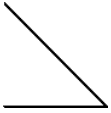


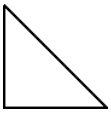
Métopost : exemples

```
input macros;
verbatimtex
\documentclass[12pt]{article}
\usepackage[T1]{fontenc}
\begin{document}
etex
```



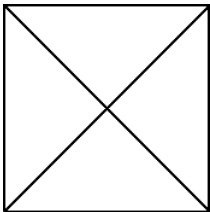
```
beginfig(1)
  pair A, B, C;
  A:=(0,0); B:=(1cm,0); C:=(0,1cm);
  draw A--B--C;

endfig;
```



```
beginfig(2)
  pair A, B, C;
  A:=(0,0); B:=(1cm,0); C:=(0,1cm);
  draw A--B--C--cycle;

endfig;
```



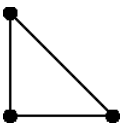
```
beginfig(3)
  pair A[];
  A[0]:=(-1cm, -1cm);
  A[1]:=( 1cm, -1cm);
  A[2]:=( 1cm,  1cm);
  A[3]:=(-1cm,  1cm);
  draw A[0]--A[1]--A[2]--A[3]--cycle;
  draw A[0]--A[2];
  draw A[1]--A[3];

endfig;
```



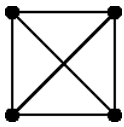
```
beginfig(4)
  pair A;
  A:=(0,0); B:=(1cm,0); C:=(0,1cm);
  draw A withpen pencircle scaled 4bp;

endfig;
```



```
beginfig(5)
  pair A, B, C;
  A:=(0,0); B:=(1cm,0); C:=(0,1cm);
  draw A--B--C--cycle;
  draw A withpen pencircle scaled 4bp;
  draw B withpen pencircle scaled 4bp;
  draw C withpen pencircle scaled 4bp;

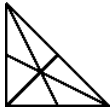
endfig;
```



```

beginfig(6)
  pair A, B, C, D;
  A:=(0,0); B:=(1cm,0);
  C:=(1cm,1cm); D:=(0,1cm);
  draw A--B--C--D--cycle;
  draw A--C;
  draw B--D;
  draw A withpen pencircle scaled 4bp;
  draw B withpen pencircle scaled 4bp;
  draw C withpen pencircle scaled 4bp;
  draw D withpen pencircle scaled 4bp;
endfig;

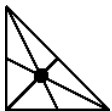
```



```

beginfig(7)
  pair A, B, C;
  A:=(0,0); B:=(1cm,0); C:=(0,1cm);
  draw A--B--C--cycle;
  draw 1/2[A,B] -- C;
  draw 1/2[B,C] -- A;
  draw 1/2[C,A] -- B;
endfig;

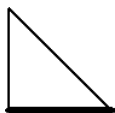
```



```

beginfig(8)
  pair A, B, C;
  A:=(0,0); B:=(1cm,0); C:=(0,1cm);
  draw A--B--C--cycle;
  draw 1/2[A,B] -- C;
  draw 1/2[B,C] -- A;
  draw 1/2[C,A] -- B;
  draw 1/3 A + 1/3 B + 1/3 C
    withpen pencircle scaled 4bp;
endfig;

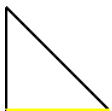
```



```

beginfig(9)
  pair A, B, C;
  A:=(0,0); B:=(1cm,0); C:=(0,1cm);
  draw A--B--C--cycle;
  draw A--B withpen pencircle scaled 2bp;
endfig;

```



```

beginfig(10)
  pair A, B, C;
  A:=(0,0); B:=(1cm,0); C:=(0,1cm);
  draw A--B--C--cycle;
  draw A--B withcolor (green + red);
endfig;

```



```

beginfig(11)
  pair A, B, C;
  A:=(0,0); B:=(1cm,0); C:=(0,1cm);

```

```

draw A--B;
draw B--C dashed evenly;
draw C--A dashed withdots;

endfig;

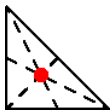
```



```

beginfig(12)
  pair A, B, C;
  A:=(0,0); B:=(1cm,0); C:=(0,1cm);
  draw A--B withpen pencircle scaled 2bp withcolor .8white;
  draw B--C withpen pencircle scaled 2bp withcolor .6white;
  draw C--A withpen pencircle scaled 2bp withcolor .4white;
endfig;

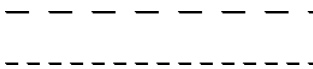
```



```

beginfig(13)
  pair A, B, C;
  A:=(0,0); B:=(1cm,0); C:=(0,1cm);
  draw A--B--C--cycle;
  draw 1/2[A,B] -- C dashed evenly;
  draw 1/2[B,C] -- A dashed evenly;
  draw 1/2[C,A] -- B dashed evenly;
  draw 1/3 A + 1/3 B + 1/3 C
    withpen pencircle scaled 4bp
    withcolor red;
endfig;

```



```

beginfig(14)
  draw (0,0)--(3cm,0) dashed evenly scaled 2;
  draw (0,-5mm)--(3cm,-5mm) dashed evenly;
endfig;

```



```

beginfig(15)
  draw (0,0)--(3cm,0)
    dashed dashpattern(on 2bp off 3bp);
endfig;

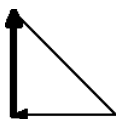
```



```

beginfig(16)
  draw (0,0)--(3cm,0) dashed dashpattern(on 1bp off 2bp on 10bp off 2bp);
endfig;

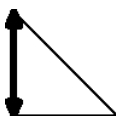
```



```

beginfig(17)
  pair A, B, C;
  A:=(0,0); B:=(1cm,0); C:=(0,1cm);
  drawarrow C--B--A;
  drawarrow A--C withpen pencircle scaled 2bp;
endfig;

```



```

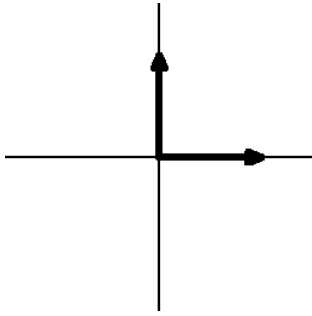
beginfig(18)
  pair A, B, C;
  A:=(0,0); B:=(1cm,0); C:=(0,1cm);

```

```

draw C--B--A--cycle;
drawdblarrow A--C withpen pencircle scaled 2bp;
endfig;

```



```

beginfig(19)
draw (-1.5cm,0)--(1.5cm,0);
draw (0,-1.5cm)--(0,1.5cm);
drawarrow (0,0)--(1cm,0)
withpen pencircle scaled 2bp;
drawarrow (0,0)--(0,1cm)
withpen pencircle scaled 2bp;
endfig;

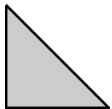
```



```

beginfig(20)
pair A, B, C;
A:=(0,0); B:=(1cm,0); C:=(0,1cm);
fill A--B--C--cycle withcolor .8 white;
endfig;

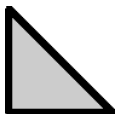
```



```

beginfig(21)
pair A, B, C;
A:=(0,0); B:=(1cm,0); C:=(0,1cm);
fill A--B--C--cycle withcolor .8 white;
draw A--B--C--cycle;
endfig;

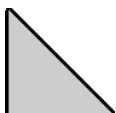
```



```

beginfig(22)
pair A, B, C;
A:=(0,0); B:=(1cm,0); C:=(0,1cm);
fill A--B--C--cycle withcolor .8 white;
draw A--B--C--cycle withpen pencircle scaled 2bp;
endfig;

```



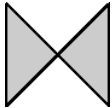
```

beginfig(23)
pair A, B, C;
A:=(0,0); B:=(1cm,0); C:=(0,1cm);
draw A--B--C--cycle withpen pencircle scaled 2bp;
fill A--B--C--cycle withcolor .8 white;
endfig;

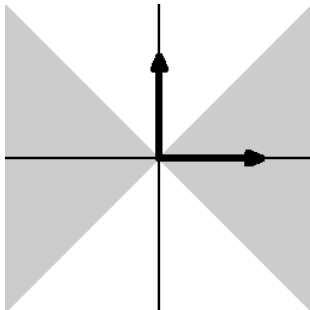
```



```
beginfig(24)
  pair A, B, C, D;
  A:=(0,0); B:=(1cm,0);
  C:=(1cm,1cm); D:=(0,1cm);
  fill A--C--B--D--cycle withcolor .8white;
endfig;
```



```
beginfig(25)
  pair A, B, C, D;
  A:=(0,0); B:=(1cm,0);
  C:=(1cm,1cm); D:=(0,1cm);
  path p;
  p := A--C--B--D--cycle;
  fill p withcolor .8white;
  draw p;
endfig;
```



```
beginfig(26)
  pair A, B, C, D;
  A:=(-1.5cm,-1.5cm); B:=(1.5cm,-1.5cm);
  C:=(1.5cm,1.5cm); D:=(-1.5cm,1.5cm);
  fill A--C--B--D--cycle withcolor .8white;
  draw (-1.5cm,0)--(1.5cm,0);
  draw (0,-1.5cm)--(0,1.5cm);
  drawarrow (0,0)--(1cm,0)
    withpen pencircle scaled 2bp;
  drawarrow (0,0)--(0,1cm)
    withpen pencircle scaled 2bp;
endfig;
```

Au dessus
 À gauche • À droite
 En dessous

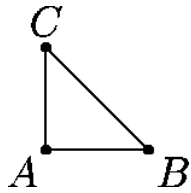
```
beginfig(27)
  pair A;
  A := (0,0);
  draw A withpen pencircle scaled 4bp;
  label.top(btex Au dessus etex, A);
  label.bot(btex En dessous etex, A);
  label.rt (btex ^^c0 droite etex, A);
  label.lft(btex ^^c0 gauche etex, A);
endfig;
```

En haut à gauche • En haut à droite
 En bas à gauche • En bas à droite

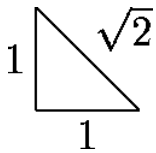
```
beginfig(28)
  pair A;
  A := (0,0);
  draw A withpen pencircle scaled 4bp;
  label.ulft(btex En haut ^^e0 gauche etex, A);
  label.urt (btex En haut ^^e0 droite etex, A);
  label.llft(btex En bas ^^e0 gauche etex, A);
  label.lrt (btex En bas ^^e0 droite etex, A);
endfig;
```

• A

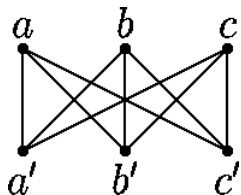
```
beginfig(29)
  pair A;
  A := (0,0);
  dotlabel.urt(btex  $A$  etex, A);
endfig;
```



```
beginfig(30)
  pair A, B, C;
  A := (0,0); B := (1cm,0); C := (0,1cm);
  draw A--B--C--cycle;
  dotlabel.llft(btex  $A$  etex, A);
  dotlabel.lrt(btex  $B$  etex, B);
  dotlabel.top(btex  $C$  etex, C);
endfig;
```



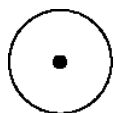
```
beginfig(31)
  pair A, B, C;
  A := (0,0); B := (1cm,0); C := (0,1cm);
  draw A--B--C--cycle;
  label.bot(btex  $1$  etex, 1/2[A,B]);
  label.lft(btex  $1$  etex, 1/2[A,C]);
  label.urt(btex  $\sqrt{2}$  etex, 1/2[B,C]);
endfig;
```



```
beginfig(32)
  u:=1cm;
  pair A,B,C,D,E,F,G;
  A := (-u,u);
  B := (0,u);
  C := (u,u);
  D := (-u,0);
  E := (0,0);
  F := (u,0);
  draw A--D; draw A--E; draw A--F;
  draw B--D; draw B--E; draw B--F;
  draw C--D; draw C--E; draw C--F;
  dotlabel.top(btex  $a$  etex, A);
  dotlabel.top(btex  $b$  etex, B);
  dotlabel.top(btex  $c$  etex, C);
  dotlabel.bot(btex  $a'$  etex, D);
  dotlabel.bot(btex  $b'$  etex, E);
  dotlabel.bot(btex  $c'$  etex, F);
endfig;
```

•

```
beginfig(33)
  draw fullcircle;
endfig;
```



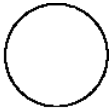
```
beginfig(34)
```

```

draw (0,0) withpen pencircle scaled 4bp;
draw fullcircle scaled 1cm;

endfig;

```

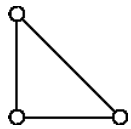


```

beginfig(35)
  draw (0,0) withpen pencircle scaled 4bp;
  draw fullcircle scaled 1cm shifted (1cm,1cm);

endfig;

```

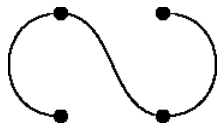


```

beginfig(36)
  pair A, B, C;
  A:=(0,0); B:=(1cm,0); C:=(0,1cm);
  draw A--B--C--cycle;
  fill fullcircle scaled 4bp shifted A withcolor white;
  fill fullcircle scaled 4bp shifted B withcolor white;
  fill fullcircle scaled 4bp shifted C withcolor white;
  draw fullcircle scaled 4bp shifted A;
  draw fullcircle scaled 4bp shifted B;
  draw fullcircle scaled 4bp shifted C;

endfig;

```



```

beginfig(37)
  draw (0,0) .. (0,1cm) .. (1cm,0) .. (1cm,1cm);
  draw (0,0) withpen pencircle scaled 4bp;
  draw (0,1cm) withpen pencircle scaled 4bp;
  draw (1cm,0) withpen pencircle scaled 4bp;
  draw (1cm,1cm) withpen pencircle scaled 4bp;

endfig;

```



```

beginfig(38)
  draw (0,0) -- (0,1cm) .. (1cm,0) .. (1cm,1cm);

endfig;

```



```

beginfig(39)
  draw (0,0) --- (0,1cm) .. (1cm,0) .. (1cm,1cm);

endfig;

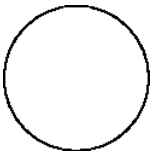
```



```

beginfig(40)
  draw (0,0) .. (0,1cm) .. (1cm,0) .. (1cm,1cm)
    .. cycle;
endfig;

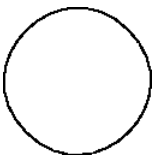
```



```

beginfig(41)
  pair A, B, C, D;
  A:=(0,0); B:=(1cm,0);
  C:=(1cm,1cm); D:=(0,1cm);
  draw A..B..C..D..cycle;
endfig;

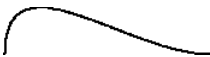
```



```

beginfig(42)
  draw (0,0) .. (1cm,1cm) .. cycle;
endfig;

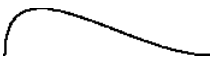
```



```

beginfig(43)
  draw (0,0){(0,1)} .. (2cm,0){(1,0)};
endfig;

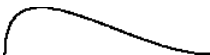
```



```

beginfig(44)
  draw (0,0){dir 90} .. (2cm,0){dir 0};
endfig;

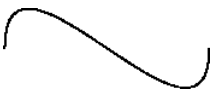
```



```

beginfig(45)
  draw (0,0){up} .. (2cm,0){right};
endfig;

```



```

beginfig(46)
  draw (0,0){up} .. (2cm,0){up};
endfig;

```



```

beginfig(47)
  draw (0,0){up} .. (2cm,0){up} .. cycle;
endfig;

```




```

beginfig(48)
  alpha := 30;
  draw (0,0) -- 2cm*dir 0;
  draw (0,0) -- 2cm*dir alpha;
  draw 1cm * dir 0 {dir 90} ..
    1cm * dir alpha {dir(90+alpha)};
endfig;

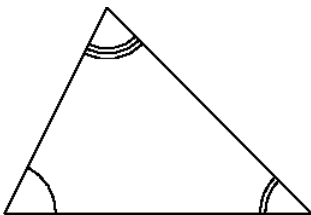
```



```

beginfig(49)
  alpha := 30;
  draw (0,0) -- 2cm*dir 0;
  draw (0,0) -- 2cm*dir alpha;
  draw 1cm * dir 0 {dir 90} ..
    1cm * dir alpha {dir(90+alpha)};
  draw 1.1cm * dir 0 {dir 90} ..
    1.1cm * dir alpha {dir(90+alpha)};
endfig;

```



```

beginfig(50)
  def draw_angle(expr A, O, B, n) =
    draw_angle_(A,O,B,5mm);
    if n>1 : draw_angle_(A,O,B,4.5mm); fi;
    if n>2 : draw_angle_(A,O,B,4mm); fi;
    if n>3 : draw_angle_(A,O,B,5.5mm); fi;
  enddef;
  def draw_angle_(expr A,O,B,d) =
    draw (O + d*unitvector(A-O))
      { d*unitvector(A-O) rotated 90 }
      ..
      { d*unitvector(B-O) rotated 90 }
      (O + d*unitvector(B-O));
  enddef;
  pair A, B, C;
  A := (0,0);
  B := (3cm,0);
  C := (1cm,2cm);
  draw A--B--C--cycle;
  draw_angle(B,A,C,1);
  draw_angle(C,B,A,2);
  draw_angle(A,C,B,3);
endfig;

```



```

beginfig(51)
  u:=1cm;
  path p;
  p := (u,0){up}..(-u,0){down}--cycle;
  fill p withcolor .8*white;
  draw p withpen pencircle scaled 1bp;
endfig;

```

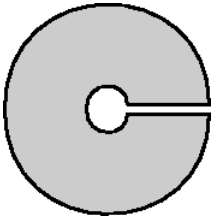


```

beginfig(52)
  u:=1cm;
  path p;
  p := (u,0){up} ..
    (-u,0){down} --
    (-.2u,0){up} ..
    (.2u,0){down} --
    cycle;
  fill p withcolor .8*white;
  draw p withpen pencircle scaled 1bp;
endfig;

```

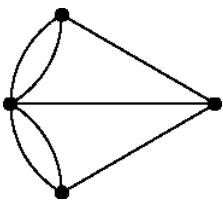




```

beginfig(53)
  u:=1cm;
  pair A,AA,B,BB,C,D;
  A := ( .2u, .05u);
  AA := ( .2u, -.05u);
  B := ( u, .05u);
  BB := ( u, -.05u);
  C := (-.2u, 0);
  D := ( -u, 0);
  path p;
  p:= B{up} .. D{down} .. BB{up} --
    AA{down} .. C{up} .. A{down} -- cycle;
  fill p withcolor .8*white;
  draw p withpen pencircle scaled 1bp;
endfig;

```



```

beginfig(54)
  u:=1cm;
  pair A,B,C,D;
  A:=(0,0);
  B:=u*dir 60;
  C:=u*dir -60;
  D:=(2u,0);
  draw A withpen pencircle scaled 4bp;
  draw B withpen pencircle scaled 4bp;
  draw C withpen pencircle scaled 4bp;
  draw D withpen pencircle scaled 4bp;
  draw A--D--B--D--C;
  draw A{up}..B;
  draw A{down}..C;
  draw A{dir 30}..B;
  draw A{dir -30}..C;
endfig;

```



```

beginfig(55)
  draw (0,0) .. (1cm,1cm) .. (2cm,0);
endfig;

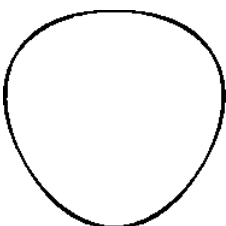
```



```

beginfig(56)
  draw (0,0) .. tension 2 ..
    (1cm,1cm) .. (2cm,0);
endfig;

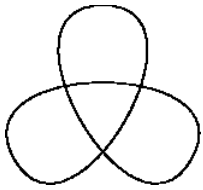
```



```

beginfig(57)
  draw (0,u) {right} ..
    ( u*dir -150 ){dir 120} ..
    ( u*dir -30 ){dir -120} ..
  cycle;
endfig;

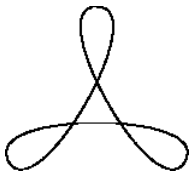
```



```

beginfig(58)
  draw (0,u) {right} .. tension 2 ..
    ( u*dir -150 ){dir 120} .. tension 2 ..
    ( u*dir -30 ){dir -120} .. tension 2 ..
  cycle;
endfig;

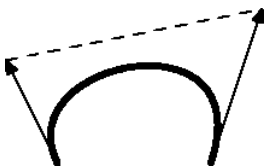
```



```

beginfig(59)
  draw (0,u) {right} .. tension 4 ..
    ( u*dir -150 ){dir 120} .. tension 4 ..
    ( u*dir -30 ){dir -120} .. tension 4 ..
  cycle;
endfig;

```



```

beginfig(60)
  u:=.5cm;
  pair A,B,C,D;
  A:=(0,0); B:=(-u,2u);
  C:=(4u,3u); D:=(3u,0);
  draw A.. controls B and C .. D
    withpen pencircle scaled 2pt;
  draw B--C dashed evenly;
  drawarrow A--B;
  drawarrow D--C;
endfig;

```



```

beginfig(61)
  pair A, B, C, D;
  A = (0,0);
  D = (2u,0);
  B = (-u,2u);
  C = (3u,3u);

  draw A withpen pencircle scaled 4bp;
  draw B withpen pencircle scaled 4bp;
  draw C withpen pencircle scaled 4bp;
  draw D withpen pencircle scaled 4bp;
  draw A .. controls B and C .. D;

  pair a[];
  a[1] := A;
  a[2] := B;
  a[3] := C;
  a[4] := D;

  a[12] := 1/2 [ a[1], a[2] ];
  a[23] := 1/2 [ a[2], a[3] ];
  a[34] := 1/2 [ a[3], a[4] ];

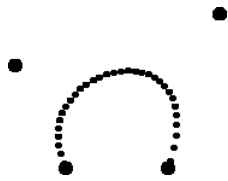
```

```

a[123] := 1/2 [ a[12], a[23] ];
a[234] := 1/2 [ a[23], a[34] ];
a[1234] := 1/2 [ a[123], a[234] ];

draw a[1234] withpen pencircle scaled 4bp;
endfig;

```



```

beginfig(62)
vardef bezier(expr n,A,B,C,D) =
  save a;
  pair a[];
  a[1] := A;
  a[2] := B;
  a[3] := C;
  a[4] := D;

  a[12] := 1/2 [ a[1], a[2] ];
  a[23] := 1/2 [ a[2], a[3] ];
  a[34] := 1/2 [ a[3], a[4] ];
  a[123] := 1/2 [ a[12], a[23] ];
  a[234] := 1/2 [ a[23], a[34] ];
  a[1234] := 1/2 [ a[123], a[234] ];

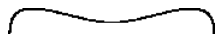
  if n>0:
    bezier(n-1, a[1], a[12], a[123], a[1234]);
    bezier(n-1, a[1234], a[234], a[34], a[4]);
  else:
    draw a[1234] withpen pencircle scaled 2bp;
  fi;
enddef;

pair A, B, C, D;
A = (0,0);
D = (2u,0);
B = (-u,2u);
C = (3u,3u);

draw A withpen pencircle scaled 4bp;
draw B withpen pencircle scaled 4bp;
draw C withpen pencircle scaled 4bp;
draw D withpen pencircle scaled 4bp;

bezier(5,A,B,C,D);
endfig;

```



```

beginfig(63)
draw (0,0){up} .. (1cm, 1mm) .. (2cm,0){down};
endfig;

```



```

beginfig(64)
draw (0,0){up} ... (1cm, 1mm) ... (2cm,0){down};
endfig;

```



```

beginfig(65)
draw (0,0){curl 0} .. (0,1cm)..(1cm,0)..(1cm,1cm);
endfig;

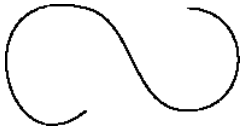
```



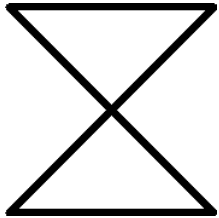
```

beginfig(66)
draw (0,0){curl 1} .. (0,1cm)..(1cm,0)..(1cm,1cm);
endfig;

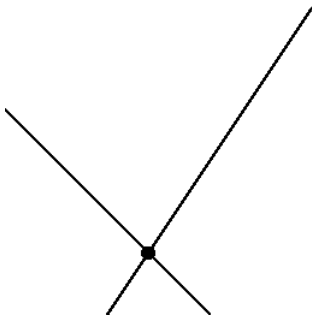
```



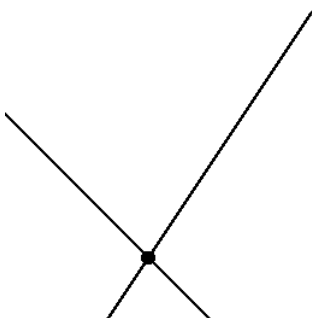
```
beginfig(67)
  draw (0,0){curl 2} .. (0,1cm)..(1cm,0)..(1cm,1cm);
endfig;
```



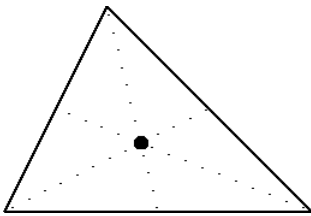
```
beginfig(68)
  pair A,B,C,D;
  xpart A = ypart A = ypart B = xpart C = 0;
  xpart B = ypart C = xpart D = ypart D = 2cm;
  draw A--B--C--D--cycle withpen pencircle scaled 2bp;
endfig;
```



```
beginfig(69)
  pair A,B,C,D,M;
  numeric lambda, mu;
  A=(0,0); B=(2cm,3cm);
  C=(1cm,0); D=(-1cm,2cm);
  M = lambda [A,B];
  M = mu [C,D];
  draw A--B;
  draw C--D;
  draw M withpen pencircle scaled 4bp;
endfig;
```



```
beginfig(70)
  pair A,B,C,D,M;
  A=(0,0); B=(2cm,3cm);
  C=(1cm,0); D=(-1cm,2cm);
  M = whatever [A,B];
  M = whatever [C,D];
  draw A--B;
  draw C--D;
  draw M withpen pencircle scaled 4bp;
endfig;
```



```

beginfig(71)
  pair A,B,C,AA,BB,CC,G;
  A=(0,0); B=(3cm,0); C=(1cm,2cm);
  AA = 1/2 [B,C];
  BB = 1/2 [C,A];
  CC = 1/2 [A,B];
  G = whatever [A,AA];
  G = whatever [B,BB];
  draw A--B--C--cycle;
  draw A--AA dashed withdots;
  draw B--BB dashed withdots;
  draw C--CC dashed withdots;
  draw G withpen pencircle scaled 4bp;
endfig;

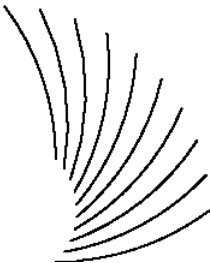
```



```

beginfig(72)
  path p;
  p := fullcircle scaled 5mm;
  draw p;
  draw p shifted (1mm,2mm);
  draw p shifted 2(1mm,2mm);
  draw p shifted 3(1mm,2mm);
  draw p shifted 4(1mm,2mm);
  draw p shifted 5(1mm,2mm);
endfig;

```



```

beginfig(73)
  path p;
  p := (5mm,-5mm) {right} .. (2cm,0);
  draw p;
  draw p rotated 10;
  draw p rotated 20;
  draw p rotated 30;
  draw p rotated 40;
  draw p rotated 50;
  draw p rotated 60;
  draw p rotated 70;
  draw p rotated 80;
  draw p rotated 90;
endfig;

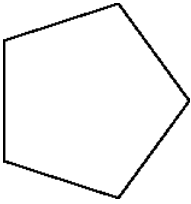
```



```

beginfig(74)
  path p;
  p := fullcircle scaled 5mm;
  draw p;
  draw p xscaled 2;
  draw p xscaled 3;
  draw p xscaled 4;
endfig;

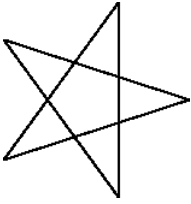
```



```

beginfig(75)
  pair A,B,C,D,E;
  A := (1cm,0);
  B := A rotated 72;
  C := B rotated 72;
  D := C rotated 72;
  E := D rotated 72;
  draw A--B--C--D--E--cycle;
endfig;

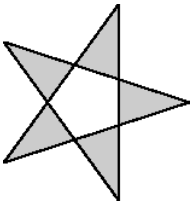
```



```

beginfig(76)
  pair A,B,C,D,E;
  A := (1cm,0);
  B := A rotated 72;
  C := B rotated 72;
  D := C rotated 72;
  E := D rotated 72;
  draw A--C--E--B--D--cycle;
endfig;

```



```

beginfig(77)
  pair A,B,C,D,E;
  A := (1cm,0);
  B := A rotated 72;
  C := B rotated 72;
  D := C rotated 72;
  E := D rotated 72;
  pair AA, BB, CC, DD, EE;
  AA = whatever [A, C];
  AA = whatever [B, D];
  BB = whatever [B, D];
  BB = whatever [C, E];
  CC = whatever [C, E];
  CC = whatever [D, A];
  DD = whatever [D, A];
  DD = whatever [E, B];
  EE = whatever [E, B];
  EE = whatever [A, C];
  fill A--C--E--B--D--cycle withcolor .8white;
  fill AA--BB--CC--DD--EE--cycle withcolor white;
  draw A--C--E--B--D--cycle;
endfig;

