

Simulating random processes in R

Example of RNG

```
n<-10000
x<-integer(n)
x[1] <- 1093
for(i in 2:n){
  x[i]<- ((2^18+1)*x[i-1]) %% 2^35
}
head(x)
```

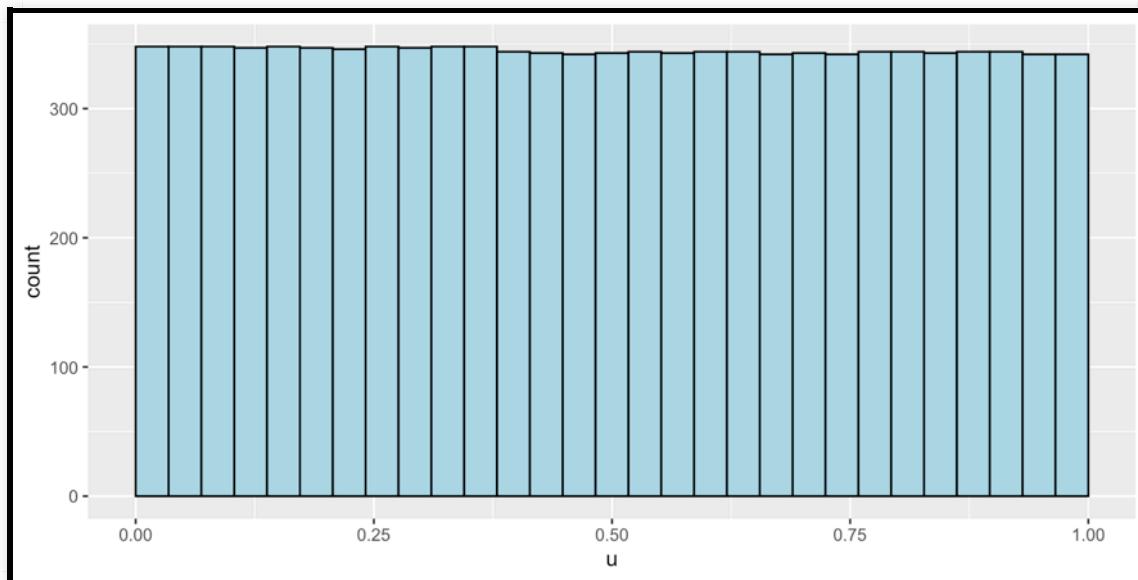
```
[1] 1093 286524485 573047877 859571269 1146094661 1432618053
```

```
head(x/(2^35))
```

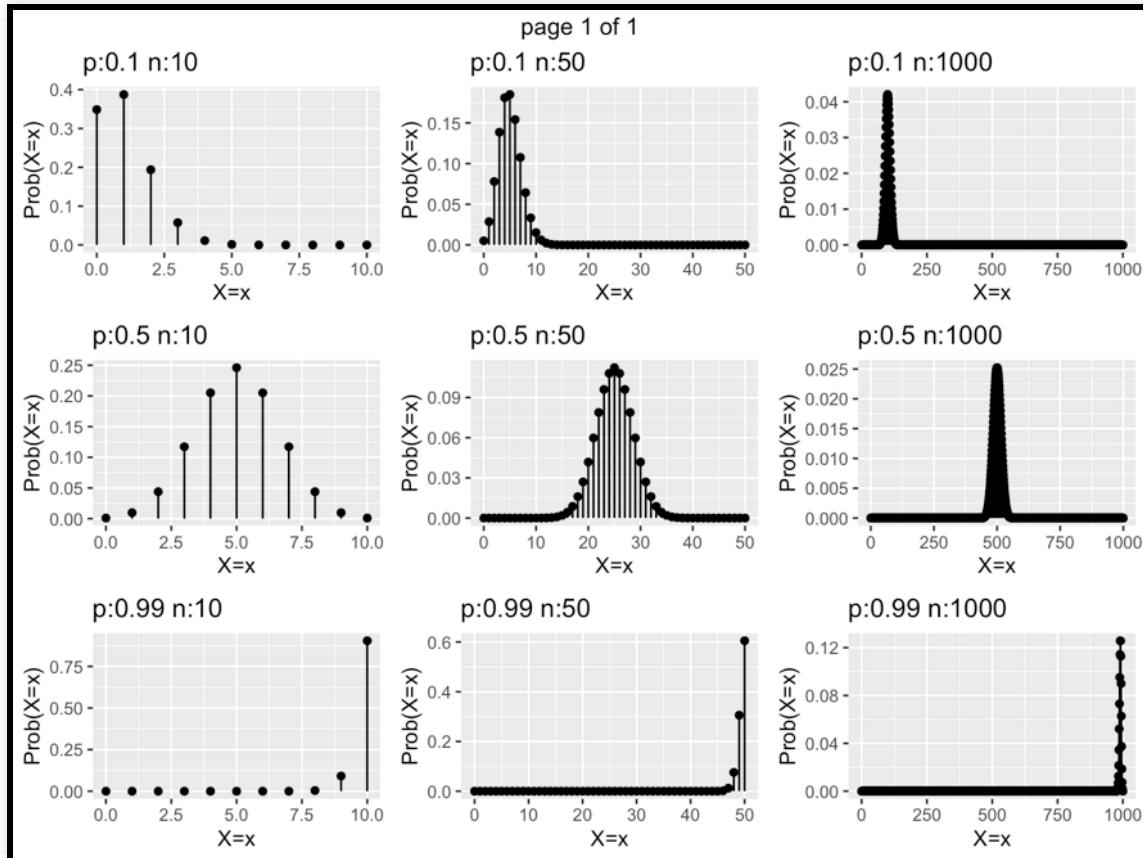
```
[1] 3.1810e-08 8.3390e-03 1.6678e-02 2.5017e-02 3.3356e-02 4.1695e-02
```

Example of RNG

```
ggplot(data.frame(u=x/2^35), aes(x=u)) +  
  geom_histogram(breaks=seq(0,1,length=30), fill="lightblue", col="black")
```

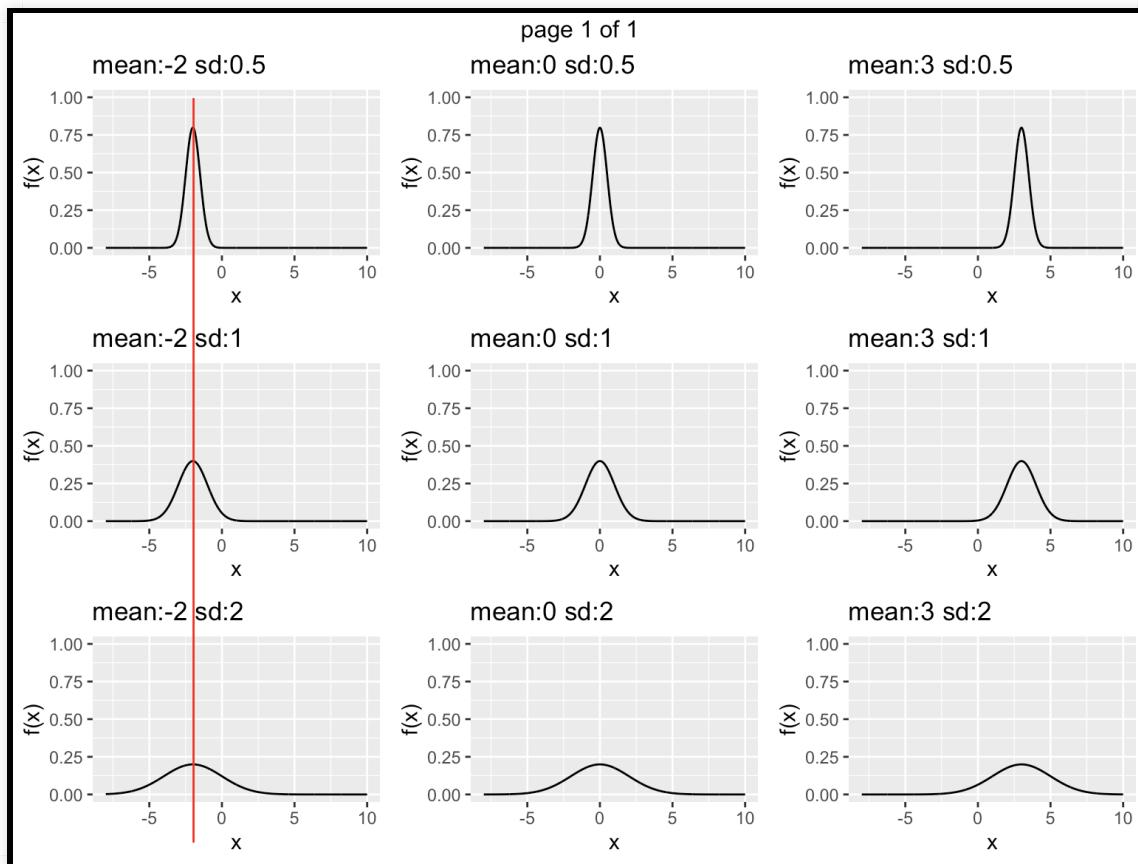


Binomial distribution with different p and n parameters.



change of the center will change the spread

Normal distribution with different μ and σ



could change center and spread separately.

