# 15-150 Summer 2017 Homework 01

Out: Monday, 22 May 2017 Due: Wednesday, 24 May 2017 at 23:59 EST

#### 1 Introduction

Welcome to 15-150! This assignment introduces the course infrastructure and the SML runtime system, then asks some simple questions related to the first week of lectures and lab.

### 1.1 Getting The Assignment

The starter files for the homework assignment have been distributed through our git repository. To learn how to use it, read the documentation at

http://www.cs.cmu.edu/~15150/resources/handouts/git.pdf

If you still need help, ask a TA promptly and get started on the non-code questions.

In the first lab, you set up a clone of this repository in your AFS space. To get the files for this homework, log in to one of the UNIX servers via SSH or sit down at a cluster machine, change into your clone of the repository, and run

git pull

This should add a directory for Homework 1 to your copy of the repository, containing a copy of this PDF and some starter code in subdirectories. If this does not work for you, contact course staff immediately.

#### 1.2 Collaboration

The homework collaboration policy can be found at

http://www.cs.cmu.edu/~15150/policy.html

In keeping with this policy, in the handout is a collab.txt file. In this file, enter the andrew ids of everyone you have collaborated with on this homework, each on a separate line.

It is very important that you do this. If you do not and you appear to have collaborated, or if you appear to have collaborated with anyone not listed in your collab.txt file, this will be considered an academic integrity violation.

#### 1.3 Submission

Submissions will be handled through Autolab, at

https://autolab.andrew.cmu.edu

In preparation for submission, your hw/01 directory should contain a file named exactly hw01.pdf containing your written solutions to the homework.

To submit your solutions, run make from the hw/01 directory (that contains a code folder and a file hw01.pdf). This should produce a file hw01.tar, containing the files that should be handed in for this homework assignment. Open the Autolab web site, find the page for this assignment, and submit your hw01.tar file via the "Handin your work" link.

The Autolab handin script does some basic checks on your submission: making sure that the file names are correct; making sure that no files are missing; making sure that your code compiles cleanly. Note that the handin script is *not* a grading script—a timely submission that passes the handin script will be graded, but will not necessarily receive full credit. You can view the results of the handin script by clicking the number (usually either 0.0 or 1.0) corresponding to the "check" section of your latest handin on the "Handin History" page. If this number is 0.0, your submission failed the check script; if it is 1.0, it passed.

Remember that your written solutions must be submitted in PDF format—we do not accept MS Word files or other formats.

Your hw01.sml file must contain all the code that you want to have graded for this assignment, and must compile cleanly in Autolab. If you have a function that happens to be named the same as one of the required functions but does not have the required type, it will not be graded.

Warning: On this homework and all future homeworks, we reserve the right to refuse to grade or to otherwise penalize submissions that do not follow specified formatting or the instructions in the handout.

If your code does not compile in Autolab you may receive a zero on all the code-related sections of the homework.

The reason for this is that even simple code errors can take hours to track down manually by someone who did not author the code, such as a TA, time better spent actually helping students understand course material. So — PLEASE PLEASE — make sure all your code compiles cleanly in Autolab. If you make a last-second submission with a tiny change, that sometimes can cause all your code to fail. So be very careful and doublecheck that every submission compiles cleanly and arrives properly in Autolab.

Check both code and pdf files — a common mistake is to submit an incorrect or empty or garbled pdf file, causing you to lose all credit on the written parts of the assignment.

Please contact course staff if you have any questions.

If you attempt to contact us close to the deadline, please be aware that we may not be able to respond before the deadline. If you cannot access the Autolab site, notify the course staff immediately.

#### 1.4 Due Date

This assignment is due on Wednesday, 24 May 2017 at 23:59 EST. Remember that you may use a maximum of one late day per assignment, and that you are allowed a total of three late days for the semester.

# 2 Course Resources and Policy

Please make sure you have access to the various course resources. We will post important information often. You can find more information about these resources in the Tools page of the course's Web site.

We are using Web-based discussion software called Piazza for the class. You are encouraged to post questions and answers, but please do not post anything that gives away answers or violates the academic integrity policy. If you think that your question might give away answers, you can make it a *private* question, visible only to the course staff.

Task 2.1 (1 pts). You should have received an e-mail message with instructions on signing up for Piazza. Activate your account. There is a pinned post there with an image. Briefly describe this image.