```



```

beginfig(78)
  path p;
  p := (0,0) -- (1cm,0);
  drawarrow p withpen pencircle scaled 2bp;
  drawarrow p zscaled (1,2);
endfig;

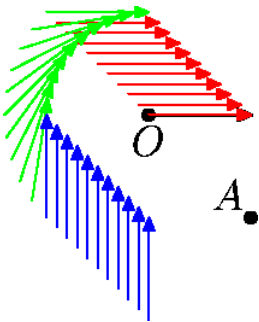
```



```

beginfig(79)
  u:=1cm;
  path p;      p := (0,0) -- (u,0);
  pair A;      A := (u,-u);
  numeric a;   a := 90;
  drawarrow p withpen pencircle scaled 1bp;
  drawarrow p rotatedaround( A, a );
  drawarrow p shifted -A rotated a shifted A
    withpen pencircle scaled 1bp dashed withdots;
endfig;

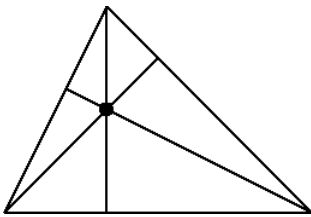
```



```

beginfig(80)
  path p;      p := (0,0) -- (u,0);
  pair A;      A := (u,-u);
  numeric a;   a := 90;
  drawarrow p withpen pencircle scaled 1bp;
  draw A withpen pencircle scaled 4bp;
  label ulft ( btex $\textit{A}$ etex, A );
  draw (0,0) withpen pencircle scaled 4bp;
  label bot ( btex $\textit{O}$ etex, (0,0) );
  for i=0 upto 10:
    drawarrow p shifted -(i*A/10) withcolor red;
  endfor;
  for i=0 upto 10:
    drawarrow p shifted -A rotated (i*a/10) withcolor green;
  endfor;
  for i=0 upto 10:
    drawarrow p shifted -A rotated a shifted (i*A/10) withcolor blue;
  endfor;
endfig;

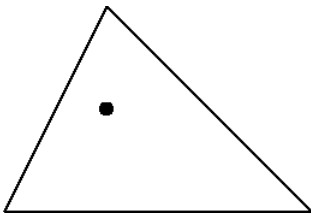
```



```

beginfig(81)
  pair A,B,C,AA,BB,CC,H;
  A=(0,0); B=(3cm,0); C=(1cm,2cm);
  AA - A = whatever * (B-C) rotated 90;
  AA = whatever [B,C];
  BB - B = whatever * (A-C) rotated 90;
  BB = whatever [A,C];
  CC - C = whatever * (A-B) rotated 90;
  CC = whatever [A,B];
  H = whatever [A,AA];
  H = whatever [B,BB];
  draw A--B--C--cycle;
  draw A--AA;
  draw B--BB;
  draw C--CC;
  draw H withpen pencircle scaled 4bp;
endfig;

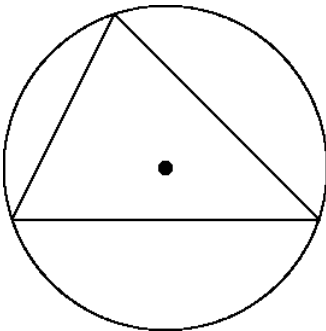
```



```

beginfig(82)
  pair A,B,C,H;
  A=(0,0); B=(3cm,0); C=(1cm,2cm);
  H - A = whatever * (B-C) rotated 90;
  H - B = whatever * (A-C) rotated 90;
  draw A--B--C--cycle;
  draw H withpen pencircle scaled 4bp;
endfig;

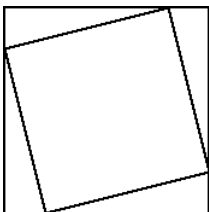
```



```

beginfig(83)
  pair A,B,C,O;
  A=(0,0); B=(3cm,0); C=(1cm,2cm);
  O - 1/2[B,C] = whatever * (B-C) rotated 90;
  O - 1/2[A,B] = whatever * (A-B) rotated 90;
  draw A--B--C--cycle;
  draw O withpen pencircle scaled 4bp;
  draw fullcircle scaled 2abs(O-A) shifted O;
endfig;

```



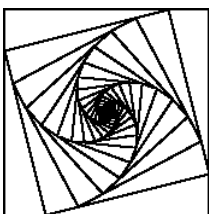
```

beginfig(84)
  pair A,B,C,D;
  u:=2cm;
  A=(0,0); B=(u,0); C=(u,u); D=(0,u);

  transform T;
  A transformed T = 1/5[A,B];
  B transformed T = 1/5[B,C];
  C transformed T = 1/5[C,D];

  path p;
  p = A--B--C--D--cycle;
  draw p;
  draw p transformed T;
endfig;

```



```

beginfig(85)
  pair A,B,C,D;
  u:=2cm;
  A=(0,0); B=(u,0); C=(u,u); D=(0,u);

  transform T;
  A transformed T = 1/5[A,B];

```

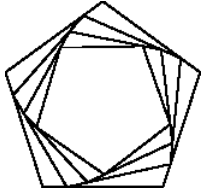
```

B transformed T = 1/5[B,C];
C transformed T = 1/5[C,D];

path p;
p = A--B--C--D--cycle;
for i=0 upto 100:
  draw p;
  p:= p transformed T;
endfor;

endfig;

```



```

beginfig(86)
u:=lcm;
pair A,B,C,D,E;
A := (0,u);
B := A rotated 72;
C := B rotated 72;
D := C rotated 72;
E := D rotated 72;
transform T;
A transformed T = 1/5[A,B];
B transformed T = 1/5[B,C];
C transformed T = 1/5[C,D];
path p;
p := A--B--C--D--E--cycle;
draw p;
p := p transformed T; draw p;
p := p transformed T; draw p;
p := p transformed T; draw p;
endfig;

```



```

beginfig(87)
u:=3mm;
fill fullcircle scaled 2u withcolor .8white;
fill fullcircle scaled u shifted (u*dir30)
  withcolor .8white;
fill fullcircle scaled u shifted (u*dir150)
  withcolor .8white;
endfig;

```



```

beginfig(88)
u:=3mm;
transform T;
(0,0) transformed T = (0,0);
(1,0) transformed T = (1,1);
(0,1) transformed T = (1,0);

fill fullcircle scaled 2u transformed T withcolor .8white;
fill fullcircle scaled u shifted (u*dir30) transformed T
  withcolor .8white;
fill fullcircle scaled u shifted (u*dir150) transformed T
  withcolor .8white;
endfig;

```



```

beginfig(89)

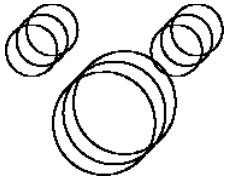
```

```

u:=3mm;
transform T;
xpart T = ypart T = 0;
xxpart T = 1;
yypart T = 2;
xypart T = 3;
yyypart T = 4;

fill fullcircle scaled 2u transformed T withcolor .8white;
fill fullcircle scaled u shifted (u*dir30) transformed T
  withcolor .8white;
fill fullcircle scaled u shifted (u*dir150) transformed T
  withcolor .8white;
endfig;

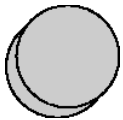
```



```

beginfig(90)
  draw fullcircle scaled 1cm;
  draw fullcircle scaled 5mm shifted (1cm*dir45);
  draw fullcircle scaled 5mm shifted (1cm*dir135);
  picture mypicture;
  mypicture := currentpicture;
  currentpicture := nullpicture;
  draw mypicture;
  draw mypicture shifted (1mm,1mm);
  draw mypicture shifted (2mm,2mm);
endfig;

```



```

beginfig(91)
  picture pic;
  pic := nullpicture;
  addto pic contour fullcircle scaled 1cm
    withcolor .8white;
  addto pic doublepath fullcircle scaled 1cm
    withpen pencircle scaled .5bp;
  addto pic also pic shifted (1mm,1mm);
  draw pic;
endfig;

```



```

beginfig(92)
  u:=3mm;
  picture mickey;
  mickey := nullpicture;
  addto mickey contour fullcircle scaled 2u
    withcolor .8white;
  addto mickey contour fullcircle scaled u
    shifted (u*dir30) withcolor .8white;
  addto mickey contour fullcircle scaled u
    shifted (u*dir150)
    withcolor .8white;
  draw mickey;
endfig;

```



```

beginfig(93)
  u:=3mm;
  picture mickey;
  mickey := nullpicture;
  addto mickey contour fullcircle scaled 2u
    withcolor .8white;
  addto mickey contour fullcircle scaled u
    shifted (u*dir30) withcolor .8white;
  addto mickey contour fullcircle scaled u
    shifted (u*dir150) withcolor .8white;

  transform T;
  (0,0) transformed T = (0,0);
  (1,0) transformed T = (1,1);
  (0,1) transformed T = (1,0);

```

```

draw mickey transformed T;
endfig;

```



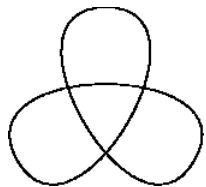
```

beginfig(94)
  u:=3mm;
  picture mickey;
  fill fullcircle scaled 2u withcolor .8white;
  fill fullcircle scaled u shifted (u*dir30)
    withcolor .8white;
  fill fullcircle scaled u shifted (u*dir150)
    withcolor .8white;
  mickey := currentpicture;
  currentpicture := nullpicture;

  transform T;
  (0,0) transformed T = (0,0);
  (1,0) transformed T = (1,1);
  (0,1) transformed T = (1,0);

  draw mickey transformed T;
endfig;

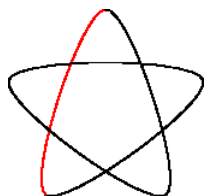
```



```

beginfig(95)
  pair A,B;
  path p;
  A = (0,1cm);
  B = A rotated 120;
  p = A{dir 0} .. tension 2 .. B{dir 120};
  draw p;
  draw p rotated 120;
  draw p rotated -120;
endfig;

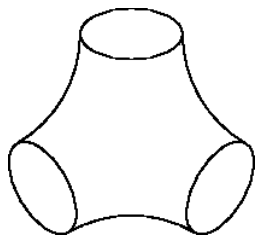
```



```

beginfig(96)
  pair A,B;
  path p;
  numeric n;
  n:=5;
  A = (0,1cm);
  B = A rotated (2*360/n);
  p = A{dir 180} .. tension 4 .. B{dir (180+2*360/n)};
  draw p withcolor red;
  draw p rotated (1*360/n);
  draw p rotated (2*360/n);
  draw p rotated (3*360/n);
  draw p rotated (4*360/n);
endfig;

```



```

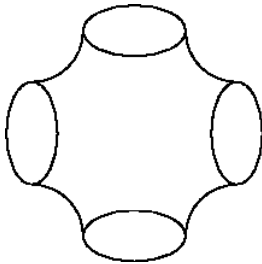
beginfig(97)
  path c[], l[];
  c[0] = fullcircle xscaled 1cm yscaled .5cm
    shifted (0,1cm);
  c[1] = c[0] rotated 120;
  c[2] = c[1] rotated 120;

```

```

pair A;
A = (-.5cm,1cm);
l[0] = A{down} ..
      (A xscaled -1 rotated 120){-down rotated 120};
l[1] = l[0] rotated 120;
l[2] = l[1] rotated 120;
draw c[0]; draw c[1]; draw c[2];
draw l[0]; draw l[1]; draw l[2];
endfig;

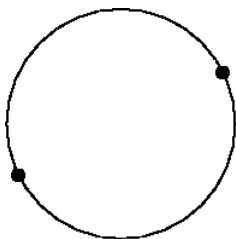
```



```

beginfig(98)
path c[], l[];
c[0] = fullcircle xscaled 1cm yscaled .5cm
      shifted (0,1cm);
c[1] = c[0] rotated (360/4);
c[2] = c[1] rotated (360/4);
c[3] = c[2] rotated (360/4);
pair A;
A = (-.5cm,1cm);
l[0] = A{down} ..
      (A xscaled -1 rotated (360/4))
      {-down rotated (360/4)};
l[1] = l[0] rotated (360/4);
l[2] = l[1] rotated (360/4);
l[3] = l[2] rotated (360/4);
draw c[0]; draw c[1]; draw c[2]; draw c[3];
draw l[0]; draw l[1]; draw l[2]; draw l[3];
endfig;

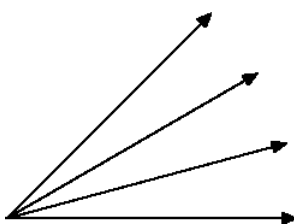
```



```

beginfig(99)
pair A, B;
A := (0,0); B := (2cm,1cm);
draw A withpen pencircle scaled 4bp;
draw B withpen pencircle scaled 4bp;
draw fullcircle scaled abs(B-A) shifted 1/2[A,B];
endfig;

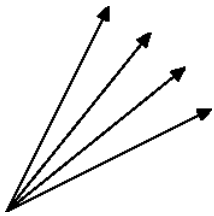
```



```

beginfig(100)
pair A;
A:=(2cm,2cm);
drawarrow origin--A;
drawarrow (origin--A) rotated -1/3 angle(A);
drawarrow (origin--A) rotated -2/3 angle(A);
drawarrow (origin--A) rotated -angle(A);
endfig;

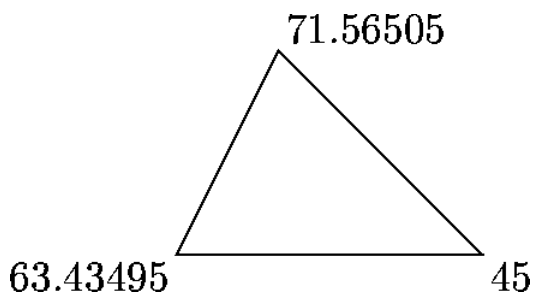
```



```

beginfig(101)
  pair A,B;
  A:=(1cm,2cm); B:=(2cm,1cm);
  numeric alpha;
  alpha = angle(A) - angle(B);
  drawarrow origin--A;
  drawarrow origin--B;
  drawarrow (origin--A) rotated -1/3 alpha;
  drawarrow (origin--A) rotated -2/3 alpha;
  drawarrow (origin--A) rotated -alpha;
endfig;

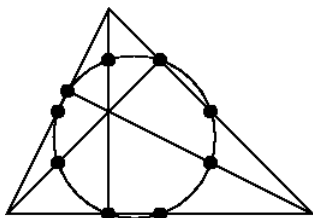
```



```

beginfig(102)
  pair A,B,C;
  A=(0,0); B=(3cm,0); C=(1cm,2cm);
  draw A--B--C--cycle;
  label.llft(TEX decimal(angle(C-A)-angle(B-A)), A);
  label.lrt(TEX decimal(angle(A-B)-angle(C-B)), B);
  label.urrt(TEX decimal(angle(B-C)-angle(A-C)), C);
endfig;

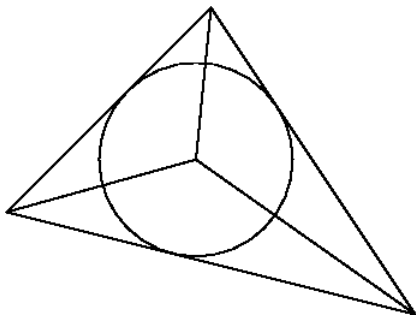
```



```

beginfig(103)
  pair A,AA,B,BB,C,CC,O,H;
  A=(0,0); B=(3cm,0); C=(1cm,2cm);
  AA = 1/2[B,C];
  BB = 1/2[A,C];
  CC = 1/2[A,B];
  O = 1/2[BB,CC] = whatever * (BB-CC) rotated 90;
  O = 1/2[AA,BB] = whatever * (AA-BB) rotated 90;
  draw A--B--C--cycle;
  draw AA withpen pencircle scaled 4bp;
  draw BB withpen pencircle scaled 4bp;
  draw CC withpen pencircle scaled 4bp;
  draw fullcircle scaled 2abs(O-AA) shifted O;
  % Il faut aussi tracer les hauteurs
  pair AA,BB,CC;
  AA - A = whatever * (B-C) rotated 90;
  AA = whatever [B,C];
  BB - B = whatever * (A-C) rotated 90;
  BB = whatever [A,C];
  CC - C = whatever * (A-B) rotated 90;
  CC = whatever [A,B];
  draw A--AA; draw B--BB; draw C--CC;
  draw AA withpen pencircle scaled 4bp;
  draw BB withpen pencircle scaled 4bp;
  draw CC withpen pencircle scaled 4bp;
  % Il passe aussi par le milieu de HA, HB, HC
  H = whatever [A,AA];
  H = whatever [B,BB];
  draw 1/2 [A,H] withpen pencircle scaled 4bp;
  draw 1/2 [B,H] withpen pencircle scaled 4bp;
  draw 1/2 [C,H] withpen pencircle scaled 4bp;
endfig;

```



```

beginfig(104)
  pair A,B,C,M,h;
  u:=2cm;
  A=(0,0); B=(2u,-.5u); C=(u,u);
  draw A--B--C--cycle;
  (M-A) = whatever * (
    (A-C) rotated 1/2( angle(B-A) - angle(C-A)) );
  (M-B) = whatever * (
    (B-A) rotated 1/2( angle(C-B) - angle(A-B)) );
  draw M--A; draw M--B; draw M--C;
  M-h = whatever * (B-C) rotated 90;
  h = whatever[B,C];
  draw fullcircle scaled 2 abs(M-h) shifted M;
endfig;

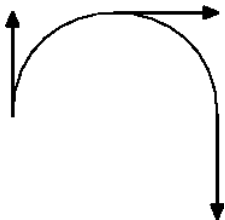
```



```

beginfig(105)
  path p;
  p = (0,0){up} .. (2cm,0){down};
  draw p;
  draw point 0 of p withpen pencircle scaled 4bp;
  draw point .5 of p withpen pencircle scaled 4bp;
  draw point 1 of p withpen pencircle scaled 4bp;
endfig;

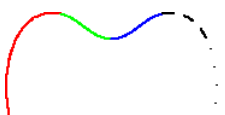
```



```

beginfig(106)
  path p;
  p = (0,0){up} .. (2cm,0){down};
  draw p;
  pair A;
  A := point 0 of p;
  B := A + 1cm*unitvector(direction 0 of p);
  drawarrow A--B withpen pencircle scaled 1bp;
  A := point .5 of p;
  B := A + 1cm*unitvector(direction .5 of p);
  drawarrow A--B withpen pencircle scaled 1bp;
  A := point 1 of p;
  B := A + 1cm*unitvector(direction 1 of p);
  drawarrow A--B withpen pencircle scaled 1bp;
endfig;

```



```

beginfig(107)
  u:=5mm;
  path p;
  p = (0,0) {curl 0} .. (u,2u) .. (2u,1.5u)
    .. (3u,2u) .. {curl 0} (4u,0);
  draw subpath(0,1) of p withcolor red;
  draw subpath(1,2) of p withcolor green;
  draw subpath(2,3) of p withcolor blue;
  draw subpath(3,3.5) of p dashed evenly;
  draw subpath(3.5,4) of p dashed withdots;
endfig;

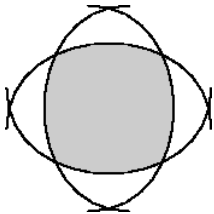
```



```

beginfig(108)
  u:=1cm;
  path p,q;
  p := (0,0){up} .. (u,2u){up};
  q := (u,0){up} .. (0,2u){up};
  draw p;
  draw subpath(0,.4) of q withpen pencircle scaled 1bp;
  draw subpath(.6,1) of q withpen pencircle scaled 1bp;
endfig;

```



```

beginfig(109)
  u:=1cm;
  path a,b,c,d;
  a = (-u,-.2u){up} .. tension 1.2 .. (u,-.2u){down};
  b = a rotated 90;
  c = b rotated 90;
  d = c rotated 90;
  fill buildcycle(a,b,c,d) withcolor .8white;
  draw a; draw b; draw c; draw d;
endfig;

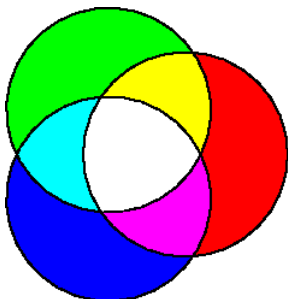
```



```

beginfig(110)
  u:=1cm;
  path c[];
  c[1] := fullcircle scaled u;
  c[2] := c[1] shifted (0,.5u);
  draw c[1] dashed evenly;
  draw c[2] dashed evenly;
  draw buildcycle(c[1],c[2]) withpen pencircle scaled 1bp;
endfig;

```

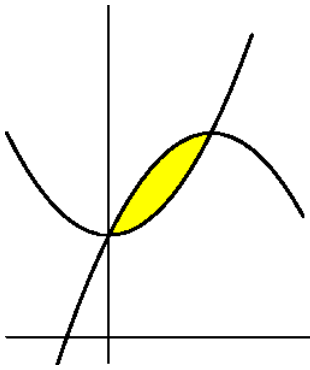


```

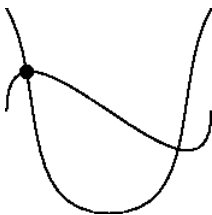
beginfig(111)
  path a,b,c;
  a = fullcircle scaled 2u shifted (.5u,0);
  b = a rotated (360/3);
  c = b rotated (360/3);
  fill a withcolor red;
  fill b withcolor green;
  fill c withcolor blue;
  fill buildcycle(a,b) withcolor red + green;
  fill buildcycle(b,c) withcolor green + blue;
  fill buildcycle(c,a) withcolor blue + red;
  fill buildcycle(a,b,c) withcolor white;
  draw a; draw b; draw c;

```

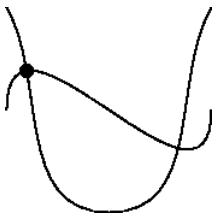

endfig;



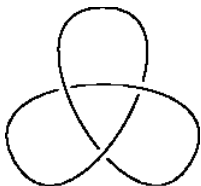
```
beginfig(112)
  def compute_curve(suffix f)(expr xmin, xmax, xinc) =
    ( (xmin,f(xmin))
      for x=xmin+xinc step xinc until xmax:
        .. (x,f(x))
      endfor )
  enddef;
  vardef f(expr x) = x**2 + 1 enddef;
  vardef g(expr x) = 2 - (x-1)**2 enddef;
  path p, q;
  p := compute_curve(f, -1, 1.5, .1) scaled 1cm;
  q := compute_curve(g, -.5, 2, .1) scaled 1cm;
  fill buildcycle(p,reverse q) withcolor red+green;
  draw p withpen pencircle scaled 1bp;
  draw q withpen pencircle scaled 1bp;
  draw (-1cm,0) -- (2cm,0);
  draw (0,g(-.5)*1cm) -- (0,f(1.5)*1cm);
endfig;
```



```
beginfig(113)
  path p, q;
  p = (0,0){up} .. (2cm,0){up};
  q = (0,1cm){dir -60}..(1cm,-1cm)..{dir 60}(2cm,1cm);
  draw p; draw q;
  draw p intersectionpoint q withpen pencircle scaled 4bp;
endfig;
```



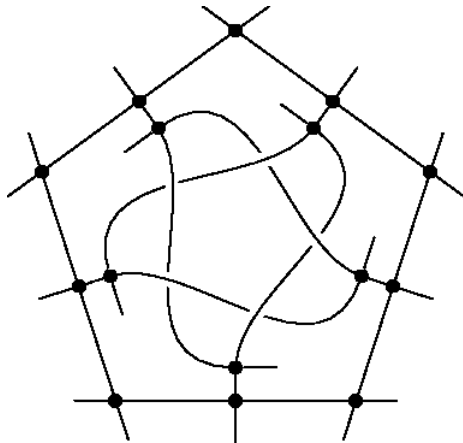
```
beginfig(114)
  path p, q;
  p = (0,0){up} .. (2cm,0){up};
  q = (0,1cm){dir -60}..(1cm,-1cm)..{dir 60}(2cm,1cm);
  draw p; draw q;
  numeric a,b;
  (a,whatever) = p intersectiontimes q;
  draw point a of p withpen pencircle scaled 4bp;
endfig;
```



```

beginfig(115)
  pair A,B;
  path p;
  A = (0,1cm);
  B = A rotated 120;
  p = A{dir 0} .. tension 2 .. B{dir 120};
  numeric a;
  (a,whatever) = p intersectiontimes (p rotated 120);
  draw subpath(0,a-.02) of p;
  draw subpath(a+.02,1) of p;
  draw subpath(0,a-.02) of p rotated 120;
  draw subpath(a+.02,1) of p rotated 120;
  draw subpath(0,a-.02) of p rotated -120;
  draw subpath(a+.02,1) of p rotated -120;
endfig;

```



```

beginfig(116)
  u:=2cm;
  pair A[], B[], C[], D[], E[];
  path p[];

  A[0] = u*up;
  for i=1 upto 10:
    A[i] := A[i-1] rotated 72;
  endfor;
  for i=0 upto 4:
    p[i] := A[i]--A[i+1];
    draw p[i];
    draw (point 1 of p[i]) --
      ( (point 1 of p[i]) + 4mm*unitvector(direction 1 of p[i]));
    draw (point 0 of p[i]) --
      ( (point 0 of p[i]) - 4mm*unitvector(direction 0 of p[i]));
  endfor;

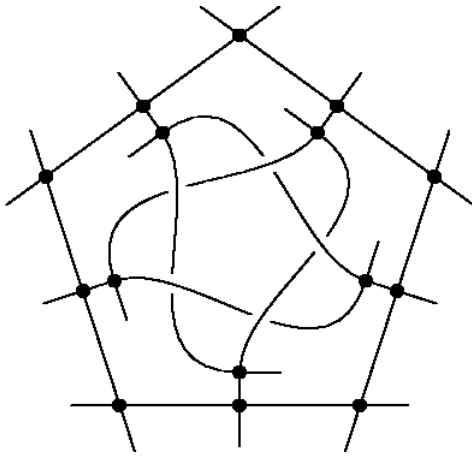
  for i=0 upto 9:
    B[i] := 1/2[ A[i], A[i+1] ];
  endfor;
  B[5]:=B[0];

  for i=0 upto 9:
    C[i] := .8*B[i];
  endfor;

  for i=0 upto 4:
    p[i] := B[i] --- C[i] .. C[i+2]{dir 72i};
    draw p[i];
    draw (point 2 of p[i]) --
      ( (point 2 of p[i]) + 4mm*unitvector(direction 2 of p[i]));
    draw (point 0 of p[i]) --
      ( (point 0 of p[i]) - 4mm*unitvector(direction 0 of p[i]));
  endfor;
  for i=0 upto 4:
    draw subpath(1,1.4) of p[i] withpen pencircle scaled 4bp withcolor white;
    draw subpath(0,1.5) of p[i];
  endfor;

  for i=0 upto 4:
    draw A[i] withpen pencircle scaled 4bp;
    draw B[i] withpen pencircle scaled 4bp;
    draw C[i] withpen pencircle scaled 4bp;
  endfor;
endfig;

```



```

beginfig(117)
  u:=2cm;
  pair A, B, C, D, E;
  path p, q, r;

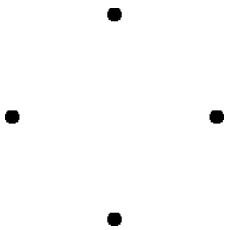
  A = u*up;
  p := (-.2)[ A, A rotated 72 ] -- (1.2)[ A, A rotated 72 ];
  for i=0 upto 5:
    draw p rotated 72i;
  endfor;
  B := 1/2[ A, A rotated 72 ];
  C := .8*B;

  p := B --- C .. (C rotated (2*72)){right};
  % On allonge le chemin p
  p := ( (point 0 of p) - 4mm*unitvector(direction 0 of p))
  --
  (point 0 of p)
  & p &
  (point 2 of p)
  --
  ( (point 2 of p) + 4mm*unitvector(direction 2 of p));

  E = p intersectionpoint (p rotated 72);
  q := p cutbefore fullcircle scaled -2mm shifted E;
  r := p cutafter fullcircle scaled 2mm shifted E;

  for i=0 upto 4:
    draw q rotated 72i;
    draw r rotated 72i;
    draw A rotated 72i withpen pencircle scaled 4bp;
    draw B rotated 72i withpen pencircle scaled 4bp;
    draw C rotated 72i withpen pencircle scaled 4bp;
  endfor;
endfig;

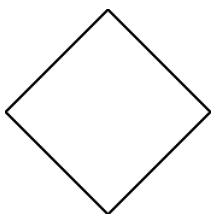
```



```

beginfig(118)
  for i=0 step 1 until 3:
    draw 1cm*right rotated (i*90)
    withpen pencircle scaled 4bp;
  endfor;
endfig;

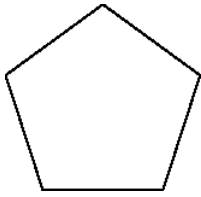
```



```

beginfig(119)
  draw for i=0 step 1 until 3:
    1cm*right rotated (i*90) --
  endfor cycle;
endfig;

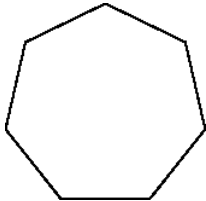
```



```

beginfig(120)
  n:=5;
  draw for i=0 step 1 until n-1:
    1cm*up rotated (i*360/n) --
  endfor cycle;
endfig;

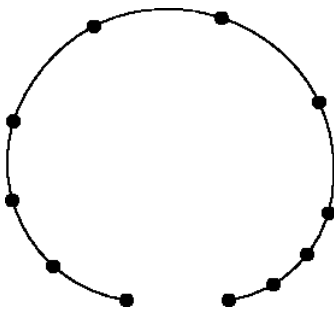
```



```

beginfig(121)
  n:=7;
  draw for i=0 step 1 until n-1:
    1cm*up rotated (i*360/n) --
  endfor cycle;
endfig;

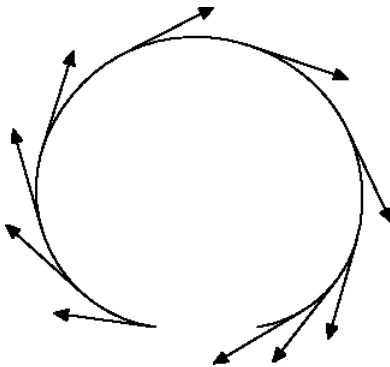
```



```

beginfig(122)
  path p;
  p = (0,0) .. (-1cm,2cm) .. (2cm,1cm) .. (1cm,0);
  draw p;
  n:=10;
  for i=0 step 1 until n:
    draw point (i/n*length(p)) of p
    withpen pencircle scaled 4bp;
  endfor;
endfig;

```

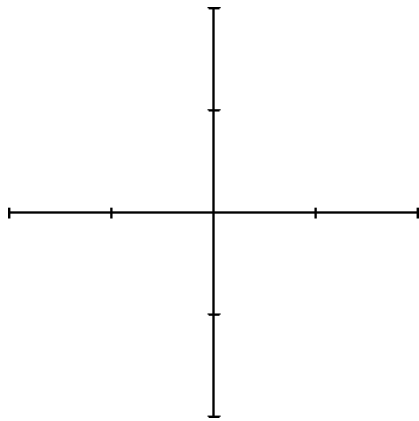


```

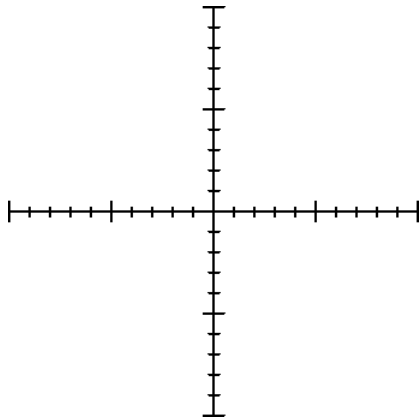
beginfig(123)
  path p;
  p = (0,0) .. (-1cm,2cm) .. (2cm,1cm) .. (1cm,0);
  draw p;
  n:=10;
  for i=0 step length(p)/n until length(p):
    drawarrow (point i of p) --
    1cm * unitvector(direction i of p)
    shifted point i of p;
  endfor;