Generating random variables from a dis. name (# samples, para) distribution

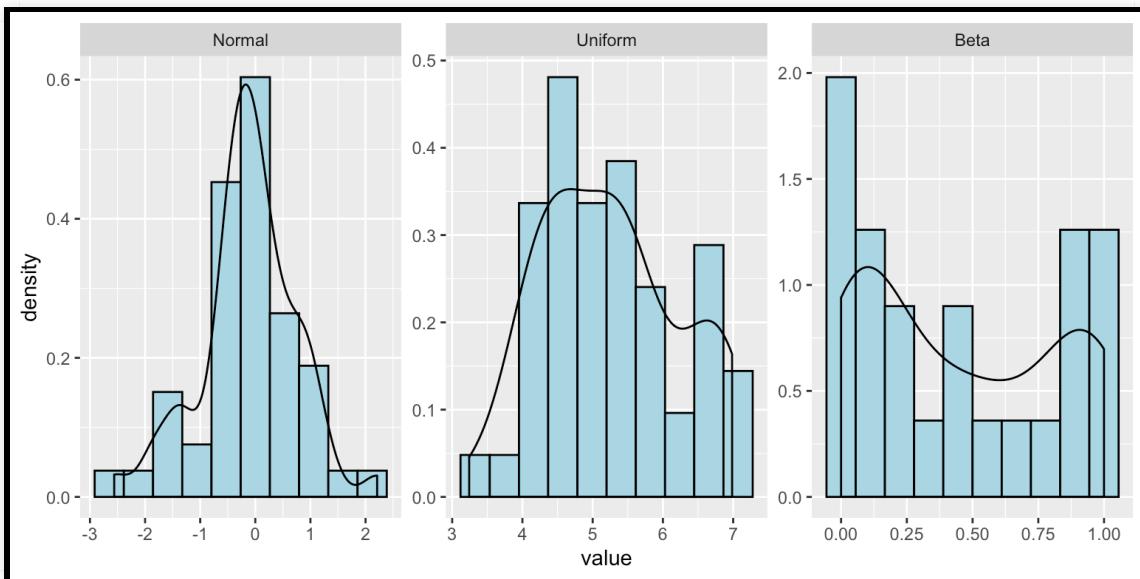
```
n<-50  
my_sims<-tibble(Normal=rnorm(n,mean=0,sd=1),  
                  Uniform=runif(n,min=3,max=7),  
                  Beta = rbeta(n,0.5,0.5))  
  
my_sims_long <- my_sims %>% pivot_longer(cols=(Normal:Beta)) %>%  
  mutate(name=fct_relevel(name,c("Normal","Uniform","Beta")))  
  by default  
  Otherwise alphabetically ("Beta"...)  
p<-ggplot(my_sims_long, aes(x=value)) +  
  
  geom_histogram(aes(y=..density..),bins=10,fill="lightblue",col=  
  +  
  geom_density() +  
  facet_wrap(~name,scales="free")  
  (?)
```

name	value
Normal	:
Uniform	:
Beta	:

N=50

p

Not enough.



N=10000

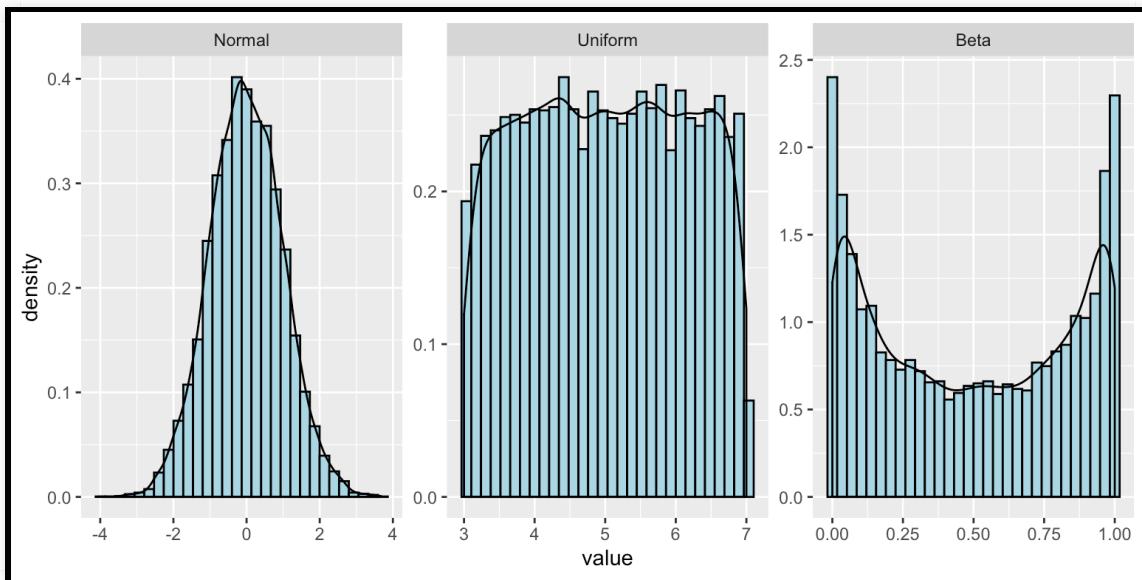
```
n<-10000
my_sims<-tibble(Normal=rnorm(n,mean=0,sd=1),
                  Uniform=runif(n,min=3,max=7),
                  Beta = rbeta(n,0.5,0.5))

my_sims_long <- my_sims %>% pivot_longer(cols=(Normal:Beta)) %>%
  mutate(name=fct_relevel(name,c("Normal","Uniform","Beta")))

p<-ggplot(my_sims_long, aes(x=value)) +
  geom_histogram(aes(y=..density..),bins=30,fill="lightblue",col='black' +
  geom_density()+
  facet_wrap(~name,scales="free")
```

N=10000

p



Setting the seed for the RNG

```
set.seed(8022012)  
rnorm(5)
```

```
[1] 0.18058 -0.40994 0.27908 0.85880 -2.35079
```

```
runif(5)
```

```
[1] 0.76560 0.36905 0.79943 0.66251 0.70653
```

```
set.seed(8022012)  
rnorm(6)
```

```
[1] 0.18058 -0.40994 0.27908 0.85880 -2.35079 0.72442
```

```
runif(5)
```

```
[1] 0.79943 0.66251 0.70653 0.37248 0.26014
```

Back to VaR

First step

```
set.seed(19200)
## Set the number of stocks
J <- 10

## Set the weights of the stocks
weights<-rep(50,J)

## If  $X_{j,t+1}$  are normal
sigma <- 0.2
X_t_plus_1 <- rnorm(J,0,sigma)

## Compute  $L_{t+1}$ 
L_t_plus_1 <- - (weights %*% (exp(X_t_plus_1) - 1))
```

First step

```
as.numeric(L_t_plus_1) # Loss
```

```
[1] -25.458
```

```
as.numeric(L_t_plus_1/sum(weights) * 100) # Percent Loss/Gain
```

```
[1] -5.0916
```

Now to replicates

```
one_VaR_sim <- function(reps=100000,J, weights, sigma,  
                      alphas=c(0.95,0.99,0.999)){  
  
  ## If  $X_j$ ,  $t+1$  are normal  
  X_t_plus_1 <- matrix(rnorm(J*reps,0,sigma),ncol=reps)  
  
  ## Compute  $L_{t+1}$   
  L_t_plus_1 <- -weights %*% (exp(X_t_plus_1) -1)  
                $J \times J$             $J \times Rep$   
  ## Find VaR for different alphas  
  VaR_alpha <- quantile(L_t_plus_1,alphas)  
  
  return(tibble(alpha=alphas,VaR=VaR_alpha))  
}
```

$$X = \begin{bmatrix} \text{---} \\ \text{---} \\ \text{---} \\ \text{---} \end{bmatrix}$$

Now to replicates

```
set.seed(19752626)
## One run
one_VaR_sim(reps=1000,J=J,weights=weights,sigma=sigma)
```

```
# A tibble: 3 x 2
  alpha    VaR
  <dbl> <dbl>
1 0.95   39.9
2 0.99   59.1
3 0.999  74.3
```

diff

```
## A second run
one_VaR_sim(reps=1000,J=J,weights=weights,sigma=sigma)
```

```
# A tibble: 3 x 2
  alpha    VaR
  <dbl> <dbl>
1 0.95   44.7
2 0.99   65.7
3 0.999  89.4
```

Now to replicates

```
set.seed(19752626)
## One run
one_VaR_sim(reps=100000,J=J,weights=weights,sigma=sigma)
```

```
# A tibble: 3 x 2
  alpha    VaR
  <dbl> <dbl>
1 0.95   41.9
2 0.99   61.5
3 0.999  81.8
```

diff
decreases

```
## A second run
one_VaR_sim(reps=100000,J=J,weights=weights,sigma=sigma)
```

```
# A tibble: 3 x 2
  alpha    VaR
  <dbl> <dbl>
1 0.95   41.2
2 0.99   61.1
3 0.999  82.2
```

Easier replication

times

```
my_VaR_reps<-replicate(100,  
                         one_VaR_sim(reps=10000,J=J,  
                         weights=weights,sigma=sigma))  
dim(my_VaR_reps)      function call
```

[1] ② 100 alpha (3x1) ...
 var (3x1) ...

```
myresults<-apply(aperm(my_VaR_reps,c(2,1)),②,unlist)
```



array version of transpose

⇒ alpha var
(6x1) (3x1)

| |

Easier replication

```
head(myresults)
```

```
    alpha      VaR
[1,] 0.950 41.758
[2,] 0.990 62.516
[3,] 0.999 86.176
[4,] 0.950 41.803
[5,] 0.990 61.920
[6,] 0.999 78.671
```

Easier replication

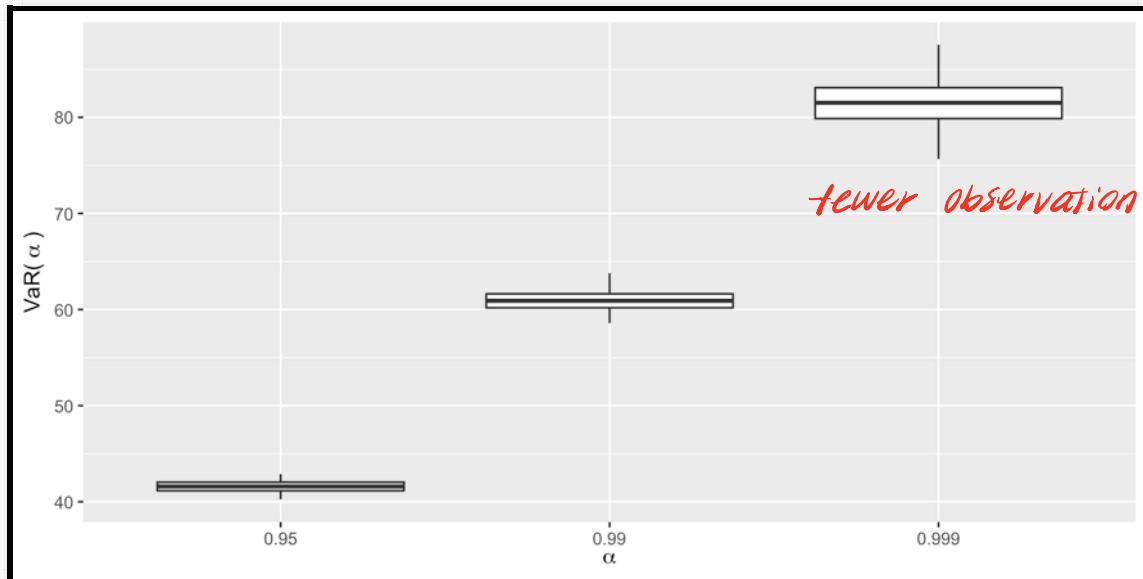
```
myresults<-as_tibble(myresults) %>% mutate(Rep=rep(1:100,each=3))  
head(myresults)
```

```
# A tibble: 6 x 3  
  alpha    VaR   Rep  
  <dbl> <dbl> <int>  
1 0.95    41.8     1  
2 0.99    62.5     1  
3 0.999   86.2     1  
4 0.95    41.8     2  
5 0.99    61.9     2  
6 0.999   78.7     2
```