# 3 Types

In this section we will explore the step-by-step reasoning of type checking to better understand when an SML expression is well-typed and, if so, what its type is.

An application expression e2 e1 has type t2 if e2 has type t1 -> t2 and e1 has type t1. In an arrow type like t1 -> t2, t1 is the argument type and t2 is the result type. Therefore, this application is well-typed if the function expression e2 has an arrow type, and the argument expression e1 has the correct argument type. The application e2 e1 then has the corresponding result type.

Using the notation from class for type bindings, we write e: t to mean that e has type t. We can summarize the above typing rule as follows:

```
[APP] If e2: t1 -> t2 and e1: t1, then (e2 e1): t2.
```

For example, suppose intToString has type int -> string. Consider the application expression intToString 7. We already said that intToString has type int -> string, an arrow type with argument type int and result type string. Clearly 7 has type int. Since this is the correct argument type, the application intToString 7 has the corresponding result type (string).

We can summarize this informal discussion as follows:

- (i) intToString : int -> string
- (ii) 7 : int
- (iii) (intToString 7) : string by [APP]

Task 3.1 (3 pts). The infix operator ^ has type string \* string -> string. An expression of the form e1 ^ e2 has type string if e1 has type string and e2 has type string.

Determine the type of the expression:

(intToString 115) ^ (intToString 35)

Describe your reasoning in the same manner as above, first informally using English(!), then summarize using the more formal notation. If part of your reasoning exactly corresponds to that found in the example feel free to cite the correspondence rather than copying everything.

Task 3.2 (2 pts). Explain why the expression intToString 2.0 is not well-typed.

### 4 Evaluation

A well-typed expression can be evaluated. If its evaluation terminates, the result is a value. If the expression is already a value (such as an integer numeral, or a function), it is not evaluated further. In an expression like e1 ^ e2, the infix concatenation operator ^ evaluates its two subexpressions, e1 and e2, from left to right, then returns the string obtained by concatenating the two strings that result from these evaluations.

Here is an example: Consider the expression (intToString 7) ^ "1". Assume that the application (intToString 7) evaluates to the value "7". The expression "1" is already a value. So the expression (intToString 7) ^ "1" evaluates to "71", the string built by concatenating "7" and "1".

Using the notation from class, we write  $e \implies e'$  when e reduces to e' (when an expression "reduces to" a value we may also say "evaluates to"). We can summarize the relevant facts about evaluation in this example as:

```
(intToString 7) ^ "1"

⇒ "7" ^ "1"

⇒ "71"
```

Now we ask you to perform a similar analysis on another example. Assume that the expression fact 4 evaluates to 24, and that intToString function has the usual behavior, e.g., intToString 42 evaluates to "42".

Task 4.1 (2 pts). Determine the value that results from the following expression:

```
"4" ^ (intToString (fact 4))
```

Explain your reasoning informally in the same manner as above.

Task 4.2 (3 pts). Now use the  $\implies$  notation from class, as above, to express the key evaluation facts in your analysis.

### 5 Interpreting Error Messages

Download the file hw01.sml from the git repository as described in Section 1.1. You can evaluate the SML declarations in this file using the command

use "hw01.sml";

at the SML REPL prompt. Unfortunately, the file has some errors that must be corrected. The next five tasks will guide you through the process of correcting these errors.

Task 5.1 (2 pts). What error message do you see when you evaluate the unmodified hw01.sml file? What caused this error? How can it be fixed?

Correct this one error in the file hw01.sml and evaluate the file again using the same command as before.

Task 5.2 (2 pts). With the first error corrected, you will encounter a set of errors. What is the first error in this set? What caused this error? How do you fix it?<sup>1</sup>

Correct this error in the file hw01.sml and evaluate the file again.

**Task 5.3** (2 pts). You should see more error messages. What are the first two error messages? They should both reference the same line of ML code. What do these error messages mean? How do you fix them?

Both errors should disappear with one correction. Fix the errors, and evaluate the file again.

Task 5.4 (2 pts). There is now yet another set of errors. What is the first error message you see now? What does this error message mean? How do you fix this error?

Once again, fix the error, then re-evaluate the file.

**Task 5.5** (2 pts). There should be one more error message. What is it? What caused it? How do you fix this error?

When you correct this final error and evaluate the file there should be no more error messages. (Be sure to fix the error and be sure to verify that your code complies cleanly on Autolab when you submit the final code file.)

