

The sum of any five consecutive integers is divisible by 5

The statement is true

Proof:

Let n be an arbitrary integer, then the five consecutive integers starting from n can be expressed as: $n, n + 1, n + 2, n + 3, n + 4$.

Sum of the five integers is:

$$n + (n + 1) + (n + 2) + (n + 3) + (n + 4) = 5n + 10 = 5(n + 2)$$

As $n + 2$ is an integer, $5(n + 2)$ is divisible by 5. So for any arbitrary five consecutive integers, their sum is divisible by 5.