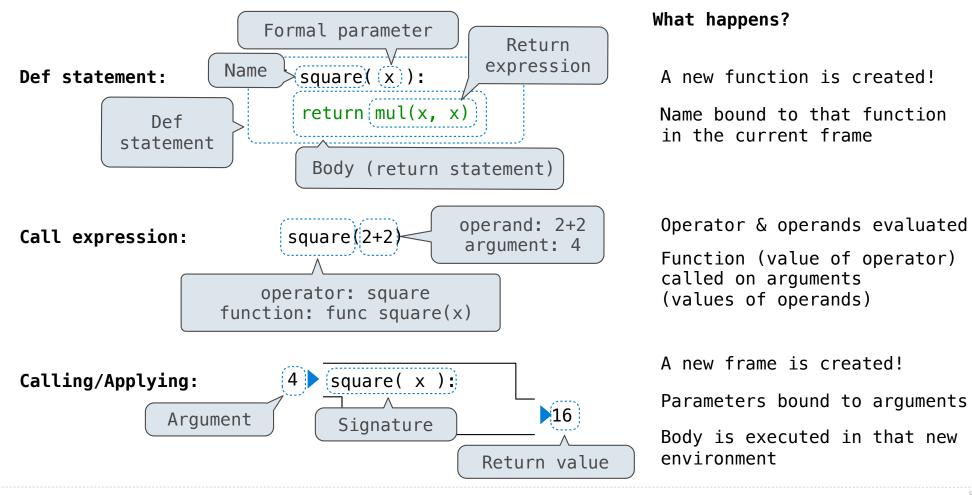


Life Cycle of a User-Defined Function



O

Multiple Environments in One Diagram!

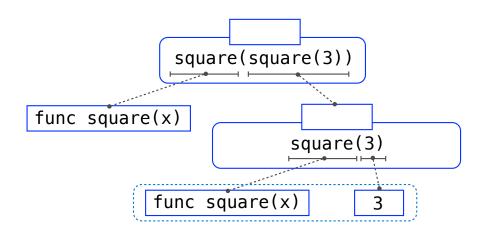
```
Global frame

func mul(...)

mul

func square(x) [parent=Global]

square
```



<u>Interactive Diagram</u>

Multiple Environments in One Diagram!

```
1 from operator import mul

→ 2 def square(x):
→ 3 return mul(x, x)
4 square(square(3))
```

```
Global frame

mul
square

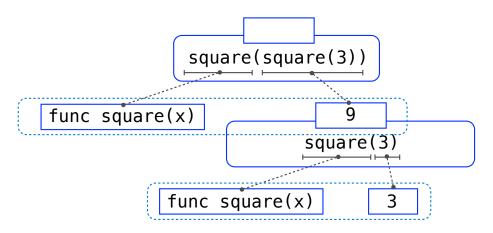
func mul(...)

func square(x) [parent=Global]

x 3

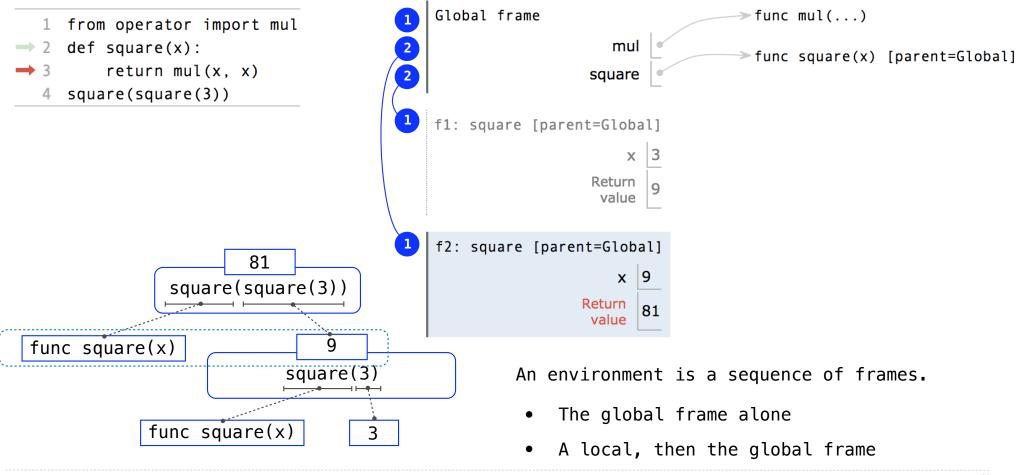
Return
value

punc mul(...)
```