```

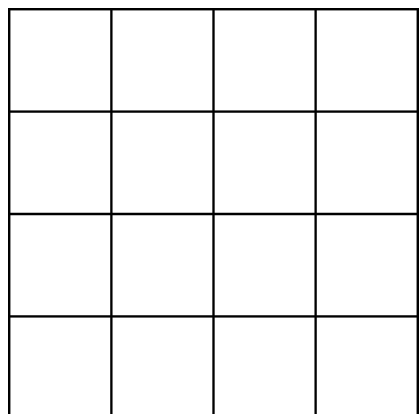
```
endfig;
```



```
beginfig(124)
u:=1cm;
draw (-2u,0)--(2u,0);
draw (0,-2u)--(0,2u);
for i=-2u step u until 2u:
  draw (i,u/20)--(i,-u/20);
  draw (u/20,i)--(-u/20,i);
endfor;
endfig;
```



```
beginfig(125)
u:=1cm;
draw (-2u,0)--(2u,0);
draw (0,-2u)--(0,2u);
for i=-2u step u until 2u:
  draw (i,u/10)--(i,-u/10);
  draw (u/10,i)--(-u/10,i);
endfor;
for i=-2u step u/5 until 2u:
  draw (i,u/20)--(i,-u/20);
  draw (u/20,i)--(-u/20,i);
endfor;
endfig;
```

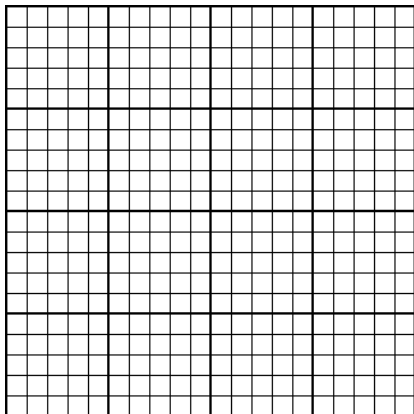


```
beginfig(126)
u:=1cm;
```

```

draw (-2u,0)--(2u,0);
draw (0,-2u)--(0,2u);
for i=-2u step u until 2u:
  draw (i,2u)--(i,-2u);
  draw (2u,i)--(-2u,i);
endfor;
endfig;

```



```

beginfig(127)
u:=1cm;
draw (-2u,0)--(2u,0);
draw (0,-2u)--(0,2u);
for i=-2u step u until 2u:
  draw (i,2u)--(i,-2u);
  draw (2u,i)--(-2u,i);
endfor;
for i=-2u step u/5 until 2u:
  draw (i,2u)--(i,-2u) withpen pencircle scaled .2bp;
  draw (2u,i)--(-2u,i) withpen pencircle scaled .2bp;
endfor;
endfig;

```



```

beginfig(128)
u := 5mm;
% vardef est n^e9cessaire pour pouvoir passer f en argument
vardef f(expr x) = x**2 -.1 enddef;
def axes(expr xmin,xmax,ymin,ymax) =
  draw ( (xmin,0) -- (xmax,0) ) scaled u;
  draw ( (0,ymin) -- (0,ymax) ) scaled u;
enddef;
def courbe(suffix f)(expr xmin, xmax, M) =
  draw ( ( xmin, f(xmin) )
  for i=1 upto M:
    -- ( xmin + (i/M)*(xmax - xmin), f( xmin + (i/M)*(xmax - xmin) ))
  endfor ) scaled u;
enddef;
vardef newton(suffix f)(expr y, h, M) =
  save x,t;
  numeric x,t; x:=y;
  for i=1 upto M:
    t := x - f(x)/( (f(x+h) - f(x))/h );
    draw ( (x,f(x)) -- (t,0) -- (t,f(t)) ) scaled u;
    x := t;
  endfor;
enddef;
axes(-.5,2,-.5,4);
courbe(f,-.5,2, 100);
newton(f, 2, .01, 10);
endfig;

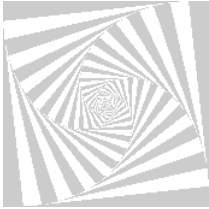
```



```

beginfig(129)
  transform T;
  u:=lcm;
  z0=(0,0); z1=(2u,0); z3 = z1 rotated 90; z2 = z1+z3;
  z0 transformed T = .1[z0,z1];
  z1 transformed T = .1[z1,z2];
  z2 transformed T = .1[z2,z3];
  path p;
  p = z0--z1--z2--z3--cycle;
  fill p withcolor .8*white;
  fill p transformed T withcolor white;
endfig;

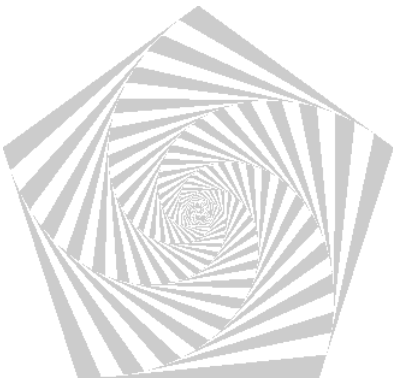
```



```

beginfig(130)
  transform T;
  u:=lcm;
  z0=(0,0); z1=(2u,0); z3 = z1 rotated 90; z2 = z1+z3;
  z0 transformed T = .1[z0,z1];
  z1 transformed T = .1[z1,z2];
  z2 transformed T = .1[z2,z3];
  path p;
  p = z0--z1--z2--z3--cycle;
  for i=0 upto 100:
    fill p withcolor .8*white;
    p := p transformed T;
    fill p withcolor white;
    p := p transformed T;
  endfor;
endfig;

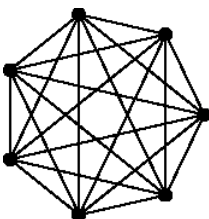
```



```

beginfig(131)
  transform T;
  u:=lcm;
  z1=(0,2u);
  n := 5;
  for i=1 upto n-1:
    z[i+1] = z1 rotated (360*i/n);
  endfor;
  z1 transformed T = .1[z1,z2];
  z2 transformed T = .1[z2,z3];
  z3 transformed T = .1[z3,z4];
  path p;
  p = for i=1 upto n: z[i] -- endfor cycle;
  for i=0 upto 100:
    fill p withcolor .8*white;
    p := p transformed T;
    fill p withcolor white;
    p := p transformed T;
  endfor;
endfig;

```



```

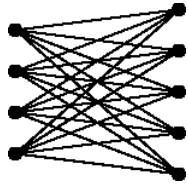
beginfig(132)
  u:=lcm;

```

```

pair A[];
numeric n; n:=7;
A[0] = (u,0);
for i=1 upto n-1:
  A[i] = A[0] rotated (360/n*i);
endfor;
for i=0 upto n-1:
  draw A[i] withpen pencircle scaled 4bp;
  for j=0 upto n-1:
    if i<>j: draw A[i]--A[j] fi;
  endfor;
endfor;
endfig;

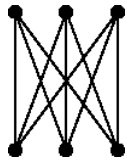
```



```

beginfig(133)
u:=2cm;
numeric n,m; n:=4; m:=5;
pair A[], B[];
for i=1 upto n-1: A[i+1]-A[i] = (0,.2u); endfor;
for j=1 upto m-1: B[j+1]-B[j] = (0,.2u); endfor;
(0,0) for i=1 upto n: + A[i] endfor = (0,0);
(0,0) for j=1 upto m: + B[j] endfor = (4u,0);
for i=1 upto n:
  draw A[i] withpen pencircle scaled 4bp;
endfor;
for j=1 upto m:
  draw B[j] withpen pencircle scaled 4bp;
endfor;
for i=1 upto n:
  for j=1 upto m:
    draw A[i]--B[j];
  endfor;
endfor;
endfig;

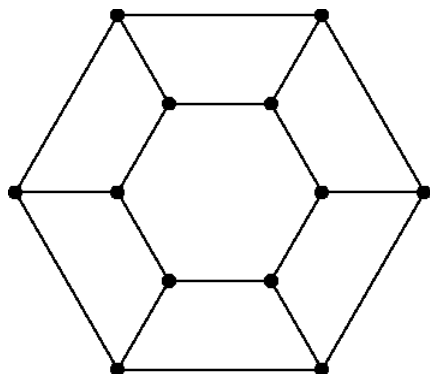
```



```

beginfig(134)
u:=lcm;
numeric n,m; n:=3; m:=3;
pair A[], B[];
for i=1 upto n-1: A[i+1]-A[i] = (.5u,0); endfor;
for j=1 upto m-1: B[j+1]-B[j] = (.5u,0); endfor;
(0,0) for i=1 upto n: + A[i] endfor = (0,0);
(0,0) for j=1 upto m: + B[j] endfor = (0,4u);
for i=1 upto n:
  draw A[i] withpen pencircle scaled 4bp;
endfor;
for j=1 upto m:
  draw B[j] withpen pencircle scaled 4bp;
endfor;
for i=1 upto n:
  for j=1 upto m:
    draw A[i]--B[j];
  endfor;
endfor;
endfig;

```



```

beginfig(135)
pair A[], B[];

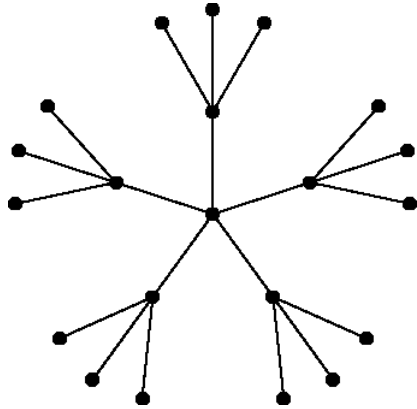
```



```

numeric n; n:=6;
for i=0 upto n-1:
  A[i] = 1cm * right rotated (i*360/n);
  B[i] = 2cm * right rotated (i*360/n);
endfor;
A[n] = A[0]; B[n] = B[0];
for i=0 upto n-1:
  draw A[i] -- A[i+1] -- B[i+1] -- B[i];
  draw A[i] withpen pencircle scaled 4bp;
  draw B[i] withpen pencircle scaled 4bp;
endfor;
endfig;

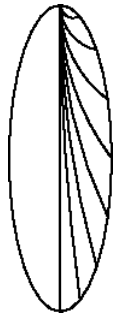
```



```

beginfig(136)
numeric n; n:=5;
pair O,A,B,C,D;
O = (0,0);
A = 1cm*up;
B = 2cm*up rotatedabout(A,30);
C = 2cm*up;
D = 2cm*up rotatedabout(A,-30);
for i=0 upto n-1:
  draw (O--A--C) rotated (i*360/n);
  draw (B--A--D) rotated (i*360/n);
  draw A rotated (i*360/n) withpen pencircle scaled 4bp;
  draw B rotated (i*360/n) withpen pencircle scaled 4bp;
  draw C rotated (i*360/n) withpen pencircle scaled 4bp;
  draw D rotated (i*360/n) withpen pencircle scaled 4bp;
endfor;
draw O withpen pencircle scaled 4bp;
endfig;

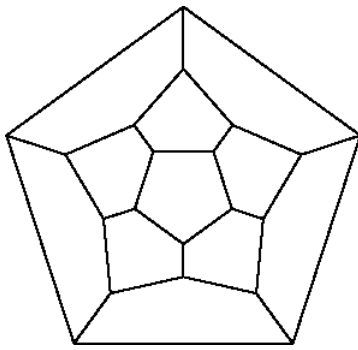
```



```

beginfig(137)
path p; u:=1cm;
p = fullcircle xscaled -u yscaled 3u;
draw p;
for i=2 step .5 until 6:
  draw (point 2 of p){down} .. (point i of p);
endfor;
endfig;

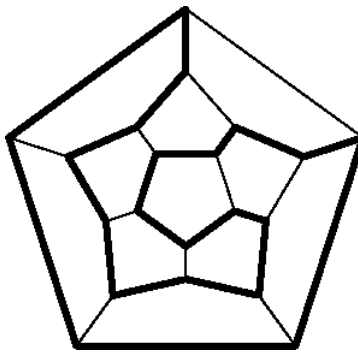
```



```

beginfig(138)
  pair P[], Q[], R[], S[];
  u:=.5cm;
  for i=0 upto 4:
    P[i] = u* down rotated (i*360/5);
  endfor;
  P[5] = P[0];
  for i=0 upto 4:
    Q[i] = 3*( 1/2[ P[i], P[i+1] ] );
  endfor;
  Q[5] = Q[0];
  for i=0 upto 4:
    R[i] = 1/3( Q[i] + Q[i+1] + P[i+1] );
  endfor;
  R[5] = R[0];
  for i=0 upto 5:
    S[i] = 1.5*Q[i];
  endfor;
  for i=0 upto 4:
    draw P[i] -- P[i+1];
    draw P[i+1] -- R[i];
    draw Q[i] -- R[i];
    draw R[i] -- Q[i+1];
    draw Q[i] -- S[i];
    draw S[i] -- S[i+1];
  endfor;
endfig;

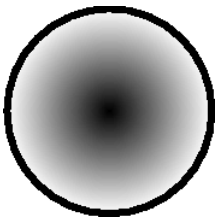
```



```

beginfig(139)
  pair P[], Q[], R[], S[];
  u:=.5cm;
  for i=0 upto 4:
    P[i] = u* down rotated (i*360/5);
  endfor;
  P[5] = P[0];
  for i=0 upto 4:
    Q[i] = 3*( 1/2[ P[i], P[i+1] ] );
  endfor;
  Q[5] = Q[0];
  for i=0 upto 4:
    R[i] = 1/3( Q[i] + Q[i+1] + P[i+1] );
  endfor;
  R[5] = R[0];
  for i=0 upto 5:
    S[i] = 1.5*Q[i];
  endfor;
  for i=0 upto 4:
    draw P[i] -- P[i+1];
    draw P[i+1] -- R[i];
    draw Q[i] -- R[i];
    draw R[i] -- Q[i+1];
    draw Q[i] -- S[i];
    draw S[i] -- S[i+1];
  endfor;
  draw P[2] -- P[3] -- P[4] -- P[0] -- P[1] --
    R[0] -- Q[0] -- R[4] -- Q[4] -- R[3]
    -- Q[3] -- R[2] -- Q[2] --
    S[2] -- S[3] -- S[4] -- S[0] -- S[1] --
    Q[1] -- R[1] -- cycle
    withpen pencircle scaled 2bp;
endfig;

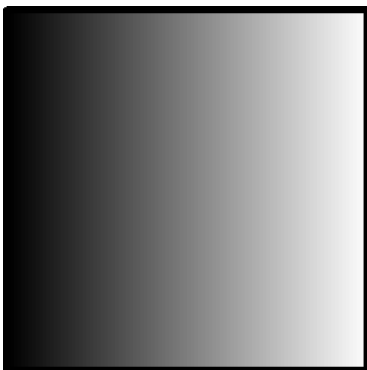
```



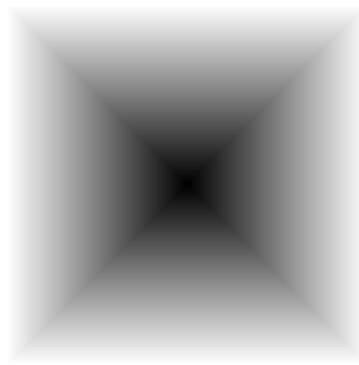
```
beginfig(140)
  for i=1 step -.01 until 0:
    fill fullcircle scaled (i*2cm) withcolor i*white;
  endfor;
  draw fullcircle scaled 2cm withpen pencircle scaled 2bp;
endfig;
```



```
beginfig(141)
  u:=5mm;
  path p;
  p = (0,0) .. (-1,1) .. (2,0) .. (0,-3) .. cycle;
  p := p shifted (-1,0);
  for i=1 step -.01 until 0:
    fill p scaled (i*u) withcolor i*white;
  endfor;
  draw p scaled u withpen pencircle scaled 2bp;
endfig;
```



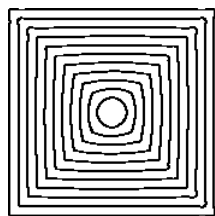
```
beginfig(142)
  z0 = (50,50);
  z1 = z0 rotated 90;
  z2 = z1 rotated 90;
  z3 = z2 rotated 90;
  path carre;
  carre = z0--z1--z2--z3--cycle;
  s := .01;
  path rect;
  z4 = s [z2,z3]; z5 = s [z1,z0];
  rect = z1--z2--z4--z5--cycle;
  for i=0 step s until 1:
    fill rect shifted (i*(z0-z1)) withcolor i*white;
  endfor;
  draw carre withpen pencircle scaled 2bp;
endfig;
```



```

beginfig(143)
  z0 = (50,50);
  z1 = z0 rotated 90;
  z2 = z1 rotated 90;
  z3 = z2 rotated 90;
  path carre;
  carre = z0--z1--z2--z3--cycle;
  s := .01;
  for i=1 step .s until 1:
    fill carre scaled i withcolor i*white;
  endfor;
endfig;

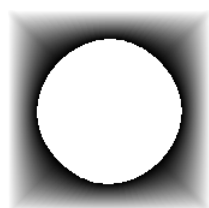
```



```

beginfig(144)
  u:=lcm;
  vardef degrade(expr p,q,M,N) =
    save a,b;
    numeric a,b;
    a := length(p);
    b := length(q);
    for i=0 upto M:
      draw (i/M) [ point 0 of p, point 0 of q ]
      for j=1 upto N:
        .. (i/M) [ point (j/N*a) of p, point (j/N*b) of q ]
      endfor;
    endfor;
  enddef;
  degrade(
    (-.1u,-.1u) .. (.1u,.1u) .. cycle,
    (-u,-u) -- (u,-u) -- (u,u) -- (-u,u) -- cycle,
    10,
    100);
endfig;

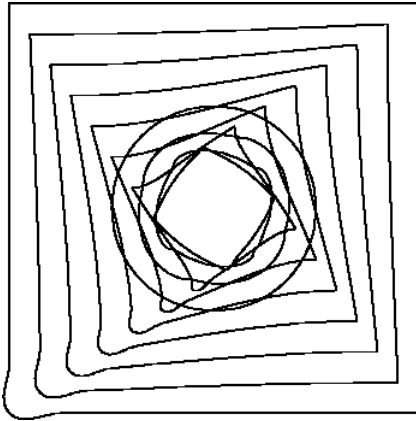
```



```

beginfig(145)
  u:=lcm;
  def couleur(expr c) = c*white enddef;
  vardef degrade(expr p,q,M,N) =
    save a,b;
    numeric a,b;
    a := length(p);
    b := length(q);
    for i=0 upto M:
      draw (i/M) [ point 0 of p, point 0 of q ]
      for j=1 upto N:
        .. (i/M) [ point (j/N*a) of p, point (j/N*b) of q ]
      endfor
      withcolor couleur(i/M);
    endfor;
  enddef;
  degrade(
    (-.5u,-.5u) .. (.5u,.5u) .. cycle,
    (-u,-u) -- (u,-u) -- (u,u) -- (-u,u) -- cycle,
    255,
    100);
endfig;

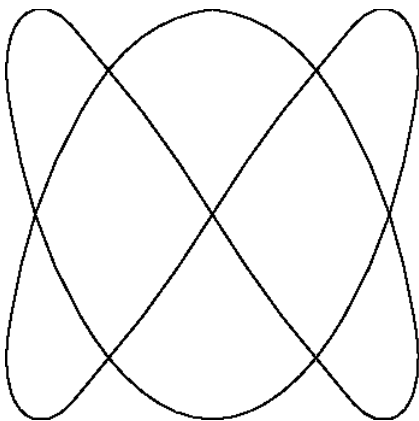
```



```

beginfig(146)
def degrade(expr p, q, N) =
  begingroup
    save n, m, M;
    numeric n, m, M;
    n := length(p);
    m := length(q);
    M := n*m; % Il faudrait prendre le ppcm
    for i=0 upto N:
      draw
        (i/N)[ point 0 of p, point 0 of q ]
        { (i/N)[ direction 0 of p, direction 0 of q ] }
      for j=1 upto M-1:
        ..
        { (i/N) [ direction 1 of subpath((j-1)*n/M, j*n/M) of p,
          direction 1 of subpath((j-1)*m/M, j*m/M) of q ] }
        (i/N)[ point (j*n/M) of p, point (j*m/M) of q ]
        { (i/N) [ direction 0 of subpath(j*n/M, (j+1)*n/M) of p,
          direction 0 of subpath(j*m/M, (j+1)*m/M) of q ] }
      endfor
      ..
      { (i/N)[ direction n of p, direction m of q ] }
      (i/N)[ point n of p, point m of q ]
    ;
  endfor;
endgroup;
enddef;
numeric u;
u := 2cm;
path p, q;
p := fullcircle scaled u;
q := (-u,-u)--(u,-u)--(u,u)--(-u,u)--cycle;
degrade(p,q,10);
endfig;

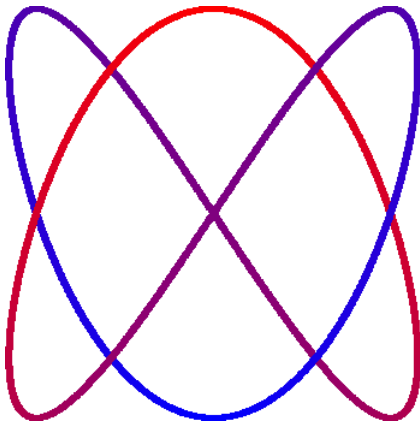
```



```

beginfig(147)
draw for i=0 step 10 until 360:
  2cm* (sind(2*i), cosd(3*i)) ..
endfor cycle;
endfig;

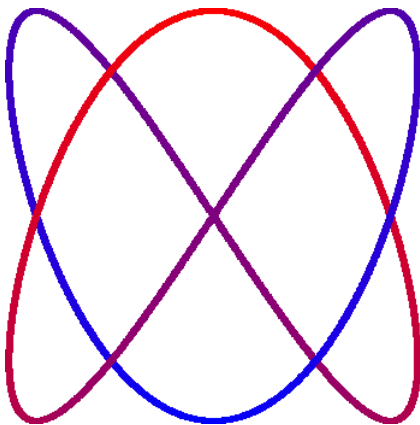
```



```

beginfig(148)
  for i=0 step .1 until 360:
    col := i/360;
    draw 2cm* (sind(2*i), cosd(3*i))
    withpen pencircle scaled 2bp
    withcolor
      if col>.5: (2*(1-col)) [red, blue]
      else:      (1-2col) [blue, red]
    fi;
  endfor;
endfig;

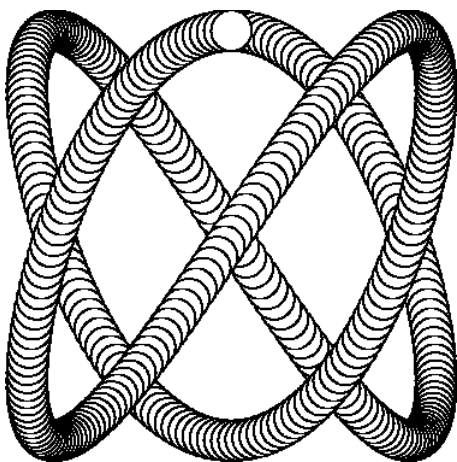
```



```

beginfig(149)
  def couleur(expr x) =
    if x>.5: (2*(1-x)) [red, blue];
    else:    (1-2x) [blue, red]
  fi
  enddef;
  for i=0 step .1 until 360:
    draw 2cm* (sind(2*i), cosd(3*i))
    withpen pencircle scaled 2bp
    withcolor couleur(i/360);
  endfor;
endfig;

```



```

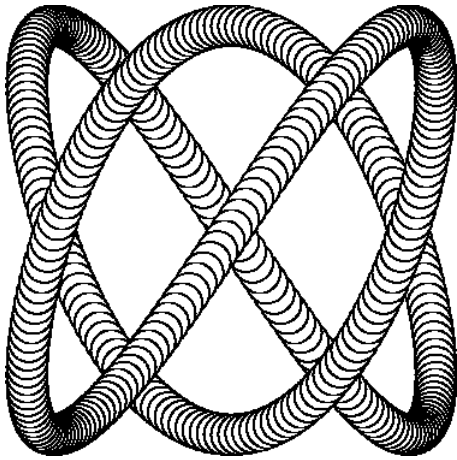
beginfig(150)
  for i=0 step 1 until 360:
    pair P;

```

```

P = 2cm* (sind(2*i), cosd(3*i));
fill fullcircle scaled 4mm shifted P withcolor white;
draw fullcircle scaled 4mm shifted P;
endfor;
endfig;

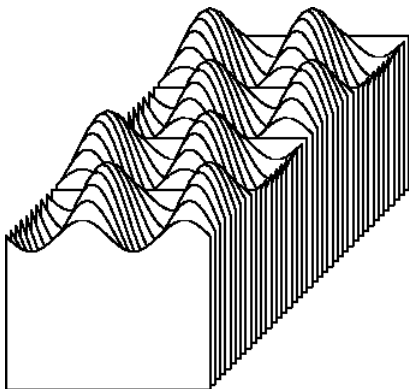
```



```

beginfig(151)
for i=0 step 1 until 360:
pair P;
P = 2cm* (sind(2*i), cosd(3*i));
fill fullcircle scaled 4mm shifted P withcolor white;
draw fullcircle scaled 4mm shifted P;
endfor;
picture p;
p:=nullpicture;
for i=-180 step 1 until 180:
pair P;
P = 2cm* (sind(2*i), cosd(3*i));
addto p contour fullcircle scaled 4mm shifted P withcolor white;
addto p doublepath fullcircle scaled 4mm shifted P
withpen pencircle scaled .5bp;
endfor;
clip p to (.5cm,2.5cm) -- (.5cm,1.5cm)--
(-.5cm,1.5cm) -- (-.5cm,2.5cm)--cycle;
draw p;
endfig;

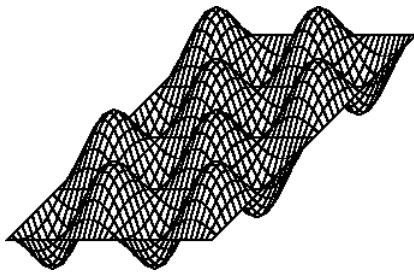
```



```

beginfig(152)
u:=5mm;
vardef project(expr x,y,z) =
x*(-1,-1) + y*(1,0) + z*(0,1)
enddef;
vardef f(expr x,y) = sind(x/u*180)*sind(y/u*180)*u enddef;
numeric m,M;
m:=-2u; M:=2u;
for i=m step .1u until M:
path p;
p =
for j=m step .1u until M:
project(i,j,f(i,j)) --
endfor
project(i,M,f(i,M));
fill (project(i,m,f(i,m)) - (0,3u)) -- p --
(project(i,M,f(i,M)) - (0,3u)) -- cycle
withcolor white;
draw (project(i,m,f(i,m)) - (0,3u)) -- p --
(project(i,M,f(i,M)) - (0,3u)) -- cycle;
draw p;
endfor;
endfig;

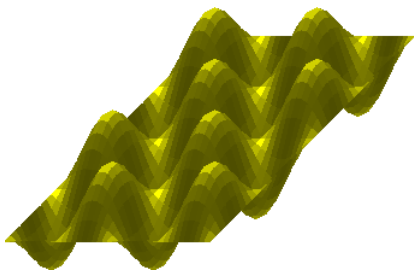
```



```

beginfig(153)
  vardef project(expr x,y,z) =
    x*(-1,-1) + y*(1,0) + z*(0,1)
  enddef;
  vardef f(expr x,y) = sind(x/u*180)*sind(y/u*180)*u enddef;
  m:=-2u; M:=2u; inc:=.1u;
  for i=m step inc until M:
    for j=m step inc until M:
      path p;
      p = project(i,j,f(i,j)) --
        project(i,j+inc,f(i,j+inc)) --
        project(i+inc,j+inc,f(i+inc,j+inc)) --
        project(i+inc,j,f(i+inc,j)) --
        cycle;
      fill p withcolor white;
      draw p;
    endfor
  endfor;
endfig;

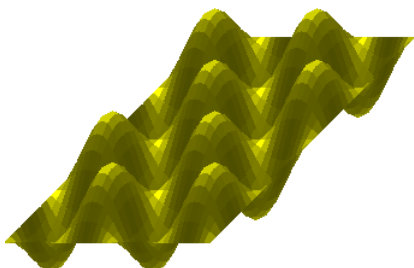
```



```

beginfig(154)
  vardef project(expr x,y,z) =
    x*(-1,-1) + y*(1,0) + z*(0,1)
  enddef;
  vardef f(expr x,y) = sind(x/u*180)*sind(y/u*180)*u enddef;
  numeric m,M,inc,couleur;
  m:=-2u; M:=2u; inc:=.1u;
  for i=m step inc until M:
    for j=m step inc until M:
      path p;
      p = project(i,j,f(i,j)) --
        project(i,j+inc,f(i,j+inc)) --
        project(i+inc,j+inc,f(i+inc,j+inc)) --
        project(i+inc,j,f(i+inc,j)) --
        cycle;
      ddx := (f(i,j) - f(i+inc,j))/inc;
      ddy := (f(i,j) - f(i,j+inc))/inc;
      couleur := 1/sqrt( ddx**2 + ddy**2 + 1);
      fill p withcolor couleur*(red+green);
    endfor
  endfor;
endfig;

```



```

beginfig(155)
  vardef f(expr x,y) = sind(x/u*180)*sind(y/u*180)*u enddef;
  boolean dessine_fil_de_fer; dessine_fil_de_fer := false;
  color dessine_couleur; dessine_couleur := red+green;

  vardef dessine(suffix f)(expr xmin, xmax, xinc, ymin, ymax, yinc) =
    save i,j,p,ddx,ddy,project;
    vardef project(expr x,y,z) =
      x*(-1,-1) + y*(1,0) + z*(0,1)
    enddef;
    for i=m step inc until M:

