

# Obsidian Language Formalism

## 1 Language Overview

## 2 Obsidian Core Calculus Grammar

The grammar is shown in Figure 1. Unless stated otherwise, assume  $\bar{I}$  means a possibly empty sequence of identifiers  $I$ ; also assume that all items in the sequence are distinct, so that “ $x, y, z$ ” is a valid sequence, but “ $x, y, x$ ” is not.

|   |   |                                  |
|---|---|----------------------------------|
| $x, y, z \in \text{LOCALVARIABLES}$   | $\text{this} \in \text{SPECIALVARIABLES}$ | $f, g \in \text{FIELDVARIABLES}$ |
| $\text{this}, a, x, y, z, f, g \in \text{VARIABLES}$  | $\ell \in \text{INDIRECTREFS}$            | $o \in \text{OBJECTREFS}$        |
| $Ct ::= \text{contract } C \{ \overline{Ct} \ \overline{St} \ \overline{\text{const } \tau f} \ \overline{\tau f} \}$                                 |   |                                  |
| $St ::= \text{state } S \{ \overline{\tau f} \ \overline{\text{MethDecl } \text{MethBody}} \}$  |   |                                  |
| $p ::= \text{owned} \mid \text{readonly} \mid \text{shared}$  |   |                                  |
| $\tau_s ::= C \mid C.S$   |   |                                  |
| $\tau_p ::= \tau_s \mid a.\tau_p$   |   |                                  |
| $\tau ::= p \triangleright \tau_p \mid \text{pack\_to}[S, \tau]$  |   |                                  |
| $TxLabel ::= \text{function} \mid \text{transaction}$   |   |                                  |
| $\text{MethDecl} ::= TL \ \tau \ m(\overline{\tau x}) \leftrightarrow \overline{S}$   |   |                                  |
| $\text{MethBody} ::= \{ e \}$   |   |                                  |
| $e ::= a \mid \text{let } x = e \text{ in } e \mid \text{new } C.S(\overline{x}) \text{ as } p \mid a.m(\overline{x})$                                |   |                                  |
| $\mid \text{throw} \mid \text{try } \{ e \} \text{ catch } \{ e \}$   |   |                                  |
| $\mid \text{pack\_to } S(\overline{x}) \text{ returns } y \mid \text{unpack } \{ e \} \mid \text{if } x : \tau_s \text{ then } e_1 \text{ else } e_2$ |   |                                  |
| $\mid \ell$   |   |                                  |

**Fig. 1.** Grammar

There are several categories of variable names in the formalism. **LOCALVARIABLES** (denoted by  $x, y, z$ ) are variables defined in the body of a method by a **let** expression, or by method arguments. **FIELDVARIABLES** (denoted by  $f, g$ ) are variables used for fields, but they can sometimes enter the local context, for example during an unpack block. **SPECIALVARIABLES** includes only the special identifier **this**. **VARIABLES** (denoted  $a, b$ ) is a catch-all category for all the aforementioned variable types.

### 3 Static Semantics

Figure 2 defines auxiliary relations that are helpful in defining the typing relation; Figure 3 defines the typing relation for expressions; Figure 4 defines extra typing judgments to check fields, methods, and contracts.

The typing relation  $\Delta \vdash_b e : \tau \dashv \Delta'$  is flow-sensitive: it outputs a typing context, in addition to giving a type to the expression  $e$ . The following invariant also holds for the typing relation:  $x \in \text{dom}(\Delta)$  if and only if  $x \in \text{dom}(\Delta')$ . Informally, this says that the contexts  $\Delta$  and  $\Delta'$  have the exact same variables in them, only differing perhaps by the type assigned to those variables.

The boolean  $b$  in the typing judgment indicates whether the expression  $e$  should be typed as if it were inside an **unpack** statement: inside an **unpack**,  $b = \text{t}$ , while outside of an **unpack**,  $b = \text{f}$ . Some typing judgments are valid for only one or the other case (e.g. T-PACK and T-INV) but others are valid in either case (e.g. T-LET).