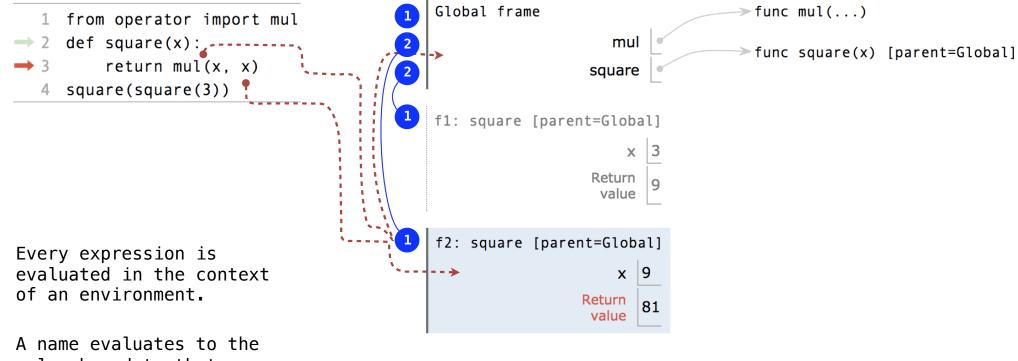
<u>Interactive Diagram</u>

Multiple Environments in One Diagram!



<u>Interactive Diagram</u>

Names Have No Meaning Without Environments



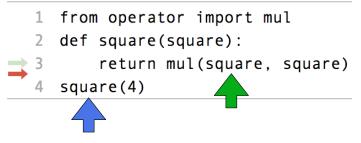
value bound to that name in the earliest frame of the current environment in which that name is found.

An environment is a sequence of frames.

- The global frame alone
- A local, then the global frame

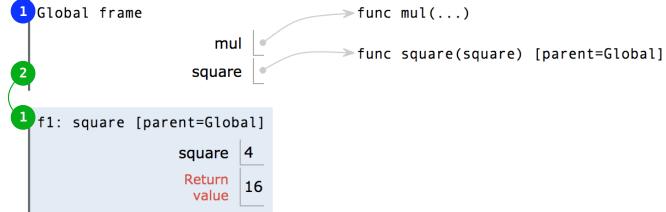
Names Have Different Meanings in Different Environments

A call expression and the body of the function being called are evaluated in different environments



Every expression is evaluated in the context of an environment.

A name evaluates to the value bound to that name in the earliest frame of the current environment in which that name is found.



Environments for Higher-Order Functions

Environments Enable Higher-Order Functions

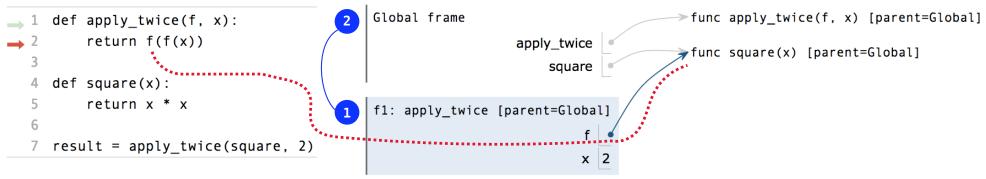
Functions are first-class: Functions are values in our programming language

Higher-order function: A function that takes a function as an argument value **or**A function that returns a function as a return value

Environment diagrams describe how higher-order functions work!

Names can be Bound to Functional Arguments

```
Global frame
                                                         func apply_twice(f, x) [parent=Global]
def apply_twice(f, x):
    return f(f(x))
                                    apply_twice
                                                         func square(x) [parent=Global]
                                        square
                                                                 Applying a user-defined function:
def square(x):
                                                                 • Create a new frame
    return x * x
                                                                  • Bind formal parameters
                                                                    (f \& x) to arguments
result = apply twice(square, 2)
                                                                  • Execute the body:
                                                                    return f(f(x))
```



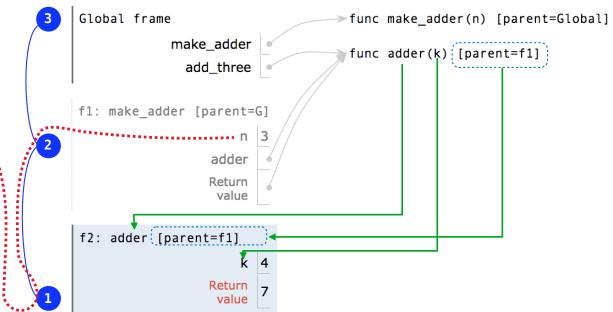
Environments for Nested Definitions

Environment Diagrams for Nested Def Statements

```
Nested def

1 def make_adder(n):
2 def adder(k):
3 return k + n
4 return adder
5
6 add_three = make_adder(3)
7 add_three(4)
```

- Every user-defined function has a parent frame (often global)
- The parent of a function is the frame in which it was defined
- Every local frame has a parent frame (often global)
- The parent of a frame is the parent of the function called