```

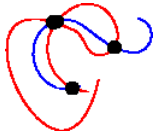


```

for j=m step inc until M:
  path p;
  p = project(i,j,f(i,j)) --
    project(i,j+inc,f(i,j+inc)) --
    project(i+inc,j+inc,f(i+inc,j+inc)) --
    project(i+inc,j,f(i+inc,j)) --
    cycle;
  dfdx := (f(i,j) - f(i+inc,j))/inc;
  dfdy := (f(i,j) - f(i,j+inc))/inc;
  couleur := 1/sqrt( dfdx**2 + dfdy**2 + 1);
  fill p withcolor couleur*dessine_couleur;
  if dessine_fil_de_fer: draw p fi;
endfor;
enddef;

% Il faudrait pouvoir choisir diff^e9rents
% types d'^ab ^e9clairage ^bb.
vardef f(expr x,y) = sind(x/u*180)*sind(y/u*180)*u enddef;
dessine(f,-2u,2u,.1u, -2u,2u,.1u);
endfig;

```



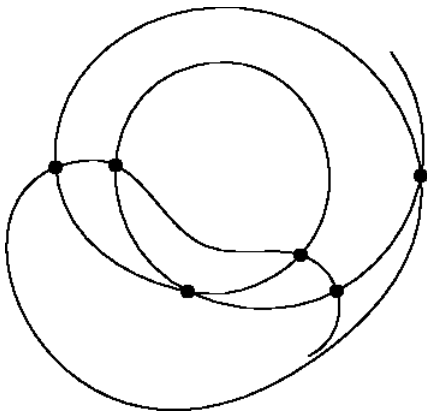
```

beginfig(156)
vardef random_path (expr n) =
  save i, A ; numeric i; pair A[];
  for i=0 upto n:
    A[i] = (uniformdeviate(2u), uniformdeviate(2u));
  endfor;
  A[0]
  for i=1 upto n:
    .. A[i]
  endfor;
enddef;

vardef intersections(expr p,q) =
  save a,b,N,i,j;
  numeric N,i,j;
  N:=10;
  for i=0 step length(p)/N until length(p):
    for j=0 step length(q)/N until length(p):
      numeric a,b;
      pair A;
      (a,b) = (subpath(i,i+length(p)/N) of p)
        intersectiontimes
        (subpath(j,j+length(q)/N) of q);
      if a <> -1:
        A = point a of subpath(i,i+length(p)/N) of p;
        show A;
        draw A withpen pencircle scaled 4bp;
      fi;
    endfor;
  endfor;
enddef;

path p,q;
p:=random_path(4);
q:=random_path(4);
draw p withcolor red;
draw q withcolor blue;
intersections(p,q);
endfig;

```



```

beginfig(157)
vardef auto_intersections(expr p) =
  save a,b,N,i,j;
  numeric N,i,j;
  N:=100;
  for i=0 step length(p)/N until length(p):
    for j=i+2*length(p)/N
      step length(p)/N
      until length(p):

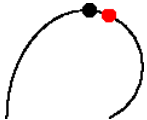
```

```

numeric a,b;
pair A;
(a,b) = (subpath(i,i+length(p)/N) of p)
intersectiontimes
(subpath(j,j+length(p)/N) of p);
if a <> -1:
  A = point a of subpath(i,i+length(p)/N) of p;
  show A;
  draw A withpen pencircle scaled 4bp;
fi;
endfor;
endfor;
enddef;

u:=2cm;
path p,q;
p:=random_path(12);
draw p;
auto_intersections(p);
endfig;

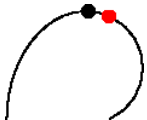
```



```

beginfig(158)
path p;
p := (0,0){up} .. (1cm,1cm) .. (1cm,0);
draw p;
draw point 1/2length(p) of p
  withpen pencircle scaled 4bp withcolor red;
draw point (arctime (1/2 arclength(p)) of p) of p
  withpen pencircle scaled 4bp;
endfig;

```

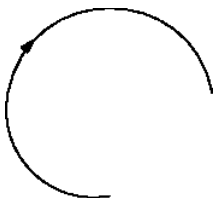


```

beginfig(159)
vardef milieu(expr p) =
  save l,i,tot,A,B;
  numeric l,tot,i;
  pair A,B;
  tot := longueur(p);
  l:=0;
  B := point 0 of p;
  for i:=0 step .01 until length(p):
    A := B;
    B := point i of p;
    l := l+abs(B-A);
    exitif l > 1/2 tot;
  endfor;
  1/2[A,B]
enddef;

path p;
p := (0,0){up} .. (1cm,1cm) .. (1cm,0);
draw p;
draw point 1/2length(p) of p withpen pencircle scaled 4bp withcolor red;
draw milieu(p) withpen pencircle scaled 4bp;
endfig;

```



```

beginfig(160)
vardef milieu_time(expr p) =
  save l,i,tot,A,B,t;
  numeric l,tot,i,t;
  pair A,B;
  tot := longueur(p);
  l:=0;
  B := point 0 of p;
  for i:=0 step .01 until length(p):
    t:=i;
    A := B;
    B := point i of p;
    l := l+abs(B-A);
    exitif l > 1/2 tot;
  endfor;
  t % Pas de point-virgule
enddef;

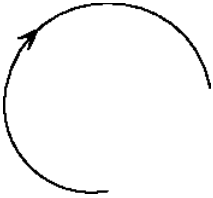
```

```

save arrowhead;
vardef arrowhead expr p =
  save A,u; pair A,u;
  A := milieu(p);
  u := unitvector(direction milieu_time(p) of p);
  A -- (A - ahlength*u rotated 15) --
  (A - ahlength*u rotated -15) -- cycle
enddef;

u:=1cm;
drawarrow (0,0) .. (-u,u) .. (u,u);
endfig;

```

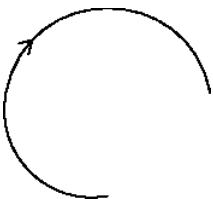


```

beginfig(161)
save arrowhead;
vardef arrowhead expr p =
  save A,B,u; pair A,B,u;
  A := milieu(p);
  B := p intersectionpoint
  (fullcircle scaled ahlength shifted A);
  u := unitvector(direction milieu_time(p) of p);
  A -- (A - ahlength*u rotated 30) -- B --
  (A - ahlength*u rotated -30) -- cycle
enddef;

u:=1cm;
drawarrow (0,0) .. (-u,u) .. (u,u);
endfig;

```

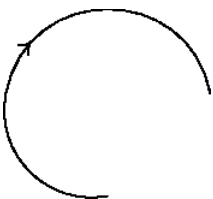


```

beginfig(162)
save arrowhead;
vardef arrowhead expr p =
  save A,u; pair A,u;
  A := milieu(p);
  u := unitvector(direction milieu_time(p) of p);
  A -- (A - ahlength*u rotated 30) --
  (A - ahlength*u rotated -30) -- cycle
enddef;

u:=1cm;
drawarrow (0,0) .. (-u,u) .. (u,u);
endfig;

```

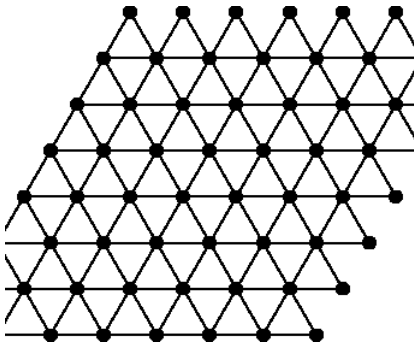


```

beginfig(163)
save arrowhead;
vardef arrowhead expr p =
  save A,u,a,b; pair A,u; path a,b;
  A := milieu(p);
  u := unitvector(direction milieu_time(p) of p);
  a := A{-u} .. (A - ahlength*u rotated 30);
  b := A{-u} .. (A - ahlength*u rotated -30);
  ( a & reverse(a) & b & reverse(b) ) --cycle
enddef;

u:=1cm;
drawarrow (0,0) .. (-u,u) .. (u,u);
endfig;

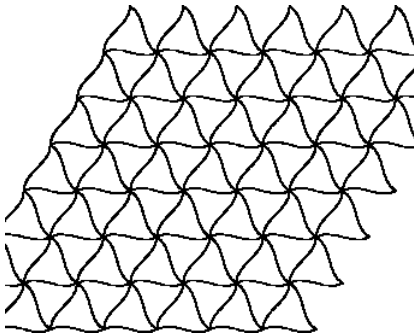
```



```

beginfig(164)
  pair A,B,C;
  C = 3mm*up;
  A = C rotated 120;
  B = C rotated -120;
  picture pic ;
  pic:=nullpicture;
  addto pic doublepath A--B--C--cycle withpen currentpen;
  addto pic doublepath A withpen pencircle scaled 4bp;
  addto pic doublepath B withpen pencircle scaled 4bp;
  addto pic doublepath C withpen pencircle scaled 4bp;
  for i=-3 upto 3:
    for j=-3 upto 3:
      draw pic shifted( i*(B-A) + j*(C-A) );
    endfor;
  endfor;
  clip currentpicture to (-2cm,-2cm)--(2cm,-2cm)--(2cm,2cm)--(-2cm,2cm)--cycle;
endfig;

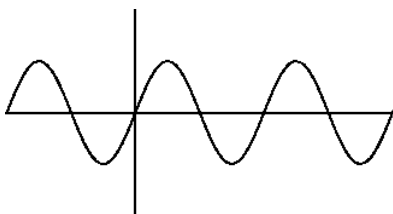
```



```

beginfig(165)
  pair A,B,C;
  C = 3mm*up;
  A = C rotated 120;
  B = C rotated -120;
  picture pic ;
  pic:=nullpicture;
  path p;
  p := A{(C-A) rotated 30} .. C{(C-A) rotated 30};
  addto pic doublepath p withpen currentpen;
  addto pic doublepath p rotated 120 withpen currentpen;
  addto pic doublepath p rotated -120 withpen currentpen;
  for i=-3 upto 3:
    for j=-3 upto 3:
      draw pic shifted( i*(B-A) + j*(C-A) );
    endfor;
  endfor;
  clip currentpicture to (-2cm,-2cm)--(2cm,-2cm)--(2cm,2cm)--(-2cm,2cm)--cycle;
endfig;

```



```

beginfig(166)
  ux:=2mm;
  uy:=5mm;
  numeric xmin, xmax, ymin, ymax, M;
  xmin := -6.3; xmax := 12.6;
  ymin := -2; ymax := 2;
  M := 100;
  draw (ux*xmin,0) -- (ux*xmax,0);
  draw (0,uy*ymin) -- (0,uy*ymax);
  pair a[];
  for i=0 upto M:
    a[i] := (

```

```

      xmin + (i/M)*(xmax-xmin),
      sind(180/3.14*( xmin + (i/M)*(xmax-xmin) ))
    ) xscaled ux yscaled uy;
  endfor;
  draw a[0] for i=1 upto M: --a[i] endfor;
endfig;

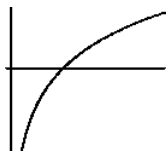
```



```

beginfig(167)
ux:=5mm;
uy:=2mm;
numeric xmin, xmax, ymin, ymax, M;
xmin := -2; xmax := 2;
ymin := -.1; ymax := 8;
M := 100;
draw (ux*xmin,0) -- (ux*xmax,0);
draw (0,uy*ymin) -- (0,uy*ymax);
pair a[];
for i=0 upto M:
  a[i] := (
    xmin + (i/M)*(xmax-xmin),
    mexp(256*( xmin + (i/M)*(xmax-xmin) ))
  ) xscaled ux yscaled uy;
endfor;
draw a[0] for i=1 upto M: --a[i] endfor;
endfig;

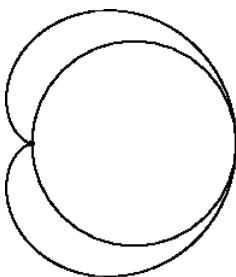
```



```

beginfig(168)
ux:=5mm;
uy:=5mm;
numeric xmin, xmax, ymin, ymax, M;
xmin := .2; xmax := 3;
ymin := -1.6; ymax := 1.2;
M := 100;
draw (ux*-.1,0) -- (ux*xmax,0);
draw (0,uy*ymin) -- (0,uy*ymax);
pair a[];
for i=0 upto M:
  a[i] := (
    xmin + (i/M)*(xmax-xmin),
    (1/256)*mlog(( xmin + (i/M)*(xmax-xmin) ))
  ) xscaled ux yscaled uy;
endfor;
draw a[0] for i=1 upto M: --a[i] endfor;
endfig;

```

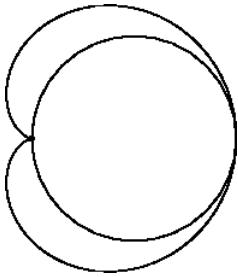


```

beginfig(169)
path p;
p = fullcircle scaled 2cm;
z0 = (-1cm,0);
draw p;
draw z0 withpen pencircle scaled 2pt;

pair A[];
for i=0 step length(p)/100 until length(p):
  pair M,N;
  M = point i of p;
  N-M = whatever * direction i of p;
  N-z0 = whatever * direction i of p rotated 90;
  A[i] := N;
endfor;
draw for i=0 step length(p)/100 until length(p):
  A[i] ..
endfor cycle;
endfig;

```

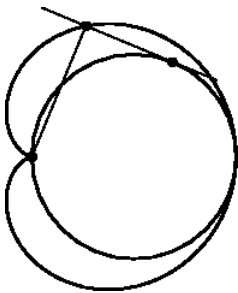


```

beginfig(170)
vardef cardiodide(expr p, O) =
  save i,M,N;
  numeric i;
  for i=0 step length(p)/100 until length(p):
    hide(
      pair M,N;
      M = point i of p;
      N-M = whatever * direction i of p;
      N-O = whatever * direction i of p rotated 90;
    )
    N ..
  endfor cycle
enddef;

path p;
p = fullcircle scaled 2cm;
z0 = (-1cm,0);
draw p;
draw z0 withpen pencircle scaled 2pt;
draw cardiodide(p,z0);
endfig;

```

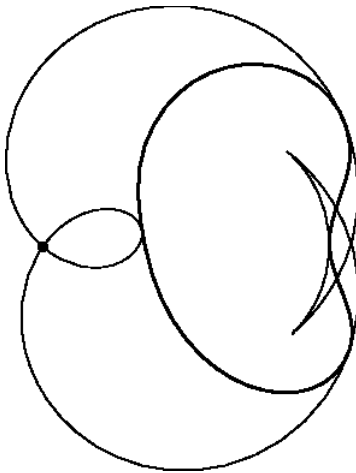


```

beginfig(171)
vardef cardiodide(expr p, O) =
  save i,M,N;
  numeric i;
  for i=0 step length(p)/100 until length(p):
    hide(
      pair M,N;
      M = point i of p;
      N-M = whatever * direction i of p;
      N-O = whatever * direction i of p rotated 90;
    )
    N ..
  endfor cycle
enddef;

path p;
p = fullcircle scaled 2cm;
z0 = (-1cm,0);
pickup pencircle scaled 1pt
draw p;
draw z0 withpen pencircle scaled 3pt;
draw cardiodide(p,z0);
pickup pencircle scaled .4pt
pair M,N;
i:=1.5;
M = point i of p;
N-M = whatever * direction i of p;
N-z0 = whatever * direction i of p rotated 90;
draw z0--N;
draw (-1/2)[N,M]--(3/2)[N,M];
draw N withpen pencircle scaled 3pt;
draw M withpen pencircle scaled 3pt;
endfig;

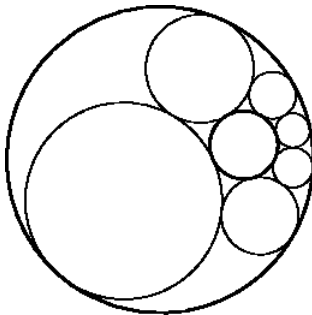
```



```

beginfig(172)
  path p;
  p := (-1cm,0) .. (1cm,-1cm) .. (8mm,0)
    .. (1cm,1cm) .. (-1cm,1cm) .. cycle;
  z0 = (-2cm,0);
  draw p withpen pencircle scaled 1bp;
  draw z0 withpen pencircle scaled 3pt;
  draw cardioid(p,z0);
endfig;

```



```

beginfig(173)
  vardef inversion (expr O,k,M) =
    if pair M:
      (O + k*unitvector(M-O)/abs(M-O))
    elseif path M:
      for i=0 step length(M)/100 until length(M):
        inversion(O,k,point i of M) ..
      endfor
    cycle
  fi
enddef;

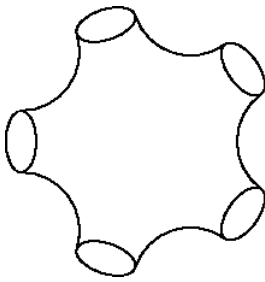
  u:=4cm;
  path p[],A,B;

  z0 = (5u,0) rotated 10;

  A = fullcircle scaled 2u;
  B = A scaled 3;
  draw inversion( z0, 2 (u**2), A )
    withpen pencircle scaled 1pt;
  draw inversion( z0, 2 (u**2), B )
    withpen pencircle scaled 1pt;

  p0 = fullcircle scaled 2u shifted (2u,0);
  for i=0 upto 5:
    if i<>0:
      p[i] = p[i-1] rotated (360/6);
    fi;
    draw inversion( z0, 2 (u**2), p[i] );
  endfor;
endfig;

```



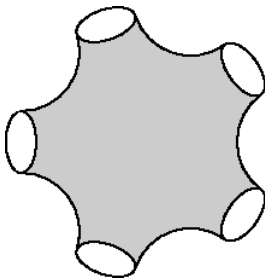
```

beginfig(174)
def curve(expr p,i,q,j,t) =
  point i of p {direction i of p} ..
  tension t ..
  point j of q {direction j of q}
enddef;

vardef sphere_with_holes (expr n) =
  save i;
  c[0] = fullcircle xscaled u yscaled 2u
    shifted (4u,0) rotated (360/(2n)) ;
  draw c[0];
  for i=1 upto n-1:
    c[i] = c[i-1] rotated (360/n);
    draw c[i];
  endfor;
  l[0] = curve(c[0], 2, c[1], -2, 1);
  draw l[0];
  for i=1 upto n-1:
    l[i] = l[i-1] rotated (360/n);
    draw l[i];
  endfor;
enddef;

u:=3mm;
path c[], l[];
sphere_with_holes(5);
endfig;

```



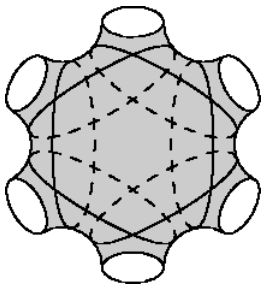
```

beginfig(175)
def curve(expr p,i,q,j,t) =
  point i of p {direction i of p} ..
  tension t ..
  point j of q {direction j of q}
enddef;

vardef sphere_with_holes (expr n) =
  save i;
  c[0] = fullcircle xscaled u yscaled 2u
    shifted (4u,0) rotated (360/(2n)) ;
  for i=1 upto n-1:
    c[i] = c[i-1] rotated (360/n);
  endfor;
  l[0] = curve(c[0], 2, c[1], -2, 1);
  for i=1 upto n-1:
    l[i] = l[i-1] rotated (360/n);
  endfor;
  fill for i=0 upto n-1:
    ( reverse subpath(2,6) of c[i] ) &
    l[i] &
  endfor
  % To turn it into a cycle (ugly)
  point length(l[n-1]) of l[n-1] -- cycle
  withcolor .8white;
  for i=0 upto n-1:
    draw c[i]; draw l[i];
  endfor;
enddef;

u:=3mm;
path c[], l[];
sphere_with_holes(5);
endfig;

```

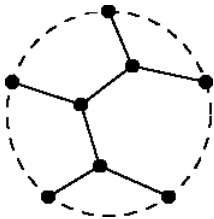



```

beginfig(176)
  path c[], l[];
  sphere_with_holes(6);
  def ellipse(expr a,b,c,d,e) =
    draw curve(a,b,c,d,e) ;
    draw curve(c,d,a,b,e) dashed evenly;
  enddef;

  ellipse (l[0], 2/3, l[2], 1/3, 4);
  ellipse (l[1], 2/3, l[3], 1/3, 4);
  ellipse (l[2], 2/3, l[4], 1/3, 4);
  ellipse (l[3], 2/3, l[5], 1/3, 4);
  ellipse (l[4], 2/3, l[0], 1/3, 4);
  ellipse (l[5], 2/3, l[1], 1/3, 4);
endfig;

```

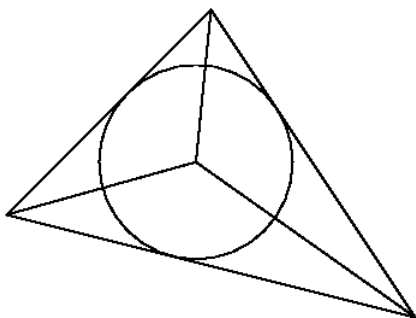


```

beginfig(177)
  vardef bar(expr m,a,b,c) =
    m = 1/3a + 1/3b + 1/3c
  enddef;
  vardef dbar(expr m,a,b,c) =
    draw m--a; draw m--b; draw m--c;
    draw m withpen pencircle scaled 4bp;
  enddef;

  pair P[], A,B,C;
  for i=0 upto 4:
    P[i] = lcm * up rotated (i*360/5);
    draw P[i] withpen pencircle scaled 4bp;
  endfor;
  bar(A, P[0], P[4], B);
  bar(B, A, P[1], C);
  bar(C, B, P[2], P[3]);
  draw fullcircle scaled 2cm dashed evenly;
  dbar(A, P[0], P[4], B);
  dbar(B, A, P[1], C);
  dbar(C, B, P[2], P[3]);
endfig;

```



```

beginfig(178)
% M est sur la bissectrice de l'angle A
vardef bissectrice(expr M,A,B,C) =
  (M-A) = whatever * (
    (A-C) rotated 1/2(angle(B-A) - angle(C-A)))
enddef;

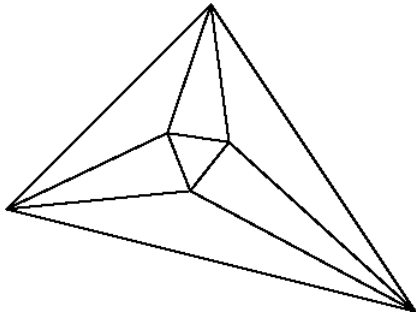
% Le cercle inscrit
vardef cercle_inscrit(expr A,B,C) =
  save M, h; pair M, h;
  bissectrice(M,A,B,C);
  bissectrice(M,B,C,A);
  M-h = whatever * (B-C) rotated 90;
  h = whatever[B,C];
  fullcircle scaled 2 length(M-h) shifted M
enddef;

```

```

pair A,B,C,M;
u:=2cm;
A=(0,0); B=(2u,-.5u); C=(u,u);
draw A--B--C--cycle;
bissectrice(M, A,B,C);
bissectrice(M, B,C,A);
draw M--A; draw M--B; draw M--C;
draw cercle_inscrit(A,B,C);
endfig;

```



```

beginfig(179)
vardef premiere_trisectrice (expr M, A,B,C) =
  (M-A) = whatever * ( (A-B) rotated 1/3 (angle(C-A) - angle(B-A)) )
enddef;

vardef deuxieme_trisectrice (expr M, A,B,C) =
  (M-A) = whatever * ( (A-B) rotated 2/3 (angle(C-A) - angle(B-A)) )
enddef;

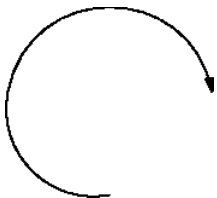
pair A,B,C,M[];
u:=2cm;
A=(0,0); B=(2u,-.5u); C=(u,u);
draw A--B--C--cycle;

premiere_trisectrice(M1,A,B,C);
deuxieme_trisectrice(M1,B,C,A);
premiere_trisectrice(M2,B,C,A);
deuxieme_trisectrice(M2,C,A,B);
premiere_trisectrice(M3,C,A,B);
deuxieme_trisectrice(M3,A,B,C);

draw M1--A; draw M1--B;
draw M2--B; draw M2--C;
draw M3--C; draw M3--A;

draw M1--M2--M3--cycle;
endfig;

```

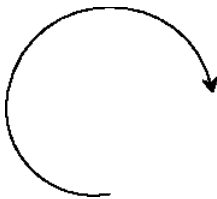


```

beginfig(180)
save arrowhead;
vardef arrowhead expr p =
  save A,u; pair A,u;
  A := point length(p) of p;
  u := unitvector(direction length(p) of p);
  A -- (A - ahlength*u rotated 15) --
  (A - ahlength*u rotated -15) -- cycle
enddef;

u:=1cm;
drawarrow (0,0) .. (-u,u) .. (u,u);
endfig;

```



```

beginfig(181)
save arrowhead;
vardef arrowhead expr p =
  save A,B,u; pair A,B,u;
  A := point length(p) of p;

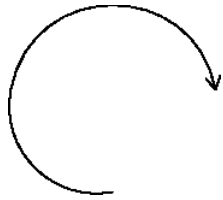
```

```

B := p intersectionpoint
      (fullcircle scaled ahlenght shifted A);
u := unitvector(direction length(p) of p);
A -- (A - ahlenght*u rotated 30) -- B --
      (A - ahlenght*u rotated -30) -- cycle
enddef;

u:=1cm;
drawarrow (0,0) .. (-u,u) .. (u,u);
endfig;

```

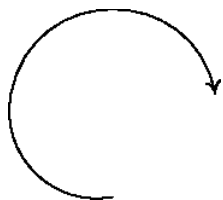


```

beginfig(182)
save arrowhead;
vardef arrowhead expr p =
save A,u; pair A,u;
A := point length(p) of p;
u := unitvector(direction length(p) of p);
A -- (A - ahlenght*u rotated 30) -- A --
      (A - ahlenght*u rotated -30) -- cycle
enddef;

u:=1cm;
drawarrow (0,0) .. (-u,u) .. (u,u);
endfig;

```

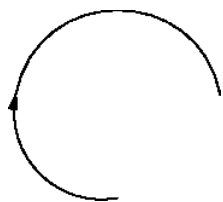


```

beginfig(183)
save arrowhead;
vardef arrowhead expr p =
save A,u,a,b; pair A,u; path a,b;
A := point length(p) of p;
u := unitvector(direction length(p) of p);
a := A{-u} .. (A - ahlenght*u rotated 30);
b := A{-u} .. (A - ahlenght*u rotated -30);
( a & reverse(a) & b & reverse(b) ) --cycle
enddef;

u:=1cm;
drawarrow (0,0) .. (-u,u) .. (u,u);
endfig;

```

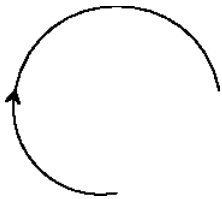


```

beginfig(184)
save arrowhead;
vardef arrowhead expr p =
save A,u; pair A,u;
A := point 1/2length(p) of p;
u := unitvector(direction 1/2length(p) of p);
A -- (A - ahlenght*u rotated 15) --
      (A - ahlenght*u rotated -15) -- cycle
enddef;

u:=1cm;
drawarrow (0,0) .. (-u,u) .. (u,u);
endfig;

```

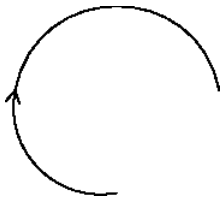


```

beginfig(185)
  save arrowhead;
  vardef arrowhead expr p =
    save A,B,u; pair A,B,u;
    A := point 1/2length(p) of p;
    B := p intersectionpoint
      (fullcircle scaled ahlength shifted A);
    u := unitvector(direction 1/2length(p) of p);
    A -- (A - ahlength*u rotated 30) -- B --
      (A - ahlength*u rotated -30) -- cycle
  enddef;

  u:=lcm;
  drawarrow (0,0) .. (-u,u) .. (u,u);
endfig;

```

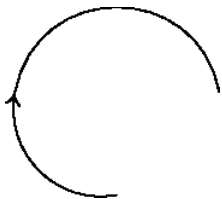


```

beginfig(186)
  save arrowhead;
  vardef arrowhead expr p =
    save A,u; pair A,u;
    A := point 1/2length(p) of p;
    u := unitvector(direction 1/2length(p) of p);
    A -- (A - ahlength*u rotated 30) -- A --
      (A - ahlength*u rotated -30) -- cycle
  enddef;

  u:=lcm;
  drawarrow (0,0) .. (-u,u) .. (u,u);
endfig;

```

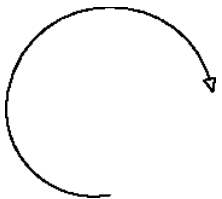


```

beginfig(187)
  save arrowhead;
  vardef arrowhead expr p =
    save A,u,a,b; pair A,u; path a,b;
    A := point 1/2length(p) of p;
    u := unitvector(direction 1/2length(p) of p);
    a := A{-u} .. (A - ahlength*u rotated 30);
    b := A{-u} .. (A - ahlength*u rotated -30);
    ( a & reverse(a) & b & reverse(b) ) --cycle
  enddef;

  u:=lcm;
  drawarrow (0,0) .. (-u,u) .. (u,u);
endfig;

```



```

beginfig(188)
  def drawwhitearrow expr p = _apth:=p; _finwhitearr enddef;

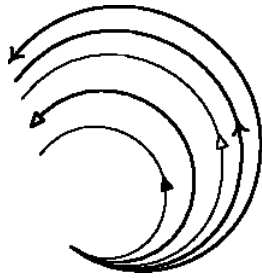
  def _finwhitearr text t =
    draw _apth t;
    fill arrowhead _apth t withcolor white;
    draw arrowhead _apth t
  enddef;

```

```

u:=1cm;
drawwhitearrow (0,0) .. (-u,u) .. (u,u);
endfig;