Easier replication

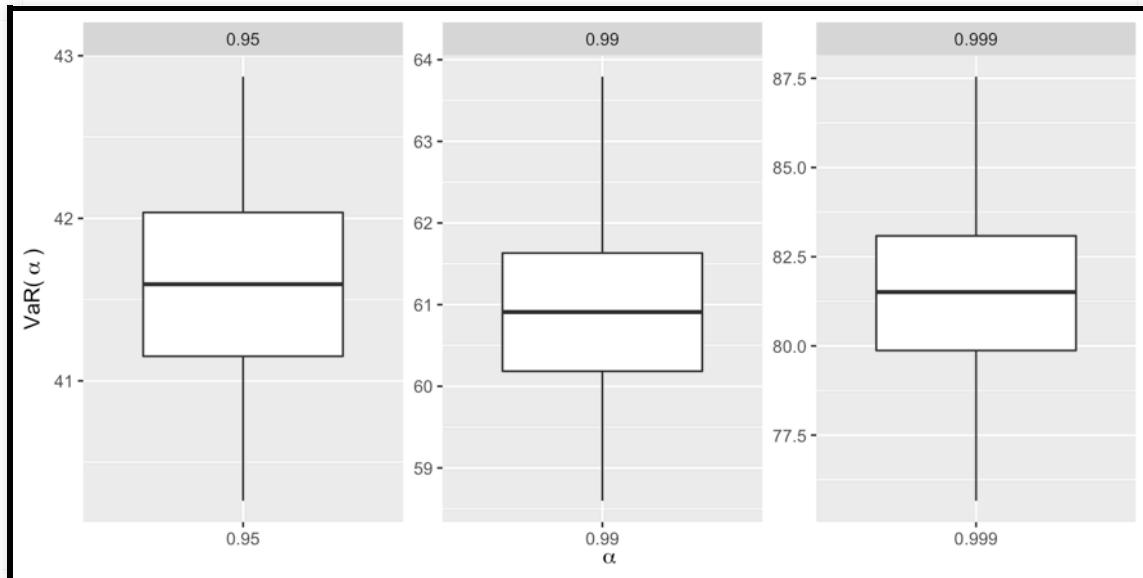
(?)

```
ggplot(myresults, aes(x=factor(alpha),y=VaR)) + geom_boxplot() +  
  labs(x=bquote(alpha),y=bquote("VaR( ~alpha~ )"))
```



Easier replication

```
ggplot(myresults, aes(x=factor(alpha),y=VaR)) + geom_boxplot() +  
  facet_wrap(~factor(alpha),scales="free") +  
  labs(x=bquote(alpha),y=bquote("VaR(~alpha~)"))
```



Even easier replication

```
set.seed(19752626)

my_results_tbl <- c(1:100) %>%
  map_dfr(~one_VaR_sim(reps=10000,J=J,
                        weights=weights,sigma=sigma)%>%
    mutate(Rep=.x))

head(my_results_tbl)
```

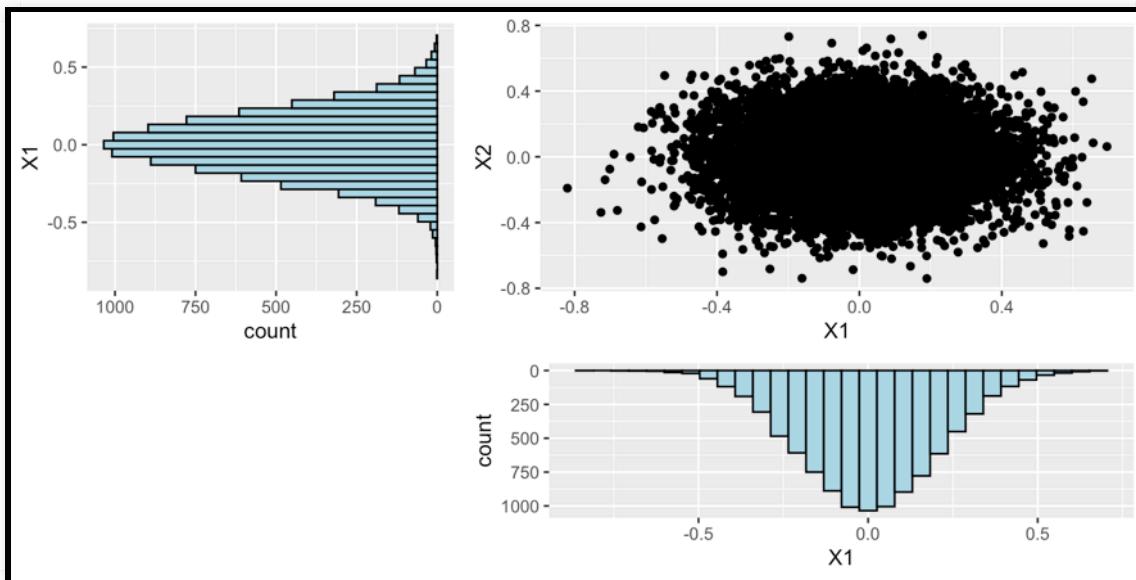
```
# A tibble: 6 x 3
  alpha   VaR   Rep
  <dbl> <dbl> <int>
1 0.95   41.8     1
2 0.99   61.6     1
3 0.999  85.1     1
4 0.95   41.4     2
5 0.99   58.4     2
6 0.999  81.3     2
```

Assessing sensitivity to assumptions

```
X <- tibble(X1=rnorm(10000,0,0.2),X2=rnorm(10000,0,0.2))
library(gridExtra)
plot_my_stuff<-function(X){
  p1<-ggplot(X,aes(x=X1)) + geom_histogram(bins=30,fill="lightblue",
                                              col="black") +
    scale_y_reverse() +
    coord_flip()
  p2<-ggplot(X,aes(x=X1,y=X2)) + geom_point()
  p3<-ggplot(X,aes(x=X1)) + geom_histogram(bins=30,fill="lightblue",
                                              col="black")+
    scale_y_reverse()
  plotlist<-list(p1,p2,p3)
  grid.arrange(p1,p2,p3,layout_matrix=
    rbind(c(1,1,2,2,2),c(1,1,2,2,2),
          c(1,1,2,2,2),c(NA,NA,3,3,3),
          c(NA,NA,3,3,3)))}
```

Assessing sensitivity to assumptions

```
plot_my_stuff(X)
```



Simulating dependence

```
rho<-0.5  
cov_mat<-matrix(rho, ncol=2, nrow=2)  
diag(cov_mat)<-1  
cov_mat
```

```
 [,1] [,2]  
[1,] 1.0 0.5  
[2,] 0.5 1.0
```

chol(cov_mat)
decomposition

$W = U^T U$
• upper triangular matrix

```
 [,1]      [,2]  
[1,] 1 0.50000  
[2,] 0 0.86603
```

Simulating dependence

```
X_star <- matrix(rnorm(10000*2), ncol=2)
X<-as_tibble(X_star%*%chol(cov_mat))
```

```
Warning: `as_tibble.matrix()` requires a matrix with column names or a
This warning is displayed once per session.
```

```
X<-X*0.2 ### Scaling step
colnames(X)<-c("X1", "X2")
```

W_{nx2}, A_{2x2}

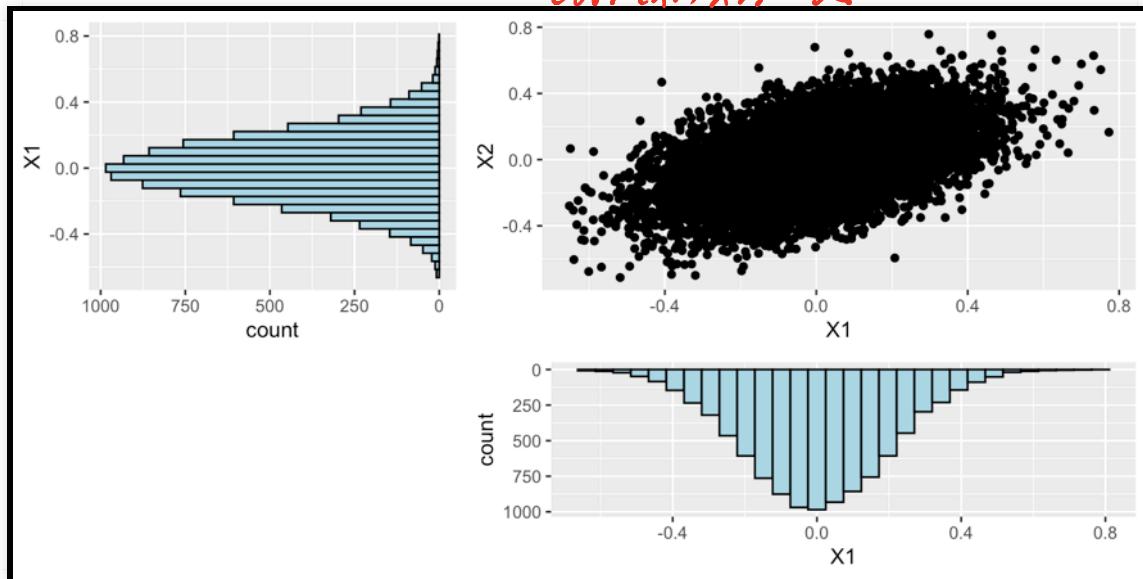
$$\text{Var}(WA) = A^T \text{Var}(W) A$$