Types can either be of contract type or of a special **pack\_to** type. Only the former sort of types, however, are allowed in the typing context. This is implicitly enforced by:

- T-LET - this rule requires the bound variable to be of contract type
- the method **Ok** judgment - this determines the initial value of the typing context when typechecking a method body, and prohibits **pack\_to** types in the initial context
- the field **Ok** judgment - this ensures that fields aren't of type **pack\_to**, and thus **pack\_to** types cannot appear in the typing context via field unpacking.

It is assumed that the type rules have access to the helper function *lookup*, *fields*, and *methods*. These helper functions retrieve, respectively, the contract signature, the set of fields, and the set of methods of a contract given the contract's name. If the type specifies a specific typestate, all the methods and fields that are available in that state (including those defined in the contract as a whole) are retrieved. There is also *mutableFields*, which retrieves the subset of *fields* that are not labeled as **const**.

We say that a context  $\Delta$  is well-formed if each type in the context is well-formed with respect to the context: a context is well-formed if

### 4 Dynamic Semantics

Auxiliary definitions for the dynamic semantics are shown in Figure 5. The small-step evaluation relation is defined in Figure 6. We augment the set of expressions  $e$  in the runtime to make it easier to express the desired semantics for exceptions: it is assumed that whole programs do not make use of the new **try-catch** and method call constructs.

|  |   |
|--|---|
| $\boxed{\text{res}(p), \text{res}(\tau), \text{res}(\bar{x}, \Delta)}$   | Residual Permission/Type/Context  |
| $\text{res}(\text{owned}) = \text{readonly} \quad \text{res}(\text{readonly}) = \text{readonly} \quad \text{res}(\text{shared}) = \text{shared}$   |   |
| $\text{res}(p \triangleright \tau_s) = \text{res}(p) \triangleright \tau_s \quad \frac{\Delta' = \Delta[x_i \mapsto \text{res}(\Delta(x_i))]}{\text{res}(\bar{x}, \Delta) = \Delta'}$  |   |
| $\boxed{\text{rm}(x, \Delta), \text{rm}(\bar{x}, \Delta)}$   | Removes variable $x$ or variables $\bar{x}$ from the context $\Delta$         |
| $\frac{p \neq \text{owned} \quad \forall (y \tau) \in \Delta, \tau_p. \tau \neq x.\tau_p}{\text{rm}(x, (\Delta, x : p \triangleright \tau)) = \Delta} \quad \frac{x \notin \text{dom}(\Delta)}{\text{rm}(x, \Delta) = \Delta}$   |   |