```



```

beginfig(189)
def draw_white_arrow expr p = _apth:=p; _fin_white_arr enddef;
def _fin_white_arr text t =
  draw _apth t;
  fill arrowhead _apth withcolor white;
  draw arrowhead _apth t
enddef;

def draw_middle_arrow expr p = _apth:=p; _fin_middle_arr enddef;
def _fin_middle_arr text t =
  draw _apth t;
  filldraw arrowhead_middle _apth t
enddef;
vardef arrowhead_middle expr p =
  save A,u; pair A,u;
  A := point (arctime (.5sarclength p) of p) of p;
  u := unitvector(direction (arctime (.5sarclength p) of p) of p);
  A -- (A - ahlength*u rotated (.5ahangle) ) --
  (A - ahlength*u rotated (-.5ahangle) ) -- cycle
enddef;

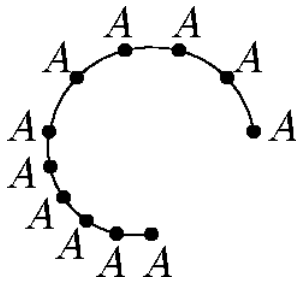
def draw_middle_white_arrow expr p = _apth:=p; _fin_middle_white_arr enddef;
let draw_white_middle_arrow = draw_middle_white_arrow;
def _fin_middle_white_arr text t =
  draw _apth t;
  fill arrowhead_middle _apth t withcolor white;
  draw arrowhead_middle _apth t
enddef;

def draw_other_arrow expr p = _apth:=p; _fin_other_arr enddef;
def _fin_other_arr text t =
  draw _apth t;
  draw arrowhead_other _apth t
enddef;
vardef arrowhead_other expr p =
  save A,u,a,b; pair A,u; path a,b;
  A := point (length p) of p;
  u := unitvector(direction (length p) of p);
  a := A{-u} .. (A - ahlength*u rotated 30);
  b := A{-u} .. (A - ahlength*u rotated -30);
  ( a & reverse(a) & b & reverse(b) ) --cycle
enddef;

def draw_other_middle_arrow expr p = _apth:=p; _fin_other_middle_arr enddef;
let draw_middle_other_arrow = draw_other_middle_arrow;
def _fin_other_middle_arr text t =
  draw _apth t;
  draw arrowhead_other_middle _apth t
enddef;
vardef arrowhead_other_middle expr p =
  save A,u,a,b; pair A,u; path a,b;
  A := point (arctime (.5sarclength p) of p) of p;
  u := unitvector(direction (arctime (.5sarclength p) of p) of p);
  a := A{-u} .. (A - ahlength*u rotated 30);
  b := A{-u} .. (A - ahlength*u rotated -30);
  ( a & reverse(a) & b & reverse(b) ) --cycle
enddef;

path p;
p := halfcircle scaled 2cm;
p := (0,0) .. (3cm,1cm) .. (-1cm,3cm);
p := p scaled .3;
draw_middle_arrow p;
draw_white_arrow p scaled 1.3 withpen pencircle scaled 1bp;
draw_white_middle_arrow p scaled 1.6;
draw_other_middle_arrow p scaled 1.8 withpen pencircle scaled 1bp;
draw_other_arrow p scaled 2 withpen pencircle scaled 1bp;
endfig;

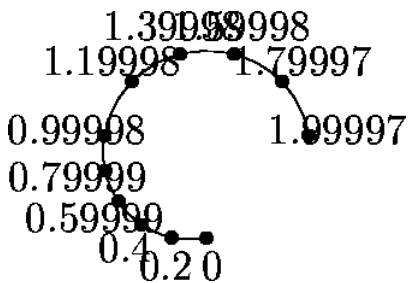
```



```

beginfig(190)
  vardef mylabel(expr pic, p, t) =
    save A; pair A;
    A = point t of p +
      8bp * unitvector(direction t of p) rotated 90;
    label(pic, A);
  enddef;
  path p; u:=1cm;
  p = (0,0)..(-u,u)..(u,u);
  draw p;
  for i=0 step .2 until length(p):
    draw point i of p withpen pencircle scaled 4bp;
    mylabel(btex  $\$A\$$  etex,p,i);
  endfor;
endfig;

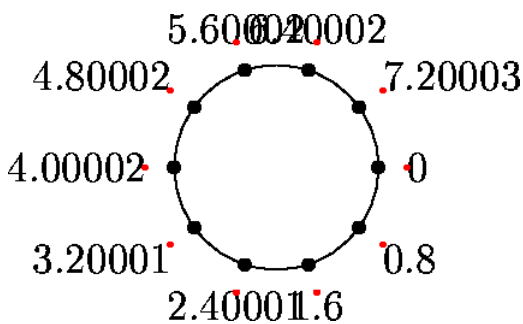
```



```

beginfig(191)
  vardef mylabel(expr pic, p, t) =
    save A; pair A;
    A = point t of p +
      8bp * unitvector(direction t of p) rotated 90;
    label(pic, A);
  enddef;
  path p; u:=1cm;
  p = (0,0)..(-u,u)..(u,u);
  draw p;
  for i=0 step .2 until length(p):
    draw point i of p withpen pencircle scaled 4bp;
    mylabel(TEX decimal(i),p,i);
  endfor;
endfig;

```



```

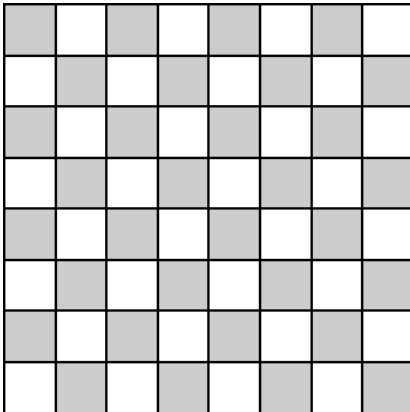
beginfig(192)
  vardef mylabel(expr pic, p, t) =
    save A,a; pair A; numeric a;
    a := angle(direction t of p rotated 90);
    show(a);
    a := a + 45/2;
    if a>180: a := a - 360 fi;
    save ll, lr, ul, ur;
    pair ul,ur,ll,lr;
    ll := llcorner pic;
    lr := lrcorner pic;
    ul := ulcorner pic;
    ur := urcorner pic;
    A = point t of p +
      8bp * unitvector(direction t of p) rotated 90;
    label(pic shifted ll, A +
      if (a >= 0) and (a <= 45): 1/2(ur-ul)
      elseif (a >= 45) and (a <= 90): 1/2(ur-ul) + 1/2(ur-lr)
      elseif (a >= 90) and (a <= 135): 1/2(ur-lr)
      elseif (a >= 135) and (a <= 180): 1/2(ll-lr) + 1/2(ur-lr)
    );
  enddef;
  path p; u:=1cm;
  p = (0,0)..(-u,u)..(u,u);
  draw p;
  for i=0 step .2 until length(p):
    draw point i of p withpen pencircle scaled 4bp;
    mylabel(TEX decimal(i),p,i);
  endfor;
endfig;

```

```

elseif (a >= -180) and (a <= -135): 1/2(l1-lr)
elseif (a >= -135) and (a <= -90): 1/2(l1-ul) + 1/2(l1-lr)
elseif (a >= -90) and (a <= -45): 1/2(l1-ul)
elseif (a >= -45) and (a <= 0): 1/2(l1-ul) - 1/2(l1-lr)
else: hide(show "BUG") (0,0)
fi);
draw A withpen pencircle scaled 2bp withcolor red;
enddef;
path p; u:=1cm;
p = (0,0)..(-u,u)..(u,u);
p := reverse fullcircle scaled 2u;
draw p;
for i=0 step length(p)/10 until length(p):
  draw point i of p withpen pencircle scaled 4bp;
  mylabel(TEX decimal(i),p,i);
endfor;
endfig;

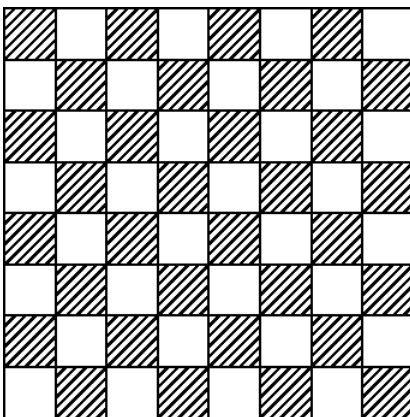
```



```

beginfig(193)
n:=8;
u:=5mm;
for i=0 upto n-1:
  for j=0 upto n-1:
    if odd(i+j):
      fill (0,0)--(u,0)--(u,u)--(0,u)--cycle
        shifted (i*u,j*u) withcolor .8white;
    fi;
  endfor;
endfor;
for i=0 upto n:
  draw (0,i*u)--(n*u,i*u);
  draw (i*u,0)--(i*u,n*u);
endfor;
endfig;

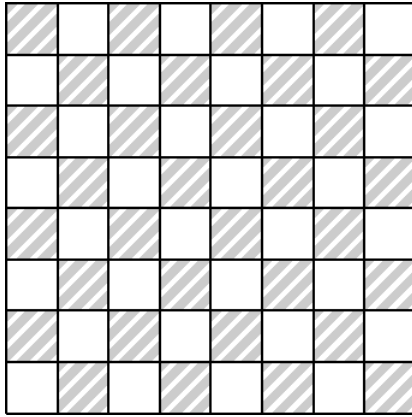
```



```

beginfig(194)
n:=8;
u:=5mm;
for i=0 upto n-1:
  for j=0 upto n-1:
    if odd(i+j):
      for k=0 step u/5 until u:
        draw ( (k,0)--(u,u-k) )
          shifted (i*u,j*u);
        draw ( (0,k)--(u-k,u) )
          shifted (i*u,j*u);
      endfor;
    fi;
  endfor;
endfor;
for i=0 upto n:
  draw (0,i*u)--(n*u,i*u);
  draw (i*u,0)--(i*u,n*u);
endfor;
endfig;

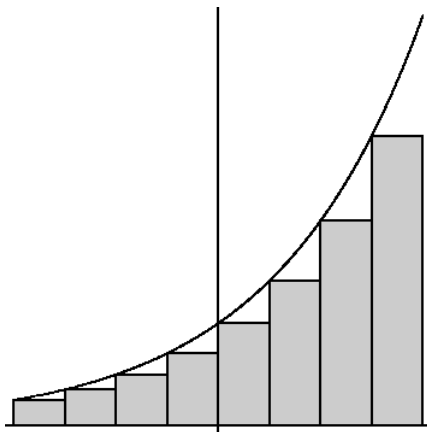
```



```

beginfig(195)
  n:=8;
  u:=5mm;
  for i=0 upto n-1:
    for j=0 upto n-1:
      if odd(i+j):
        for k=0 step u/5 until 4/5 u:
          if odd(k*5/u):
            fill ( (k,0)--(u,u-k)--(u,u-k-u/5)--
              (k+u/5,0)--cycle )
              shifted (i*u,j*u) withcolor .8white;
          else:
            fill ( (0,k)--(u-k,u)--(u-k-u/5,u)--
              (0,k+u/5)--cycle )
              shifted (i*u,j*u) withcolor .8white;
          fi;
        endfor;
      fi;
    endfor;
  endfor;
  for i=0 upto n:
    draw (0,i*u)--(n*u,i*u);
    draw (i*u,0)--(i*u,n*u);
  endfor;
endfig;

```



```

beginfig(196)
  vardef trace (suffix f)(expr a,b,inc) =
    save i; numeric i;
    for i=a step inc until b:
      (i*1cm, f(i)*1cm) ..
    endfor (b*1cm, f(b)*1cm)
  enddef;

  vardef axes =
    save p; picture p;
    p:=nullpicture;
    addto p doublepath (-infinity,0)--(infinity,0) withpen currentpen;
    addto p doublepath (0,-infinity)--(0,infinity) withpen currentpen;
    clip p to bbox currentpicture;
    draw p;
  enddef;

  vardef trace_rectangles_left (suffix f)(expr a,b,inc) =
    save i; numeric i;
    for i=a step inc until b-inc:
      path p;
      p = (i,0)--(i+inc,0)--(i+inc,f(i))--(i,f(i))--cycle;
      p := p scaled 1cm;
      fill p withcolor .8*white;
      draw p;
    endfor;
  enddef;

```

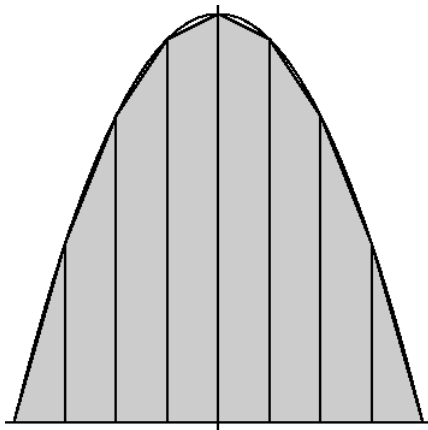


```

vardef f(expr x) = 2 ** x enddef;

trace_rectangles_left(f,-2,2,.5);
draw trace(f, -2,2,.1);
axes;
endfig;

```



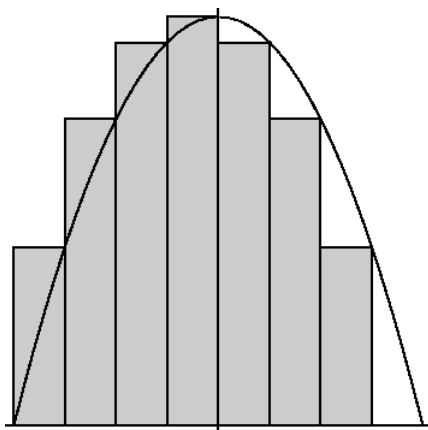
```

beginfig(197)
vardef trace_trapezes (suffix f)(expr a,b,inc) =
  save i; numeric i;
  for i=a step inc until b-inc:
    path p;
    p = (i,0)--(i+inc,0)--(i+inc,f(i+inc))--(i,f(i))--cycle;
    p := p scaled lcm;
    fill p withcolor .8*white;
    draw p;
  endfor;
enddef;

vardef f(expr x) = 4 - x**2 enddef;

trace_trapezes(f,-2,2,.5);
draw trace(f, -2,2,.1);
axes;
endfig;

```

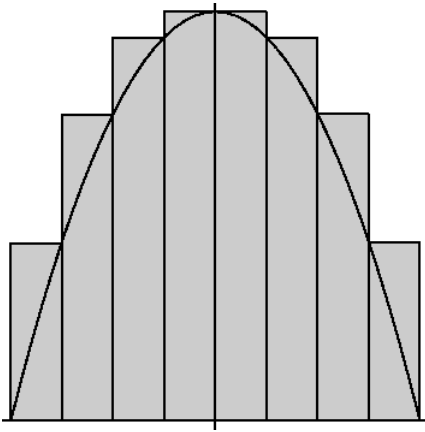


```

beginfig(198)
vardef trace_rectangles_right (suffix f)(expr a,b,inc) =
  save i; numeric i;
  for i=a step inc until b-inc:
    path p;
    p = (i,0)--(i+inc,0)--(i+inc,f(i+inc))--(i,f(i+inc))--cycle;
    p := p scaled lcm;
    fill p withcolor .8*white;
    draw p;
  endfor;
enddef;

trace_rectangles_right(f,-2,2,.5);
draw trace(f, -2,2,.1);
axes;
endfig;

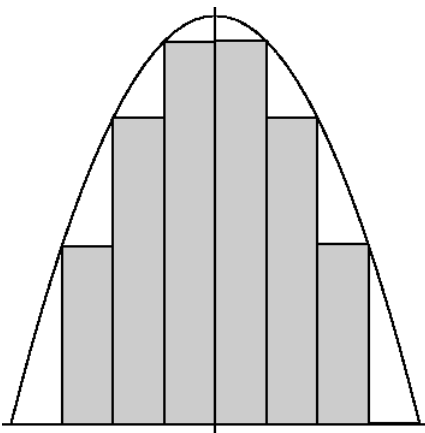
```



```

beginfig(199)
  vardef maxf(suffix f)(expr a,b) =
    save m,i; numeric m,i;
    m:=f(a);
    for i=a step (b-a)/100 until b:
      if m

```



```

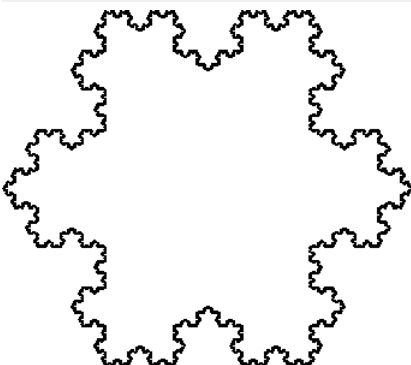
beginfig(200)
  vardef minf(suffix f)(expr a,b) =
    save m,i; numeric m,i;
    m:=f(a);
    for i=a step (b-a)/100 until b:
      if m>f(i): m:=f(i); fi;
    endfor;
    m
  enddef;

  vardef trace_rectangles_min (suffix f)(expr a,b,inc) =
    save i; numeric i;
    for i=a step inc until b-inc:
      path p; numeric m;
      m:=minf(f,i,i+inc);
      p = (i,0)--(i+inc,0)--(i+inc,m)--(i,m)--cycle;
      p := p scaled lcm;
      fill p withcolor .8*white;
      draw p;
    endfor;
  enddef;

  vardef f(expr x) = 4 - x**2 enddef;

  trace_rectangles_min(f,-2,2,.5);
  draw trace(f, -2,2,.1);
  axes;
endfig;

```



```

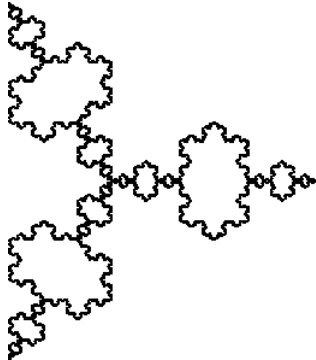
beginfig(201)
  u:=2cm;
  vardef koch(expr A,B,n) =

```

```

save C; pair C;
C = A rotatedaround(1/3[A,B], 120);
if n>0:
  koch( A,          1/3[A,B], n-1);
  koch( 1/3[A,B], C,    n-1);
  koch( C,          2/3[A,B], n-1);
  koch( 2/3[A,B], B,    n-1);
else:
  draw A--1/3[A,B]--C--2/3[A,B]--B;
fi;
enddef;
z0=(u,0);
z1=z0 rotated 120;
z2=z1 rotated 120;
koch( z0, z1, 4 );
koch( z1, z2, 4 );
koch( z2, z0, 4 );
endfig;

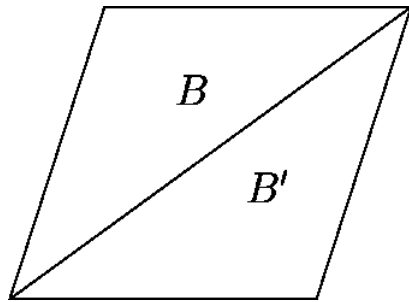
```



```

beginfig(202)
u:=2cm;
vardef koch(expr A,B,n) =
  save C; pair C;
  C = A rotatedaround(1/3[A,B], -120);
  if n>0:
    koch( A,          1/3[A,B], n-1);
    koch( 1/3[A,B], C,    n-1);
    koch( C,          2/3[A,B], n-1);
    koch( 2/3[A,B], B,    n-1);
  else:
    draw A--1/3[A,B]--C--2/3[A,B]--B;
  fi;
enddef;
z0=(u,0);
z1=z0 rotated 120;
z2=z1 rotated 120;
koch( z0, z1, 4 );
koch( z1, z2, 4 );
koch( z2, z0, 4 );
endfig;

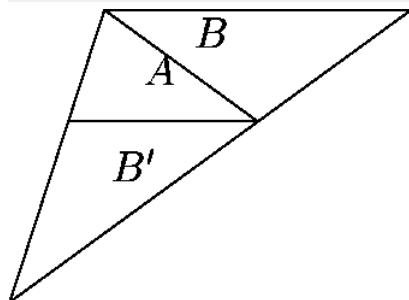
```



```

beginfig(203)
pair A,B,C,D;
u := 3cm;
A := (0,0);
B := (u,0);
D := B rotated 72;
C := (u,0) + D;
draw A--B--C--D--cycle;
draw A--C;
draw btex $B'$ etex shifted 1/3 (A+B+C);
draw btex $B$ etex shifted 1/3 (A+D+C);
endfig;

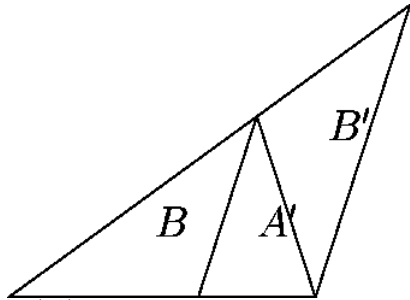
```



```

beginfig(204)
  pair A,B,C,D,E,F;
  numeric d[];
  u := 3cm;
  A := (0,0);
  B := (u,0);
  D := B rotated 72;
  C := (u,0) + D;
  d[0] := 1;
  d[1] := sqrt( 2*(1+cosd(72)) );
  d[2] := sqrt( 2*(1-cosd(36)) );
  A := A;
  B := C;
  C := D;
  draw A--B--C--cycle;
  E := (d1/(d0+d1)) [A,C];
  F := (d0/(d0+d2)) [A,B];
  draw E--C--F--cycle;
  draw btex $A$ etex shifted 1/3(E+C+F);
  draw B--C--F--cycle;
  draw btex $B$ etex shifted 1/3(B+C+E);
  draw E--F--A--cycle;
  draw btex $B'$ etex shifted 1/3(E+F+A);
endfig;

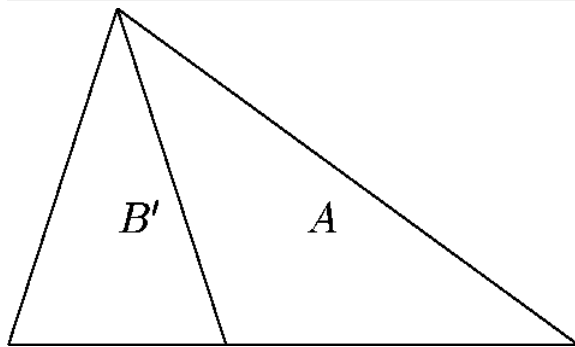
```



```

beginfig(205)
  pair A,B,C,D,E,F;
  numeric d[];
  u := 3cm;
  A := (0,0);
  B := (u,0);
  D := B rotated 72;
  C := (u,0) + D;
  draw A--B--C--cycle;
  d[0] := 1;
  d[1] := sqrt( 2*(1+cosd(72)) );
  d[2] := sqrt( 2*(1-cosd(36)) );
  E := (d1/(d0+d1)) [A,C];
  F := (d0/(d0+d2)) [A,B];
  draw E--F--B--cycle;
  draw btex $A'$ etex shifted 1/3(E+F+B);
  draw E--A--F--cycle;
  draw btex $B$ etex shifted 1/3(E+A+F);
  draw C--E--B--cycle;
  draw btex $B'$ etex shifted 1/3(C+E+B);
endfig;

```



```

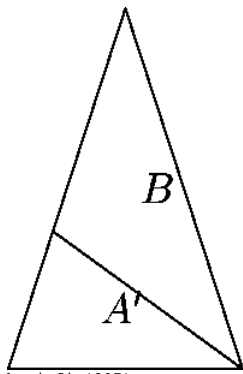
beginfig(206)
  pair A,B,C,D,E,F;
  numeric d[];
  u := 3cm;
  A := (0,0);
  B := (u,0);
  D := B rotated 72;
  C := (u,0) + D;
  d[0] := 1;
  d[1] := sqrt( 2*(1+cosd(72)) );
  d[2] := sqrt( 2*(1-cosd(36)) );
  A := A;
  B := C;
  C := D;
  E := (d1/(d0+d1)) [A,C];
  F := (d0/(d0+d2)) [A,B];
  B := 3*(C-E);
  C := 3*(F-E);

  draw A--B--C--cycle;

  D := (d0/(d0+d2)) [C,A];
  draw B--C--D--cycle;
  draw btex $A$ etex shifted 1/3(B+C+D);
  draw B--D--A--cycle;
  draw btex $B'$ etex shifted 1/3(B+D+A);
endfig;

```

endfig;



```

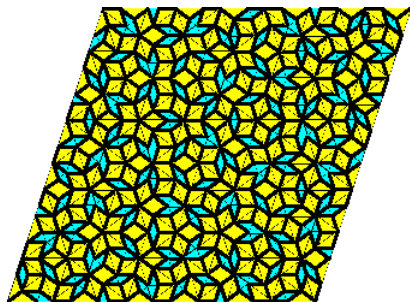
beginfig(207)
  pair A,B,C,D,E,F;
  numeric d[];
  u := 3cm;
  A := (0,0);
  B := (u,0);
  D := B rotated 72;
  C := (u,0) + D;
  d[0] := 1;
  d[1] := sqrt( 2*(1+cosd(72)) );
  d[2] := sqrt( 2*(1-cosd(36)) );

  % B'
  E := (d1/(d0+d1)) [A,C];
  F := (d0/(d0+d2)) [A,B];

  % A'
  A := 2*(E-E);
  C := 2*(B-E);
  B := 2*(F-E);

  draw A--B--C--cycle;
  D := (d0/(d0+d2)) [A,B];
  draw C--D--B--cycle;
  draw btex $A'$ etex shifted 1/3(C+D+B);
  draw C--A--D--cycle;
  draw btex $B$ etex shifted 1/3(C+A+D);
endfig;

```



```

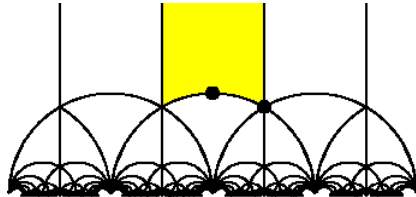
beginfig(208)
  vardef pave(expr t, A, B, C, n) =
    save D, E, d;
    pair D,E;
    numeric d[];
    d[0] := 1;
    d[1] := sqrt( 2*(1+cosd(72)) );
    d[2] := sqrt( 2*(1-cosd(36)) );
    if n>0:
      if t=1:
        D := (d0/(d0+d2)) [A,C];
        pave(1,B,C,D,n-1);
        pave(4,B,D,A,n-1);
      elseif t=2:
        D := (d0/(d0+d2)) [A,B];
        pave(2,C,D,B,n-1);
        pave(3,C,A,D,n-1);
      elseif t=3:
        D := (d1/(d0+d1)) [A,B];
        E := (d0/(d0+d2)) [A,C];
        pave(1,D,C,E,n-1);
        pave(3,B,C,D,n-1);
        pave(4,D,E,A,n-1);
      elseif t=4:
        D := (d1/(d0+d1)) [A,C];
        E := (d0/(d0+d2)) [A,B];
        pave(2,D,E,B,n-1);
        pave(3,D,A,E,n-1);
        pave(4,C,D,B,n-1);
      fi;
    else:
      draw A--B--C--cycle;
      if t=1:
        fill A--B--C--cycle withcolor green + blue;
        draw A--C withpen pencircle scaled lbp;
        draw A--B withpen pencircle scaled lbp;
      elseif t=2:
        fill A--B--C--cycle withcolor green + blue;
        draw A--B withpen pencircle scaled lbp;
        draw A--B withpen pencircle scaled lbp;
      fi;
    fi;
  enddef;

```

```

elseif t=3:
  fill A--B--C--cycle withcolor green + red;
  draw A--C withpen pencircle scaled lbp;
  draw C--B withpen pencircle scaled lbp;
elseif t=4:
  fill A--B--C--cycle withcolor green + red;
  draw B--C withpen pencircle scaled lbp;
  draw A--B withpen pencircle scaled lbp;
fi;
fi;
enddef;
numeric M;
M := 6;
pair A,B,C,D;
u := 3cm;
A := (0,0);
B := (u,0);
D := B rotated 72;
C := (u,0) + D;
pave(3,A,C,D,M);
pave(4,A,B,C,M);
endfig;

```



```

beginfig(209)
u:=1cm;

def milieu (expr s, ss, n) =
  if n<>0:
    for i="A","BA","BBA":
      milieu(s&i, ss, n-1);
    endfor;
  else:
    dessine(s&ss);
  fi;
enddef;

def doit(expr N) =
  for n=1 upto N:
    for i="A","BA","BBA":
      for j="","B","BB":
        milieu(i,j,n-1);
      endfor;
    endfor;
  endfor;
  milieu("","",0);
enddef;

vardef A(expr a) =
  save x,y,n;
  numeric x,y,n;
  x := xpart a;
  y := ypart a;
  n:=x*x+y*y;
  (-x/n, y/n)
enddef;

vardef B(expr a) =
  save x,y,n;
  numeric x,y,n;
  x := 1 + xpart a;
  y := ypart a;
  n := x*x+y*y;
  (-x/n, y/n)
enddef;

def dessine(expr s) =
  _dessine(s, dir(60), up, dir(120));
  _dessine(s, dir(60), dir(31), dir(2));
  _dessine(s, dir(120), dir(149), dir(178));
enddef;

def _dessine(expr s, a,b,c) =
  pair p[];
  p[0] := a;
  p[1] := b;
  p[2] := c;

  for i=0 upto length(s)-1:
    if (substring(i,i+1) of s) = "A":
      for j=0 upto 2: p[j] := A( p[j] ); endfor;
    elseif (substring(i,i+1) of s) = "B":
      for j=0 upto 2: p[j] := B( p[j] ); endfor;
    else: show("Ceci n'est pas un g^e9n^e9rateur : "&substring(i,i+1) of s)
    fi;
  endfor;
  if (xpart p[0] < 2) and (xpart p[0] > -2) and
    (xpart p[2] > -2) and (xpart p[2] < 2) and
    (ypart p[0] < 2) and (ypart p[2] < 2):
    draw ( p[0] .. p[1] .. p[2] ) scaled u;
  fi;
enddef;

fill (dir(60) .. up .. dir(120) --
  (dir120+up) -- (dir60+up) -- cycle) scaled u
  withcolor red+green;
doit(7);

