# Correlation Among Durham City's Water Supply, Wastewater Discharge, and Population from 2012 to 2021

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### R. Markdown

This is an R Markdown document. Markdown is a simple formatting syntax for authoring HTML, PDF, and MS Word documents. For more details on using R Markdown see http://rmarkdown.rstudio.com.

When you click the  $\mathbf{Knit}$  button a document will be generated that includes both content as well as the output of any embedded R code chunks within the document. You can embed an R code chunk like this:

```
getwd()
```

```
## [1] "/home/guest/ENV872/ENV872 Group"
library(tidyverse)
```

```
## -- Attaching packages ---
                                            ----- tidyverse 1.3.2 --
## v ggplot2 3.3.6
                    v purrr
                             0.3.4
                             1.0.10
## v tibble 3.1.8
                     v dplyr
## v tidvr
          1.2.0
                    v stringr 1.4.1
## v readr
           2.1.2
                     v forcats 0.5.2
## -- Conflicts -----
                                        ## x dplyr::filter() masks stats::filter()
## x dplyr::lag()
                  masks stats::lag()
library(dplyr)
library(cowplot)
library(lubridate)
```

```
##
##
  Attaching package: 'lubridate'
##
## The following object is masked from 'package:cowplot':
##
##
       stamp
##
## The following objects are masked from 'package:base':
##
##
       date, intersect, setdiff, union
mytheme <- theme_classic(base_size = 10) + theme(axis.text = element_text(color = "black"),
    legend.position = "bottom")
theme_set(mytheme)
```

## 1. Introduction

Water shortages around US due to climate change is becoming worse and reported by several

studies. Also we are in the situation that two of the largest reservoirs in America, which provide water and electricity tomillions, are in danger of reaching 'dead pool status. With the rapid urbanization in cities around the world and in US, the amount of population is rapidly increasing and the imperviousness of urban surface is increasing as well, which could raise the need for water withdrawal from the lake bodies or reservoirs and the amount of wastewater discharge from daily life.

At the same time, the intemperate discharge of wastewater in US is becoming a critical issue so in this way, we would like to investigate two main questions in our report: 1) Is there any clear correlation between the monthly average water withdrawal and the monthly average wastewater discharge? 2) Is population a key influencing factor to water withdrawal and wastewater discharge over the years?

#### 2. Data

#### 2.1 Read Datasets

To solve these problems, we gathered three main datasets from the website of NC DEQ Division of Water Resources-Local Water Supply Planning (https://www.ncwater.org/WUDC/app/LWS P/search.php) for monthly water withdrawal data and monthly wastewater discharge data; from the website of Data Commons (https://datacommons.org/place/geoId/3719000?category=Demog raphics#Population) for population data in Durham county from 2012-2021.

## 2.2 Data Wrangling

In the data wrangling part, we first filtered population data we need for ten years and adjusted the formats of every column of data into the one more convenient for later steps. Then we joined the table for withdrawal data, discharge data and population data by year and added the column of month to distinguish. Also, we created one dataset which summmarized the mean discharge amount and the mean withdrawal amount in each month among years.

```
pop_water_final$Population <- as.numeric(pop_water_final$Population)

pop_water_summaries <- pop_water_final %>%
    group_by(Year, Population) %>%
    summarise(mean.discharge = mean(Monthly.Discharge.Wastewater),
        sd.discharge = sd(Monthly.Discharge.Wastewater),
        mean.withdraw = mean(Monthly.Water.Withdraw),
        sd.withdraw = sd(Monthly.Water.Withdraw))
```

```
## `summarise()` has grouped output by 'Year'. You can override using the
## `.groups` argument.
```

In the data wrangling part, first we read the population data; the monthly water withdrawal data and the monthly wastewater discharge data into our file.

```
write.csv(pop_water_final, row.names = FALSE,
    file = "./data/Durham_water&population_2012-2021.csv")
write.csv(pop_water_summaries, row.names = FALSE,
    file = "./data/Durham_county_water_withdraw&diacharge_summary.csv")
```