| $\text{rm}(\emptyset, \Delta) = \Delta \quad \text{rm}(\{x_1, \dots, x_n, x_{n+1}\}, \Delta) = \text{rm}(\{x_1, \dots, x_n\}, \text{rm}(x_{n+1}, \Delta))$   |   |
| $\boxed{\tau <: \tau'}$  | Subtyping   |
| $\tau <: \tau \quad p \triangleright C.S <: p \triangleright C \quad p \triangleright P.C.S <: p \triangleright P.C$   |   |
| $\boxed{\text{mergeable}(\Delta; \Delta_1, \dots, \Delta_n), \text{merge}(\Delta; \Delta_1, \dots, \Delta_n)}$   |   |
| Merges contexts $\Delta_1, \dots, \Delta_n$ after branching from the original context $\Delta$   |   |
| $\frac{\text{mergeable}(\Delta; \Delta_1, \dots, \Delta_n) \quad \exists \tau'. (\forall i. \Delta_i(x) <: \tau')}{\text{mergeable}((\Delta, x : \tau); \Delta_1, \dots, \Delta_n)} \quad \text{mergeable}(\emptyset; \Delta_1, \dots, \Delta_n)$  |   |
| $\frac{\text{mergeable}(\Delta; \Delta_1, \dots, \Delta_n)}{\text{merge}(\Delta; \Delta_1, \dots, \Delta_n) = \{(x, \tau) \mid x \in \Delta \ \& \ \Delta_i(x) <: \tau\}}$   |   |
| $\boxed{\text{wf}(\Delta, \tau), \text{wf}(C, \tau)}$  | Assures wellformedness of type $\tau$ w.r.t. $\Delta$ or $C$                  |
| $\frac{\neg \text{hasParent}(\text{contractOf}(\tau_s))}{\text{wf}(\Delta, p \triangleright \tau_s)} \quad \frac{\text{contractOf}(\Delta(\text{this})) = \text{contractOf}(\tau_s)}{\text{wf}(\Delta, p \triangleright \tau_s)}$  |   |
| $\frac{\text{contractOf}(\Delta(a)) = C \quad \text{wf}(\Delta, C, p \triangleright \tau_p)}{\text{wf}(\Delta, p \triangleright a.\tau_p)} \quad \frac{(\tau_f \ f) \in \text{constFields}(C) \quad \text{wf}(\text{contractOf}(\tau_f), p \triangleright \tau_p)}{\text{wf}(C, p \triangleright f.\tau_p)}$ |   |
| $\frac{C = \text{parent}(\text{contractOf}(\tau_s))}{\text{wf}(C, p \triangleright \tau_s)}$   |   |
| $\boxed{\text{subst}(\tau, \tau', M)}$   | Changes perspective of $\tau$ using mapping $M$ , with recipient type $\tau'$ |
| $\frac{M(z) = y}{\text{subst}(p \triangleright z.\tau_p, \tau, M) = p \triangleright y.\tau_p} \quad \frac{\neg \text{hasParent}(\text{contractOf}(\tau_s))}{\text{subst}(p \triangleright \tau_s, \tau, M) = p \triangleright \tau_s}$  |   |
| $\frac{\text{contractOf}(\tau_s) = \text{contractOf}(\tau_{s'})}{\text{subst}(p \triangleright \tau_s, a.f_1 \dots .f_n.\tau_{s'}, M) = p \triangleright a.f_1 \dots .f_n.\tau_s}$   |   |

