

## UNIVERSITY NAME

Final Exam - 2017 variant: 1

## Course Title

INDEX555

Teacher Name

Student Information	$(fill\ completely)$
First Name	
Last Name	
ID	

Attention Good luck!

• Exam Duration: 2 hours

• Permitted Materials: Permitted materials

• Any Caution

№1. Problem

Joint distribution given by table.

$$\begin{array}{c|ccccc} X & -1 & 0 & 1 \\ \hline -1 & 0.2 & 0.2 & 0.1 \\ 0 & 0 & 0.1 & 0.2 \\ 1 & 0 & 0 & 0.2 \\ \end{array}$$

Are random variables correlated?

Solution:

№2. Problem 5 point

Source code on Python:

```
import random, math
                                                              # this is comment
                                                                                              1
                                                                                              2
c = 2.2039
                                                                                              3
                                                                                              4
while True :
                                                                                              5
  u = random.random()
                                                                                              6
  y = -1.0 * math.log(random.random())
  if c * u < y * (math.exp(-1.0 * y ** 2 / 2) + y) : \# \ this \ line \ is \ extra \dots too
                                                                                              8
    long
    print y
                                                                                              9
    break
                                                                                              10
```

Another method for code input (see source code):

```
for (i in 1:100) {
  if (i %% 2 == 0) print(i)
  }
}
```

Listings package was used. Now mean(1:100) inline code.

Solution:

№3. Question 3 point

Let X and Y are independent random variables. Find E(XY). Where E – expectation of random variable.

Answer:

Full Name:	Student ID:								
<b>№4.</b> Selective Test	2 poin								
What planet do you live on?									
Selection:									
A. Earth B. Mars C. Jupiter	D. Saturn								
№5. Placement Test	3 poin								
Let $EX = 2$ and $EY = 1$ . $E(2X + Y) = + EY$ .									
№6. Placement Test	3 poin								
Attila was king of the .									

Total point 21

 $*** The \ End \ of \ Examination \ ***$ 



## UNIVERSITY NAME

Final Exam – 2017 variant: 2

## Course Title

INDEX555

Teacher Name

Student Information	$(fill\ completely)$
First Name	
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ID	

Attention Good luck!

• Exam Duration: 2 hours

• Permitted Materials: Permitted materials

• Any Caution

№1. Problem 5 point

Joint distribution given by table.

$$\begin{array}{c|ccccc} & & Y & \\ \hline X & -1 & 0 & 1 \\ \hline -1 & 0.2 & 0.2 & 0.1 \\ 0 & 0 & 0.1 & 0.2 \\ 1 & 0 & 0 & 0.2 \\ \end{array}$$

Are random variables correlated?

Solution:

 $\mathbf{N}^{\underline{\bullet}}\mathbf{2}$ . Problem

Which probability distribution was simulated?

```
import random, math
Lambda = float( raw_input("Lambda = ") )
print -1.0 * math.log( random.random() ) / Lambda
3
```

Prove actual formula was used here.

Solution:

№3. Question

Let X and Y are independent random variables. Find E(XY). Where E – expectation of random variable.

Answer:

№4. Selective Test

What planet do you live on?

Selection:

A. Earth B. Mars C. Jupiter D. Saturn

Full	Name:											

№5. Placement Test

3 point

Let EX = 2 and EY = 1.  $E(2X + Y) = ___ + EY$ .

№6. Placement Test

3 point

Attila was king of the \_\_\_\_\_.

**№7.** Problem

5 point

Joint distribution given by table.

$$\begin{array}{c|ccccc} X & -1 & 0 & 1 \\ \hline -1 & 0.2 & 0.2 & 0.1 \\ 0 & 0 & 0.1 & 0.2 \\ 1 & 0 & 0 & 0.2 \\ \end{array}$$

Are random variables correlated?

Solution:

№8. Question

3 point

Let X and Y are independent random variables. Find E(XY). Where E – expectation of random variable.

Answer:

№9. Selective Test

2 point

What planet do you live on?

Selection:

A. Earth

B. Mars

C. Jupiter

D. Saturn

№10. Placement Test

3 point

Let EX = 2 and EY = 1.  $E(2X + Y) = ___ + EY$ .

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3 point

Attila was king of the . .

Total point 37

\*\*\* The End of Examination \*\*\*