#### 3. Data Visualization

## `geom\_smooth()` using formula 'y ~ x'
## `geom\_smooth()` using formula 'y ~ x'

### 3.1 Line Plot

We created some data visualizations to make the data that we collected easy to understand. Frist, we made line plots for the average annual wastewater discharge, water withdrawal, and population for Durham from 2012 to 2021 using ggplot. A line plot is used for continuous variables over time. Over the course of 10 years, we can see in Figure 1 below that all three variables have an overall increasing trend.

```
discharge_linechart <- ggplot(pop_water_summaries,</pre>
    aes(x = Year, y = mean.discharge)) + geom_line() +
    labs(title = "Mean Wastewater Discharge From 2012-2021",
        y = "Mean Discharge (MGD)", x = "Year") +
    labs(title = "Figure 1. Mean Wastewater Discharge",
        subtitle = "From 2012-2021", y = "Mean Discharge (MGD)",
        x = "Year") + geom smooth(method = lm)
withdraw_linechart <- ggplot(pop_water_summaries,</pre>
    aes(x = Year, y = mean.withdraw)) + geom_line() +
    labs(title = "Mean Water Withdraw From 2012-2021",
        y = "Mean Withdraw (MGD)", x = "Year") +
    geom_smooth(method = lm, color = "red")
pop_linechart <- ggplot(pop_water_summaries, aes(x = Year,</pre>
    y = Population)) + geom_line() + labs(title = "Population",
    subtitle = "From 2012-2021", y = "People",
    x = "Year") + geom_smooth(method = lm, color = "green")
plot_grid(discharge_linechart, withdraw_linechart,
    pop_linechart, ncol = 1, align = "v", axis = "l")
## `geom_smooth()` using formula 'y ~ x'
```

Figure 1. Mean Wastewater Discharge From 2012-2021 Mean Discharge (MGD) Year Mean Water Withdraw From 2012-2021 Mean Withdraw (MGD) Year Population From 2012-2021 

# $3.2~\mathrm{Box}~\mathrm{Plot}$

To examine the seasonal change of wastewater discharge and water withdrawal and the relationship between them, we made box plots (Figure 2) to see if there's any significant difference between each month in the last ten years for Durham. The monthly wastewater discharges from July to November are significantly different from the wastewater discharges from January to April. Therefore, during most of the summer and fall time, wastewater discharges are significantly lesser wastewater discharge than in most of the spring and winter time. Moreover, water withdrawals from January to March and November are significantly lower than from April to October. The water withdrawal in December is significantly lower than in all the other months, except in January. We conclude that summer's and most of the fall's water withdrawals are the highest. Also, winter has the lowest water withdrawal.

Year

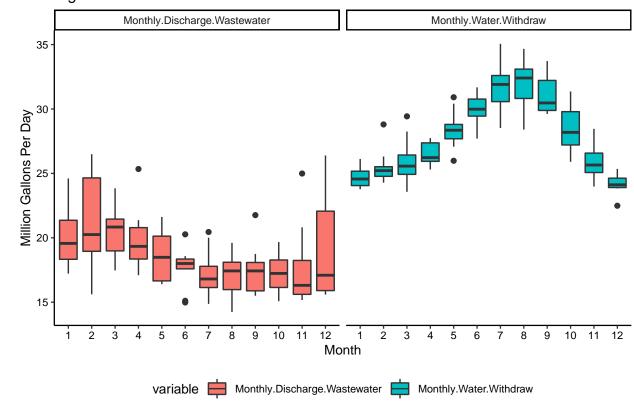
We were expecting water withdrawal and wastewater discharge to be proportional before we were making the data analysis. Using common sense that high water withdrawal means high water

demand, which results in high was tewater discharge. However, the box plots show differently. The water with drawals and wastewater discharges in Durham from 2012 to 2021 have an inverse relationship. The water with drawals during summer and fall are the highest, but the wastewater discharges are the lowest.

```
library(MASS)
##
## Attaching package: 'MASS'
## The following object is masked from 'package:dplyr':
##
##
       select
library(reshape2)
##
## Attaching package: 'reshape2'
## The following object is masked from 'package:tidyr':
##
##
       smiths
library(reshape)
##
## Attaching package: 'reshape'
  The following objects are masked from 'package:reshape2':
##
##
       colsplit, melt, recast
   The following object is masked from 'package:lubridate':
##
##
##
       stamp
## The following object is masked from 'package:cowplot':
##
##
       stamp
  The following object is masked from 'package:dplyr':
##
##
##
       rename
## The following objects are masked from 'package:tidyr':
##
       expand, smiths
##
discharge_withdraw_grouped <- melt(water_final,</pre>
    id = c("Year", "Month"))
Wastewater_box <- ggplot(discharge_withdraw_grouped,</pre>
    aes(x = Month, y = value, group = Month, fill = variable))
Wastewater_box <- ggplot(discharge_withdraw_grouped,</pre>
    aes(x = as.factor(Month), y = value, group = as.factor(Month),
        fill = variable)) + geom_boxplot() + facet_wrap(~variable) +
    labs(title = "Figure 2.", x = "Month", y = "Million Gallons Per Day") +
    mytheme
```

print(Wastewater\_box)