$$\begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$$

Simulating dependence

```
plot_my_stuff(X)
```

$$\text{Corr}(X_1, X_2) = 0.5$$



Simulating dependence

```
rho<-0.9
cov_mat<-matrix(rho, ncol=2, nrow=2)
diag(cov_mat)<-1

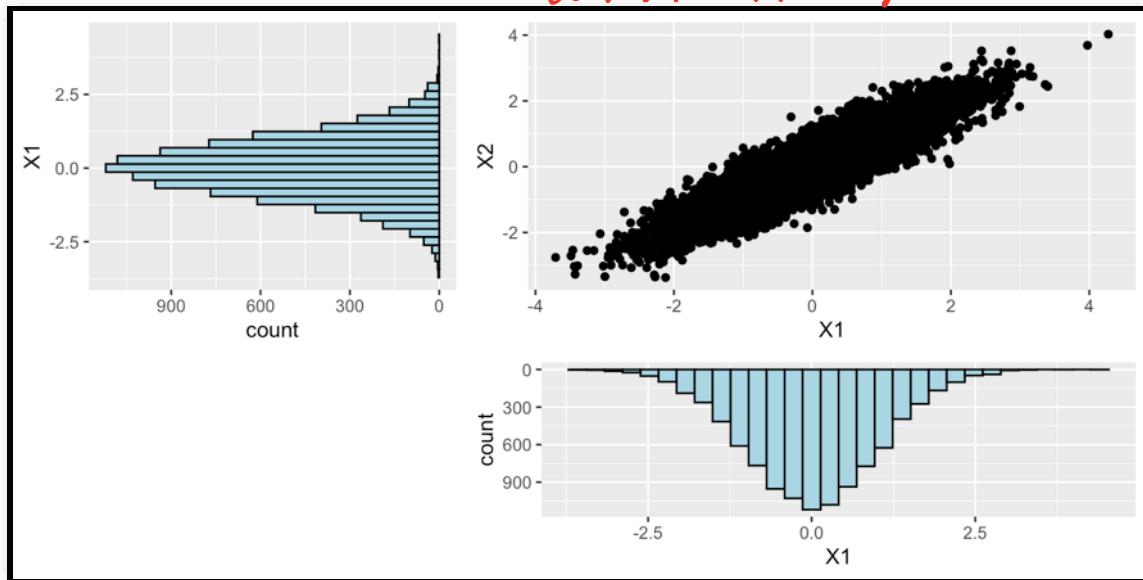
X_star <- matrix(rnorm(10000*2), ncol=2)
X<-as_tibble(X_star%*%chol(cov_mat))

colnames(X)<-c("X1", "X2")
```

Simulating dependence

```
plot_my_stuff(X)
```

$$\text{Corr}(X_1, X_2) = 0.9$$



Simulating dependence

```
rho<- -0.9
cov_mat<-matrix(rho, ncol=2, nrow=2)
diag(cov_mat)<-1

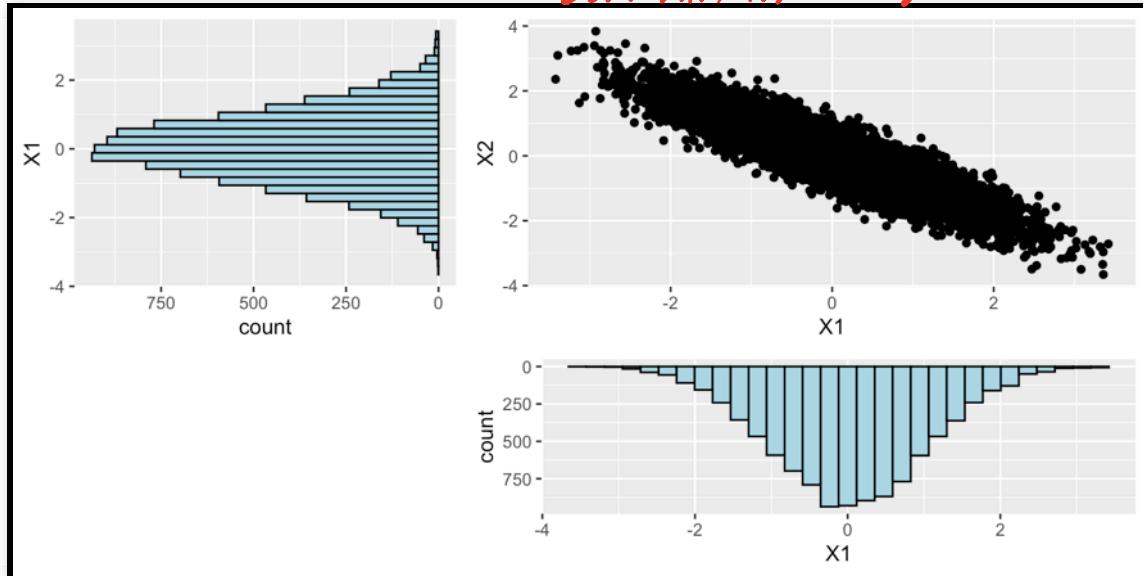
X_star <- matrix(rnorm(10000*2), ncol=2)
X<-as_tibble(X_star%*%chol(cov_mat))

colnames(X)<-c("X1", "X2")
```

Simulating dependence

```
plot_my_stuff(X)
```

$$\text{Corr}(X_1, X_2) = -0.9$$



Simulating dependence

```
one_VaR_dep_sim <- function(reps=100000,J, weights, sigma,
                           alphas=c(0.95,0.99,0.999),mean=0,
                           rho=0){ independents
  ## Setting covariance matrix
  cov_mat<-matrix(rho,ncol=J,nrow=J)
  diag(cov_mat)<-1
  X_star <- matrix(rnorm(10000*J),ncol=J)
  X_t_plus_1 <- t(sigma*X_star%*%chol(cov_mat)) ## transpose for old
dependent normal
  ## Compute L_t+1
  L_t_plus_1 <- - weights %*% (exp(X_t_plus_1) -1)
  ## Find VaR for different alphas
  VaR_alpha <- quantile(L_t_plus_1,alphas)
  return(tibble(alpha=alphas,VaR=VaR_alpha))
}
```

Simulating dependence

```
set.seed(19752626)

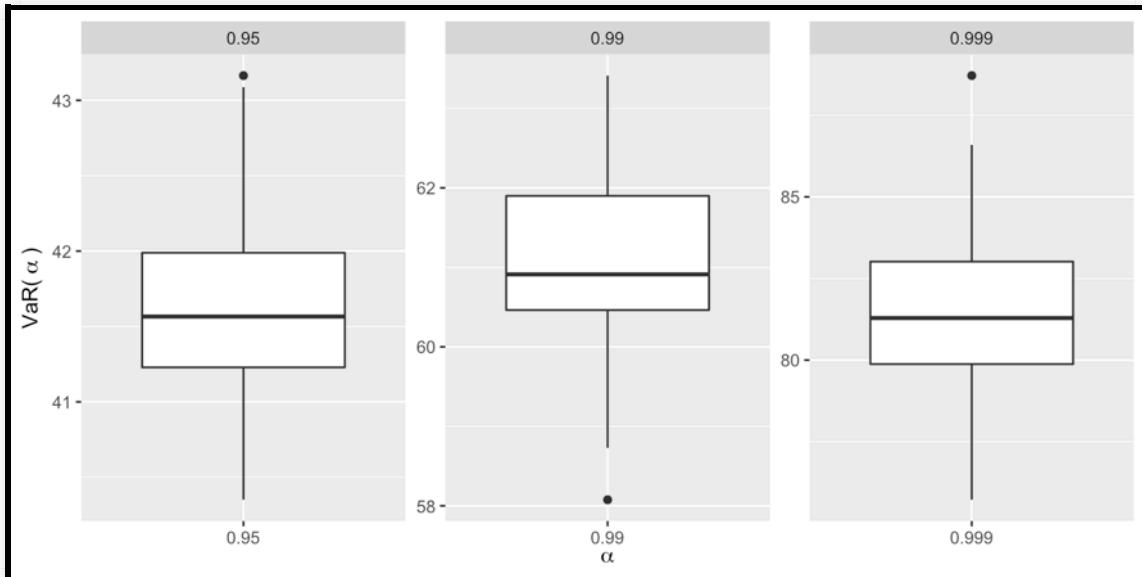
my_results_tbl <- c(1:100) %>%
  map_dfr(~one_VaR_dep_sim(reps=10000,J=J,
                            weights=weights,sigma=sigma,rho=0)%>%
    mutate(Rep=.x))

my_results_tbl %>% group_by(alpha) %>% summarise(Est=mean(VaR))
```

```
# A tibble: 3 x 2
  alpha   Est
  <dbl> <dbl>
1 0.95   41.7
2 0.99   61.1
3 0.999  81.5
```

Simulating dependence

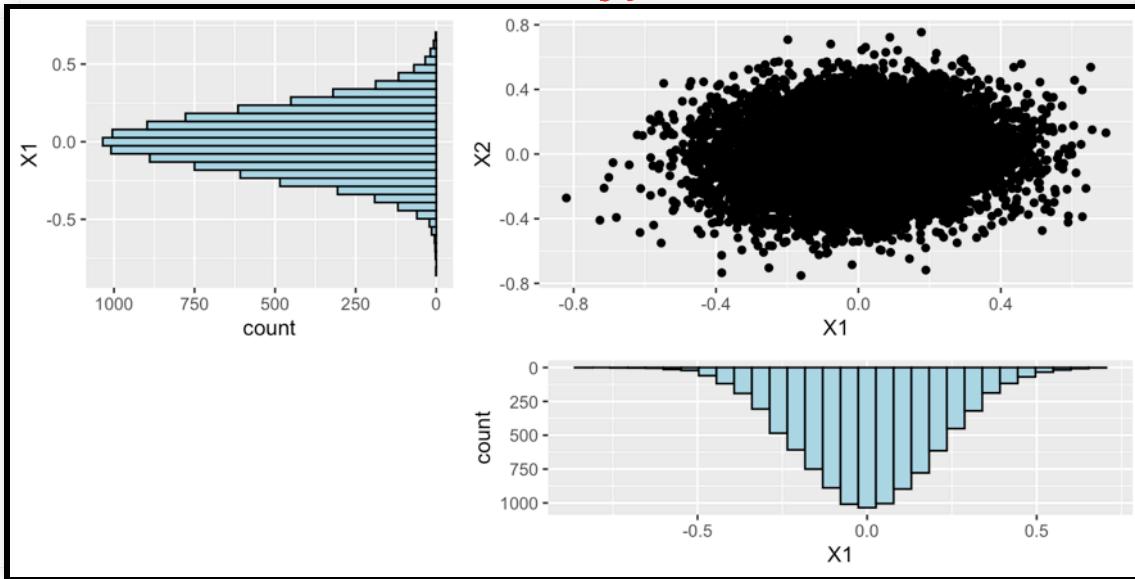
```
ggplot(my_results_tbl, aes(x=factor(alpha),y=VaR)) + geom_boxplot() +  
  facet_wrap(~factor(alpha),scales="free") +  
  labs(x=bquote(alpha),y=bquote("VaR(~alpha~)"))
```



