## Documentation for forcing.py

### 1 Introduction

forcing.py is essentially a class that computes the radiative forcing for the EZ-Climate model. It helps determine the excess energy created by GHGs in the atmosphere.

### 2 Model of Excess Energy from GHGs

# 3 Inputs

The methods embedded in the Forcing class require similar inputs that are explained below.

- m: an array of fractional mitigation levels that are denoted  $x_t$  in the paper.
- **node**: an integer that represents the node in the **TreeModel** for which forcing is to be calculated.
- tree: the TreeModel object whose tree structure is to be used.
- bau: the BusinessAsUsual object that gives the emission levels under the business-as-usual scenario.
- **subinterval\_len**: a float that represents the length of a subinterval.
- returning: an optional string that selects the output. Valid returns include "forcing", "ghg", and "both".
  - "forcing": returns the forcing only;
  - "ghg": returns the GHGs level only;
  - "both": returns both the GHGs level and forcing.

## 4 Python: Forcing

```
from __future__ import division
import numpy as np
```

#### 4.1 Attributes

The attributes of the Forcing class are basically parameters of the theoretical model, so they are all of the float type.

- sink\_start: Its default value is 35.596.
- forcing\_start: Its default value is 4.926.
- forcing\_p1: Its default value is 0.13173.
- forcing\_p2: Its default value is 0.607773.
- forcing\_p3: Its default value is 315.3785.
- absorption\_p1: Its default value is 0.94835.
- absorption\_p2: Its default value is 0.741547.
- lsc\_p1: Its default value is 285.6268.
- $lsc_p2$ : Its default value is 0.88414.

#### class Forcing(object):

"""Radiative forcing for the  $\it EZ-Climate$  model. Determines the excess energy  $\it cr$  by  $\it GHGs$  in the atmosphere.

```
Attributes
_____
sink\_start : float
        sinking constant
forcing\_start : float
        forcing start constant
forcing_p1 : float
        forcing constant
forcing_p2 : float
        forcing constant
forcing_p3 : float
        forcing constant
absorption\_p1 : float
        absorption constant
absorption\_p2:float
        absorption constant
lsc_p1 : float
        class constant
lsc_p2 : float
        class constant
n n n
# parameters that I have no idea about
sink_start = 35.596
forcing\_start = 4.926
forcing_p1 = 0.13173
```

 $forcing_p2 = 0.607773$ 

```
forcing_p3 = 315.3785
absorption_p1 = 0.94835
absorption_p2 = 0.741547
lsc_p1 = 285.6268
lsc_p2 = 0.88414
```

#### 4.2 Methods

forcing\_and\_ghg\_at\_node: calculates the radiative forcing based on GHGs evolution that leads up to damage calculation.

```
@classmethod
def forcing_and_ghg_at_node(cls, m, node, tree, bau, subinterval_len, returning=
        """Calculates the radiative forcing based on GHG evolution leading up
        damage calculation in `node`.
        Parameters
        m : ndarray
                array of mitigations
        node: int
                node for which forcing is to be calculated
        tree : `TreeModel` object
                tree structure used
        bau : `BusinessAsUsual` object
                business-as-usual scenario of emissions
        subinterval\_len : float
                subinterval length
        returning: string, optional
                * "forcing": implies only the forcing is returned
                * "qhq": implies only the GHG level is returned
                * "both": implies both the forcing and GHG level is returned
Returns
_____
tuple or float
        if `returning` is
                * "forcing": only the forcing is returned
                * "ghq": only the GHG level is returned
                * "both": both the forcing and GHG level is returned
        11 11 11
```

• Specify the case when the node is 0.

```
#for the start state, return 0 for forcing and ghg_start for the g
#call bau to get the ghg level
if node == 0:
    if returning == "forcing":
        return 0.0
    elif returning== "ghg":
        return bau.ghg_start
    else:
        return 0.0, bau.ghg_start
```

- Based on the node given, find its period, path, and decision times through **TreeModel**.
- Determine the number of increments measured at the length specified by **subinter-val\_len**.

```
# get the period and the path that the target node are in
period = tree.get_period(node)
path = tree.get_path(node, period)
# the decision time is the time when we make a mitigation, i.e. ar
period_lengths = tree.decision_times[1:period+1] - tree.decision_ti
#increments are the number counts of subintervals within a period
increments = period_lengths/subinterval_len
```

• Assign the starting values of forcing and GHGs level.

```
#assign beginning values
cum_sink = cls.sink_start
cum_forcing = cls.forcing_start
ghg_level = bau.ghg_start
```

- For each period that a node has undergone, determine its beginning and ending emission level through **bau.emission\_by\_decisions**. We assume that the emission level remains constant since the second to last period.
- For each period that a node has undergone, round its number of increments to an integer.

• Within each period that a node has undergone, allocate the emission level change

across time, and find corresponding ...

```
- p_{co2}
```

- $p_c$
- $add_p_pm$
- absorption
- cum\_forcing

```
# for each increment in a period, the forcing is affecting
for i in range(0, increment):
    #allocate the emission level change across time
    p_co2_emission = start_emission + i * (end_emission
    p_co2 = 0.71 * p_co2_emission
    p_c = p_co2 / 3.67
    add_p_ppm = subinterval_len * p_c / 2.13
    lsc = cls.lsc_p1 + cls.lsc_p2 * cum_sink
    absorption = 0.5 * cls.absorption_p1 * np.sign(ghg_cum_sink += absorption
    cum_forcing += cls.forcing_p1*np.sign(ghg_level-cls
    ghg_level += add_p_ppm - absorption
```

• Return the outcome according to the selection.

Returns

forcing\_at\_node: returns the forcing based mitigation at a given node that leads up to the damage calculation.

```
Oclassmethod
def forcing_at_node(cls, m, node, tree, bau, subinterval_len):
    """Calculates the forcing based mitigation leading up to the
    damage calculation in `node`.

Parameters
    -----
    m : ndarray
        array of mitigations in each node.
    node : int
        the node for which the forcing is being calculated.
```

```
float
forcing
```

return cls.forcing\_and\_ghg\_at\_node(m, node, tree, bau, subinterval\_len, ghg\_level\_at\_node: returns the GHGs level at a given node that leads up to the damage calculation.