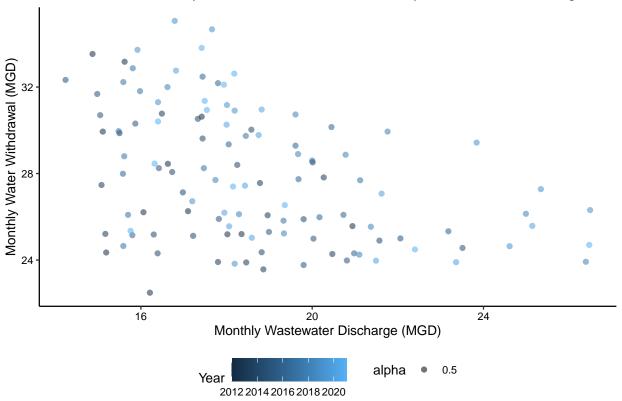
Figure 2.



> 3.3 Data Analysis > 3.3.1 Methodology To explore the relationship between population, monthly water withdrawal, and monthly wastewater discharge. We first did a scatterplot between each of the variables to observe a trend. Then, we created linear models to examine results and visualize results. > 3.3.2 Water Dicharge and Water withdrawal The Scatter plot of monthly water discharge and withdrawal exhibited a negative trend between the two despite some cluttering. Monthly wastewater discharge increased as monthly water withdrawal decreased.

```
# draw scatterplot to see if a trend exsist
discharge_withdraw <- ggplot(pop_water_final,
    aes(x = Monthly.Discharge.Wastewater, y = Monthly.Water.Withdraw)) +
    geom_point(aes(color = Year, alpha = 0.5)) +
    labs(title = "Scatter Plot of Monthly Water Withdrawal and Monthly Wastewater Discharge",
        x = "Monthly Wastewater Discharge (MGD)",
        y = "Monthly Water Withdrawal (MGD)") +
        mytheme
print(discharge_withdraw)</pre>
```

# Scatter Plot of Monthly Water Withdrawal and Monthly Wastewater Discharge



> We used linear regression to determine if there is a significant relationship. P-value is close to zero which indicates that there is a high significance between monthly wastewater discharge and water withdrawal. The distribution of the residuals is not strongly symmetrical, meaning that predicted water discharge points fall far away from the actual observed points. The residual standard error is 2.5, given that the mean monthly water withdrawal is 29.18, and the percentage error is 8.57%. These all point to a high relevance between water discharge and water withdrawal. However, the multiple R-squared shows that only 17.5% percent of the variance can be explained by water discharge.

```
# Format the lm() function
discharge_withdraw <- lm(data = pop_water_final,</pre>
    Monthly.Discharge.Wastewater ~ Monthly.Water.Withdraw)
summary(discharge_withdraw)
##
## Call:
##
   lm(formula = Monthly.Discharge.Wastewater ~ Monthly.Water.Withdraw,
##
       data = pop_water_final)
##
##
  Residuals:
##
       Min
                1Q Median
                                 3Q
                                         Max
   -4.7646 -1.6944 -0.2257
                             1.3752
##
##
##
  Coefficients:
```

Estimate Std. Error t value Pr(>|t|)

2.12915

0.07597

29.18001

13.705 < 2e-16 \*\*\*

-4.987 2.13e-06 \*\*\*

##

##

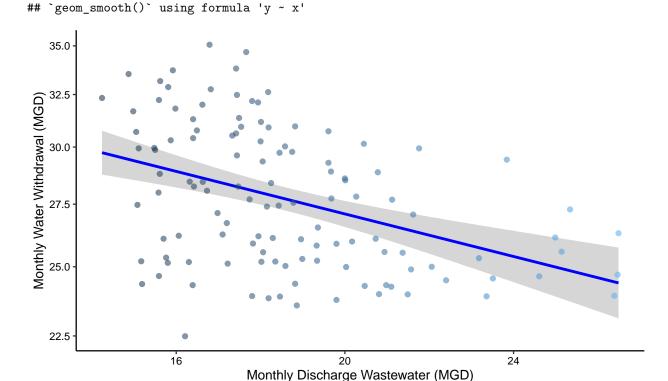
##

(Intercept)

