

Problem 3:

a).  $\text{Relu}(X_n^T w_i^*) = X_n^T w_i^* \quad (X_n^T \geq 0 \text{ and } w_i^* \geq 0)$

$$f_{w^*}(x_n) = \text{Relu}(\text{Relu}(\text{Relu}(X_n^T w_1^*) \cdot w_2^*) \dots w_L^*) \cdot w_{L+1}^*$$
$$= X_n^T w_1^* \cdot w_2^* \dots w_L^* \cdot w_{L+1}^*$$
$$= X_n^T w_{NN}^* \quad \text{has the same format as } w^T x_n$$

so  $w_{LS}^* = w_{NN}^*$

$$L_{NN}(w_{NN}^*) = L_{LS}(w_{LS}^*)$$

b).  $x_n \geq 0 \quad w_{LS}^* \geq 0$

$$\Rightarrow w_{LS}^* x_n \geq 0 \quad w_{NN}^* \in \mathbb{R}$$

$$w_{LS}^* x_n \in X_n^T w_{NN}^*$$

so  $x_n^T w_{NN}^*$  can reach any value that  $w_{LS}^* x_n$ ,

but due to the value limitation of  $w_{LS}^*$ , it may not reach to the global minimum. so,  $L_{NN}(w_{NN}^*) \leq L_{LS}(w_{LS}^*)$