.argmax(1)
In [16]: print(f"test set accuracy = {accuracy_score(y_test_true, y_test_pred):.3f}")
        test set accuracy = 0.953
```

Feed-forward neural network (with backpropagation)

```
In [17]: def xavier_init(shape):
    """Initialize a weight matrix according to Xavier initialization.

See pytorch.org/docs/stable/nn.init#torch.nn.init.xavier_uniform_ for details.
    """
    a = np.sqrt(6.0 / float(np.sum(shape)))
    return np.random.uniform(low=-a, high=a, size=shape)
```

Task 4: Implement a two-layer FeedForwardNeuralNet model

You can use the LogisticRegression class for reference

```
# Initialize the model parameters
   self.params = {
      "W1": xavier_init([input_size, hidden_size]),
      "b1": np.zeros([hidden_size]),
      "W2": xavier_init([hidden_size, output_size]),
      "b2": np.zeros([output_size]),
   }
   # Define Layers
   # TODO
   # Your code here
   self.affine1 = Affine()
   self.relu = ReLU()
   self.affine2 = Affine()
   self.cross_entropy = CategoricalCrossEntropy()
   def predict(self, X):
   """Generate predictions for one minibatch.
   Args:
      X: data matrix, shape (N, D)
   Returns:
      Y_pred: predicted class probabilities, shape (N, D)
      Y_pred[n, k] = probability that sample n belongs to class k
   # TODO
   # Your code here
   logits1 = self.affine1.forward(X, self.params["W1"], self.params["b1"])
   hidden = self.relu.forward(logits1)
   logits2 = self.affine2.forward(hidden, self.params["W2"], self.params["b2"]
   Y_pred = softmax(logits2, axis=1)
   return Y_pred
def step(self, X, Y):
   """Perform one step of gradient descent on the minibatch of data.
   1. Compute the cross-entropy loss for given (X, Y).
   2. Compute the gradients of the loss w.r.t. model parameters.
   3. Update the model parameters using the gradients.
   Args:
      X: data matrix, shape (N, D)
      Y: target labels in one-hot format, shape (N, K)
   Returns:
      loss: loss for (X, Y), float, (a single number)
   # TODO
```

```
logits1 = self.affine1.forward(X, self.params["W1"], self.params["b1"])
                hidden = self.relu.forward(logits1)
                logits2 = self.affine2.forward(hidden, self.params["W2"], self.params["b2"]
                loss = self.cross_entropy.forward(logits2, Y)
                grads = \{\}
                d_logits2, _ = self.cross_entropy.backward()
                d hidden, grads["W2"], grads["b2"] = self.affine2.backward(d logits2)
                d_logits1 = self.relu.backward(d_hidden)
                _, grads["W1"], grads["b1"] = self.affine1.backward(d_logits1)
                for p in self.params:
                    self.params[p] = self.params[p] - self.learning_rate * grads[p]
                return loss
In [19]: H = 32 # size of the hidden Layer
         # Specify optimization parameters
         learning_rate = 1e-2
         max epochs = 501
         report_frequency = 50
In [20]: model = FeedforwardNeuralNet(
            input_size=D, hidden_size=H, output_size=K, learning_rate=learning_rate
In [21]: for epoch in range(max_epochs):
            loss = model.step(X_train, Y_train)
            if epoch % report_frequency == 0:
                print(f"Epoch {epoch:4d}, loss = {loss:.4f}")
       Epoch 0, loss = 8.5876
       Epoch 50, loss = 0.6002
       Epoch 100, loss = 0.3517
       Epoch 150, loss = 0.2510
       Epoch 200, loss = 0.1975
       Epoch 250, loss = 0.1631
       Epoch 300, loss = 0.1401
       Epoch 350, loss = 0.1231
       Epoch 400, loss = 0.1098
       Epoch 450, loss = 0.0989
       Epoch 500, loss = 0.0897
In [22]: y_test_pred = model.predict(X_test).argmax(1)
        y_test_true = Y_test.argmax(1)
In [23]: print(f"test set accuracy = {accuracy_score(y_test_true, y_test_pred):.3f}")
       test set accuracy = 0.938
```

Your code here