## Monthly.Water.Withdraw -0.37887

```
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 2.505 on 118 degrees of freedom
## Multiple R-squared: 0.1741, Adjusted R-squared: 0.1671
## F-statistic: 24.87 on 1 and 118 DF, p-value: 2.127e-06

# Add a line and standard error for the
# linear regression
discharge_withdraw_regression <- ggplot(pop_water_final,
    aes(x = Monthly.Discharge.Wastewater, y = Monthly.Water.Withdraw)) +
    geom_smooth(method = "lm", color = "blue") +
    scale_y_log10() + geom_point(aes(color = Monthly.Discharge.Wastewater,
    alpha = 0.5)) + labs(x = "Monthly Discharge Wastewater (MGD)",
    y = "Monthly Water Withdrawal (MGD)") + mytheme</pre>
```



> 3.3.3 Population and Water withdrawal > Due to the time-scale difference in population and water withdrawal data, this analysis uses two scatter plots: annual mean water withdrawal and population, and monthly water withdrawal and population. They both show a positive trend. Monthly water withdrawal has increase as the population expanded during the last ten years.

15

18

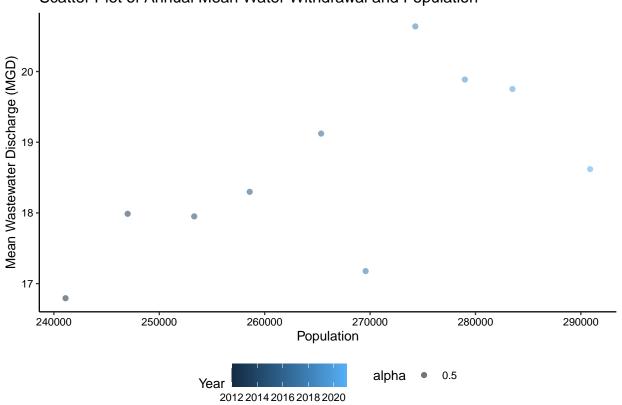
Monthly.Discharge.Wastewater

alpha

0.5

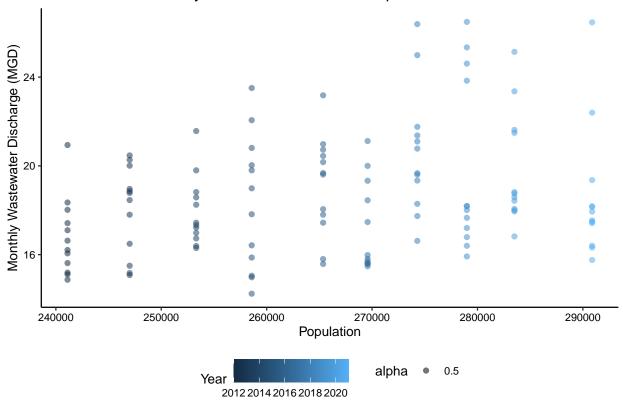
```
# scatterplot of annual population and
# annual mean discharge
population_discharge <- ggplot(pop_water_summaries,
    aes(x = Population, y = mean.discharge)) +</pre>
```

# Scatter Plot of Annual Mean Water Withdrawal and Population



```
# scatterplot of annual population and
# monthly mean discharge
population_discharge_scatter <- ggplot(pop_water_final,
    aes(x = Population, y = Monthly.Discharge.Wastewater)) +
    geom_point(aes(color = Year, alpha = 0.5)) +
    labs(title = "Scatter Plot of Monthly Water Withdrawal and Population",
        x = "Population", y = "Monthly Wastewater Discharge (MGD)") +
    mytheme</pre>
print(population_discharge_scatter)
```