```

```

draw (u*dir(60)) withpen pencircle scaled 4bp;
draw (0,u) withpen pencircle scaled 4bp;
draw (u*dir(60) -- u*dir(60)+u*up) shifted (0u,0);
draw (u*dir(60) -- u*dir(60)+u*up) shifted (1u,0);
draw (u*dir(60) -- u*dir(60)+u*up) shifted (-u,0);
draw (u*dir(60) -- u*dir(60)+u*up) shifted (-2u,0);
endfig;

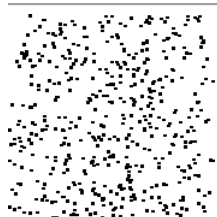
```



```

beginfig(210)
u:=5mm;
pickup pencircle scaled 1pt;
for i=0 upto 500:
draw (u*normaldeviate, u*normaldeviate);
endfor;
endfig;

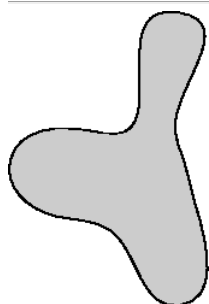
```



```

beginfig(211)
u:=2cm;
pickup pencircle scaled 1pt;
for i=0 upto 500:
draw (u*uniformdeviate(1), u*uniformdeviate(1));
endfor;
endfig;

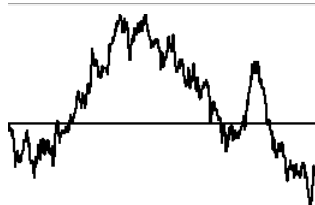
```



```

beginfig(212)
numeric n;
n:=10;
path p;
p := for i=0 upto n-1:
((1cm + 3mm*normaldeviate,0) rotated (i*360/n)) ..
endfor cycle;
fill p withcolor .8white;
draw p;
endfig;

```

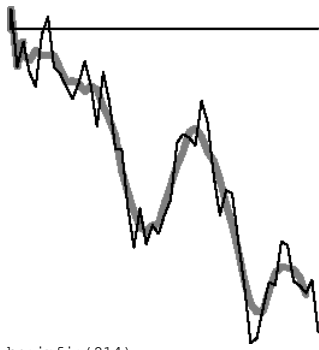


```

beginfig(213)
m:=500;
u:=1cm;
pair A,B;
A:=(0,0);
for i=0 upto m:
B:=(i/m*3u, (ypart A)+normaldeviate/m*30u);
draw A--B;
A:=B;
endfor;
draw (0,0)--(3u,0);
endfig;

```

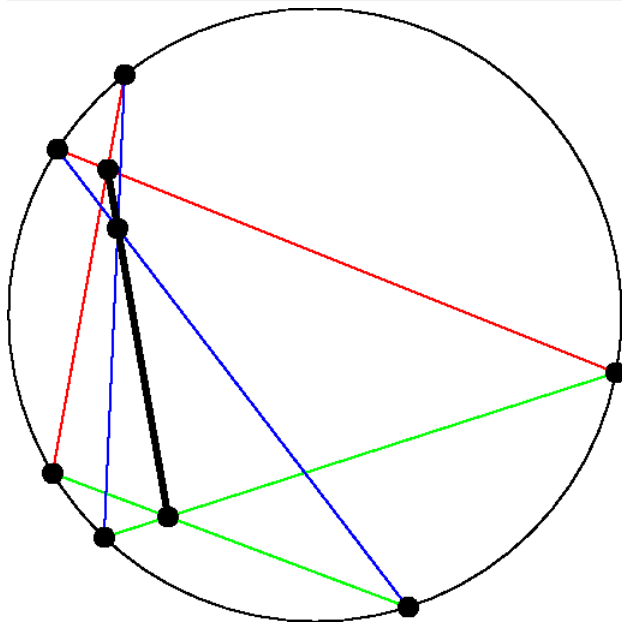




```

beginfig(214)
m:=50;
pair A[], B[];
A[0]=(0,0);
for i=0 upto m:
  A[i+1]=(i/m*3u, (ypart A[i])+(uniformdeviate(2)-1)/m*30u);
endfor;
B[0]=A[0];
B[1]=A[1];
B[2]=A[2];
B[3]=A[3];
for i=4 upto m+1:
  B[i] = ( A[i-4] + A[i-3] + A[i-2] + A[i-1] + A[i])/5;
endfor;
for i=0 upto m:
  draw B[i]--B[i+1] withpen pencircle scaled 2pt
  withcolor .5*white;
endfor;
for i=0 upto m:
  draw A[i]--A[i+1];
endfor;
draw (0,0)--(3u,0);
endfig;

```



```

beginfig(215)
vardef check_pascal =
save again;
boolean again;
again := false;
% Distance entre deux points sur le cercle : au moins 1mm
for i=0 upto 5:
  for j=i+1 upto 5:
    show( decimal(i) & " & decimal(j) & " & decimal(abs(A[i]-A[j])/2mm) );
    if abs(A[i]-A[j]) < 2mm:
      again := true;
    fi;
  endfor;
endfor;
% Distance entre deux des M[i] : au moins 2mm, au plus 10cm
for i=0 upto 2:
  for j=i+1 upto 2:
    if (abs(M[i]-M[j]) > 10cm) or (abs(M[i]-M[j]) < 2mm):
      again := true;
    fi;
  endfor;
endfor;
% Distance entre un A[i] et un M[i] : au moins 2mm
for i=0 upto 5:
  for j=0 upto 2:
    if abs(A[i]-M[j]) < 2mm:
      again := true;
    fi;
  endfor;
endfor;
% Distance entre le cercle et l'un des M[i] : au plus 10cm

```



```

if abs(M[0])>10cm:
  again:=true;
fi;
show again;
not again
enddef;

forever:
  path C;
  C := fullcircle scaled 6cm;
  pair A[], M[];
  for i=0 upto 5:
    A[i] := point uniformdeviate(length(C)) of C;
  endfor;
  M[0] = whatever[ A[0], A[1] ];
  M[0] = whatever[ A[3], A[4] ];
  M[1] = whatever[ A[1], A[2] ];
  M[1] = whatever[ A[4], A[5] ];
  M[2] = whatever[ A[2], A[3] ];
  M[2] = whatever[ A[5], A[0] ];
  exitif check_pascal;
endfor;

draw C;
draw A[0]--A[1] withcolor red;
draw A[3]--A[4] withcolor red;
draw A[0]--M[0] withcolor red dashed evenly;
draw A[3]--M[0] withcolor red dashed evenly;

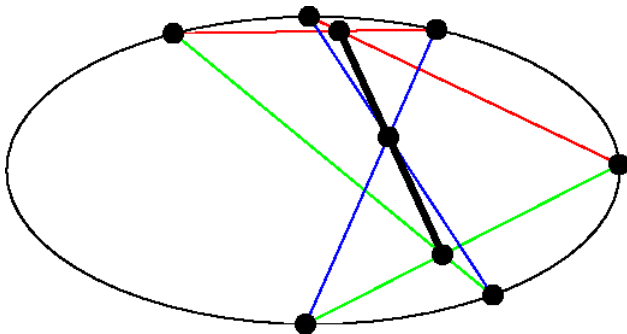
draw A[1]--A[2] withcolor green;
draw A[4]--A[5] withcolor green;
draw A[1]--M[1] withcolor green dashed evenly;
draw A[4]--M[1] withcolor green dashed evenly;

draw A[2]--A[3] withcolor blue;
draw A[5]--A[0] withcolor blue;
draw A[2]--M[2] withcolor blue dashed evenly;
draw A[5]--M[2] withcolor blue dashed evenly;

draw M[0]--M[1]--M[2]--cycle withpen pencircle scaled 2bp;
for i=0 upto 2:
  draw M[i] withpen pencircle scaled 6bp;
endfor;
for i=0 upto 5:
  draw A[i] withpen pencircle scaled 6bp;
endfor;

if xpart (lrcorner currentpicture - llcorner currentpicture) > 4cm:
  currentpicture := currentpicture scaled 4cm /
    xpart (lrcorner currentpicture - llcorner currentpicture);
fi;
endfig;

```



```

beginfig(216)
vardef pascal(expr C) =
  forever:
    pair A[], M[];
    for i=0 upto 5:
      A[i] := point uniformdeviate(length(C)) of C;
    endfor;
    M[0] = whatever[ A[0], A[1] ];
    M[0] = whatever[ A[3], A[4] ];
    M[1] = whatever[ A[1], A[2] ];
    M[1] = whatever[ A[4], A[5] ];
    M[2] = whatever[ A[2], A[3] ];
    M[2] = whatever[ A[5], A[0] ];
    exitif check_pascal;
  endfor;

  draw C;
  draw A[0]--A[1] withcolor red;
  draw A[3]--A[4] withcolor red;
  draw A[0]--M[0] withcolor red dashed evenly;
  draw A[3]--M[0] withcolor red dashed evenly;

  draw A[1]--A[2] withcolor green;
  draw A[4]--A[5] withcolor green;
  draw A[1]--M[1] withcolor green dashed evenly;
  draw A[4]--M[1] withcolor green dashed evenly;

  draw A[2]--A[3] withcolor blue;
  draw A[5]--A[0] withcolor blue;
  draw A[2]--M[2] withcolor blue dashed evenly;
  draw A[5]--M[2] withcolor blue dashed evenly;

  draw M[0]--M[1]--M[2]--cycle withpen pencircle scaled 2bp;
  for i=0 upto 2:
    draw M[i] withpen pencircle scaled 6bp;
  endfor;

```

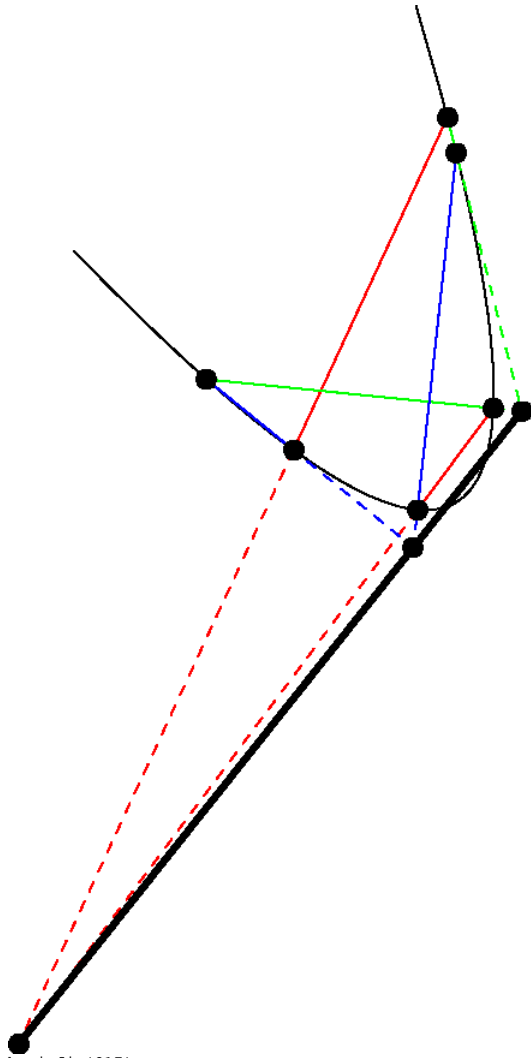
```

for i=0 upto 5:
  draw A[i] withpen pencircle scaled 6bp;
endfor;
enddef;

pascal(fullcircle xscaled 6cm yscaled 3cm);

if xpart (lrcorner currentpicture - llcorner currentpicture) > 4cm:
  currentpicture := currentpicture scaled 4cm /
    xpart (lrcorner currentpicture - llcorner currentpicture);
fi;
endfig;

```

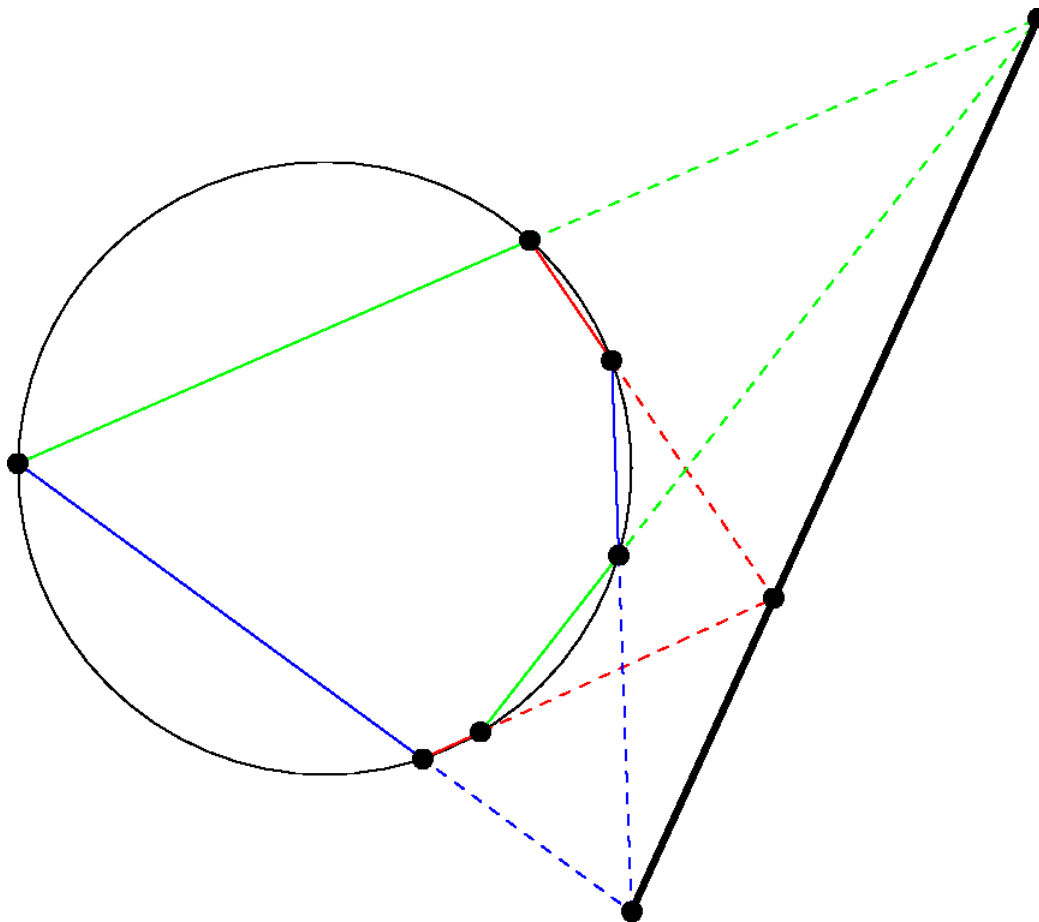


```

beginfig(217)
  pascal((for i=-2cm step .1cm until 2cm:
    (i, (i/1cm)**2 *1cm) ..
  endfor (2.1cm,4.41cm)) rotated 30);

  if xpart (lrcorner currentpicture - llcorner currentpicture) > 4cm:
    currentpicture := currentpicture scaled 4cm /
      xpart (lrcorner currentpicture - llcorner currentpicture);
  fi;
endfig;

```



```

beginfig(218)
vardef pascal(expr C) =
  forever:
    pair A[], M[];

    numeric t[];
    for i=0 upto 5:
      t[i] = uniformdeviate(length(C));
    endfor;
    for i=0 upto 5:
      for j=0 upto 4:
        if t[j]>t[j+1]:
          tt:=t[j]; t[j]:=t[j+1]; t[j+1]:=tt;
        fi;
      endfor;
    endfor;
    for i=0 upto 5:
      A[i] = point t[i] of C;
    endfor;

    M[0] = whatever[ A[0], A[1] ];
    M[0] = whatever[ A[3], A[4] ];
    M[1] = whatever[ A[1], A[2] ];
    M[1] = whatever[ A[4], A[5] ];
    M[2] = whatever[ A[2], A[3] ];
    M[2] = whatever[ A[5], A[0] ];
    exitif check_pascal;
  endfor;

  draw C;
  draw A[0]--A[1] withcolor red;
  draw A[3]--A[4] withcolor red;
  draw A[0]--M[0] withcolor red dashed evenly;
  draw A[3]--M[0] withcolor red dashed evenly;

  draw A[1]--A[2] withcolor green;
  draw A[4]--A[5] withcolor green;
  draw A[1]--M[1] withcolor green dashed evenly;
  draw A[4]--M[1] withcolor green dashed evenly;

  draw A[2]--A[3] withcolor blue;
  draw A[5]--A[0] withcolor blue;
  draw A[2]--M[2] withcolor blue dashed evenly;
  draw A[5]--M[2] withcolor blue dashed evenly;

  draw M[0]--M[1]--M[2]--cycle withpen pencircle scaled 2bp;
  for i=0 upto 2:
    draw M[i] withpen pencircle scaled 6bp;
  endfor;
  for i=0 upto 5:
    draw A[i] withpen pencircle scaled 6bp;
  endfor;
enddef;

pascal(fullcircle scaled 6cm);

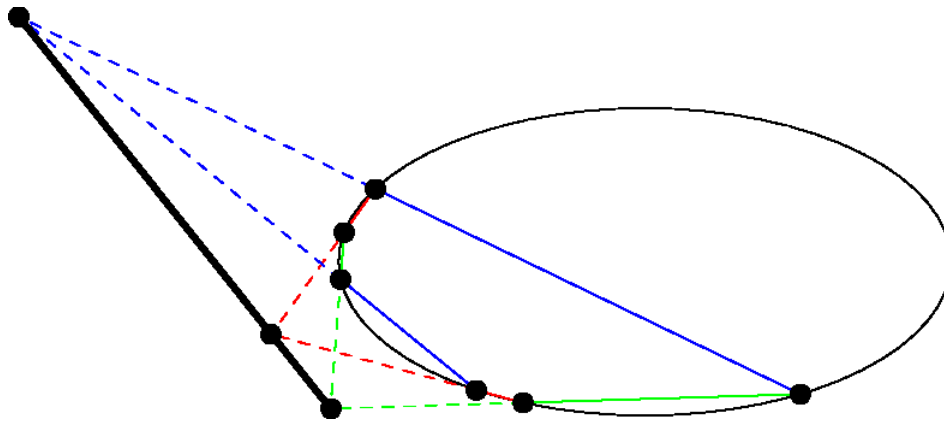
if xpart (lrcorner currentpicture - llcorner currentpicture) > 4cm:

```

```

currentpicture := currentpicture scaled 4cm /
  xpart (lrcorner currentpicture - llcorner currentpicture);
fi;
endfig;

```

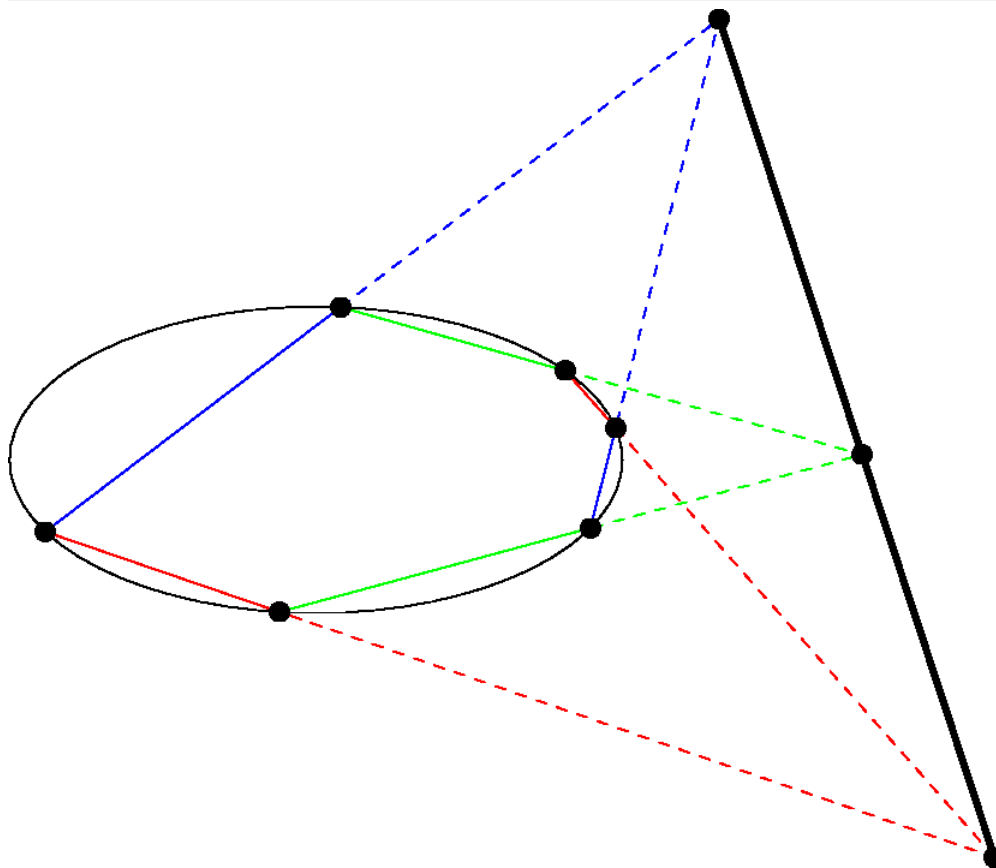


```

beginfig(219)
  pascal(fullcircle xscaled 6cm yscaled 3cm);

  if xpart (lrcorner currentpicture - llcorner currentpicture) > 4cm:
    currentpicture := currentpicture scaled 4cm /
      xpart (lrcorner currentpicture - llcorner currentpicture);
  fi;
endfig;

```

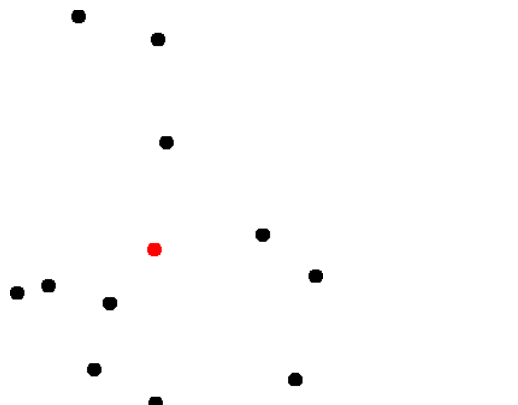


```

beginfig(220)
  pascal(fullcircle xscaled 6cm yscaled 3cm);

  if xpart (lrcorner currentpicture - llcorner currentpicture) > 4cm:
    currentpicture := currentpicture scaled 4cm /
      xpart (lrcorner currentpicture - llcorner currentpicture);
  fi;
endfig;

```

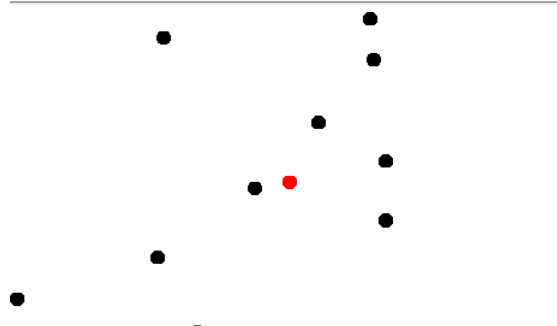


```

beginfig(221)
  vardef barycentre(text t) =
    save n, G;
    pair G; numeric n;
    G := origin; n:=0;
    for a=t:
      G:=G+a;
      n:=n+1;
    endfor;
    G/n
  enddef;

  pair A[];
  n:=10;
  for i=0 upto n:
    A[i] = lcm*(normaldeviate, normaldeviate);
    draw A[i] withpen pencircle scaled 4bp;
  endfor;
  draw barycentre(A[0] for i=1 upto 10: ,A[i] endfor)
    withpen pencircle scaled 4bp withcolor red;
endfig;

```



```

beginfig(222)
  vardef barycentre(text t) =
    save a, i, n, G, X;
    pair G,X; numeric n,i;
    G := origin; n:=0; i:=0;
    for a=t:
      show("i = "& decimal(i));
      show a;
      if odd(i):
        show("odd");
        n:=n+a;
        G:= G + a*X;
      else:
        show("even");
        X:=a;
      fi;
      i:=i+1;
    endfor;
    G/n
  enddef;

  pair A[];
  n:=10;
  for i=0 upto n:
    A[i] = lcm*(normaldeviate, normaldeviate);
    draw A[i] withpen pencircle scaled 4bp;
  endfor;
  draw barycentre(A[0],0 for i=1 upto 10: ,A[i],i endfor)
    withpen pencircle scaled 4bp withcolor red;
endfig;

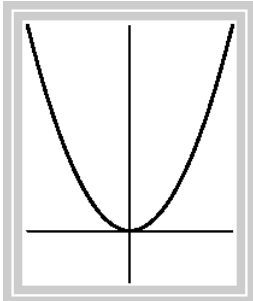
```



```

beginfig(223)
  numeric n;
  n:=10;
  path p;
  p := for i=0 upto n-1:
    ((1cm + 3mm*normaldeviate,0) rotated (i*360/n)) ..
  endfor cycle;
  for i=0 step 2mm until 3cm:
    draw fullcircle scaled i;
  endfor;
  clip currentpicture to p;
  draw p;
endfig;

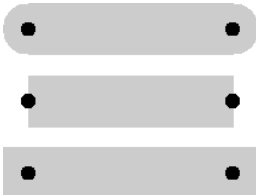
```



```

beginfig(224)
  u := 5mm;
  draw (-2u,0) -- (2u,0);
  draw (0,-u) -- (0,4u);
  draw (-2u,4u) for i=-1.9 step .1 until 2.01: .. (i*u, i*i*u) endfor
  withpen pencircle scaled 1bp;
  draw bbox currentpicture withpen pensquare scaled 2bp withcolor .8white;
  draw bbox currentpicture withpen pensquare scaled 2bp withcolor .8white;
endfig;

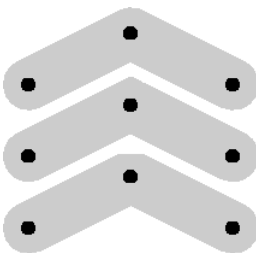
```



```

beginfig(225)
  path p;
  p := (0,0) -- (2cm,0);
  def doit (suffix p)(expr t) =
    begingroup
      interim linecap := t;
      draw p withpen pencircle scaled 5mm withcolor .8white;
    endgroup;
    draw point 0 of p withpen pencircle scaled 4bp;
    draw point 1 of p withpen pencircle scaled 4bp;
    p := p shifted (0,-7mm)
  enddef;
  doit(p,rounded);
  doit(p,butt);
  doit(p,squared);
endfig;

```



```

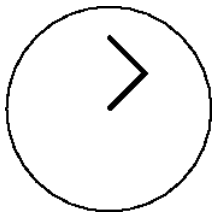
beginfig(226)
  path p;
  p := (0,0) -- (1cm,5mm) -- (2cm,0);
  def doit (suffix p)(expr t) =
    begingroup
      interim linejoin := t;
      draw p withpen pencircle scaled 5mm withcolor .8white;
    endgroup;
    draw point 0 of p withpen pencircle scaled 4bp;
    draw point 1 of p withpen pencircle scaled 4bp;
    draw point 2 of p withpen pencircle scaled 4bp;
    p := p shifted (0,-7mm)
  enddef;
  doit(p,rounded);
  doit(p,mitered);
  doit(p,beveled);
endfig;

```

```

beginfig(227)
  path p;
  p := (0,0) -- (2cm,0);
  vardef doit (suffix p)(expr t) =
    interim linecap := t;
    draw p withpen pencircle scaled 5mm withcolor .8white;
    draw point 0 of p withpen pencircle scaled 4bp;
    draw point 1 of p withpen pencircle scaled 4bp;
    draw point 2 of p withpen pencircle scaled 4bp;
    p := p shifted (0,-7mm)
  enddef;
  doit(p,rounded);
  doit(p,butt);
  doit(p,squared);
endfig;

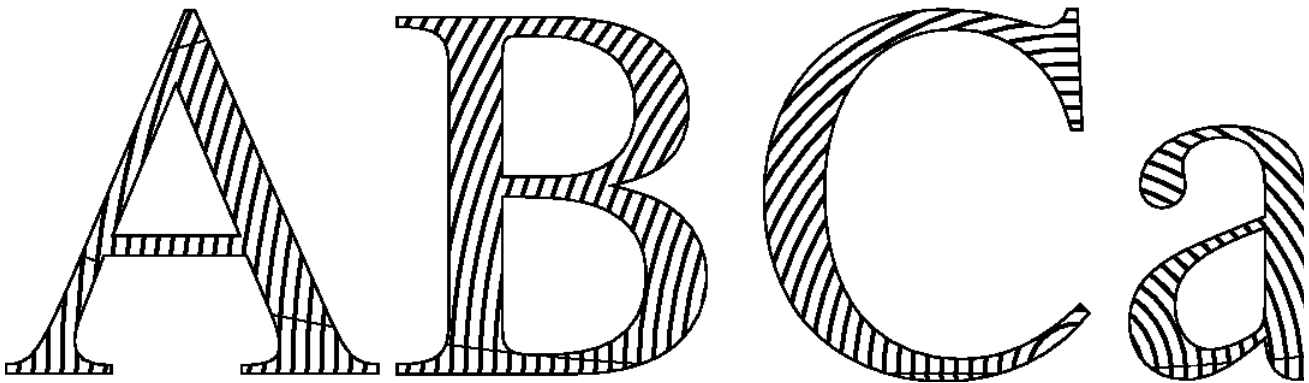
```



```

beginfig(228)
  draw fullcircle scaled 2cm;
  special("0 0 moveto 10 10 rlineto -10 10 rlineto stroke");
endfig;

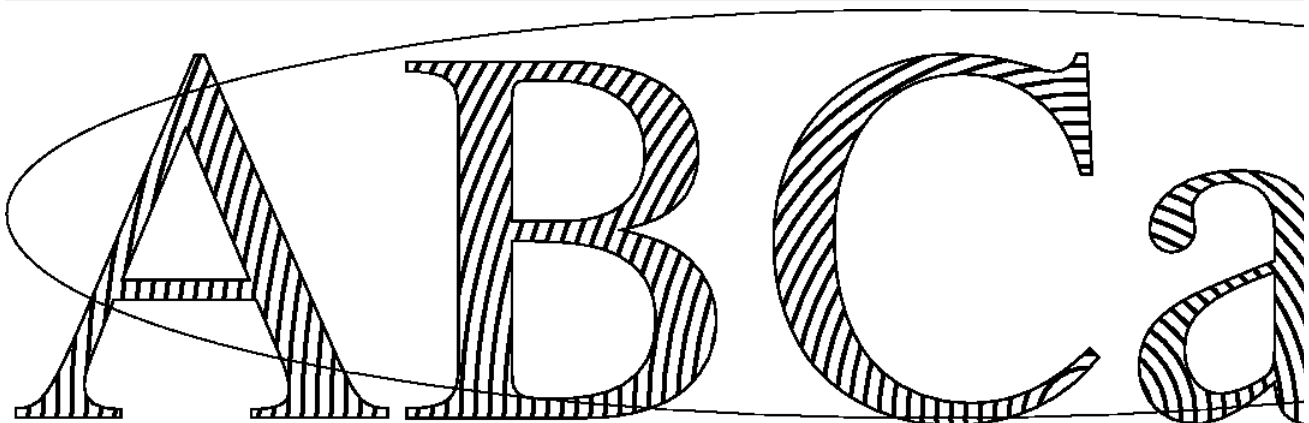
```



```

beginfig(229)
  draw fullcircle shifted (.5,.5) xscaled 18.2cm yscaled 4cm;
  special(
    "/Times-Roman findfont 150 scalefont setfont " &
    "0 0 moveto (ABCabc) false charpath clip stroke " &
    "gsave 300 0 translate " &
    " 2 4 600 {dup 0 moveto 0 exch 0 exch 0 360 arc stroke} for " &
    "grestore "
  );
endfig;