<sup>&</sup>lt;sup>1</sup>*Hint:* Think about types.

# 6 Specs and Functions

Consider the following function:

```
(* decimal : int -> int list *)
fun decimal (n:int):int list =
   if n<10 then [n] else (n mod 10) :: decimal(n div 10)
   A specification for this function has typical form

(* decimal : int -> int list
   * REQUIRES: . . .
   * ENSURES: . . .
*)
```

The function satisfies this spec if for all values n of type int that satisfy the REQUIRES condition, decimal n evaluates as described in the ENSURES condition and if the function itself makes no recursive calls that violate the REQUIRES condition.

For each of the following specifications, say whether or not this function satisfies the specification. If not, give an example to illustrate what goes wrong.

Note: A (decimal) digit is an integer value in the range 0 - 9.

```
Task 6.1 (2 pts).

(* decimal: int -> int list
  * REQUIRES: n>0
  * ENSURES: decimal(n) evaluates to a non-empty list of digits
  *)

Task 6.2 (2 pts).

(* decimal: int -> int list
  * REQUIRES: n>=0
  * ENSURES: decimal(n) evaluates to a non-empty list of digits
  *)

Task 6.3 (2 pts).

(* decimal: int -> int list
  * REQUIRES: true
  * ENSURES: decimal(n) evaluates to a non-empty list of digits
  *)
```

#### **Task 6.4** (2 pts).

```
(* decimal: int -> int list
  * REQUIRES: n>=0
  * ENSURES: decimal(n) evaluates to a list of digits
  *)
```

**Task 6.5** (2 pts). Which *one* of these specifications gives the *most* useful information about the applicative behavior of the function decimal? Say why, briefly.

# 7 Parallel Computing

In lab we showed how to draw a computation tree for an expression, whose structure reflects the order in which its sub-expressions can be evaluated. Each non-leaf node should be labeled with an operator. The children of such a node are sub-trees representing the sub-expressions to be combined by that operator. Leaf nodes are labeled with values, such as integer numerals.

Task 7.1 (2 pts). Draw the computation tree for the following expression:

$$(8 + 7) * (16 + 2)$$

We define the *work* of a computation tree to be the total number of non-leaf nodes (i.e., the number of nodes labeled with operations). The *span* of a computation tree is the number of edges along the longest path from the root to a leaf.

Task 7.2 (2 pts). What are the work and span for the above computation tree?

Suppose we have an expression whose computation tree has work W and span S. No matter how many processors are usable for parallel evaluation, the number of steps required to evaluate the expression must be at least S, because to evaluate (the expression represented by) a node we must first evaluate the node's children (i.e., the immediate sub-expressions). That is because the value at the node depends on the values of these sub-expressions; this is a data dependency. Also note that if each of P processors performs one evaluation step in parallel during each time cycle, it would require at least W/P time cycles to perform all of the W operations required to fully evaluate the expression. These observations give the intuition behind Brent's Theorem:

**Theorem 1 (Brent's Theorem)** If an expression e evaluates to a value with work W and span S, then evaluating e on a P-processor machine requires at least  $\max(W/P, S)$  steps.

Task 7.3 (2 pts). Use Brent's Theorem to find a lower bound on the number of steps required to evaluate the computation tree for (8 + 7) \* (16 + 2) on a machine with P = 2 processors.

Task 7.4 (2 pts). Describe a possible assignment of the nodes in this computation tree to two processors that achieves this lower bound. In particular, for each time step, say what node each processor is evaluating. If a processor is idle during a time step say so.

Consider the task of planting n pear trees in a garden using diggers, sowers, and sprinklers. For each pear tree, a digger first takes t minutes to dig a hole for the tree, then a sower takes t minutes to bury the seed for that tree, and then finally it takes a sprinkler t minutes to sprinkle water on the tree.

Task 7.5 (3 pts). How much *time* would it take to complete the task with one digger, one sower, and one sprinkler? Keep in mind that they can do their jobs simultaneously, but they need to follow the correct sequence of tasks, and they cannot work on the same tree at the same time. Justify your answer briefly.

Task 7.6 (3 pts). If you had an infinite number of diggers, sowers, and sprinklers, how much *time* would it take to finish the task? Justify your answer briefly.

This assignment has a total of 45 points.