## Scatter Plot of Monthly Water Withdrawal and Population



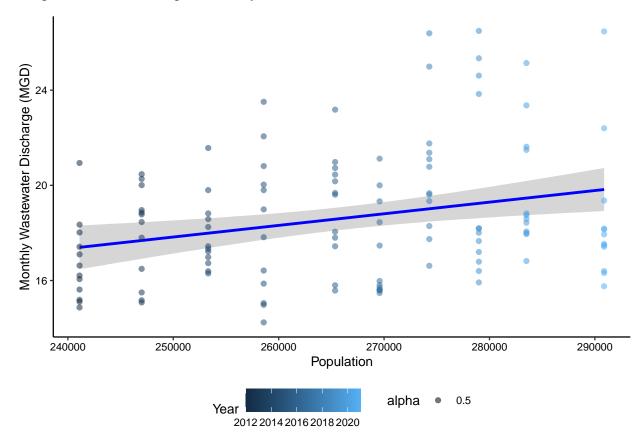
> P-value is close to zero which means there is a significant relationship between monthly water discharge and population. The distribution of the residuals is fairly symmetrical, meaning that predicted water discharge points fall near the actual observed points. The residual standard error is 14930, given that the mean monthly water discharge is 231371, and the percentage error is 6.45%. Thus, we can conclude that Durham's population growth is a significant influencing factor on monthly water discharge over the last ten years.

```
# Format the lm() function
population_discharge <- lm(data = pop_water_final,</pre>
    Population ~ Monthly.Discharge.Wastewater)
summary(population_discharge)
##
## Call:
## lm(formula = Population ~ Monthly.Discharge.Wastewater, data = pop_water_final)
##
## Residuals:
##
        Min
                  1Q
                        Median
                                     3Q
                                              Max
   -28748.4 -12494.5
                         449.3
                                11463.6
                                         29057.2
##
##
## Coefficients:
##
                                 Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                                 237371.9
                                               9387.1
                                                        25.29
                                                               < 2e-16 ***
## Monthly.Discharge.Wastewater
                                   1551.3
                                                498.7
                                                         3.11 0.00234 **
##
                   0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Signif. codes:
##
```

```
## Residual standard error: 14930 on 118 degrees of freedom
## Multiple R-squared: 0.07578, Adjusted R-squared: 0.06794
## F-statistic: 9.675 on 1 and 118 DF, p-value: 0.002343

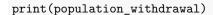
# Add a line and standard error for the
# linear regression
population_discharge_regression <- ggplot(pop_water_final,
    aes(x = Population, y = Monthly.Discharge.Wastewater)) +
    geom_smooth(method = "lm", color = "blue") +
    geom_point(aes(color = Year, alpha = 0.5)) +
    labs(x = "Population", y = "Monthly Wastewater Discharge (MGD)") +
    mytheme
print(population_discharge_regression)</pre>
```

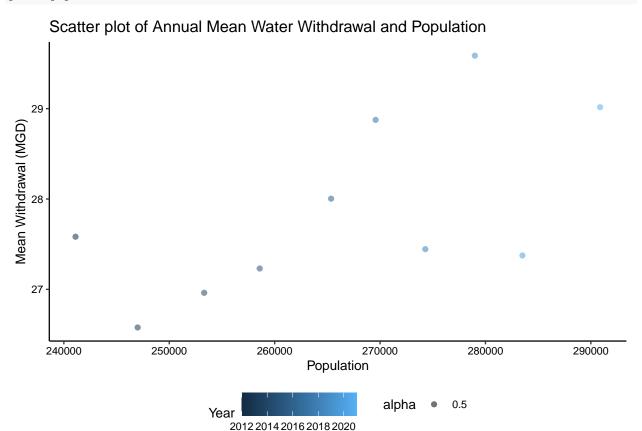
## `geom\_smooth()` using formula 'y ~ x'



> 3.3.4 Population and Wastewater withdrawal > > Similar to population~withdrawal, this analysis uses two scatter plots: annual mean water withdrawal and population, and monthly water withdrawal and population. Both monthly water withdrawals increased as the population grew.