Simulating dependence

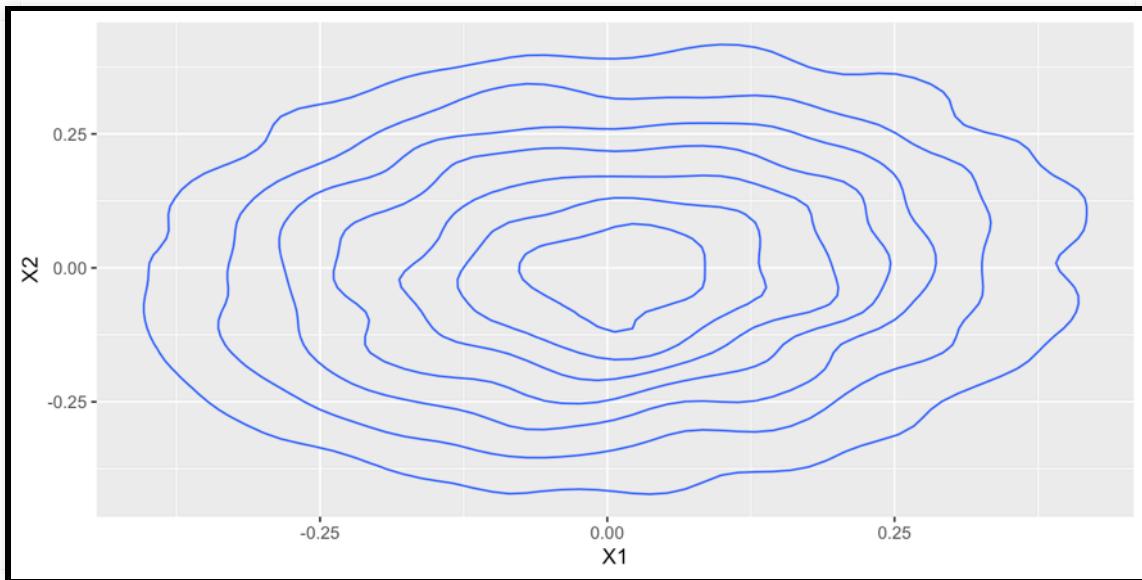
```
rho<- 0.1
cov_mat<-matrix(rho,ncol=2,nrow=2)
diag(cov_mat)<-1
X_star <- 0.2*matrix(rnorm(10000*2),ncol=2)
X<-as_tibble(X_star%*%chol(cov_mat))
colnames(X)<-c("X1","X2")
plot_my_stuff(X)
```

Corr = 0.1



Simulating dependence

```
ggplot(X, aes(x=X1, y=X2)) + geom_density_2d()
```



Simulating dependence

```
set.seed(19752626)

my_results_tbl_0.1 <- c(1:100) %>%
  map_dfr(~one_VaR_dep_sim(reps=10000,J=J,
                             weights=weights,sigma=sigma,rho=0.1)%>%
    mutate(Rep=.x))

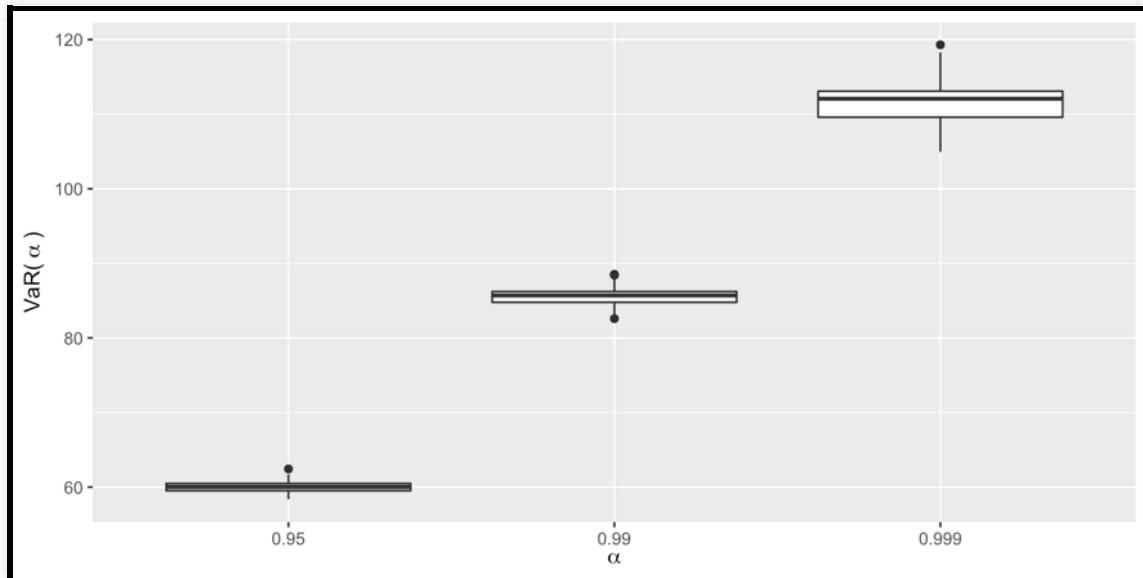
my_results_tbl_0.1 %>% group_by(alpha) %>% summarise(Est=mean(VaR))
```

```
# A tibble: 3 x 2
  alpha   Est
  <dbl> <dbl>
1 0.95   60.0
2 0.99   85.6
3 0.999  112.
```

*risk increases a lot
due to small correlation.*

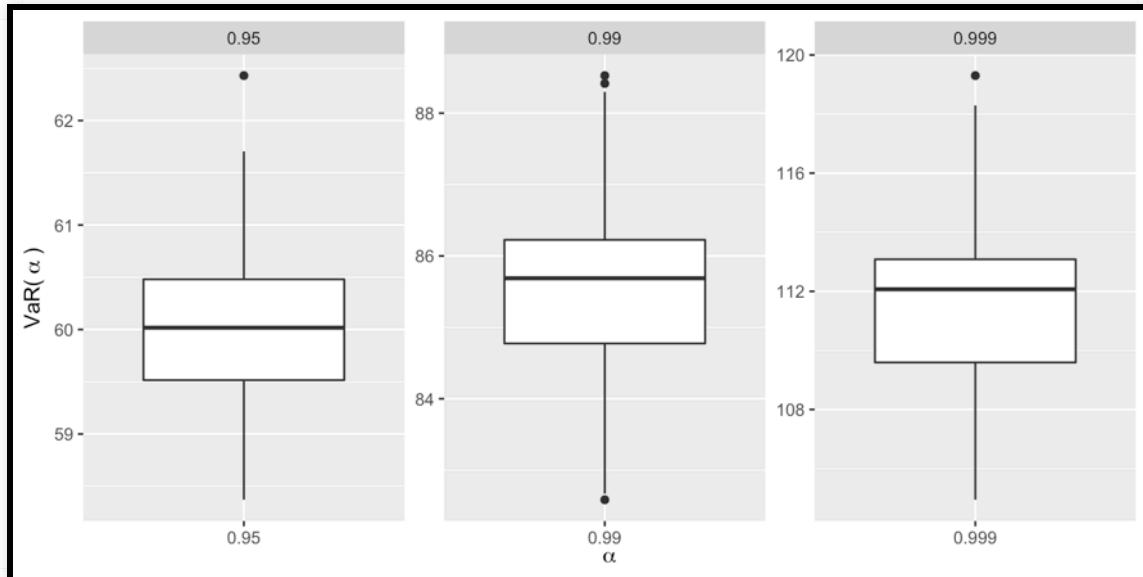
Simulating dependence

```
ggplot(my_results_tbl_0.1, aes(x=factor(alpha),y=VaR)) + geom_boxplot()  
+  
  labs(x=bquote(alpha),y=bquote("VaR(~alpha~)"))
```



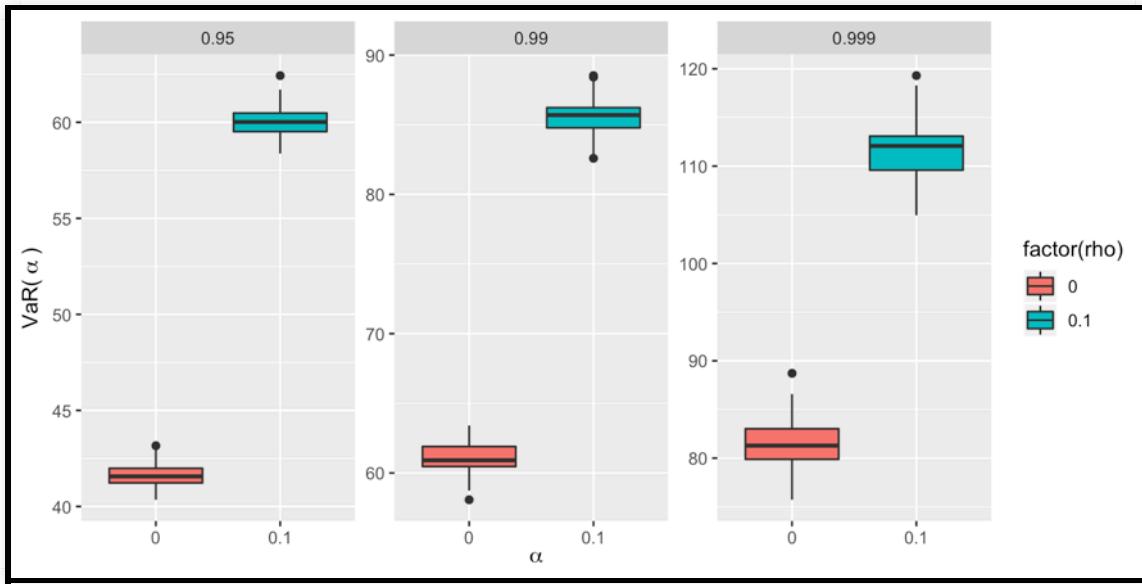
Simulating dependence

```
ggplot(my_results_tbl_0.1, aes(x=factor(alpha),y=VaR)) + geom_boxplot()  
+ facet_wrap(~factor(alpha),scales="free")  
labs(x=bquote(alpha),y=bquote("VaR(~alpha~)"))
```