Fig. 2. Auxiliary Relations

|  |   |
|--|---|
| $\Delta \vdash_b e : \tau \dashv \Delta'$  |   |
| $\frac{\tau <: \tau' \quad \Delta \vdash_b e : \tau \dashv \Delta'}{\Delta \vdash_b e : \tau' \dashv \Delta'} \text{T-SUB}$  | $\frac{a \neq \text{this}}{\Delta, a : \tau \vdash_b a : \tau \dashv \Delta, a : \text{res}(\tau)} \text{T-VAR}$                          |
| $\frac{\Delta(\text{this}) = \tau}{\Delta \vdash_f \text{this} : \text{res}(\tau) \dashv \Delta} \text{T-THIS}$  | $\frac{(\tau \ f) \in \text{fields}(\Delta(\text{this}))}{\Delta \vdash_f \text{res}(f) : \text{res}(\tau) \dashv \Delta} \text{T-FIELD}$ |
| $\frac{\forall \tau_p. \tau \neq x.\tau_p \quad \forall \tau. (\tau \ x) \notin \text{constFields}(\Delta(\text{this})) \quad x \notin \Delta \quad \Delta \vdash_b e_1 : p \triangleright \tau_s \dashv \Delta_1 \quad \Delta_1, x : p \triangleright \tau_s \vdash_b e_2 : \tau \dashv \Delta_2}{\Delta \vdash_b \text{let } x = e_1 \text{ in } e_2 : \tau \dashv \text{rm}(x, \Delta_2)} \text{T-LET}$   |   |
| $\frac{\text{hasParent}(C) \Rightarrow \exists p'. \Delta(\text{this}) <: p' \triangleright \text{parent}(C) \quad \overline{\tau \ f} = \text{fields}(C.S)}{\Delta, \overline{x} : \tau \vdash_b \text{new } C.S(\overline{x}) \text{ as } p : p \triangleright C.S \dashv \Delta, x : \text{res}(\tau)} \text{T-NEW}$  |   |
| $\frac{\begin{array}{l} M = \emptyset[\overline{z} \mapsto \overline{y}][\text{this} \mapsto x] \\ (TL \ \tau_{ret} \ m(\overline{\tau \ z}) \hookrightarrow \overline{S}) \in \text{methods}(\tau_{recip}) \quad \tau'_{ret} = \text{subst}(\tau_{ret}, \tau_{recip}, M) \\ p = \text{readonly} \Rightarrow TL = \text{function} \quad \forall i. \tau'_i = \text{subst}(\tau_i, \tau_{recip}, M) \end{array}}{\Delta, x : p \triangleright \tau_{recip}, \overline{y} : \tau' \vdash_f x.m(\overline{y}) : \tau'_{ret} \dashv \Delta, x : p \triangleright \text{trans}(\overline{S}, \tau_{recip}), \overline{y} : \text{res}(\tau')} \text{T-INV-1}$ |   |
| $\frac{\begin{array}{l} M = \emptyset[\overline{z} \mapsto x][\text{this} \mapsto \text{this}.f] \quad (p \triangleright \tau_{recip} \ f) \in \text{fields}(\Delta(\text{this})) \\ (TL \ \tau_{ret} \ m(\overline{\tau \ z}) \hookrightarrow \overline{S}) \in \text{methods}(\tau_{recip}) \\ p = \text{readonly} \Rightarrow TL = \text{function} \quad \text{trans}(\overline{S}, \tau_{recip}) <: \tau_{recip} \end{array}}{\Delta, \overline{x} : \tau' \vdash_f f.m(\overline{x}) : \text{subst}(\tau_{ret}, \tau_{recip}, M) \dashv \Delta, x : \text{res}(\text{subst}(\tau, \tau_{recip}, M))} \text{T-INV-2}$                                |   |
| $\frac{\overline{\tau \ f} = \text{mutableFields}(\Delta(\text{this})) \quad p \neq \text{readonly} \quad \Delta, f : \tau \vdash_t e : \text{pack\_to}[S, \tau_{ret}] \dashv \Delta'}{\Delta \vdash_f \text{unpack } \{e\} : \tau_{ret} \dashv \text{rm}(\overline{f}, \Delta'), \text{this} : \text{trans}(S, \Delta(\text{this}))} \text{T-UNPACK}$   |   |
| $\frac{\overline{\tau \ f} = \text{mutableFields}(\Delta(\text{this})) \quad \Delta' = \Delta, y : \text{res}(\tau'), x : \text{res}(\tau)}{\Delta, y : \tau', \overline{x} : \tau \vdash_t \text{pack\_to } S(\overline{x}) \text{ returns } y : \text{pack\_to}[S, \tau'] \dashv \Delta'} \text{T-PACK}$   |   |
| $\frac{\Delta \vdash_b e_1 : \tau \dashv \Delta_1 \quad \Delta \vdash_b e_2 : \tau \dashv \Delta_2}{\Delta \vdash_b \text{try } \{e_1\} \text{ catch } \{e_2\} : \tau \dashv \text{merge}(\Delta; \Delta_1, \Delta_2)} \text{T-TRY}$   |   |
| $\overline{\Delta \vdash_b \text{throw} : \tau \dashv \Delta'} \text{T-THR}$   |   |
| $\frac{\Delta, x : p \triangleright \tau'_s \vdash_b e_1 : \tau \dashv \Delta_1 \quad \Delta, x : p \triangleright \tau_s \vdash_b e_2 : \tau \dashv \Delta_2}{\Delta, x : p \triangleright \tau_s \vdash_t \text{if } x : \tau'_s \text{ then } e_1 \text{ else } e_2 \dashv \text{merge}(\Delta; \Delta_1, \Delta_2)} \text{T-DYN}$  |   |