How to Draw an Environment Diagram

When a function is defined:

Create a function value: func <name>(<formal parameters>) [parent=<label>]
Its parent is the current frame.

```
f1: make_adder func adder(k) [parent=f1]
```

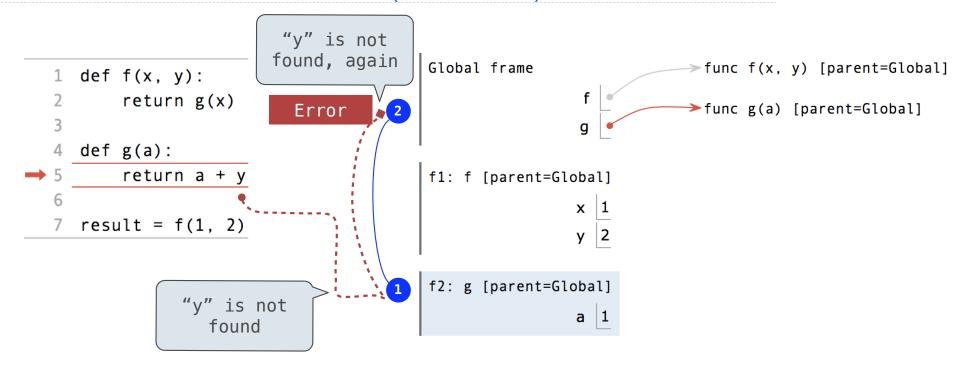
Bind <name> to the function value in the current frame

When a function is called:

- 1. Add a local frame, titled with the <name> of the function being called.
- ★ 2. Copy the parent of the function to the local frame: [parent=<label>]
 - 3. Bind the <formal parameters> to the arguments in the local frame.
 - 4. Execute the body of the function in the environment that starts with the local frame.

Local Names

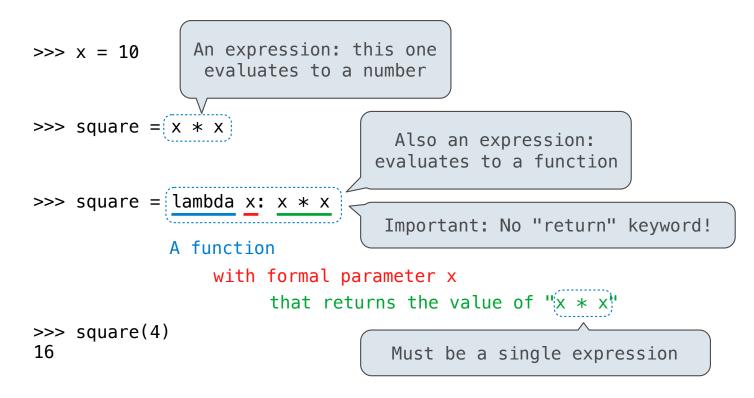
Local Names are not Visible to Other (Non-Nested) Functions



- An environment is a sequence of frames.
- The environment created by calling a top-level function (no def within def) consists of one local frame, followed by the global frame.

Lambda Expressions

Lambda Expressions

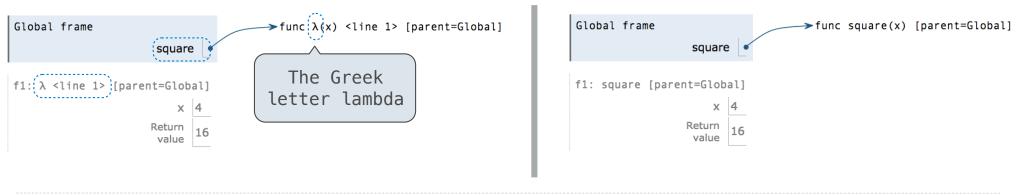


Lambda expressions are not common in Python, but important in general Lambda expressions in Python cannot contain statements at all!