Simulating dependence

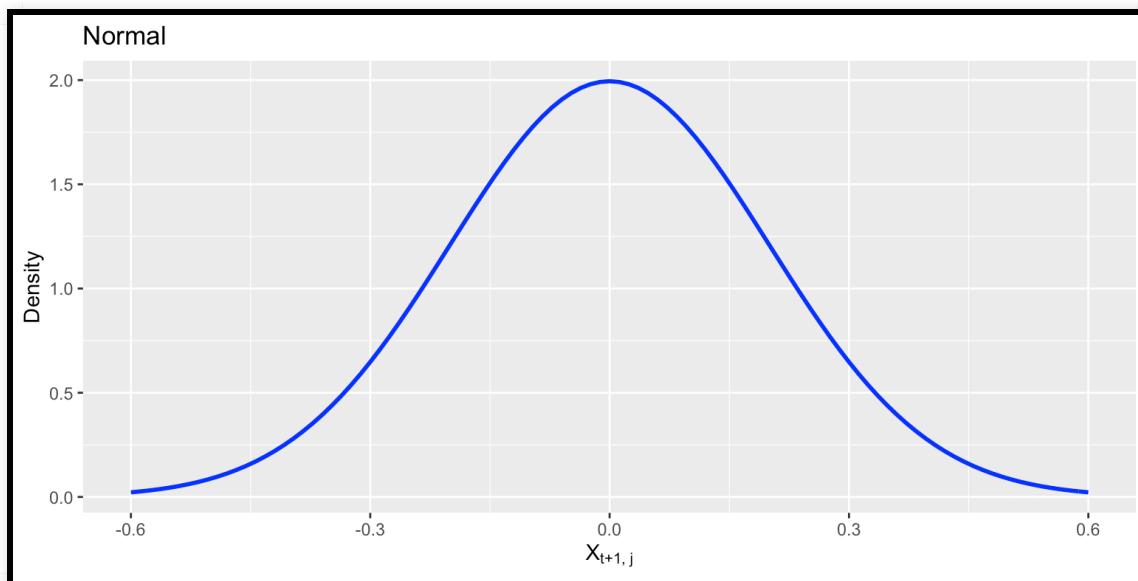
```
my_results_tbl_0.1 <- my_results_tbl_0.1 %>% mutate(rho=0.1)
my_results_tbl <- my_results_tbl %>% mutate(rho=0)
both_results_tbl<-bind_rows(my_results_tbl_0.1,my_results_tbl)
ggplot(both_results_tbl, aes(x=factor(rho),y=VaR,
                           fill=factor(rho))) + geom_boxplot() +
facet_wrap(~factor(alpha),scales="free")+
labs(x=bquote(alpha),y=bquote( "VaR(~alpha~)"))
```



Designing a multi-factor experiment

Allowing for more extreme observations

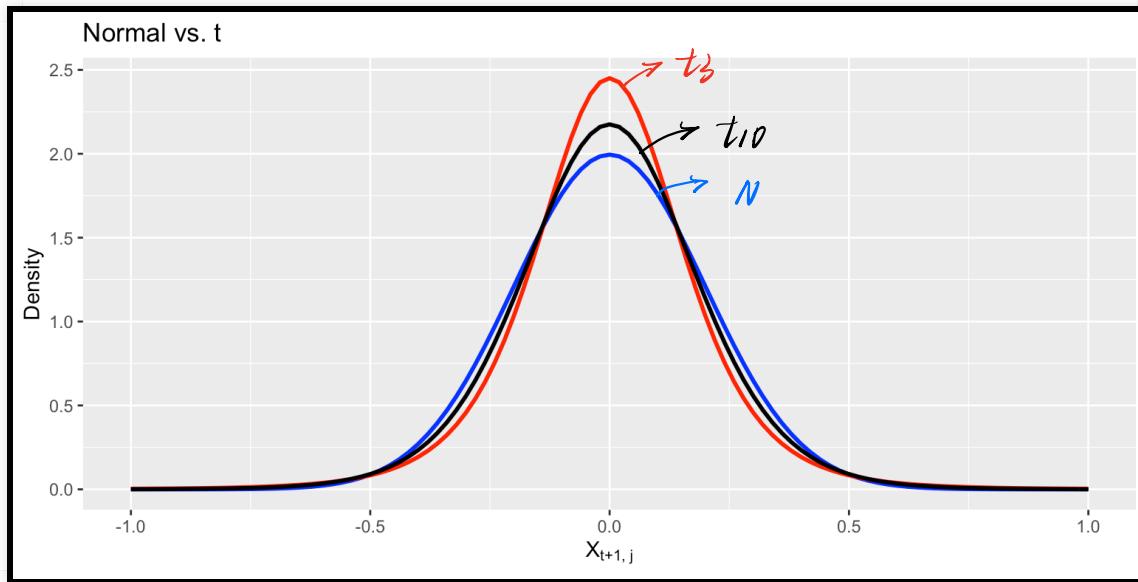
```
plot_grid<-tibble(x=seq(-0.6,0.6,length=1000))  
ggplot(plot_grid,aes(x=x)) +  
  stat_function(fun=dnorm,args=list(mean=0,sd=0.2),  
                lwd=1,col="blue") +  
  labs(x=bquote(X["t+1, j"]),y="Density", title="Normal")
```



Allowing for more extreme observations

```
plot_grid<-tibble(x=seq(-1,1,length=1000))
ggplot(plot_grid,aes(x=x)) +
  stat_function(fun=dnorm,args=list(mean=0,sd=0.2),
                lwd=1,col="blue") +
  labs(x=bquote(X[ "t+1, j"]),y="Density", title="Normal") +
  stat_function(fun=function(x,df,s){
    scale_c<-s/sqrt(df/(df-2))
    1/scale_c*dt(x/scale_c,df)
  },args=list(df=5,s=0.2), lwd=1,col="red") +
  labs(x=bquote(X[ "t+1, j"]),y="Density", title="Normal vs. t") +
  stat_function(fun=function(x,df,s){
    scale_c<-s/sqrt(df/(df-2))
    1/scale_c*dt(x/scale_c,df)
  },args=list(df=10,s=0.2),lwd=1,col="black") +
  labs(x=bquote(X[ "t+1, j"]),y="Density", title="Normal vs. t")
```

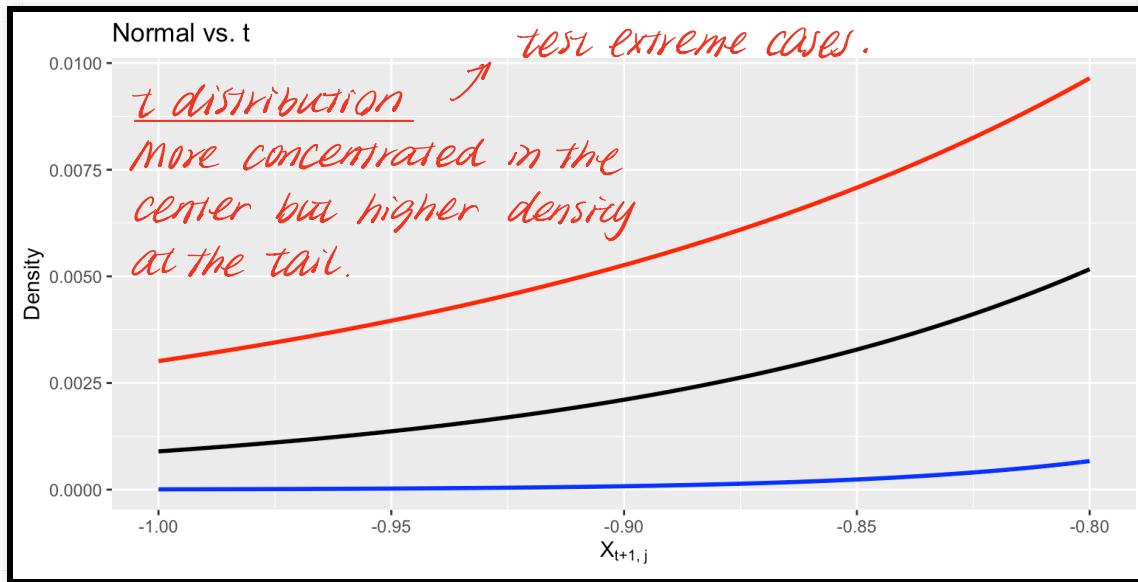
Allowing for more extreme observations



Allowing for more extreme observations

```
plot_grid<-tibble(x=seq(-1,1,length=1000))
ggplot(plot_grid,aes(x=x)) +
  stat_function(fun=dnorm,args=list(mean=0,sd=0.2),
                lwd=1,col="blue") +
  labs(x=bquote(X[ "t+1, j"]),y="Density", title="Normal") +
  stat_function(fun=function(x,df,s){
    scale_c<-s/sqrt(df/(df-2))
    1/scale_c*dt(x/scale_c,df)
  },args=list(df=5,s=0.2),lwd=1,col="red") +
  labs(x=bquote(X[ "t+1, j"]),y="Density", title="Normal vs. t") +
  stat_function(fun=function(x,df,s){
    scale_c<-s/sqrt(df/(df-2))
    1/scale_c*dt(x/scale_c,df)},
    args=list(df=10,s=0.2),lwd=1,col="black") +
  labs(x=bquote(X[ "t+1, j"]),y="Density", title="Normal vs. t") +
  xlim(c(-1,-0.8))
```