Fig. 3. Statics

|   |                      |
|---|----------------------|
| $(\tau \ f) \text{ Ok in } C$   | Field Consistency    |
| $\frac{\tau = p \triangleright a.f_1 \dots .f_n.C \quad \text{wf}(\emptyset[\text{this} \mapsto \text{readonly} \triangleright D], \tau)}{(\tau \ f) \text{ Ok in } D}$   |                      |
| $\frac{\tau = \text{owned} \triangleright a.f_1 \dots .f_n.C.S \quad \text{wf}(\emptyset[\text{this} \mapsto \text{readonly} \triangleright D], \tau)}{(\tau \ f) \text{ Ok in } D}$  |                      |
| $(\text{MethDecl} \ \text{MethBody}) \text{ Ok in } C.S$  | Method Consistency   |
| $\frac{\begin{array}{l} \Delta = \emptyset, \text{this} : \text{owned} \triangleright C.S, \bar{x} : \bar{\tau} \quad \forall i. \text{wf}(\Delta, \tau_i) \\ \Delta \vdash_{\text{f}} e : \tau' \dashv \Delta' \quad \forall a, \tau_p. \Delta'(a) = \text{owned} \triangleright \tau_p \text{ iff } a = \text{this} \\ \Delta'(\text{this}) <: \text{trans}(\bar{S}, \text{owned} \triangleright C.S) \end{array}}{\text{transaction } \tau' \ m(\bar{\tau} \ \bar{x}) \hookrightarrow \bar{S} \ \{e\} \text{ Ok in } C.S}$ |                      |
| $\frac{\begin{array}{l} \Delta = \emptyset, \text{this} : \text{readonly} \triangleright C.S, \bar{x} : \bar{\tau} \quad \forall i. \text{wf}(\Delta, \tau_i) \\ \Delta \vdash_{\text{f}} e : \tau' \dashv \Delta' \quad \forall a, \tau_p. \Delta'(a) \neq \text{owned} \triangleright \tau_p \end{array}}{\text{function } \tau' \ m(\bar{\tau} \ \bar{x}) \ \{e\} \text{ Ok in } C.S}$   |                      |
| $\text{state } S \ \{ \dots \} \text{ Ok in } C$  | State Consistency    |
| $\frac{\forall i. (\text{MethDecl}_i \ \text{MethBody}_i) \text{ Ok in } C.S \quad \forall i. (\tau_i \ f_i) \text{ Ok in } C}{\text{state } S \ \{ \bar{\tau} \ f \ \text{MethDecl} \ \text{MethBody} \}}$   |                      |
| $\text{contract } C \ \{ \dots \} \text{ Ok}$   | Contract Consistency |
| $\frac{\begin{array}{l} \forall i. (\tau_{f_i} \ f_i) \text{ Ok in } C \quad \forall i. (\tau_{g_i} \ g_i) \text{ Ok in } C \quad \forall i. St_i \text{ Ok in } C \quad \forall i. Ct_i \text{ Ok} \\ \forall \tau, i, j. ((\tau \ f_i) \notin \text{fields}(St_j) \wedge (\tau \ g_i) \notin \text{fields}(St_j) \wedge f_i \neq g_j) \end{array}}{\text{contract } C \ \{ \bar{Ct} \ \bar{St} \ \text{const } \tau_f \ f \ \bar{\tau}_g \ g \}}$   |                      |

