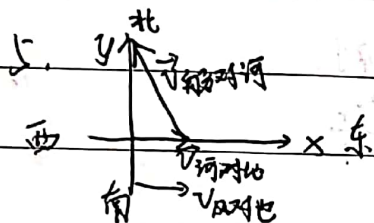


### 习题三

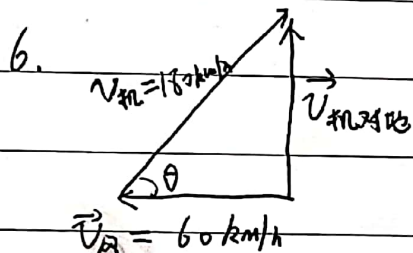
1. C      2. B      3.  $-R\omega \sin \omega t \vec{i} + R\omega \cos \omega t \vec{j}$        $\omega^2 R$

4.  $\sqrt{u^2 + v^2 + 2uv \cos \alpha}$        $\arcsin \frac{v \sin \alpha}{(u^2 + v^2 + 2uv \cos \alpha)^{\frac{1}{2}}}$



$\vec{v}_{\text{船对地}} = \vec{v}_{\text{船对河}} + \vec{v}_{\text{河对地}} = 10\sqrt{3} \text{ km/h}$ , 方向向北。

$\therefore \vec{v}_{\text{风对船}} = \vec{v}_{\text{风对地}} + \vec{v}_{\text{地对船}} = 20 \text{ km/h}$ , 方向南偏东  $30^\circ$



应采取北偏东  $\theta$  角且  $\cos \theta = \frac{1}{3}$

$|\vec{v}_{\text{机对地}}| = \sqrt{180^2 - 60^2} \text{ km/h} = 120\sqrt{2} \text{ km/h}$

### 习题四

1. C      2. B      3.  $f_0$       4.  $3\sqrt{3} \text{ N}$

5. 设向上为正方向 对  $m_1$ :  $T - m_1 g = -m_1 a_1$

环对地  $-a_0 = -a_2 + a_1$  对环:  $f - m_2 g = -m_2 a_0$

对绳:  $T = f$

解得  $a_1 = \frac{(m_1 - m_2)g + m_2 a_2}{m_1 + m_2}$        $a_0 = \frac{m_1 a_2 - (m_1 - m_2)g}{m_1 + m_2}$

$T = m_1 g - m_1 \frac{(m_1 - m_2)g + m_2 a_2}{m_1 + m_2}$

6. (1)  $-Kv = m \frac{dv}{dt} \Rightarrow -\frac{m}{K} \int_{v_0}^v \frac{1}{v} dv = \int_0^t dt \Rightarrow v = v_0 e^{-\frac{Kt}{m}}$

(2)  $x = \int_0^\infty v dt$  当  $t \rightarrow \infty$  时,  $v \rightarrow 0$

$x = \int_0^\infty v(t) dt = \int_0^\infty v_0 e^{-\frac{Kt}{m}} dt = \frac{mv_0}{K}$

# 习题五

$$1. A \quad 2. A \quad 3. (1) \frac{mg}{\cos \theta} \quad (2) v = \sqrt{mgl \tan \theta \sin \theta}$$

$$4. -\frac{m_3 g}{m_2} \quad 0$$

5. 设弹簧原长为  $L$ , 弹性系数为  $k$ , 当  $\omega = \omega_0$  时,  $f = f_0$  时,

$$k(f_0 L - L) = m \omega_0^2 f_0 L \Rightarrow \frac{k}{m} = \frac{\omega_0^2 f_0}{f_0 - 1}$$

$$\therefore k(f - 1)L = m \omega^2 f L$$

$$\omega = \omega_0 \sqrt{\frac{f_0(f - 1)}{f(f_0 - 1)}}$$

$$6. (1) T + mg \cos \theta = m \frac{v^2}{R} \Rightarrow T = m \frac{v^2}{R} - mg \cos \theta$$

$$mg \sin \theta = ma_t \quad a_t = g \sin \theta$$

(2) 从最上面的点开始, 大小先增大, 在绳子水平时最大; 再减小, 在最下面变为 0, 再增大最后减小。

\* 左半圆方向与  $v$  相同, 右半圆与  $v$  相反