```



```

beginfig(230)
  draw fullcircle shifted (.5,.5) xscaled 18.2cm yscaled 4cm;
  special(
    "gsave " &
    "/Times-Roman findfont 150 scalefont setfont " &
    "0 0 moveto (ABCabc) false charpath clip stroke " &

```

```

"gsave 300 0 translate " &
" 2 4 600 {dup 0 moveto 0 exch 0 exch 0 360 arc stroke} for " &
"grestore " &
"grestore "
);

```

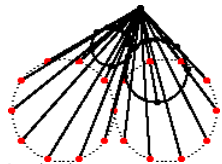
```
endfig;
```



```

beginfig(231)
path p;
p =
(0,u)
for i=.1 step .1 until 10:
hide( pair A; A = (i*u, (sind (i*180/3.14))/i *u);
draw A withpen pencircle scaled 2pt )
.. A
endfor;
draw p;
endfig;

```



```

beginfig(232)
vardef inversion (expr O,k,M) =
if pair M:
(O + k*unitvector(M-O)/abs(M-O))
elseif path M:
for i=0 step length(M)/10 until length(M):
hide(
draw O--inversion(O,k,point i of M)--(point i of M);
draw inversion(O,k,point i of M) withpen pencircle scaled 2pt;
draw point i of M withpen pencircle scaled 2pt withcolor red;
draw O withpen pencircle scaled 2pt;
)
inversion(O,k,point i of M) ..
endfor
cycle
fi
enddef;

```

```

path p[];
p1=fullcircle scaled 2u shifted (u,0);
p2=fullcircle scaled 2u shifted (-u,0);
draw p1 dashed withdots scaled .25;
draw p2 dashed withdots scaled .25;
z0 = (.5u,2u);
draw inversion( z0, 2 (u**2), p1 );
draw inversion( z0, 2 (u**2), p2 );
endfig;

```



```

beginfig(233)
path p;
p := (0,0) -- (1cm,0);
show ahangle;
begingroup
interim ahangle := 30;
interim linejoin := mitered;
interim linecap := butt;
drawarrow p withpen pencircle scaled 2bp;
endgroup;
begingroup
interim ahangle := 60;
drawarrow p shifted (0,-5mm) withpen pencircle scaled 2bp;
endgroup;

```

```
endfig;
```

$\sin 60 = 0.86603$

```

beginfig(234)
numeric x;
x = sind(60);
draw TEX("$\sin 60 = " & decimal(x) & "$");

```

```
endfig;
```



```

beginfig(235)
picture _TEX_pic;

def largeur(expr p) =
if picture p:
xpart( lrcorner(p) - llcorner(p) )
elseif string p:
hide(_TEX_pic := TEX(p));
xpart( lrcorner(_TEX_pic) - llcorner(_TEX_pic) )
else:
hide( errmsg("largeur: wrong type"); 0)
fi

```



```

enddef;

def hauteur(expr p) =
  if picture p:
    ypart(ulcorner(p))
  elseif string p:
    hide(_TEX_pic := TEX(p));
    ypart(ulcorner(_TEX_pic))
  else:
    hide( errmessage("hauteur: wrong type"); 0)
  fi
enddef;

def profondeur (expr p) =
  if picture p:
    -ypart(llcorner(p))
  elseif string p:
    hide(_TEX_pic := TEX(p));
    -ypart(llcorner(_TEX_pic))
  else:
    hide( errmessage("profondeur: wrong type"); 0)
  fi
enddef;

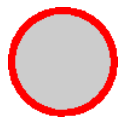
picture p;
string s;
s := "\huge\LaTeX";
p := TEX(s);
drawarrow (0,0) -- (largeur(s),0) withcolor red;
drawarrow (0,0) -- (0,hauteur(s)) withcolor green;
drawarrow (0,0) -- (0,-profondeur(s)) withcolor blue;
draw p;
draw bbox p;
endfig;

```

```

beginfig(236)
def redraw text t = draw t withcolor red enddef;
draw (0,0) -- (2cm,0);
redraw (0,0) -- (2cm,5mm) withpen pencircle scaled 2bp;
endfig;

```



```

beginfig(237)
path _myfill_p;

def myfill expr p =
  _myfill_p := p;
  _myfill
enddef;

def _myfill text t =
  fill _myfill_p t;
  draw _myfill_p t withcolor red;
enddef;

myfill fullcircle scaled 1cm withcolor .8white withpen pencircle scaled 2bp;
endfig;

```



```

beginfig(238)
boxit.a(btex Essai etex);
a.c = (0,0);
drawboxed(a);
endfig;

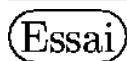
```



```

beginfig(239)
circleit.a(btex Essai etex);
a.c = (0,0);
drawboxed(a);
endfig;

```



```

beginfig(240)
rboxit.a(btex Essai etex);
a.c = (0,0);
drawboxed(a);
endfig;

```



```

beginfig(241)
boxit.a(btex Essai etex);
a.c = (0,0);
drawunboxed(a);
endfig;

```

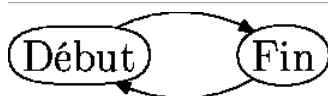
```
endfig;
```



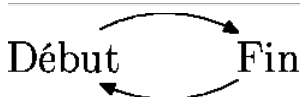
```
beginfig(242)
  circleit.a(btex Essai etex);
  a.c = (0,0);
  a.dx = a.dy;
  drawboxed(a);
endfig;
```



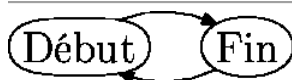
```
beginfig(243)
  circleit.a(btex Essai etex);
  a.c = (0,0);
  a.dx = a.dy;
  drawunboxed(a);
  for i=0 step 10 until 360:
    draw (0,0) -- 1cm*right rotated i cutbefore bpath.a;
  endfor;
endfig;
```



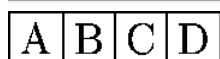
```
beginfig(244)
  circleit.a(btex D^e9but etex);
  a.c = (0,0);
  a.dx = a.dy;
  circleit.b(btex Fin etex);
  b.c = (2cm,0);
  b.dx = b.dy;
  drawboxed(a,b);
  drawarrow a.c {dir 45} .. b.c {dir -45}
  cutbefore bpath.a cutafter bpath.b;
  drawarrow b.c {dir -135} .. a.c {dir 135}
  cutbefore bpath.b cutafter bpath.a;
endfig;
```



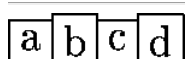
```
beginfig(245)
  circleit.a(btex D^e9but etex);
  a.c = (0,0);
  a.dx = a.dy;
  circleit.b(btex Fin etex);
  b.c = (2cm,0);
  b.dx = b.dy;
  drawunboxed(a,b);
  drawarrow a.c {dir 45} .. b.c {dir -45}
  cutbefore bpath.a cutafter bpath.b;
  drawarrow b.c {dir -135} .. a.c {dir 135}
  cutbefore bpath.b cutafter bpath.a;
endfig;
```



```
beginfig(246)
  boxjoin(
    a.dx = a.dy;
    b.dx = b.dy;
    a.e + (5mm,0) = b.w;
  );
  circleit.a(btex D^e9but etex);
  a.c = (0,0);
  circleit.b(btex Fin etex);
  drawboxed(a,b);
  drawarrow a.c {dir 45} .. b.c {dir -45}
  cutbefore bpath.a cutafter bpath.b;
  drawarrow b.c {dir -135} .. a.c {dir 135}
  cutbefore bpath.b cutafter bpath.a;
endfig;
```



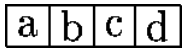
```
beginfig(247)
  % Toujours mettre la commande boxjoin au d^e9but.
  boxjoin(a.e = b.w);
  boxit.a(btex A etex);
  boxit.b(btex B etex);
  boxit.c(btex C etex);
  boxit.d(btex D etex);
  drawboxed(a,b,c,d);
endfig;
```



```

beginfig(248)
  boxjoin(a.e = b.w);
  boxit.a(btex a etex);
  boxit.b(btex b etex);
  boxit.c(btex c etex);
  boxit.d(btex d etex);
  drawboxed(a,b,c,d);
endfig;

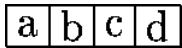
```



```

beginfig(249)
  boxjoin(a.se = b.sw; a.ne = b.nw);
  boxit.a(btex a etex);
  boxit.b(btex b etex);
  boxit.c(btex c etex);
  boxit.d(btex d etex);
  drawboxed(a,b,c,d);
endfig;

```



```

beginfig(250)
  boxjoin(a.se = b.sw; a.ne = b.nw);
  boxit.a1(btex a etex);
  boxit.a2(btex b etex);
  boxit.a3(btex c etex);
  boxit.a4(btex d etex);
  drawboxed(a1,a2,a3,a4);
endfig;

```



```

beginfig(251)
  draw (0,0) -- (5cm,0) withcolor red;
  draw btex a etex ;
  draw btex b etex shifted (1cm,0);
  draw btex c etex shifted (2cm,0);
  draw btex d etex shifted (3cm,0);
  draw btex e etex shifted (4cm,0);
endfig;

```



```

beginfig(252)
  draw (0,0) -- (5cm,0) withcolor red;
  boxjoin(b.c - a.c = (1cm,0));
  boxit a (btex a etex);
  boxit b (btex b etex);
  boxit c (btex c etex);
  boxit d (btex d etex);
  boxit e (btex e etex);
  drawunboxed(a,b,c,d,e);
endfig;

```

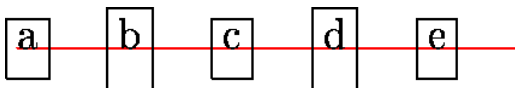


```

beginfig(253)
  vardef boxTEX expr s =
    save p,h,l;
    picture p;
    numeric h,l;
    p := TEX(s);
    h := max(ypart ulcorner(p), abs(ypart llcorner(p)));
    l := xpart llcorner(p);
    setbounds p to (0,-h)--(l,-h)--(l,h)--(0,h)--cycle;
  p
enddef;

  draw (0,0) -- (5cm,0) withcolor red;
  boxjoin(b.c - a.c = (1cm,0));
  boxit a (boxTEX "a");
  boxit b (boxTEX "b");
  boxit c (boxTEX "c");
  boxit d (boxTEX "d");
  boxit e (boxTEX "e");
  drawunboxed(a,b,c,d,e);
endfig;

```



```

beginfig(254)
  draw (0,0) -- (5cm,0) withcolor red;
  boxjoin(b.c - a.c = (1cm,0));
  boxit a (boxTEX "a");
  boxit b (boxTEX "b");
  boxit c (boxTEX "c");
  boxit d (boxTEX "d");
  boxit e (boxTEX "e");
  drawboxed(a,b,c,d,e);
endfig;

```



```

beginfig(255)
  let OLD_beginbox_ = beginbox_;
  def beginbox_(expr pp,sp)(suffix $(text t) =
    _n := str $;
    generic_declare(pair) _n.off, _n.c;
    generic_declare(string) pproc_._n, sproc_._n;
    generic_declare(picture) pic_._n;
    pproc_$:=pp; sproc_$:=sp;
    pic_$ = nullpicture;
    for _p=t:
      pic_$:=

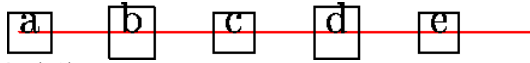
```

```

    if picture _p: _p_
    else: _p_ infont defaultfont scaled defaultscale
    fi;
  endfor
  $c = $off + (.5[xpart llcorner pic_$, xpart urcorner pic_$], 0)
enddef;

draw (0,0) -- (5cm,0) withcolor red;
boxjoin(b.c - a.c = (1cm,0));
boxit a (btex a etex);
boxit b (btex b etex);
boxit c (btex c etex);
boxit d (btex d etex);
boxit e (btex e etex);
drawunboxed(a,b,c,d,e);
endfig;

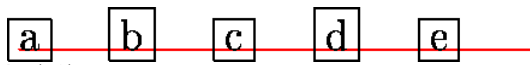
```



```

beginfig(256)
  draw (0,0) -- (5cm,0) withcolor red;
  boxjoin(b.c - a.c = (1cm,0));
  boxit a (btex a etex);
  boxit b (btex b etex);
  boxit c (btex c etex);
  boxit d (btex d etex);
  boxit e (btex e etex);
  drawboxed(a,b,c,d,e);
endfig;

```



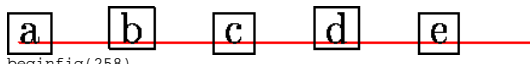
```

beginfig(257)
let OLD_boxit = boxit;
let OLD_sizebox_ = sizebox_;
let OLD_clearb_ = clearb_;

vardef boxit@#(text tt) =
  beginbox_("boxpath_", "sizebox_", @#, tt);
  generic_declare(pair) _n.sw, _n.s, _n.se, _n.e, _n.ne, _n.n, _n.nw, _n.w;
  0 = xpart (@#nw-@#sw) = ypart(@#se-@#sw);
  0 = xpart(@#ne-@#se) = ypart(@#ne-@#nw);
  @#s = .5[@#sw, @#se];
  @#n = .5[@#ne, @#nw];
  xpart @#w = xpart @#nw;
  xpart @#e = xpart @#ne;
  ypart @#w = ypart @#c = ypart @#e;
  @#ne-@#c = (@#dx, @#dy) +
    (xpart(.5*(urcorner pic_@# - llcorner pic_@#)), ypart urcorner pic_@#);
  @#c-@#sw = (@#dx, @#dy) +
    (xpart(.5*(urcorner pic_@# - llcorner pic_@#)), -ypart lrcorner pic_@#);
  endbox_(clearb_, @#);
enddef;

draw (0,0) -- (5cm,0) withcolor red;
boxjoin(b.c - a.c = (1cm,0));
boxit a (btex a etex);
boxit b (btex b etex);
boxit c (btex c etex);
boxit d (btex d etex);
boxit e (btex e etex);
drawboxed(a,b,c,d,e);
endfig;

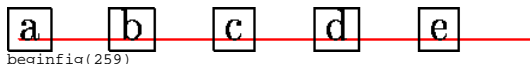
```



```

beginfig(258)
  draw (0,0) -- (5cm,0) withcolor red;
  boxjoin(b.c - a.c = (1cm,0); b.ne - b.se = a.nw - a.sw);
  boxit a (btex a etex);
  boxit b (btex b etex);
  boxit c (btex c etex);
  boxit d (btex d etex);
  boxit e (btex e etex);
  drawboxed(a,b,c,d,e);
endfig;

```



```

beginfig(259)
vardef boxit@#(text tt) =
  beginbox_("boxpath_", "sizebox_", @#, tt);
  generic_declare(pair) _n.sw, _n.s, _n.se, _n.e, _n.ne, _n.n, _n.nw, _n.w;
  0 = xpart (@#nw-@#sw) = ypart(@#se-@#sw);
  0 = xpart(@#ne-@#se) = ypart(@#ne-@#nw);
  @#s = .5[@#sw, @#se];
  @#n = .5[@#ne, @#nw];
  xpart @#w = xpart @#nw;
  xpart @#e = xpart @#ne;
  ypart @#w = ypart @#c = ypart @#e;
  @#ne-@#c = (@#dx, @#dyup) +
    (xpart(.5*(urcorner pic_@# - llcorner pic_@#)), ypart urcorner pic_@#);
  @#c-@#sw = (@#dx, @#dydown) +
    (xpart(.5*(urcorner pic_@# - llcorner pic_@#)), -ypart lrcorner pic_@#);
  endbox_(clearb_, @#);
enddef;

def sizebox_(suffix $) =
  if unknown $.dx: $.dx=defaultdx; fi
  if unknown $.dyup:
    if unknown $.dy:
      $.dyup=defaultdy
    else:
      $.dyup=$.dy
    fi
  fi
enddef;

```

```

fi;
fi;
if unknown $.dydown:
  if unknown $.dy:
    $.dydown=defaultdy
  else:
    $.dydown=$.dy
  fi;
fi;
enddef;

vardef clearb_(suffix $) =
  _n_ := str $;
  generic_redeclare(numeric) _n.sw, _n.s, _n.se, _n.e, _n.ne, _n.n, _n.nw, _n.w,
  _n.c, _n.off, _n.dx, _n.dy, _n.dyup, _n.dydown;
enddef;

draw (0,0) -- (5cm,0) withcolor red;
boxjoin(b.c - a.c = (1cm,0); ypart( b.ne - a.ne ) = 0; ypart( b.se - a.se ) = 0);
boxit a (btex a etex);
boxit b (btex b etex);
boxit c (btex c etex);
boxit d (btex d etex);
boxit e (btex e etex);
drawboxed(a,b,c,d,e);
endfig;

```



```

beginfig(260)
draw (0,0) -- (5cm,0) withcolor red;
picture p;
numeric h;
p := btex b etex;
h = ypart ( ulcorner p - llcorner p );
boxjoin(
  b.c - a.c = (1cm,0);
  ypart( b.ne - a.ne ) = 0;
  ypart( a.ne - a.se ) = h+2defaultdy;
);
boxit a (btex a etex);
boxit b (btex b etex);
boxit c (btex c etex);
boxit d (btex d etex);
boxit e (btex e etex);
drawboxed(a,b,c,d,e);
endfig;

```



```

beginfig(261)
% Les lignes suivantes n'ont pas l'effet escompté...
let beginbox_ = OLD_beginbox_;
let boxit_ = OLD_boxit_;
let sizebox_ = OLD_sizebox_;
let clearb_ = OLD_clearb_;

% On recopie donc les définitions initiales des macros que l'on a modifiées...
extra_beginfig := "";
extra_endfig := "";
input boxes;

% Et on regarde sur un exemple si ça marche...
draw (0,0) -- (5cm,0) withcolor red;
boxjoin(b.c - a.c = (1cm,0));
boxit a (btex a etex);
boxit b (btex b etex);
boxit c (btex c etex);
boxit d (btex d etex);
boxit e (btex e etex);
drawboxed(a,b,c,d,e);
endfig;

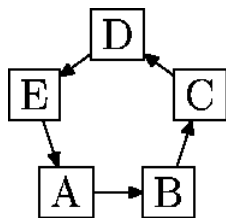
```



```

beginfig(262)
boxit.a1(btex $a$ etex);
boxit.b1(btex etex);
boxit.a2(btex $b$ etex);
boxit.b2(btex etex);
boxit.a3(btex $c$ etex);
boxit.b3(btex etex);
boxit.a4(btex $d$ etex);
boxit.b4(btex etex);
for i=1 upto 4:
  % Les boîtes a[i] et b[i] sont collées
  a[i].e = b[i].w;
  % Il y a un peu d'espace entre b[i] et a[i+1]
  b[i].e + (5mm,0) = a[i+1].w;
  % La hauteur des boîtes est la même
  a[i].n - a[i].s = a[i+1].n - a[i+1].s = b[i].n - b[i].s ;
  % Les b[i] ne sont pas très larges
  b[i].e - b[i].w = (2mm,0);
endfor;
drawboxed(a1,b1,a2,b2,a3,b3,a4,b4);
for i=1 upto 3:
  drawarrow b[i].c {up} .. a[i+1].c {down}
  cutafter bpath.a[i+1];
endfor;
endfig;

```



```

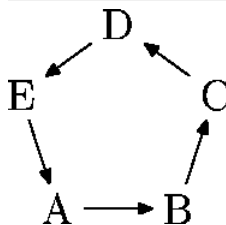
beginfig(263)
  boxit.a(btex A etex);
  boxit.b(btex B etex);
  boxit.c(btex C etex);
  boxit.d(btex D etex);
  boxit.e(btex E etex);

  b.c-a.c = (1cm,0);
  c.c-b.c = (b.c-a.c) rotated 72;
  d.c-c.c = (c.c-b.c) rotated 72;
  e.c-d.c = (d.c-c.c) rotated 72;
  a.c-e.c = (e.c-d.c) rotated 72;
  b.c-a.c = (a.c-e.c) rotated 72;

  drawboxed(a,b,c,d,e);

  drawarrow a.c -- b.c cutbefore bpath.a cutafter bpath.b;
  drawarrow b.c -- c.c cutbefore bpath.b cutafter bpath.c;
  drawarrow c.c -- d.c cutbefore bpath.c cutafter bpath.d;
  drawarrow d.c -- e.c cutbefore bpath.d cutafter bpath.e;
  drawarrow e.c -- a.c cutbefore bpath.e cutafter bpath.a;
endfig;

```



```

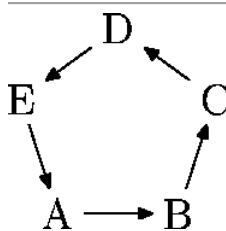
beginfig(264)
  boxit.a(btex A etex);
  boxit.b(btex B etex);
  boxit.c(btex C etex);
  boxit.d(btex D etex);
  boxit.e(btex E etex);

  d.c = 1cm*up;
  e.c = 1cm*up rotated (1*72);
  a.c = 1cm*up rotated (2*72);
  b.c = 1cm*up rotated (3*72);
  c.c = 1cm*up rotated (4*72);

  drawunboxed(a,b,c,d,e);

  drawarrow a.c -- b.c cutbefore bpath.a cutafter bpath.b;
  drawarrow b.c -- c.c cutbefore bpath.b cutafter bpath.c;
  drawarrow c.c -- d.c cutbefore bpath.c cutafter bpath.d;
  drawarrow d.c -- e.c cutbefore bpath.d cutafter bpath.e;
  drawarrow e.c -- a.c cutbefore bpath.e cutafter bpath.a;
endfig;

```



```

beginfig(265)
  def linkboxes(suffix a,b) =
    drawarrow a.c -- b.c cutbefore bpath.a cutafter bpath.b;
  enddef;

  boxit.a(btex A etex);
  boxit.b(btex B etex);
  boxit.c(btex C etex);
  boxit.d(btex D etex);
  boxit.e(btex E etex);

  d.c = 1cm*up;
  e.c = 1cm*up rotated (1*72);
  a.c = 1cm*up rotated (2*72);
  b.c = 1cm*up rotated (3*72);
  c.c = 1cm*up rotated (4*72);

  drawunboxed(a,b,c,d,e);

  linkboxes(a,b);
  linkboxes(b,c);
  linkboxes(c,d);
  linkboxes(d,e);
  linkboxes(e,a);
endfig;

```

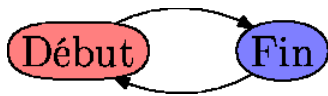
Essai

```
beginfig(266)
  boxit a(btex Essai etex);
  fill bpath a withcolor .5[red,white];
  drawboxed(a);
endfig;
```



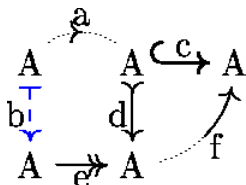
```
beginfig(267)
  def drawredboxed(text t) =
    forsuffices a=t:
      fill bpath a withcolor .5[red,white];
    endfor;
  drawboxed(t);
  enddef;

  circleit.a(btex D^e9but etex);
  a.c = (0,0);
  a.dx = a.dy;
  circleit.b(btex Fin etex);
  b.c = (2cm,0);
  b.dx = b.dy;
  drawredboxed(a,b);
  drawarrow a.c {dir 45} .. b.c {dir -45}
  cutbefore bpath.a cutafter bpath.b;
  drawarrow b.c {dir -135} .. a.c {dir 135}
  cutbefore bpath.b cutafter bpath.a;
endfig;
```



```
beginfig(268)
  def drawcoloredboxed(expr c)(text t) =
    forsuffices a=t:
      fill bpath a withcolor c;
    endfor;
  drawboxed(t);
  enddef;

  circleit.a(btex D^e9but etex);
  a.c = (0,0);
  a.dx = a.dy;
  circleit.b(btex Fin etex);
  b.c = (2cm,0);
  b.dx = b.dy;
  drawcoloredboxed(.5[red,white], a);
  drawcoloredboxed(.5[blue,white], b);
  drawarrow a.c {dir 45} .. b.c {dir -45}
  cutbefore bpath.a cutafter bpath.b;
  drawarrow b.c {dir -135} .. a.c {dir 135}
  cutbefore bpath.b cutafter bpath.a;
endfig;
```



```
beginfig(269)
def_begindiag =
  begingroup;
  save _diag_x, _diag_x_max, _diag_y, _diag_y_max, _diag;
  numeric _diag_x, _diag_x_max, _diag_y, _diag_y_max;
  string _diag[];
  % Num^e9ro de ligne et de colonne courrants
  _diag_x = -1; _diag_y = 0;
  % Num^e9ro de ligne et de colonne maximaux
  _diag_x_max = _diag_y_max = 0;
  save _diag_ar_n, _diag_ar_source, _diag_ar_but, _diag_ar_up, _diag_ar_down;
  % Nombre de fl^e8ches
  numeric _diag_ar_n; _diag_ar_n=-1;
  % Source et but de la fl^e8che
  pair _diag_ar_source[], _diag_ar_but[];
  % Ce qu'il faut ^e9crire au dessus ou au dessous
  string _diag_ar_up[], _diag_ar_down[];
  save _diag_ar_curved, _diag_ar_shape, _diag_ar_color, _diag_ar_width;
  % ^^ab courbure ^^bb (c'est une distance)
  numeric _diag_ar_curved[];
  % Forme de la fl^e8che
  string _diag_ar_shape[];
  % Couleur, ^^e9paisseur, pointill^^e9s
  color _diag_ar_color[];
  numeric _diag_ar_width[];
  picture _diag_ar_dashed[];
enddef;

def node expr A =
  _diag_x := _diag_x + 1;
  _diag_x_max := max(_diag_x, _diag_x_max);
  _diag[_diag_x][_diag_y] := A;
enddef;
```

```

def nextline =
  _diag_x := -1;
  _diag_y := _diag_y + 1;
  _diag_y_max := max(_diag_y, _diag_y_max);
enddef;

tertiarydef a => b = a, b enddef;
def even (expr a) = not odd(a) enddef;

vardef rarrowto(expr a,b)(text t) =
  save i,p;
  _diag_ar_n := _diag_ar_n + 1;
  _diag_ar_source[_diag_ar_n] = (_diag_x, _diag_y);
  _diag_ar_but[_diag_ar_n] = (_diag_x + a, _diag_y + b);

  numeric i; i:=0;
  string current;
  for p=t:
    if even(i):
      current := p;
    else:
      if current = "above":
        _diag_ar_up[_diag_ar_n] = p;
      elseif current = "below":
        _diag_ar_down[_diag_ar_n] = p;
      elseif current = "shape":
        _diag_ar_shape[_diag_ar_n] = p;
      elseif current = "curved":
        _diag_ar_curved[_diag_ar_n] = p;
      elseif current = "color":
        _diag_ar_color[_diag_ar_n] = p;
      elseif current = "width":
        _diag_ar_width[_diag_ar_n] = p;
      elseif current = "dashed":
        _diag_ar_dashed[_diag_ar_n] = p;
      else:
        errmessage("rarrowto: Wrong argument "&ditto&t&ditto);
      fi;
    fi;
    i := i + 1;
  endfor;
  if odd i:
    errmessage("rarrowto: Odd number of arguments "&decimal(i));
  fi;
enddef;

%% Les t^eates de fl^e8ches

picture withsmalldots, notdashed;
withsmalldots := withdots scaled .3;
notdashed := dashpattern(on 50cm);

vardef diag_arrow_head (expr p, t) =
  save A,B,C,u; pair A,B,C,u;
  B := point t of p;
  u := -unitvector(direction t of p);
  A := B + ahlength*u rotated(-ahangle);
  C := B + ahlength*u rotated(+ahangle);
  A .. {-u} B {u} .. C
enddef;

vardef diag_arrow_bar (expr p, t) =
  save A,B,C,u; pair A,B,C,u;
  B := point t of p;
  u := unitvector(direction t of p);
  A := B + ahlength*sind(ahangle)*u rotated(90);
  C := B + ahlength*sind(ahangle)*u rotated(-90);
  A .. B .. C
enddef;

%% Les fl^e8ches

def diag_draw_arrow_default(suffix a,b)(expr curved, w, col, dash) =
  p = a.c ..
  (1/2 [a.c,b.c] + curved*unitvector(b.c-a.c) rotated 90)
  .. b.c;
  pp := p cutbefore bpath.a cutafter bpath.b;
  draw pp
  withcolor col withpen pencircle scaled w dashed dash;
  draw diag_arrow_head (pp, length(pp))
  withcolor col withpen pencircle scaled w;
enddef;

def diag_draw_arrow_middle(suffix a,b)(expr curved, w, col, dash) =
  p = a.c ..
  (1/2 [a.c,b.c] + curved*unitvector(b.c-a.c) rotated 90)
  .. b.c;
  pp := p cutbefore bpath.a cutafter bpath.b;
  draw pp
  withcolor col withpen pencircle scaled w dashed dash;
  draw diag_arrow_head(p,1)
  withcolor col withpen pencircle scaled w;
enddef;

def diag_draw_arrow_epi(suffix a,b)(expr curved, w, col, dash) =
  p = a.c ..
  (1/2 [a.c,b.c] + curved*unitvector(b.c-a.c) rotated 90)
  .. b.c;
  pp := p cutbefore bpath.a cutafter bpath.b;
  draw pp
  withcolor col withpen pencircle scaled w dashed dash;
  draw diag_arrow_head (pp, length(pp))
  withcolor col withpen pencircle scaled w;
  path ppp;
  ppp := pp cutafter (fullcircle scaled lmm shifted point length(pp) of pp);
  draw diag_arrow_head(ppp, length(ppp))