Lambda Expressions Versus Def Statements

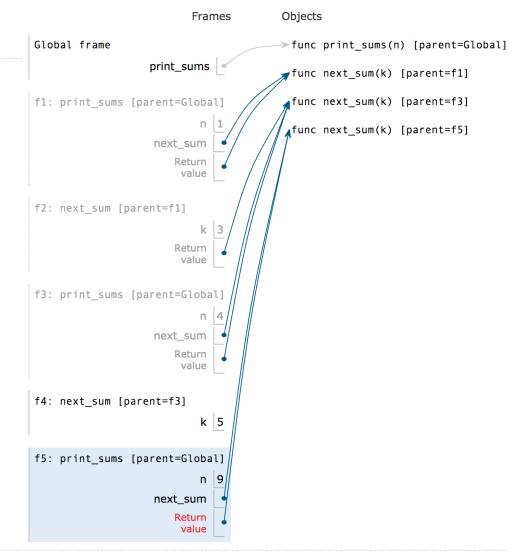


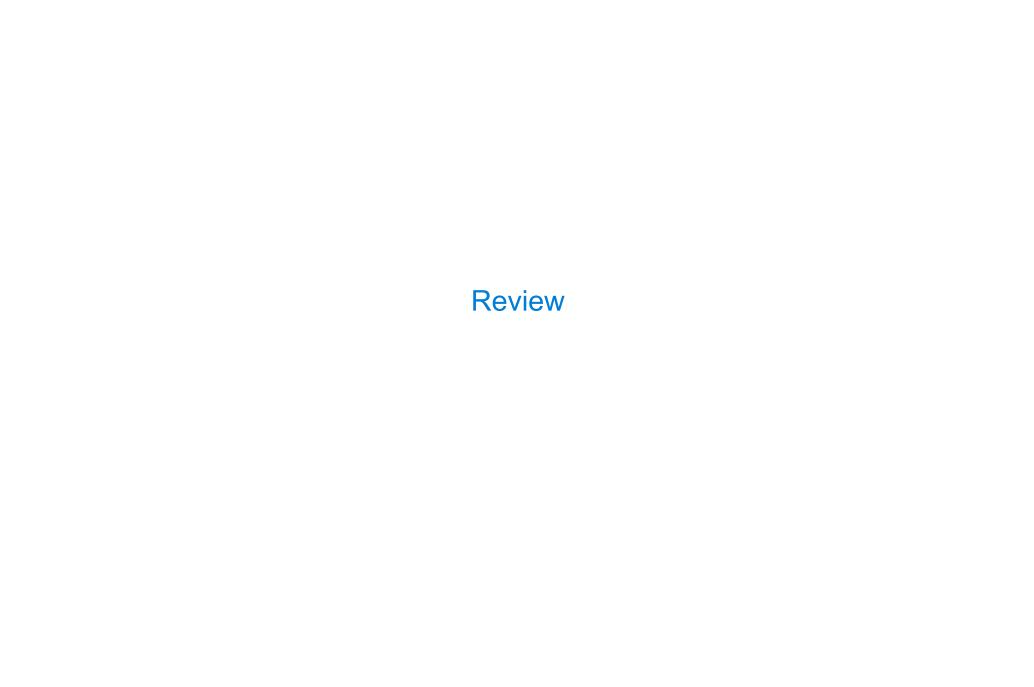
- Both create a function with the same domain, range, and behavior.
- Both bind that function to the name square.
- Only the def statement gives the function an intrinsic name, which shows up in environment diagrams but doesn't affect execution (unless the function is printed).



Self-Reference

Returning a Function Using Its Own Name





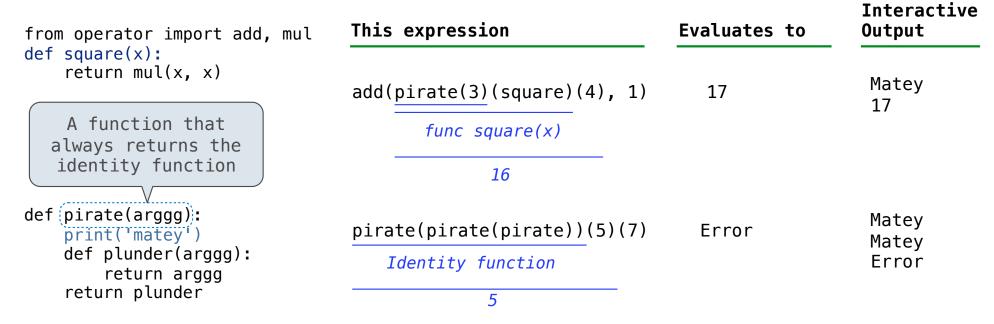
What Would Python Display?

The print function returns None. It also displays its arguments (separated by spaces) when it is called.

<pre>from operator import add, mul def square(x):</pre>	This expression	Evaluates to	Output
return mul(x, x)	5	5	5
A function that takes any argument and returns a	print(5)	None	5
function that returns that arg	<pre>print(print(5)) None</pre>	None	5 None
<pre>def (delay(arg): print('delayed') def g(): return (arg) return g</pre>	delay(delay)()(6)()	6	delayed delayed 6
Names in nested def statements can refer to their enclosing scope	<pre>print(delay(print)()(4))</pre>	None	delayed 4 None

What Would Python Print?

The print function returns None. It also displays its arguments (separated by spaces) when it is called.



A name evaluates to the value bound to that name in the earliest frame of the current environment in which that name is found.