Fig. 4. Auxiliary Judgments

|  |
|--|
| $\mu \in \text{LOCATIONS} \rightarrow \text{OBJECTS}$  |
| $\rho \in \text{VARIABLES} \rightarrow \text{LOCATIONS}$   |
| $T ::= C.S \mid \ell.C.S$  |
| $\text{OBJECTS} = \{(T, f_{map}) \mid f_{map} \in \text{FIELDNAMES} \rightarrow \text{LOCATIONS}\}$  |
| $field(f, (T, f_{map})) = f_{map}(f)$  |
| $type((T, f_{map})) = T$   |
| $(T, f_{map})[f \mapsto \ell] = (T, f_{map}[f \mapsto \ell])$  |
| $\ell \in \text{LOCATIONS}$  |
| $e ::= \dots \mid \text{try}(\mu) \{e_1\} \text{ catch } \{e_2\} \mid \ell \mid \text{Ex} \mid \text{call}(\rho) \{e\}$  |
| $v ::= \ell \mid \text{pack\_to } S(\bar{\ell}) \text{ returns } \ell$   |
| $\boxed{\mathbb{E}, \mathbb{E}[e]}$ Evaluation Context, Substitution   |
| $\mathbb{E} ::= \square \mid \text{let } x = \mathbb{E} \text{ in } e \mid \text{let } x = \ell \text{ in } \mathbb{E} \mid \text{unpack } \{\mathbb{E}\} \mid \text{call}(\rho) \{\mathbb{E}\}$   |
| $\square[e] = e$   |
| $(\text{let } x = \mathbb{E} \text{ in } e')[e] = (\text{let } x = \mathbb{E}[e] \text{ in } e')$  |
| $(\text{let } x = \ell \text{ in } \mathbb{E})[e] = (\text{let } x = \ell \text{ in } \mathbb{E}[e])$  |
| $(\text{unpack } \{\mathbb{E}\})[e] = (\text{unpack } \{\mathbb{E}[e]\})$  |
| $(\text{call}(\rho) \{\mathbb{E}\})[e] = (\text{call}(\rho) \{\mathbb{E}[e]\})$  |
| $\boxed{context(\mu, \rho, \mathbb{E})}$ Calculates a suitable $\rho'$ for evaluation inside of $\mathbb{E}$   |
| $context(\mu, \rho, \square) = \rho \quad context(\mu, \rho, \text{let } x = \mathbb{E} \text{ in } e) = context(\mu, \rho, \mathbb{E})$   |
| $context(\mu, \rho, \text{let } x = \ell \text{ in } \mathbb{E}) = context(\mu, \rho[x \mapsto \ell], \mathbb{E})$   |
| $\overline{\tau f} = fields(type(\mu(\rho(\mathbf{this}))))$   |
| $\frac{\rho' = \rho[f_1 \mapsto field(f_1, \mu(\rho(\mathbf{this}))] \dots [f_n \mapsto field(f_n, \mu(\rho(\mathbf{this}))]]}{context(\mu, \rho, \text{unpack } \{\mathbb{E}\}) = context(\mu, \rho' \setminus \{\mathbf{this}\}, \mathbb{E})}$ |
| $context(\mu, \rho, \text{call}(\rho') \{\mathbb{E}\}) = context(\mu, \rho', \mathbb{E})$  |