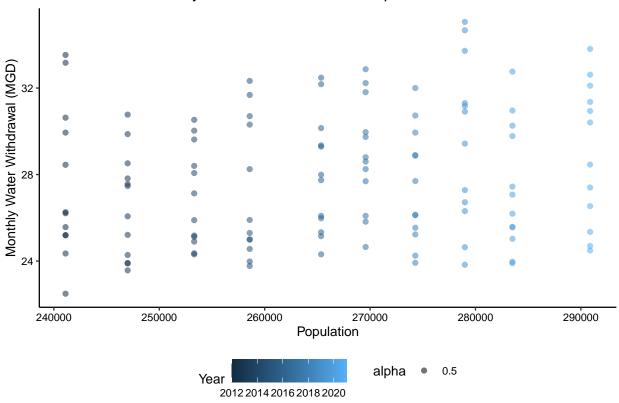
```
# scatterplot of annual population and
# annual mean withdraw
population_withdrawal <- ggplot(pop_water_summaries,
    aes(x = Population, y = mean.withdraw)) +
    geom_point(aes(color = Year, alpha = 0.5)) +
    labs(title = "Scatter plot of Annual Mean Water Withdrawal and Population",
        x = "Population", y = "Mean Withdrawal (MGD)") +
    mytheme</pre>
```





```
population_withdraw_scatter <- ggplot(pop_water_final,
    aes(x = Population, y = Monthly.Water.Withdraw)) +
    geom_point(aes(color = Year, alpha = 0.5)) +
    labs(title = "Scatter Plot of Monthly Water Withdrawal and Population",
        x = "Population", y = "Monthly Water Withdrawal (MGD)") +
    mytheme
print(population_withdraw_scatter)</pre>
```

## Scatter Plot of Monthly Water Withdrawal and Population



> P-value(0.0334) is smaller than 0.05, showing a significant relationship between population growth and monthly water withdrawal The distribution of the residuals is fairly symmetrical, but it has a larger difference on the end, which means that predicted water withdrawal points fall far from the actual observed points on the extremes. The residual standard error is 15230, given that the mean monthly water discharge is 238544, and the percentage error is 6.38%. All combined, over the past decade, the population is also a key influence factor on monthly water withdrawal.

```
population_withdraw <- lm(data = pop_water_final,</pre>
    Population ~ Monthly.Water.Withdraw)
summary(population_withdraw)
##
## Call:
## lm(formula = Population ~ Monthly.Water.Withdraw, data = pop_water_final)
##
## Residuals:
##
      Min
              1Q Median
                             3Q
                                    Max
   -30788 -12143
                    1102
                          11709
##
                                 27974
##
##
  Coefficients:
##
                           Estimate Std. Error t value Pr(>|t|)
##
  (Intercept)
                           238544.4
                                        12950.7
                                                 18.419
                                                           <2e-16 ***
## Monthly.Water.Withdraw
                              994.6
                                          462.1
                                                   2.153
                                                           0.0334 *
##
## Signif. codes:
                   0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

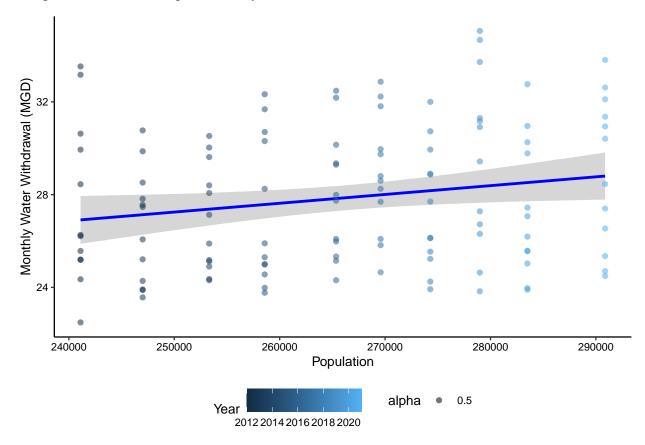
# Format the lm() function

##

```
## Residual standard error: 15230 on 118 degrees of freedom
## Multiple R-squared: 0.03778, Adjusted R-squared: 0.02963
## F-statistic: 4.634 on 1 and 118 DF, p-value: 0.03339

# Add a line and standard error for the
# linear regression
population_withdraw_regression <- ggplot(pop_water_final,
    aes(x = Population, y = Monthly.Water.Withdraw)) +
    geom_smooth(method = "lm", color = "blue") +
    geom_point(aes(color = Year, alpha = 0.5)) +
    labs(x = "Population", y = "Monthly Water Withdrawal (MGD)") +
    mytheme
print(population_withdraw_regression)</pre>
```

## `geom\_smooth()` using formula 'y ~ x'



> 4. Conclusion > > Both water withdrawal and wastewater discharge increased during the last 10 years show different patterns within the year. Water withdrawals during summer and fall are the highest, while wastewater discharges are the lowest. By using linear regression, we can conclude that water withdrawal and population show correlation between each two variables, of which wastewater discharge and water withdrawal have the highest significance difference, and population and monthly water discharge have highest coefficiency.