```



```

        withcolor col withpen pencircle scaled w;
    enddef;

def diag_draw_arrow_mono(suffix a,b)(expr curved, w, col, dash) =
    p = a.c ..
    (1/2 [a.c,b.c] + curved*unitvector(b.c-a.c) rotated 90)
    .. b.c;
    pp := p cutbefore bpath.a cutafter bpath.b;
    path ppp;
    ppp := pp cutbefore (fullcircle scaled 1mm shifted point 0 of pp);
    draw ppp
        withcolor col withpen pencircle scaled w dashed dash;
    draw diag_arrow_head (pp, length(pp))
        withcolor col withpen pencircle scaled w;
    draw diag_arrow_head(ppp, 0)
        withcolor col withpen pencircle scaled w;
enddef;

vardef diag_draw_arrow_inj(suffix a,b)(expr curved, w, col, dash) =
    p = a.c ..
    (1/2 [a.c,b.c] + curved*unitvector(b.c-a.c) rotated 90)
    .. b.c;
    pp := p cutbefore bpath.a cutafter bpath.b;
    path ppp;
    ppp := pp cutbefore (fullcircle scaled 1mm shifted point 0 of pp);
    draw ppp
        withcolor col withpen pencircle scaled w dashed dash;
    draw diag_arrow_head (pp, length(pp))
        withcolor col withpen pencircle scaled w;
    save u,A,B,C;
    pair u,A,B,C;
    A := point 0 of ppp;
    u := unitvector(direction 0 of ppp);
    B := A + ahlength*(-u) rotated (-ahangle);
    C := A + 2 ahlength*sind(ahangle)*u rotated 90;
    draw C {-u} .. B .. A {u}
        withcolor col withpen pencircle scaled w dashed dash;
enddef;

def diag_draw_arrow_mapsto(suffix a,b)(expr curved, w, col, dash) =
    p = a.c ..
    (1/2 [a.c,b.c] + curved*unitvector(b.c-a.c) rotated 90)
    .. b.c;
    pp := p cutbefore bpath.a cutafter bpath.b;
    draw pp
        withcolor col withpen pencircle scaled w dashed dash;
    draw diag_arrow_head (pp, length(pp))
        withcolor col withpen pencircle scaled w;
    draw diag_arrow_bar (pp, 0)
        withcolor col withpen pencircle scaled w;
enddef;

def diag_draw_arrow_half_dotted(suffix a,b)(expr curved, w, col, dash) =
    p = a.c ..
    (1/2 [a.c,b.c] + curved*unitvector(b.c-a.c) rotated 90)
    .. b.c;
    pp := p cutbefore bpath.a cutafter bpath.b;
    draw subpath(0,1) of pp
        withcolor col withpen pencircle scaled w dashed withsmalldots;
    draw subpath(1,2) of pp
        withcolor col withpen pencircle scaled w;
    draw diag_arrow_head (pp, length(pp))
        withcolor col withpen pencircle scaled w;
enddef;

%% Fin des fl^^e8ches

def color_to_string (expr a) =
    "&
    decimal(redpart a)
    &","&
    decimal(greenpart a)
    &","&
    decimal(bluepart a)
    &")"
enddef;

def enddiag =
    save i,j,k,l,mm,a,A,p,b;
    for i=0 upto _diag_x_max:
        for j=0 upto _diag_y_max:
            if known _diag[i][j]:
                circleit.a[i][j]( _diag[i][j] );
                a[i][j].dx = a[i][j].dy;
                a[i][j].c = 1cm * (i,-j);
                drawunboxed( a[i][j] );
            fi;
        endfor;
    endfor;
    for m=0 upto _diag_ar_n:
        % V^^e9rifier que le but existe
        i := xpart _diag_ar_source[m];
        j := ypart _diag_ar_source[m];
        k := xpart _diag_ar_but[m];
        l := ypart _diag_ar_but[m];

        % On trace la fl^^e8che. Le chemin est mis dans la variable p.
        path p,pp;
        if unknown _diag_ar_shape[m]: _diag_ar_shape[m] := "default" fi;
        if unknown _diag_ar_color[m]: _diag_ar_color[m] := black fi;
        if unknown _diag_ar_width[m]: _diag_ar_width[m] := .5bp fi;
        if unknown _diag_ar_curved[m]: _diag_ar_curved[m] := 0 fi;
        if unknown _diag_ar_dashed[m]: _diag_ar_dashed[m] := notdashed fi;
        % On ne peut PAS utiliser m dans une cha^^eene ce caract^^e8res que l'on donne
        % ^^e0 scantokens, car m est une variable de boucle. C'est vraiment sp^^e9cial,
        % une variable de boucle.
        mm := m;

```

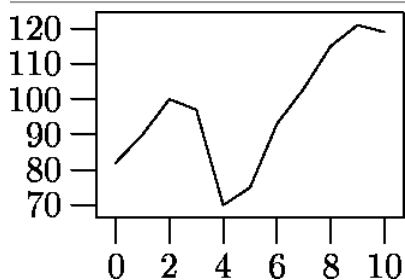
```

scantokens(
  "diag_draw_arrow_"& _diag_ar_shape[m]
  &"("
  &"a[i][j], a[k][l],_diag_ar_curved[mm],_diag_ar_width[mm],"
  &"_diag_ar_color[mm],_diag_ar_dashed[mm]"
  &");"
);

% On ^^e9crit des choses au dessus ou au dessous des fl^^e8ches
pair A;
A = point 1/2 length(p) of p;
if known _diag_ar_up[m]:
  boxit.b[m](_diag_ar_up[m]);
  b[m].c = A + 4bp*unitvector(direction 1/2 length(p) of p rotated 90);
  drawunboxed(b[m]);
fi;
if known _diag_ar_down[m]:
  boxit.c[m](_diag_ar_down[m]);
  c[m].c = A + 4bp*unitvector(direction 1/2 length(p) of p rotated -90);
  drawunboxed(c[m]);
fi;
endfor;
endgroup;
enddef;

begindiag;
node "A";
  rarrowto(1,0, "above" => "a",
    "shape" => "middle",
    "curved" => 3mm,
    "dashed" => withsmalldots);
  rarrowto(0,1, "below" => "b",
    "color" => blue,
    "shape" => "mapsto",
    "dashed" => evenly);
node "A";
  rarrowto(1,0, "above" => "c", "width" => 1bp, "shape" => "inj");
  rarrowto(0,1, "below" => "d", "shape" => "mono");
node "A";
nextline;
node "A";
  rarrowto(1,0, "below" => "e", "shape" => "epi");
node "A";
  rarrowto(1,-1, "below" => "f", "curved" => -3mm, "shape" => "half_dotted");
enddiag;
endfig;

```

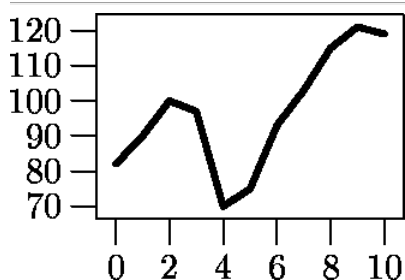


```

beginfig(270)
  draw begingraph(3cm,2cm)
  gdraw "data1";
endgraph;

```

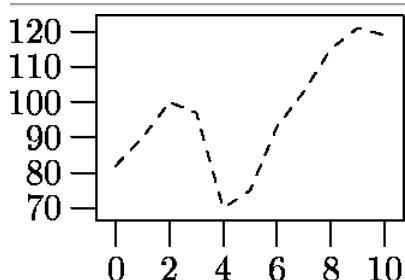
```
endfig;
```



```

beginfig(271)
  draw begingraph(3cm,2cm)
  gdraw "data1" withpen pencircle scaled 2bp;
endgraph;
endfig;

```

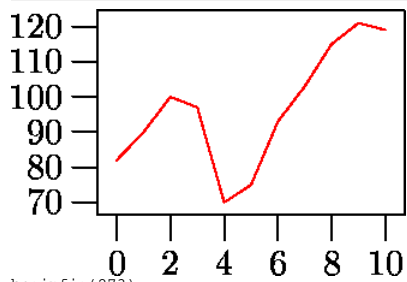


```

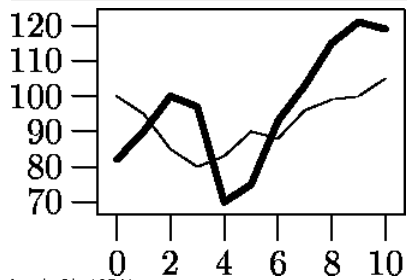
beginfig(272)
  draw begingraph(3cm,2cm)
  gdraw "data1" dashed evenly;

```

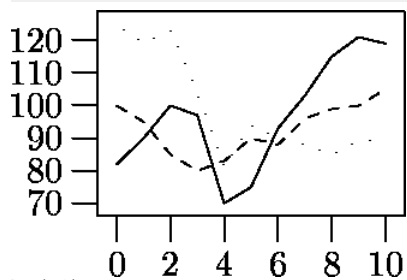
```
endgraph;
endfig;
```



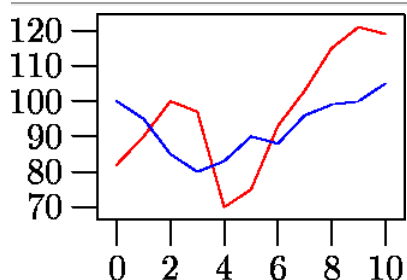
```
beginfig(273)
draw begingraph(3cm,2cm)
gdraw "data1" withcolor red;
endgraph;
endfig;
```



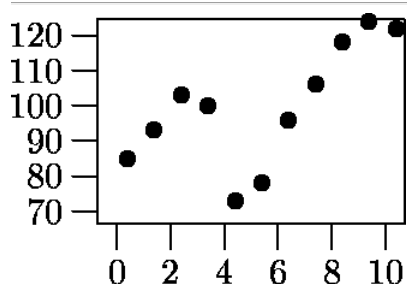
```
beginfig(274)
draw begingraph(3cm,2cm)
gdraw "data1" withpen pencircle scaled 2bp;
gdraw "data2" ;
endgraph;
endfig;
```



```
beginfig(275)
draw begingraph(3cm,2cm)
gdraw "data1" ;
gdraw "data2" dashed evenly;
gdraw "data3" dashed withdots;
endgraph;
endfig;
```



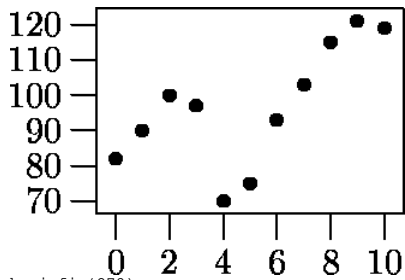
```
beginfig(276)
draw begingraph(3cm,2cm)
gdraw "data1" withcolor red;
gdraw "data2" withcolor blue;
endgraph;
endfig;
```



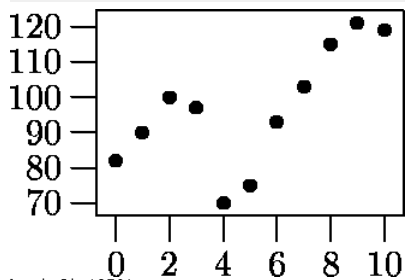
```
beginfig(277)
draw begingraph(3cm,2cm)
```

```
gdraw "data1" plot btex $\bullet$ etex;
endgraph;
```

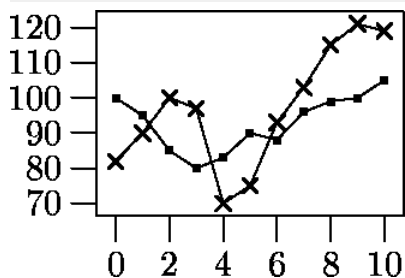
```
endfig;
```



```
beginfig(278)
picture gros_point;
draw (0,0) withpen pencircle scaled 4bp;
gros_point := currentpicture;
currentpicture := nullpicture;
draw beginingraph(3cm,2cm)
gdraw "data1" plot gros_point;
endgraph;
endfig;
```

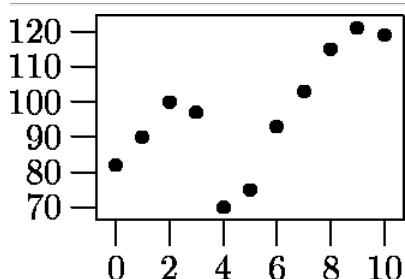


```
beginfig(279)
picture gros_point;
gros_point := nullpicture;
addto gros_point doublepath (0,0)
withpen pencircle scaled 4bp;
draw beginingraph(3cm,2cm)
gdraw "data1" plot gros_point;
endgraph;
endfig;
```



```
beginfig(280)
picture croix;
croix := nullpicture;
addto croix doublepath (-2bp,2bp)--(2bp,-2bp)
withpen pencircle scaled 1bp;
addto croix doublepath (-2bp,-2bp)--(2bp,2bp)
withpen pencircle scaled 1bp;
picture gros_carre;
gros_carre := nullpicture;
addto gros_carre contour unitsquare shifted (-.5,-.5) scaled 2bp;

draw beginingraph(3cm,2cm)
gdraw "data1";
gdraw "data1" plot croix;
gdraw "data2";
gdraw "data2" plot gros_carre;
endgraph;
endfig;
```

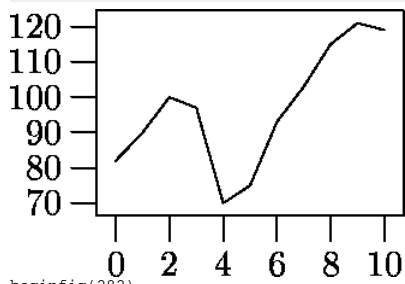


```
beginfig(281)
draw beginingraph(3cm,2cm)
gdata("data1",
v,
```

```

        glabel(gros_point, v1, v2);
    };
endgraph;
endfig;

```

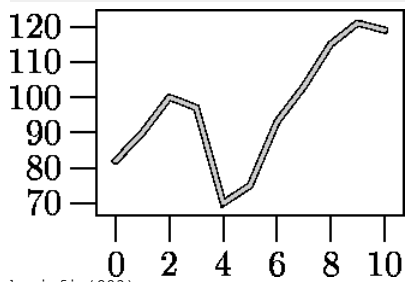


```

beginfig(282)
draw begingraph(3cm,2cm)
path p;
gdata("data1",
v,
augment.p(v1,v2);
);
gdraw p;
endgraph;

```

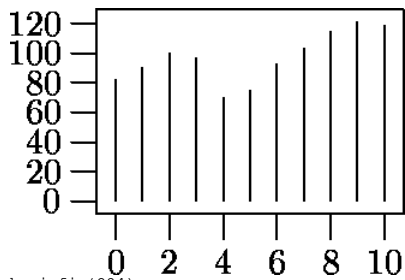
```
endfig;
```



```

beginfig(283)
interim linecap := squared;
interim linejoin := mitered;
draw begingraph(3cm,2cm)
path p;
gdata("data1",
v,
augment.p(v1,v2);
);
gdraw p withpen pencircle scaled 2bp;
gdraw p withpen pencircle scaled 1bp withcolor .8white;
endgraph;
endfig;

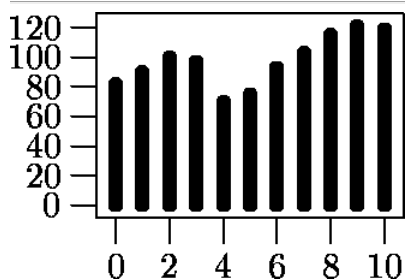
```



```

beginfig(284)
draw begingraph(3cm,2cm)
gdata("data1",
v,
path p;
augment p (v1,0);
augment p (v1,v2);
gdraw p;
);
endgraph;
endfig;

```



```

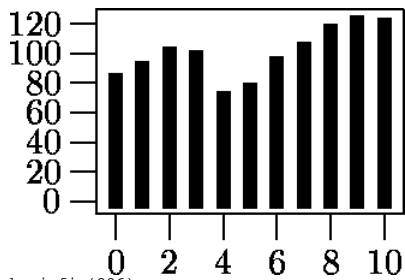
beginfig(285)
draw begingraph(3cm,2cm)
gdata("data1",
v,

```

```

path p;
augment p (v1,0);
augment p (v1,v2);
gdraw p withpen pencircle scaled 4bp;
);
endgraph;
endfig;

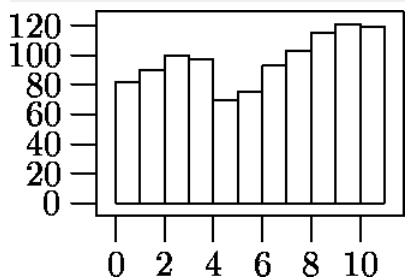
```



```

beginfig(286)
interim linecap:=2;
draw beginingraph(3cm,2cm)
gdata("data1",
v,
path p;
augment p (v1,0);
augment p (v1,v2);
gdraw p withpen pencircle scaled 4bp;
);
endgraph;
endfig;

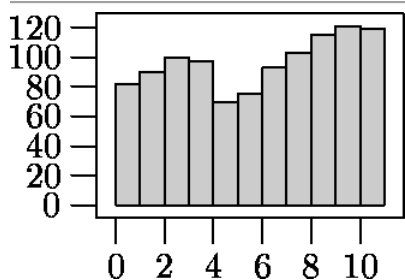
```



```

beginfig(287)
draw beginingraph(3cm,2cm)
gdata("data1", v,
path p;
augment p (v1,0);
augment p (v1,v2);
augment p (v1 Sadd "1",v2);
augment p (v1 Sadd "1",0);
gdraw p--cycle;
);
endgraph;
endfig;

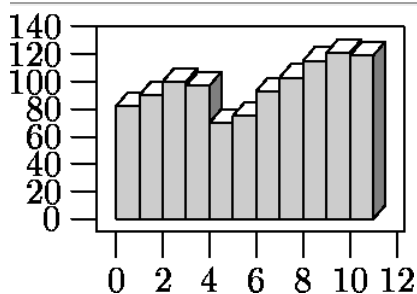
```



```

beginfig(288)
draw beginingraph(3cm,2cm)
gdata("data1", v,
path p;
augment p (v1,0);
augment p (v1,v2);
augment p (v1 Sadd "1",v2);
augment p (v1 Sadd "1",0);
gfill p--cycle withcolor .8white;
gdraw p--cycle;
);
endgraph;
endfig;

```



```

beginfig(289)
draw begingraph(3cm,2cm)
  gdata("data1", v,

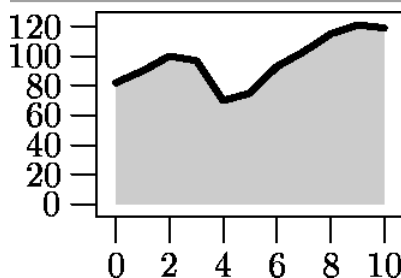
    % Le dessus
    path p;
    augment p (v1,v2);
    augment p (v1 Sadd "1",v2);
    augment p (v1 Sadd "1.5", v2 Sadd "10");
    augment p (v1 Sadd ".5", v2 Sadd "10");
    gfill p--cycle withcolor white;
    gdraw p--cycle;

    % Le c^^f4t^^e9
    path p;
    augment p (v1 Sadd "1",0);
    augment p (v1 Sadd "1",v2);
    augment p (v1 Sadd "1.5", v2 Sadd "10");
    augment p (v1 Sadd "1.5", "10");
    gfill p--cycle withcolor .5white;
    gdraw p--cycle;

    % Le devant
    path p;
    augment p (v1,0);
    augment p (v1,v2);
    augment p (v1 Sadd "1",v2);
    augment p (v1 Sadd "1",0);
    gfill p--cycle withcolor .8white;
    gdraw p--cycle;

  );
endgraph;
endfig;

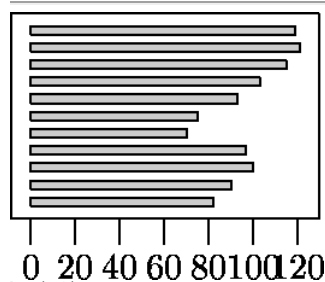
```



```

beginfig(290)
draw begingraph(3cm,2cm)
  path p,q;
  gdata("data1", v,
    augment.p(v1,v2);
  );
  q:= (xpart point 0 of p, 0) -- p --
      (xpart point length(p) of p, 0) -- cycle;
  gfill q withcolor .8white;
  gdraw p withpen pencircle scaled 2bp;
endgraph;
endfig;

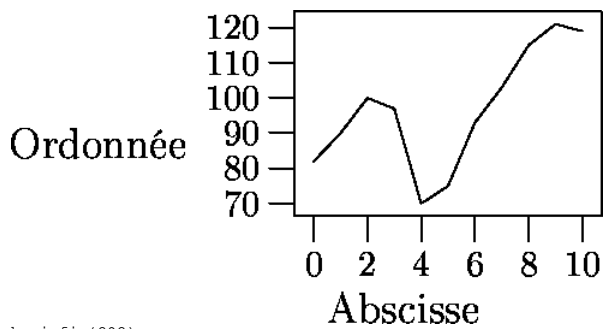
```



```

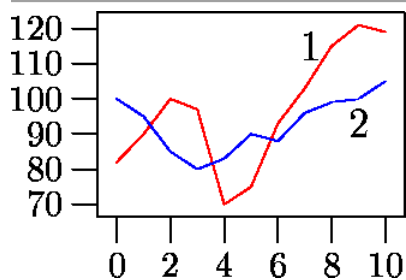
beginfig(291)
draw begingraph(3cm,2cm)
  gdata("data1",
    v,
    path p;
    augment p ("0", i);
    augment p (v2, i);
    augment p (v2, i Sadd ".5");
    augment p (0, i Sadd ".5");
    gfill p--cycle withcolor .8white;
    gdraw p--cycle;
  );
  autogrid(otick.bot,);
endgraph;
endfig;

```



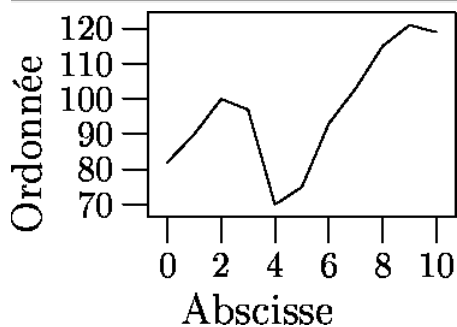
```
beginfig(292)
draw begingraph(3cm,2cm)
gdraw "data1";
glabel.bot(btex Abscisse etex, OUT);
glabel.lft(btex Ordonnee etex, OUT);
endgraph;
```

endfig;



```
beginfig(293)
draw begingraph(3cm,2cm)
gdraw "data1" withcolor red;
glabel.lft(btex 1 etex, 8);
gdraw "data2" withcolor blue;
glabel.bot(btex 2 etex, 9);
endgraph;
```

endfig;

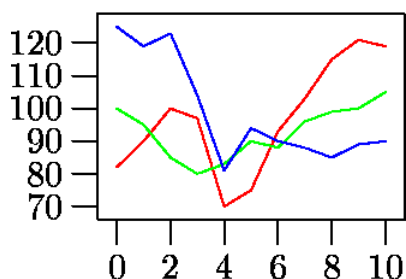


```
beginfig(294)
draw begingraph(3cm,2cm)
gdraw "data1";
glabel.bot(btex Abscisse etex, OUT);
glabel.lft(btex Ordonnee etex rotated 90, OUT);
endgraph;
endfig;
```

— Courbe 1

— Courbe 2

— Courbe 3



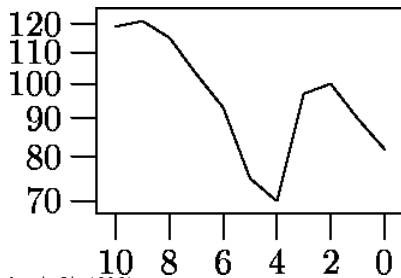
```
beginfig(295)
% La legende
color couleur[];
couleur[0] := red;
couleur[1] := green;
couleur[2] := blue;
picture p[], legende;
legende := nullpicture;
```



```

for i=0 upto 2:
  p[i] := nullpicture;
  addto p[i] also TEX("Courbe " & decimal(i+1))
  withcolor couleur[i];
  addto legende doublepath ( (0,0)--(5mm,0) )
    shifted (0, -5mm*i)
  withpen currentpen withcolor couleur[i];
  addto legende also p[i]
    shifted 1/2(lrcorner p[i] - ulcorner p[i])
    shifted (0, -5mm*i);
endfor;
% Les courbes
draw beginingraph(3cm,2cm)
  for i=1 upto 3:
    gdraw "data" & decimal(i) withcolor couleur[i-1];
  endfor;
glabel.top(legende,OUT);
endgraph;
endfig;

```

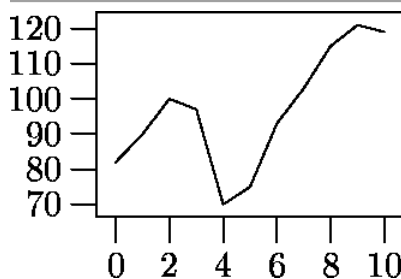


```

beginfig(296)
  draw beginingraph(3cm,2cm)
    setcoords(-linear,log);
  gdraw "data1";
endgraph;

```

endfig;

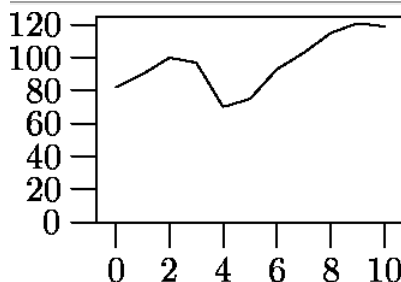


```

beginfig(297)
  draw beginingraph(3cm,2cm)
    gdraw "data1";
endgraph;

```

endfig;

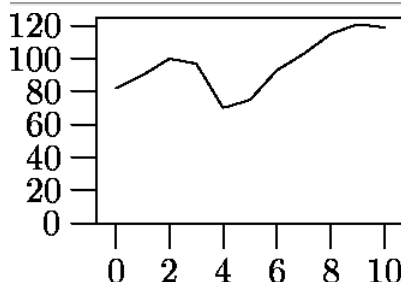


```

beginfig(298)
  draw beginingraph(3cm,2cm)
    setrange( (whatever,0), (whatever,whatever) );
  gdraw "data1";
endgraph;

```

endfig;

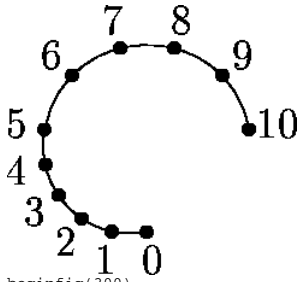


```

beginfig(299)
  draw beginingraph(3cm,2cm)
    setrange(whatever, 0, whatever, whatever);
  gdraw "data1";
endgraph;

```

```
endfig;
```



```
beginfig(300)
  vardef TEX primary s =
    write "verbatimtex" to "mptextmp.mp";
    write "\documentclass[12pt]{article}" to "mptextmp.mp";
    write "\usepackage[T1]{fontenc}" to "mptextmp.mp";
    write "\usepackage{amsmath,amssymb}" to "mptextmp.mp";
    write "\begin{document}" to "mptextmp.mp";
    write "etex" to "mptextmp.mp";
    write "btex "&s&" etex" to "mptextmp.mp";
    write EOF to "mptextmp.mp";
    scantokens "input mptextmp"
  enddef;
  vardef mylabel(expr pic, p, t) =
    save A; pair A;
    A = point t of p +
      8bp * unitvector(direction t of p) rotated 90;
    label(pic, A);
  enddef;
  path p; u:=1cm;
  p = (0,0)..(-u,u)..(u,u);
  draw p;
  for i=0 step .2 until length(p):
    draw point i of p withpen pencircle scaled 4bp;
    mylabel(TEX("$&decimal(round(5*i))&$"),p,i);
  endfor;
endfig;
```



```
beginfig(301)
  path p;
  p := subpath(1,3) of fullcircle scaled 2cm;
  interim linejoin := mitered;
  interim linecap := butt;

  interim ahangle := 30;
  drawarrow p withpen pencircle scaled 2bp;

  interim ahangle := 45;
  drawarrow p shifted (0,-5mm) withpen pencircle scaled 2bp;

  interim ahangle := 60;
  drawarrow p shifted (0,-10mm) withpen pencircle scaled 2bp;
endfig;
```



```
beginfig(302)
  path p;
  p := subpath(1,3) of fullcircle scaled 2cm;
  interim linejoin := mitered;
  interim linecap := butt;
  interim ahangle := 30;

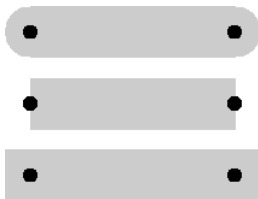
  interim ahlenght := 2bp;
  drawarrow p withpen pencircle scaled 2bp;

  interim ahlenght := 4bp;
  drawarrow p shifted (0,-5mm) withpen pencircle scaled 2bp;

  interim ahlenght := 6bp;
  drawarrow p shifted (0,-10mm) withpen pencircle scaled 2bp;
endfig;
```

Nous sommes le 31/1/2000.

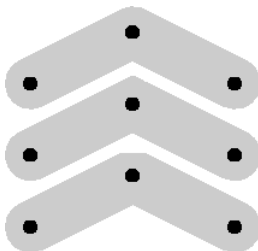
```
beginfig(303)
  draw TEX( "Nous sommes le "&
    decimal(day) &"/"&
    decimal(month) &"/"&
    decimal(year) &". " );
endfig;
```



```

beginfig(304)
  path p;
  p := (0,0) -- (2cm,0);
  def doit (suffix p)(expr t) =
    begingroup
      interim linecap := t;
      draw p withpen pencircle scaled 5mm withcolor .8white;
    endgroup;
    draw point 0 of p withpen pencircle scaled 4bp;
    draw point 1 of p withpen pencircle scaled 4bp;
    p := p shifted (0,-7mm)
  enddef;
  doit(p,rounded);
  doit(p,butt);
  doit(p,squared);
endfig;

```



```

beginfig(305)
  path p;
  p := (0,0) -- (1cm,5mm) -- (2cm,0);
  def doit (suffix p)(expr t) =
    begingroup
      interim linejoin := t;
      draw p withpen pencircle scaled 5mm withcolor .8white;
    endgroup;
    draw point 0 of p withpen pencircle scaled 4bp;
    draw point 1 of p withpen pencircle scaled 4bp;
    draw point 2 of p withpen pencircle scaled 4bp;
    p := p shifted (0,-7mm)
  enddef;
  doit(p,rounded);
  doit(p,mitered);
  doit(p,beveled);
endfig;

```

```
bye;
```