Fig. 5. Auxiliary Definitions

|   |  |
|---|--|
| $\mu, \rho, e \rightarrow \mu, e$   |  |
| $\frac{}{\mu, \rho, x \rightarrow \mu, \rho(x)} \text{E-VAR}$   | $\frac{}{\mu, \rho, f \rightarrow \mu, \text{field}(f, \mu(\rho(\mathbf{this})))} \text{E-READ}$   |
| $\frac{}{\mu, \rho, \mathbb{E}[\mathbf{Ex}] \rightarrow \mu, \mathbf{Ex}} \text{E-BUBBLE-UP}$   | $\frac{\text{context}(\mu, \rho, \mathbb{E}) = \rho' \quad \mu, \rho', e \rightarrow \mu', e'}{\mu, \rho, \mathbb{E}[e] \rightarrow \mu', \mathbb{E}[e']} \text{E-EV}$ |
| $\frac{}{\mu, \rho, \mathbf{let } x = \ell \text{ in } v \rightarrow \mu, v} \text{E-LET}$  | $\frac{}{\mu, \rho, \mathbf{throw} \rightarrow \mu, \mathbf{Ex}} \text{E-THROW}$   |
| $\frac{\text{lookup}(\text{type}(\mu(\rho(x))), m) = \tau \quad m(\bar{\tau} \bar{z}) \hookrightarrow \bar{S} \{e\} \quad \rho' = \emptyset[z_i \mapsto \rho(y_i)][\mathbf{this} \mapsto \rho(x)]}{\mu, \rho, x.m(\bar{y}) \rightarrow \mu, \text{call}(\rho') \{e\}} \text{E-METHOD}$  |  |
| $\frac{}{\mu, \rho, \text{call}(\rho') \{ \ell \} \rightarrow \mu, \ell} \text{E-RETURN}$   |  |
| $\frac{\ell \notin \text{Dom}(\mu) \quad \bar{\tau} \bar{f} = \text{fields}(C.S) \quad f_{\text{map}} = \{(f_1, \rho(x_1)), \dots, (f_n, \rho(x_n))\}}{\mu, \rho, \mathbf{new } C.S(\bar{x}) \text{ as } p \rightarrow \mu[\ell \mapsto (C.S, f_{\text{map}})], \ell} \text{E-NEW}$   |  |
| $\frac{\forall i. \rho(x_i) = \ell_i \quad \rho(y) = \ell'}{\mu, \rho, \mathbf{pack\_to } S(\bar{x}) \text{ returns } y \rightarrow \mu, \mathbf{pack\_to } S(\bar{\ell}) \text{ returns } \ell'} \text{E-PACK}$  |  |
| $\frac{\bar{\tau} \bar{f} = \text{fields}(\text{type}(\mu(\rho(\mathbf{this})))) \quad O_{\text{this}} = \rho(\mathbf{this})[f_1 \mapsto \ell_1] \dots [f_n \mapsto \ell_n] \quad \mu' = \mu[\rho(\mathbf{this}) \mapsto O_{\text{this}}]}{\mu, \rho, \mathbf{unpack } \{ \mathbf{pack\_to } S(\bar{\ell}) \text{ returns } \ell' \} \rightarrow \mu', \ell'} \text{E-TRANS}$ |  |
| $\frac{\text{type}(\mu(\rho(x))) \text{ instanceOf } \tau_s}{\mu, \rho, \mathbf{if } x : \tau_s \text{ in } e \rightarrow \mu', \mathbf{Ex}} \text{E-DYN-EX}$   | $\frac{\text{type}(\mu(\rho(x))) \text{ instanceOf } \tau_s}{\mu, \rho, \mathbf{if } x : \tau_s \text{ in } e \rightarrow \mu', e} \text{E-DYN-OK}$                    |
| $\frac{}{\mu, \rho, \mathbf{try } \{e_1\} \text{ catch } \{e_2\} \rightarrow \mu, \mathbf{try}(\mu) \{e_1\} \text{ catch } \{e_2\}} \text{E-TRY-1}$   |  |
| $\frac{\mu, \rho, e_1 \rightarrow \mu', e'_1}{\mu, \rho, \mathbf{try}(\mu_1) \{e_1\} \text{ catch } \{e_2\} \rightarrow \mu', \mathbf{try}(\mu_1) \{e'_1\} \text{ catch } \{e_2\}} \text{E-TRY-2}$  |  |
| $\frac{}{\mu, \rho, \mathbf{try}(\mu) \{ \ell \} \text{ catch } \{e_2\} \rightarrow \mu, \ell} \text{E-TRY-3}$  |  |
| $\frac{}{\mu, \rho, \mathbf{try}(\mu_1) \{ \mathbf{Ex} \} \text{ catch } \{e_2\} \rightarrow \mu_1, e_2} \text{E-CATCH}$  |  |

Fig. 6. Dynamics