Allowing for more extreme observations



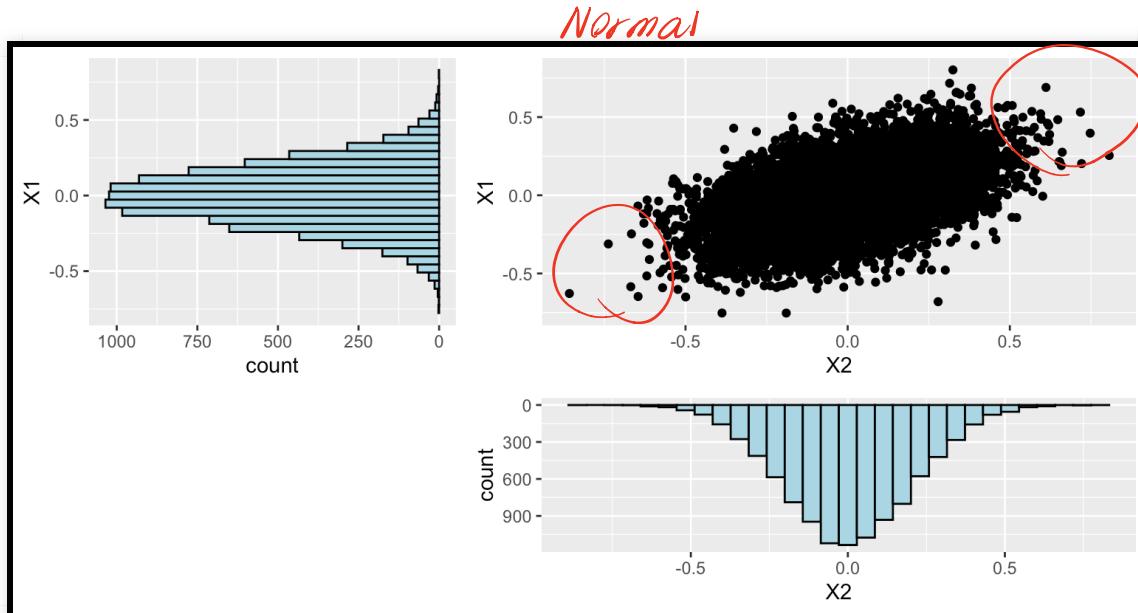
Generating dependent t - random variables

```
rho<-0.5
df<-5
sigma<-0.2
J<-2
cov_mat<-matrix(rho, ncol=J, nrow=J)
diag(cov_mat)<-1
t_scale<-rchisq(10000*J, df) (0,00)
X_star <- matrix(rnorm(10000*J), ncol=J)
X_tilde<- matrix(rnorm(10000*J)/sqrt(df/t_scale), ncol=J) t distribution
X_t_plus_1 <- t(sigma*X_star%*%chol(cov_mat)) ## transpose for old code
X_t_t_plus_1<- t(sigma*X_tilde%*%chol(cov_mat)) ## transpose for old
code
X<-as_tibble(t(X_t_plus_1))
X_t<-as_tibble(t(X_t_t_plus_1))

colnames(X)<-c("X1", "X2")
```

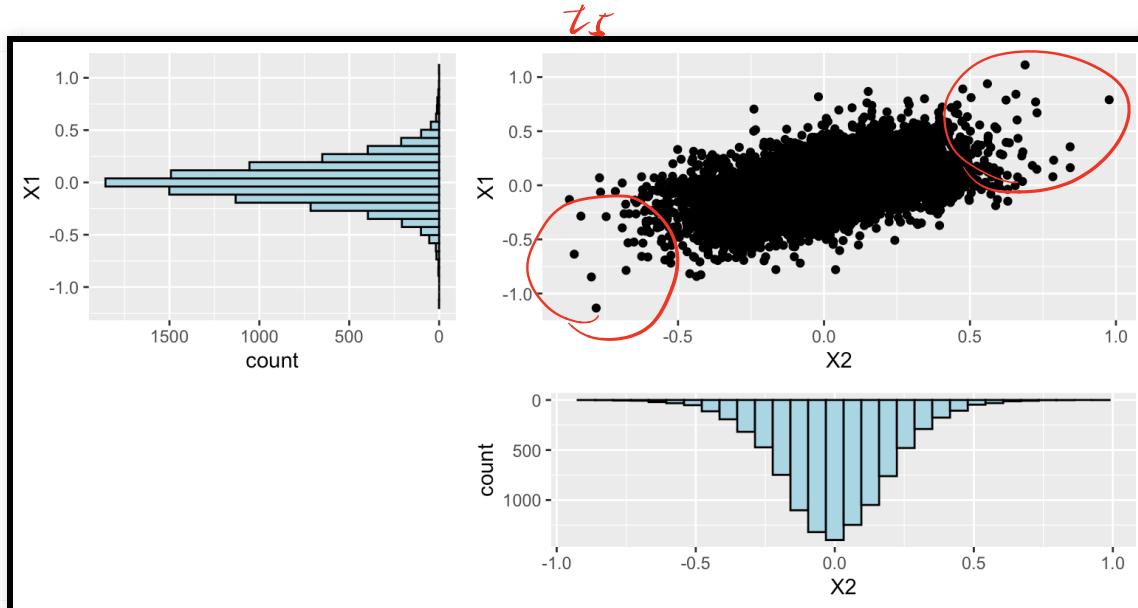
Generating dependent t — random variables

```
plot_my_stuff(X)
```



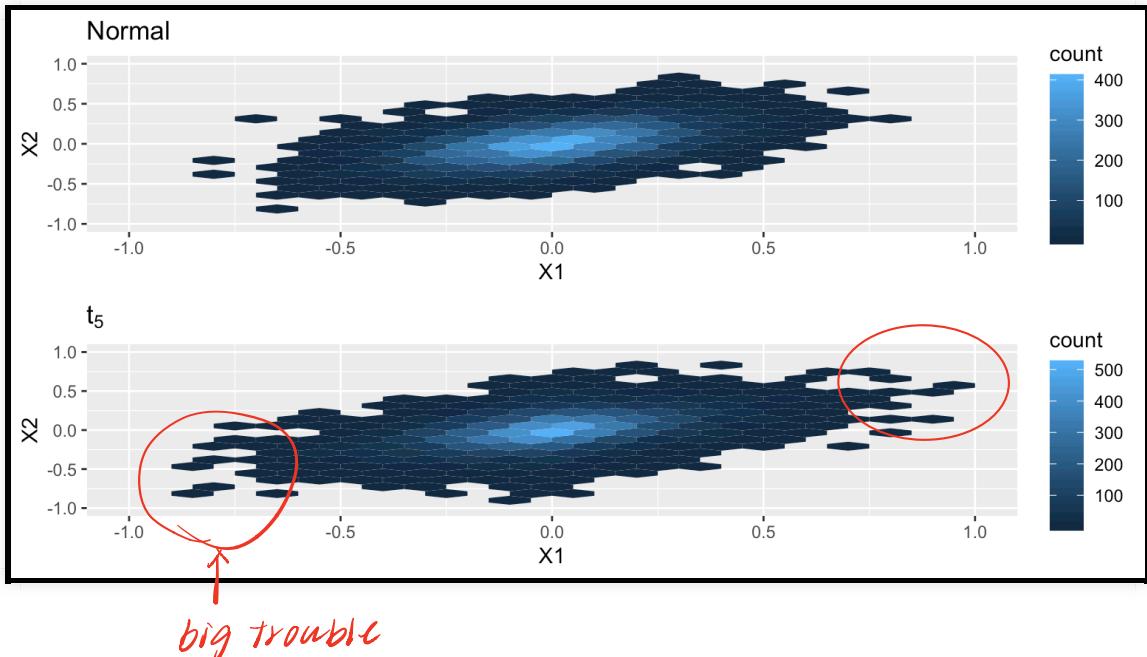
Generating dependent t — random variables

```
plot_my_stuff(X_t)
```



Generating dependent t - random variables

```
p1<-ggplot(X,aes(x=X1,y=X2)) + geom_hex(bins=20) + ggtitle("Normal") +
  ylim(c(-1,1)) + xlim(c(-1,1))
p2<-ggplot(X_t,aes(x=X1,y=X2)) + geom_hex(bins=20) +
  ggtitle(bquote(t[5])) +
  ylim(c(-1,1)) + xlim(c(-1,1))
grid.arrange(p1,p2)
```



Factorial simulation design

```
### First define correlations and df

rho<-c(0,0.1,0.4)
df<-c(3,10, 100)      df → ∞ t → N
iter<-c(1:100) # Number of iterations of each combination

conditions<-crossing(rho,df,iter)
head(conditions %>% arrange(iter))
```

```
# A tibble: 6 x 3
  rho     df   iter
  <dbl> <dbl> <int>
1 0       3     1
2 0       10    1
3 0       100   1
4 0.1    3     1
5 0.1    10    1
6 0.1    100   1
```

Factorial simulation design

default arguments

```
one_VaR_dep_t_sim <- function(reps=100000,J=10,weights=rep(50,J),  
                                sigma=0.2,  
                                alphas=c(0.95,0.99,0.999),  
                                rho=0,df=3){  
  ## Setting covariance matrix  
  cov_mat<-matrix(rho,ncol=J,nrow=J)  
  diag(cov_mat)<-1  
  t_scale<-rchi sq(reps*J,df)  
  X_tilde<- matrix(rnorm(reps*J)/sqrt(df/t_scale),ncol=J)  
  X_t_t_plus_1<- t(sigma*X_tilde%*%chol(cov_mat)) ## transpose for old  
  code  
  X_t<-as_tibble(t(X_t_t_plus_1))  
  L_t_plus_1 <- - weights %*% (exp(X_t_t_plus_1) -1)  
  ## Find VaR for different alphas  
  VaR_alpha <- quantile(L_t_plus_1,alphas)  
  return(tibble(alpha=alphas,VaR=VaR_alpha))
```

Factorial simulation design

```
library(tictoc)
tic()
results<-conditions %>% group_by(rho,df, iter) %>%
  mutate(
    ind_results = pmap(list(rho=rho,df=df),one_VaR_dep_t_sim)
  )
toc()
```

time

group_by (rho, df, iter) \Rightarrow each row

mutate

ind_results = *pmap* (*list* (*rho=rho, df=df*), *one_VaR_dep_t_sim*)

arguments *function*

```
234.263 sec elapsed
```

Factorial simulation design

```
head(results %>% arrange(iter))
```

```
# A tibble: 6 x 4
# Groups:   rho, df, iter [6]
  rho    df  iter ind_results
  <dbl> <dbl> <int> <list>
1 0        3      1 <tibble [3 x 2]>
2 0        10     1 <tibble [3 x 2]>
3 0       100     1 <tibble [3 x 2]>
4 0.1      3      1 <tibble [3 x 2]>
5 0.1      10     1 <tibble [3 x 2]>
6 0.1     100     1 <tibble [3 x 2]>
```

Factorial simulation design

```
results<-results %>% unnest(cols=ind_results)  
head(results)
```

```
# A tibble: 6 x 5  
# Groups: rho, df, iter [2]  
  rho      df    iter alpha   VaR  
  <dbl> <dbl> <int> <dbl> <dbl>  
1 0       3     1  0.95  41.3  
2 0       3     1  0.99  60.8  
3 0       3     1  0.999 81.9  
4 0       3     2  0.95  40.8  
5 0       3     2  0.99  59.9  
6 0       3     2  0.999 82.1
```

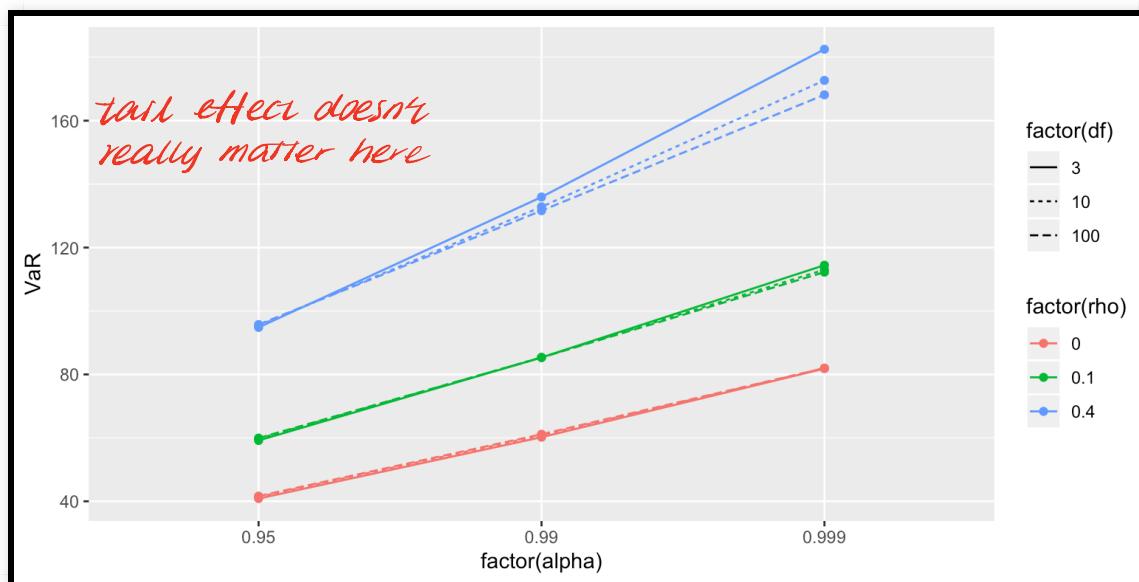
Factorial simulation design

```
summarise_for_plot<-results %>% group_by(rho,df,alpha) %>%
  summarise(VaR = mean(VaR))
head(summarise_for_plot)
```

```
# A tibble: 6 x 4
# Groups:   rho, df [2]
  rho     df alpha    VaR
  <dbl> <dbl> <dbl> <dbl>
1 0       3   0.95  40.9
2 0       3   0.99  60.2
3 0       3   0.999 81.8
4 0      10   0.95  41.4
5 0      10   0.99  60.8
6 0      10   0.999 82.0
```

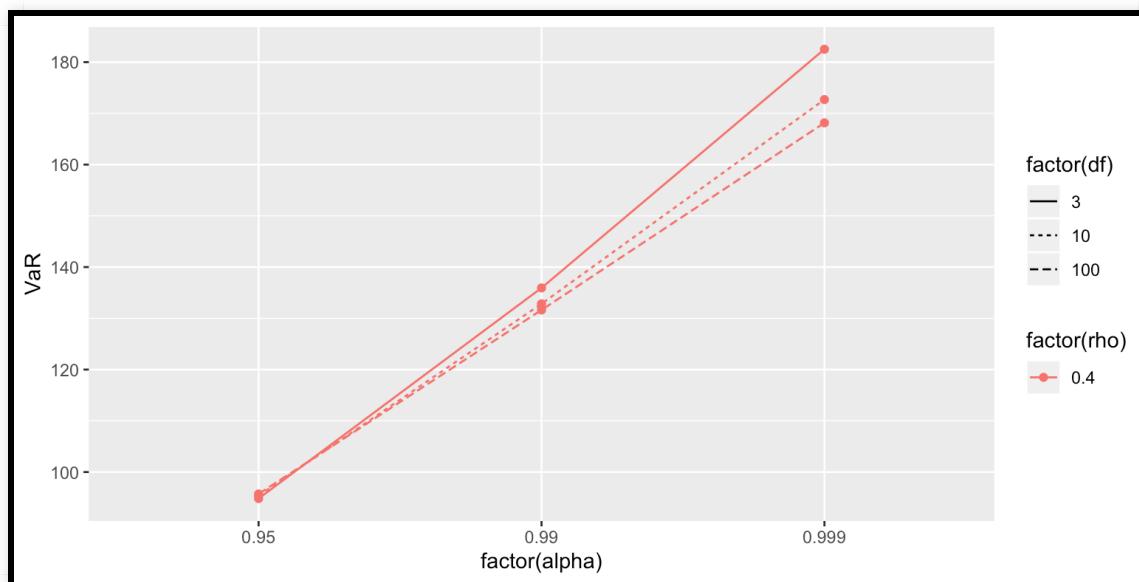
Factorial simulation design

```
ggplot(summarise_for_plot,aes(x=factor(alpha),y=VaR,  
                               col=factor(rho),  
                               linetype=factor(df),  
                               group=interaction(df,rho))) +  
  geom_point() +geom_line()
```



Factorial simulation design

```
ggplot(summarise_for_plot %>%
        filter(rho==0.4),aes(x=factor(alpha),y=VaR,
                             col=factor(rho),linetype=factor(df),
                             group=interaction(df,rho))) +
  geom_point() +geom_line()
```

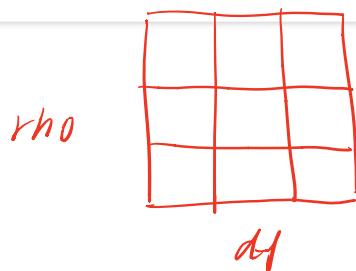


Not in final

Simsalapar

```
library(simsalapar)
rho<-c(0,0.1,0.4)
df<-c(3,10, 100)

varList<-varlist(
  n.sim=list(type="N",expr=quote(N[sim]), value=100), number of replication
  rho = list(type="grid",value=rho),
  df = list(type="grid", value=df)
)
```



type = "inner"
to same dataset using different variables.

Simsalapar

```
do_one_VaR_dep_t_sim <- function(reps=100000,J=10,weights=rep(50,J),  
                                sigma=0.2,  
                                alphas=c(0.95,0.99,0.999),  
                                rho=0,df=3){  
  ## Setting covariance matrix  
  cov_mat<-matrix(rho,ncol=J,nrow=J)  
  diag(cov_mat)<-1  
  t_scale<-rchi sq(reps*J,df)  
  X_tilde<- matrix(rnorm(reps*J)/sqrt(df/t_scale),ncol=J)  
  X_t_t_plus_1<- t(sigma*X_tilde%*%chol(cov_mat)) ## transpose for old  
  code  
  X_t<-as_tibble(t(X_t_t_plus_1))  
  L_t_plus_1 <- - weights %*% (exp(X_t_t_plus_1) -1)  
  ## Find VaR for different alphas  
  VaR_alpha <- quantile(L_t_plus_1,alphas)  
  return(VaR_alpha) ### THIS IS DIFFERENT  
  numeric vector
```

Simsalapar

```
tic() do lapply 1 Processors
tic()
res<-doMcclapply(varList, sfile="res_lapply_seq.rds",
                  doOne=do_one_VaR_dep_t_sim,
                  monitor=interactive())
toc()
```

```
74.624 sec elapsed
```

```
class(res)
```

```
[1] "array"
```

```
dim(res)
```

```
rho      df n.sim
      3      3    100
```

Simsalapar

```
res[1,1,1]
```

```
[[1]]
[[1]]$value
  95%    99%  99.9%
40.945 60.086 82.011
```

```
[[1]]$error
NULL
```

```
[[1]]$warning
NULL
```

```
[[1]]$time
[1] 388
```

Simsalapar

```
val <- getArray(res)
mytime <- getArray(res, "time")

df<-array2df(val)
str(df)
```

```
'data.frame': 2700 obs. of 5 variables:
 $ Var1 : Factor w/ 3 levels "95%","99%","99.9%": 1 2 3 1 2 3 1 2 3 1 ...
 $ rho   : Factor w/ 3 levels "0.0","0.1","0.4": 1 1 1 2 2 2 3 3 3 1 ...
 $ df    : Factor w/ 3 levels "3","10","100": 1 1 1 1 1 1 1 1 1 2 ...
 $ n.sim: Factor w/ 100 levels "1","2","3","4",...: 1 1 1 1 1 1 1 1 1 1 ...
 $ value: num 40.9 60.1 82 59.5 85.6 ...
```

```
head(df)
```

	Var1	rho	df	n.sim	value
1	95%	0.0	3	1	40.945
2	99%	0.0	3	1	60.086
3	99.9%	0.0	3	1	82.011
4	95%	0.1	3	1	59.463
5	99%	0.1	3	1	85.644
6	99.9%	0.1	3	1	114.964